

Sea Ice Modeling for Climate Applications

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and Elizabeth Hunke (LANL)



1 km



10 m

From:
Feltham,
2008
(photos by
Hajo Eicken)

Sea Ice

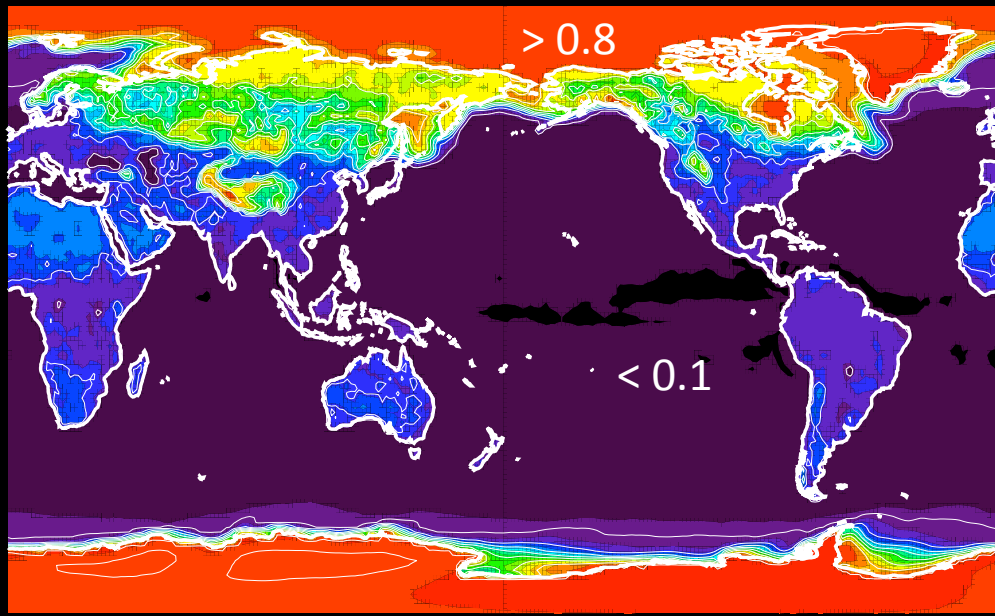
- Composed of floes (can freeze to form a continuous cover)
- Typical thickness of meters
- Riddled with cracks (leads) and ridges
- Complex mosaic of ice types within small area

Photo courtesy of Don Perovich

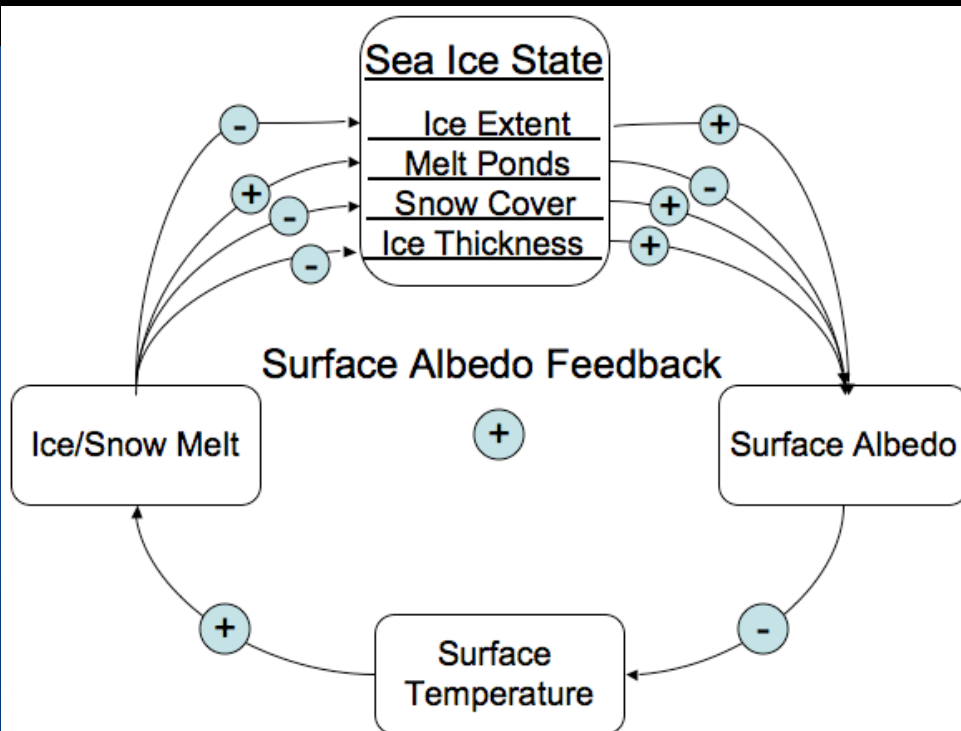
440 m



Surface albedo

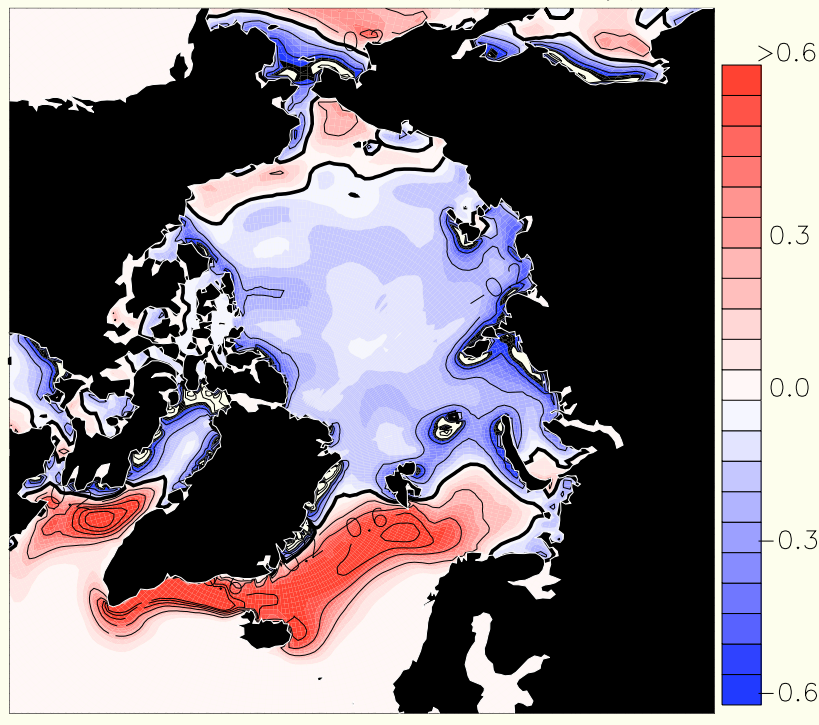


Why do we care about sea ice?
Surface energy (heat) budget



- High albedo of sea ice modifies radiative fluxes
- Sea ice insulates ocean from atmosphere influencing turbulent heat & moisture exchange

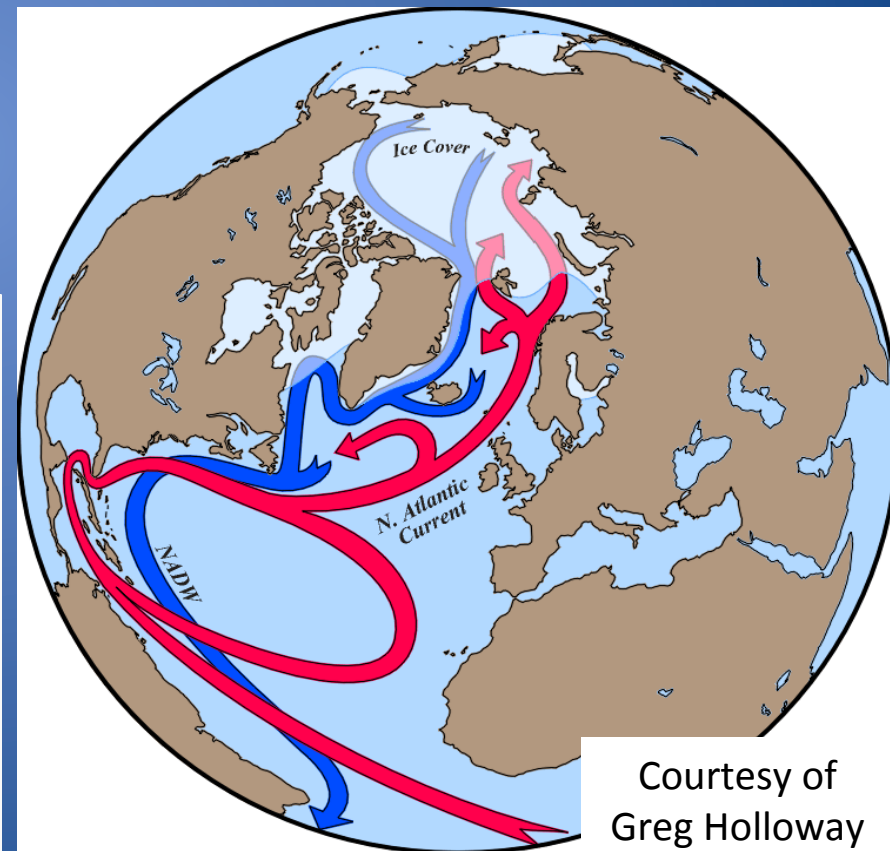
Fresh Water Flux (cm/day)



Ice-Ocean Freshwater Exchange

- Salt rejection during ice formation leaves sea ice relatively fresh (salt flux to ocean)
- Ice melt releases freshwater back to the ocean
- Can modify ocean circulation

Why do we care about sea ice? Hydrological Cycle



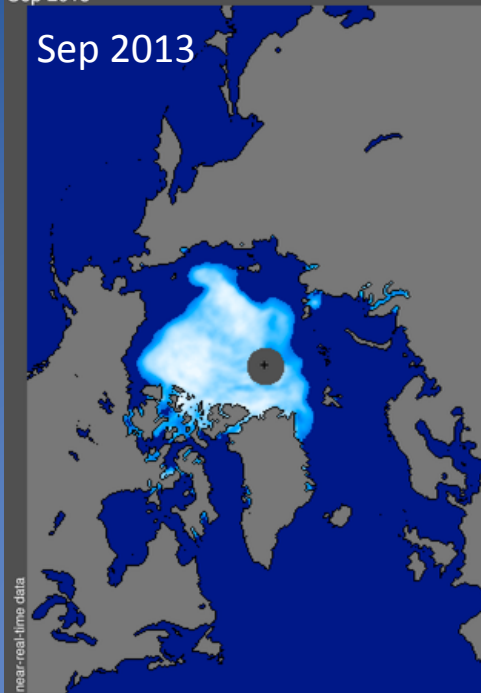
Courtesy of
Greg Holloway

Contrasting the Hemispheres

- Arctic Ocean surrounded by land (thicker ice).
- Southern Ocean unbounded (free drift).
- Larger seasonal cycle in south.
- Winter extent set by ocean in south and land/ocean in north.

Sea Ice Concentration
Sep 2013

Sep 2013



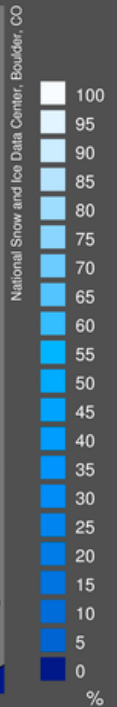
Total area = 3.5 million sq km

Sea Ice Concentration
Mar 2013

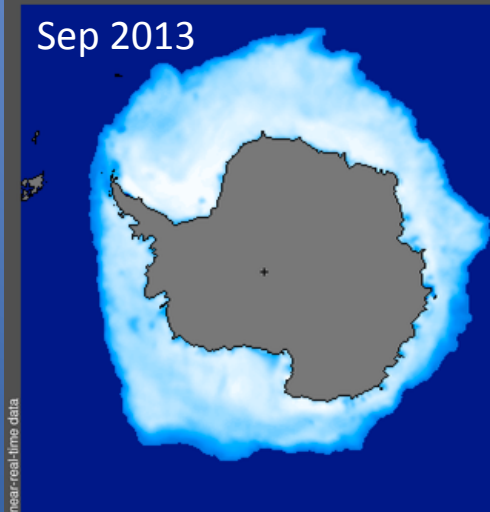
Mar 2013



Total area = 13.0 million sq km

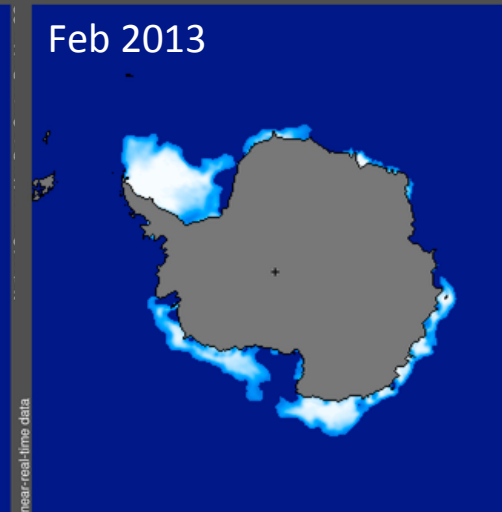


Sep 2013

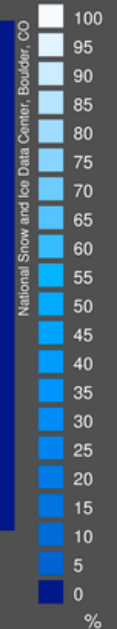


Total area = 15.1 million sq km

Feb 2013



Total area = 2.5 million sq km



NSIDC

What do we need in a sea ice model for climate applications?

- Model which simulates a reasonable mean state/variability of sea ice
 - Concentration, thickness, mass budgets
- Realistically simulates ice-ocean-atmosphere exchanges of heat and moisture
- Realistically simulates response to climate perturbations - key climate feedbacks

CICE: the Los Alamos Sea Ice Model
Documentation and Software User's Manual
Version 4.1
LA-CC-06-012

Elizabeth C. Hunke and William H. Lipscomb
T-3 Fluid Dynamics Group, Los Alamos National Laboratory
Los Alamos NM 87545

May 5, 2010

CESM1 uses the CICE Los Alamos Sea
Ice Model (Hunke and Lipscomb)

Full documentation available online

Sea Ice Models Used in Climate Simulations

- Two primary components
 - Dynamics
 - Solves force balance to determine sea ice motion
 - Thermodynamics
 - Solves for vertical ice temperature profile
 - Vertical/lateral melt and growth rates
- Some (about 30% of IPCC-AR4, 50% for AR5?) models also include
 - Ice Thickness Distribution
 - Subgridscale parameterization
 - Accounts for high spatial heterogeneity in ice

Dynamics



Sea Ice Model – Dynamics

- Force balance between wind stress, water stress, internal ice stress, coriolis and stress associated with sea surface slope
- Ice treated as a continuum with an effective large-scale rheology describing the relationship between stress and deformation
- Ice freely diverges (no tensile strength)
- Ice resists convergence and shear

(e.g. Hibler, 1979)

$$m \frac{D\mathbf{u}}{Dt} = -mf\mathbf{k} \times \mathbf{u} + \boldsymbol{\tau}_a + \boldsymbol{\tau}_w - mg_r \nabla Y + \nabla \cdot \boldsymbol{\sigma}$$

Total derivative

Coriolis

Air stress

Ocean stress

Sea Surface Slope

Internal Ice Stress

Sea Ice Model – Dynamics

- Air Stress

$$\vec{\tau}_a = \frac{\rho_a u^{*2} \vec{U}_a}{|\vec{U}_a|},$$

$$u^* = c_u |\vec{U}_a|$$

- Ocean Stress

$$\vec{\tau}_w = c_w \rho_w |\vec{U}_w - \vec{u}| \left[(\vec{U}_w - \vec{u}) \cos \theta + \hat{k} \times (\vec{U}_w - \vec{u}) \sin \theta \right]$$

(e.g. Hibler, 1979)

$$m \frac{D\mathbf{u}}{Dt} = -mf\mathbf{k} \times \mathbf{u} + \boldsymbol{\tau}_a + \boldsymbol{\tau}_w - mg_r \nabla Y + \nabla \cdot \boldsymbol{\sigma}$$

↑
Total derivative

↑
Coriolis

↑
Air stress

↑
Ocean stress

↑
Sea Surface Slope

↑
Internal Ice Stress

Sea Ice Model – Dynamics

- Ice Interaction Term (Internal Ice Stress)
 - Requires a constitutive law to relate ice stress (σ) to ice strain rate ($\dot{\epsilon}$)

(e.g. Hibler, 1979)

$$m \frac{Du}{Dt} = -mf\mathbf{k} \times \mathbf{u} + \boldsymbol{\tau}_a + \boldsymbol{\tau}_w - mg_r \nabla Y + \nabla \cdot \boldsymbol{\sigma}$$

Total derivative

Coriolis

Air
stress

Ocean
stress

Sea Surface
Slope

Internal
Ice Stress

Sea Ice Model – Dynamics

- Ice Interaction Term (Internal Ice Stress)
 - Requires a constitutive law to relate ice stress (σ) to ice strain rate ($\dot{\epsilon}$)

For example - A compressive stress test

At first:

Ice floe side view

Length L

After applying a compressive force, the ice deforms...

σ

Volume conserved so ice becomes thicker

σ

Strain: $\epsilon = \delta L / L$

Strain Rate: $\dot{\epsilon} = \delta L / L dt$

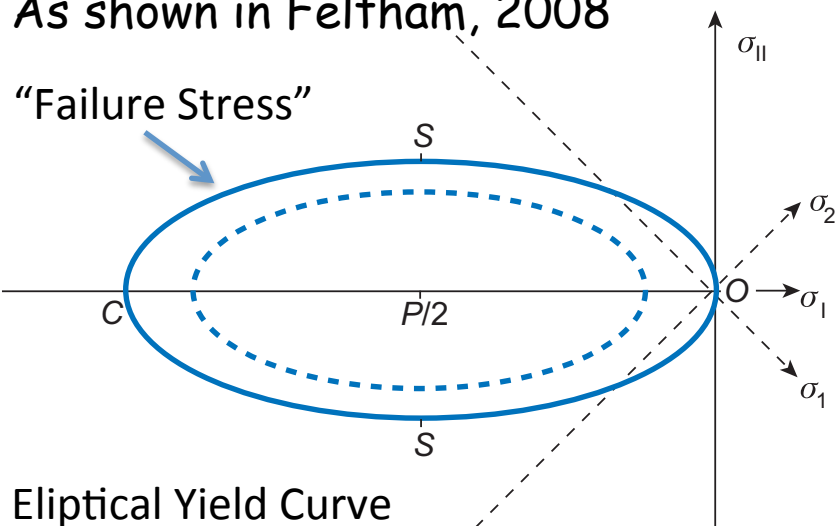
$L + \delta L$

Sea Ice Model – Dynamics

- Ice Interaction Term (Internal Ice Stress)
 - Use variant of Viscous-Plastic Rheology (Hibler, 1979)
 - Treats ice as a continuum - plastic at normal strain rates and viscous at very small strain rates.
 - Ice has no tensile strength (freely diverges) but resists convergence and shear (strength dependent on ice state)

As shown in Feltham, 2008

“Failure Stress”

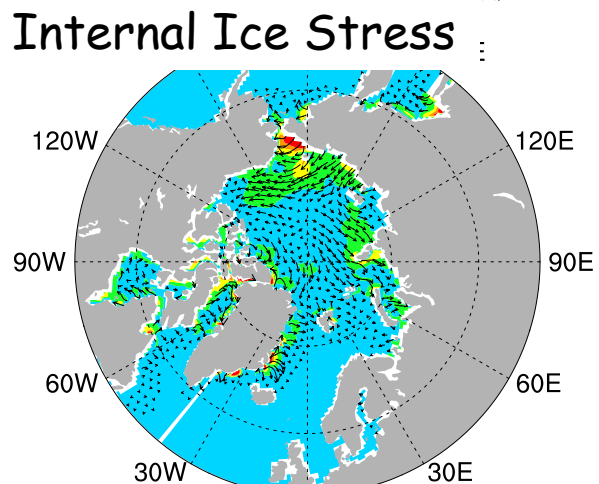
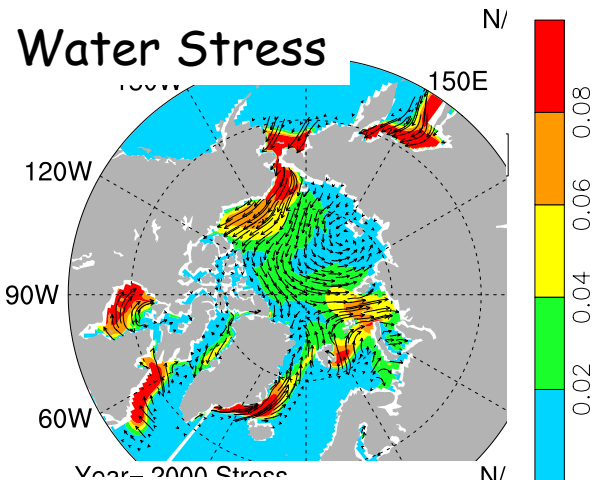
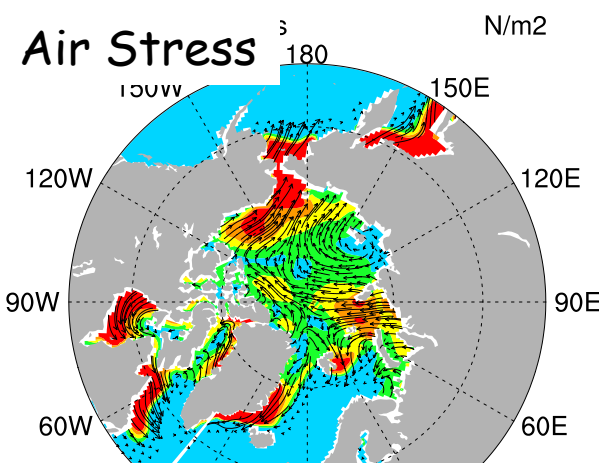


Elliptical Yield Curve

Elastic-Viscous-Plastic Model

EVP model uses explicit time stepping by adding elastic waves to constitutive law (Hunke and Dukowicz, 1997)

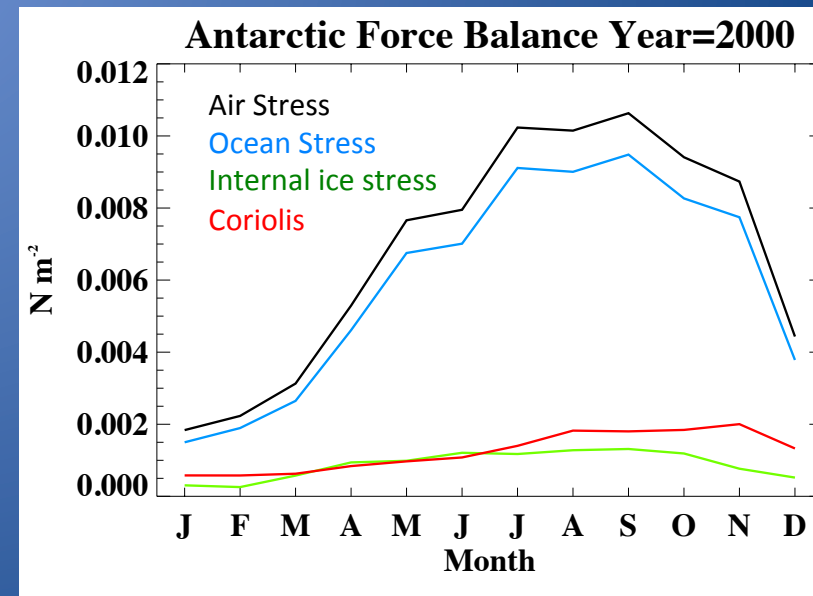
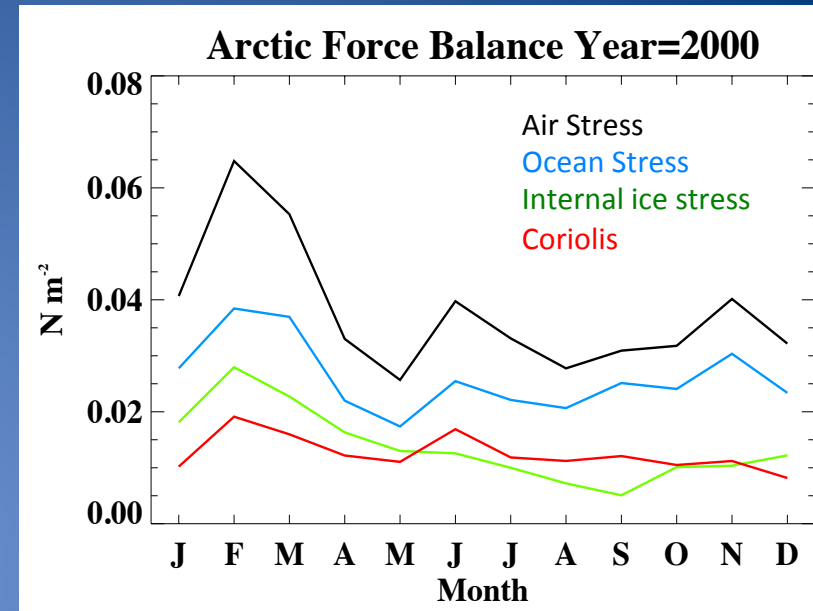
Simulated Force Balance



- Air stress largely balanced by ocean stress.

- Internal ice stress has smaller role

- In Antarctic ice in nearly free drift - weak ice interaction term



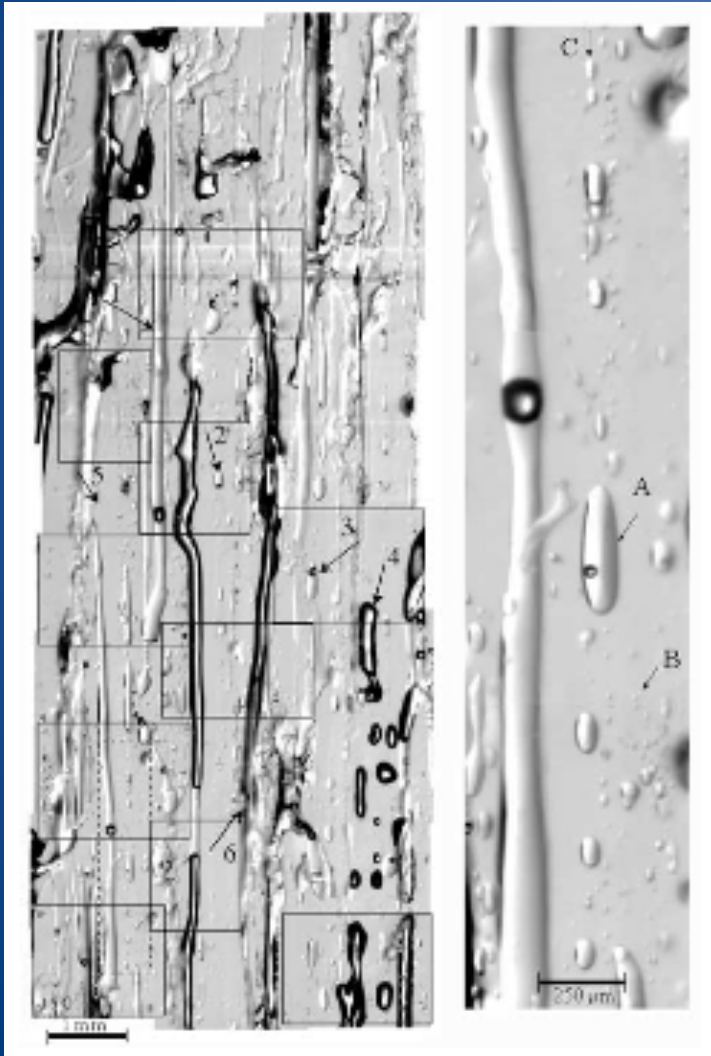
Thermodynamics



Thermodynamics

Vertical heat transfer

$$\rho c \frac{\partial T}{\partial t} = \frac{\partial}{\partial z} k \frac{\partial T}{\partial z} + Q_{SW}$$



- Assume brine pockets are in thermal equilibrium with ice
- Heat capacity and conductivity are functions of T/S of ice
- Assume constant salinity profile
- Assume non-varying density
- Assume pockets/channels are brine filled
- Traditionally:

$$Q_{SW} = -\frac{d}{dz} I_{SW} e^{-\kappa z} \quad \text{where}$$
$$I_{SW} = i_0 (1 - \alpha) F_{SW}$$

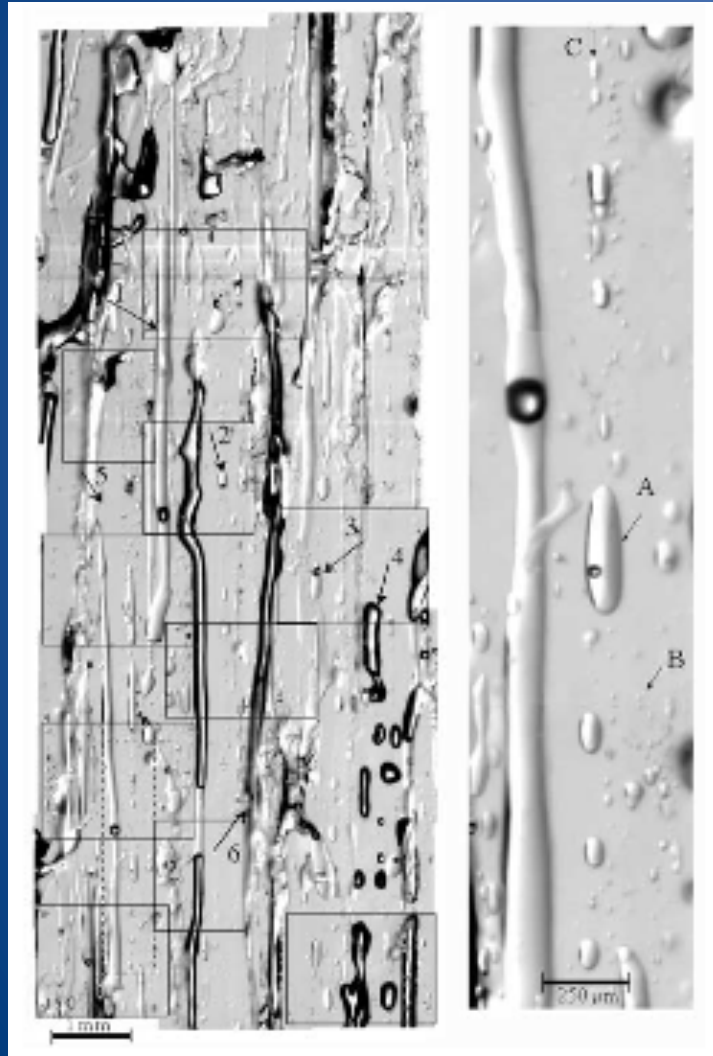
(from Light, Maykut, Grenfell, 2003)

(Maykut and Untersteiner, 1971; Bitz and Lipscomb, 1999; others)

Thermodynamics

Vertical heat transfer

$$\rho c \frac{\partial T}{\partial t} = \frac{\partial}{\partial z} k \frac{\partial T}{\partial z} + Q_{sw}$$



$$c(T, S) = c_0 + \frac{\gamma S}{T^2}$$

where T is in Celsius,

$$\gamma = L_0 \mu \quad \text{and} \quad T_m = -\mu S$$

Untersteiner, 1961

Enthalpy:

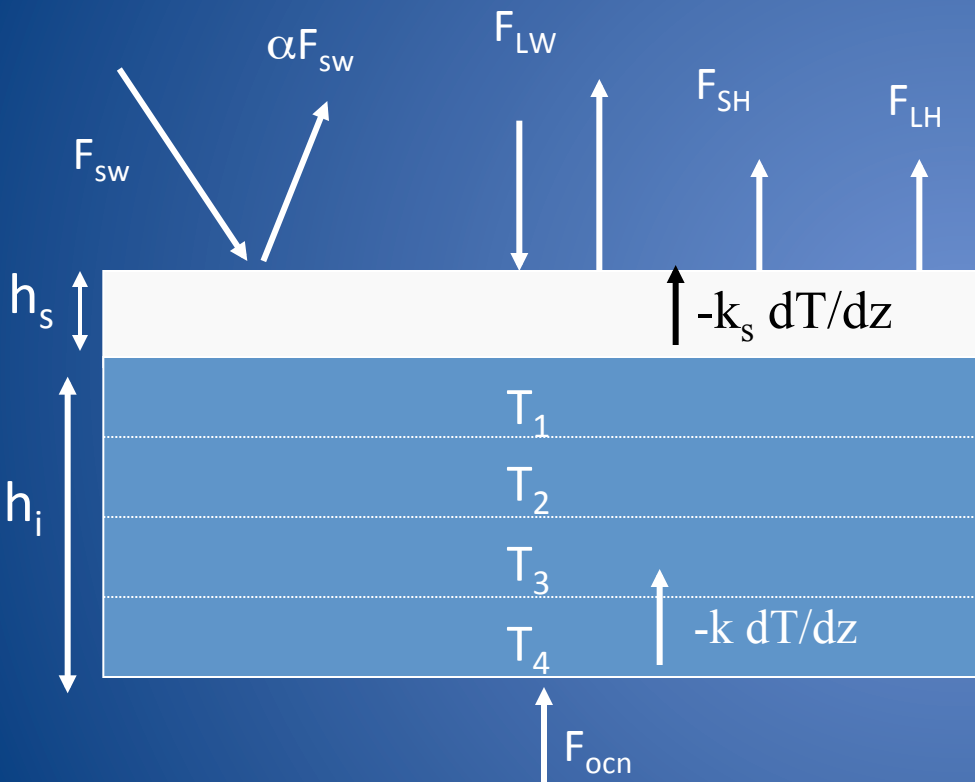
Heat required to melt a unit of ice

$$q(S, T) = \rho c_0 (-\mu S - T) + \rho L_0 \left(1 + \frac{\mu S}{T} \right)$$

(from Light, Maykut, Grenfell, 2003)

(Maykut and Untersteiner, 1971; Bitz and Lipscomb, 1999; others)

Sea ice thermodynamics



Balance of fluxes at surface

$$(1 - \alpha)F_{SW} + F_{LW} - \sigma T^4 + F_{SH} + F_{LH} + k \frac{\partial T}{\partial z} = -q \frac{dh}{dt}$$

Vertical heat transfer
(conduction, SW absorption)

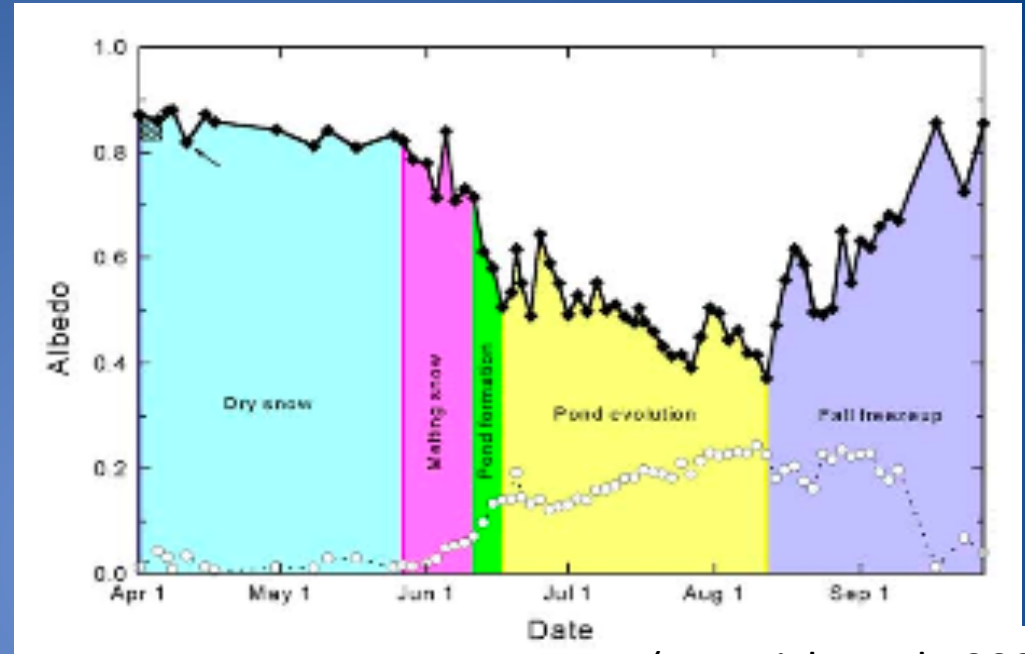
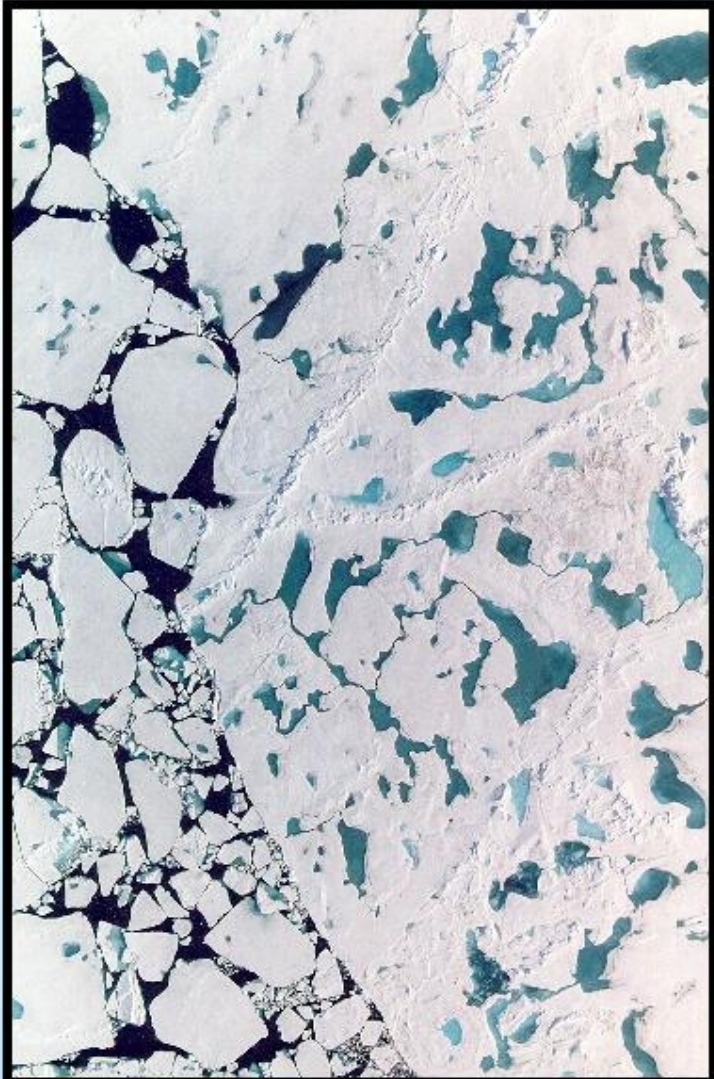
$$\rho c \frac{\partial T}{\partial t} = \frac{\partial}{\partial z} k \frac{\partial T}{\partial z} + Q_{SW}$$

Balance of fluxes at ice base

$$F_{ocn} - k \frac{\partial T}{\partial z} = -q \frac{dh}{dt}$$

Allows us to compute surface melt (snow or ice), ice basal melt and ice growth

Albedo



(Perovich et al., 2002)

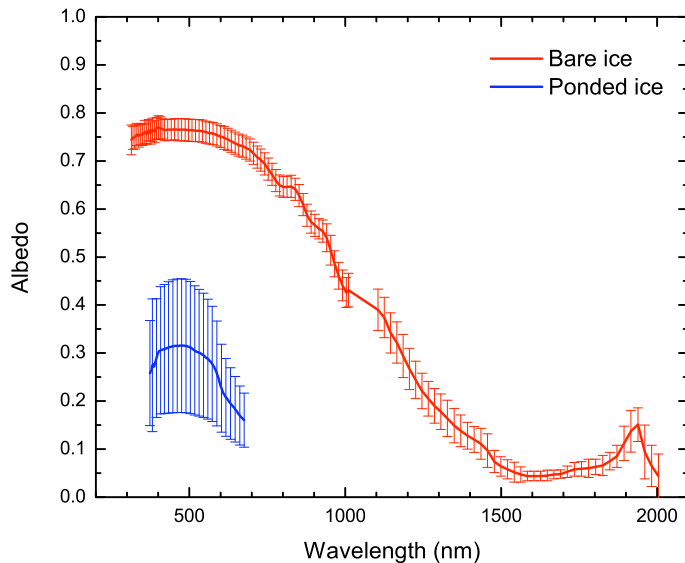
Often the parameterized sea ice albedo depends on characteristics of surface state (snow, temp, ponding, h_i).

Surface albedo accounts for fraction of gridcell covered by ice vs open ocean

February 2007

A Delta-Eddington Multiple Scattering Parameterization for Solar Radiation in the Sea Ice Component of the Community Climate System Model

B. P. Briegleb and B. Light



CLIMATE AND GLOBAL DYNAMICS DIVISION

NATIONAL CENTER FOR ATMOSPHERIC RESEARCH
BOULDER, COLORADO

New Solar Radiation parameterization

Better physics:

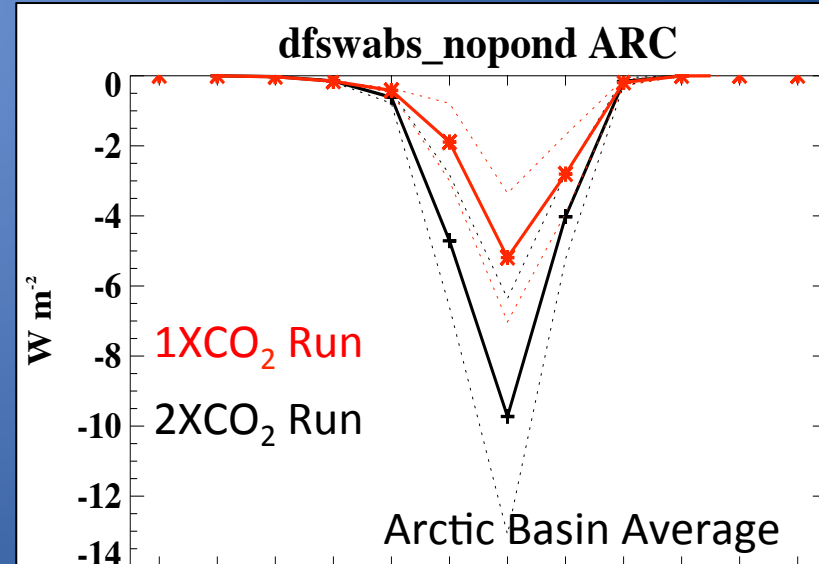
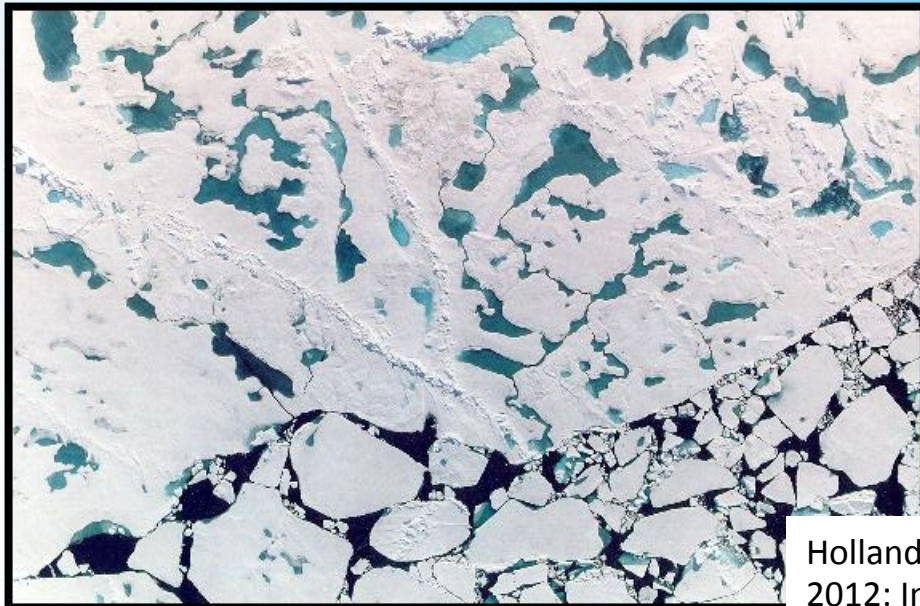
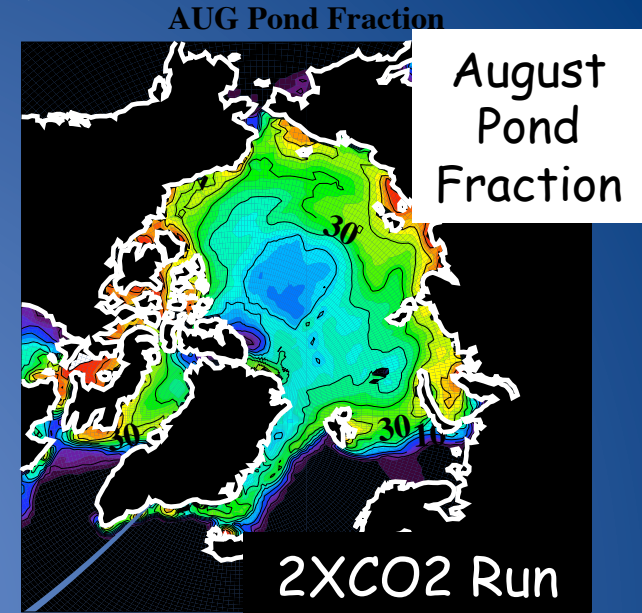
- makes use of inherent optical properties to define scattering and absorption of snow, sea ice and included absorbers

More flexible

- Explicitly allows for included absorbers in sea ice

Melt Pond Parameterization

- New radiative transfer allows (requires) a pond parameterization
- Only influences radiation
- Pond volume depends on surface meltwater, assuming a runoff fraction

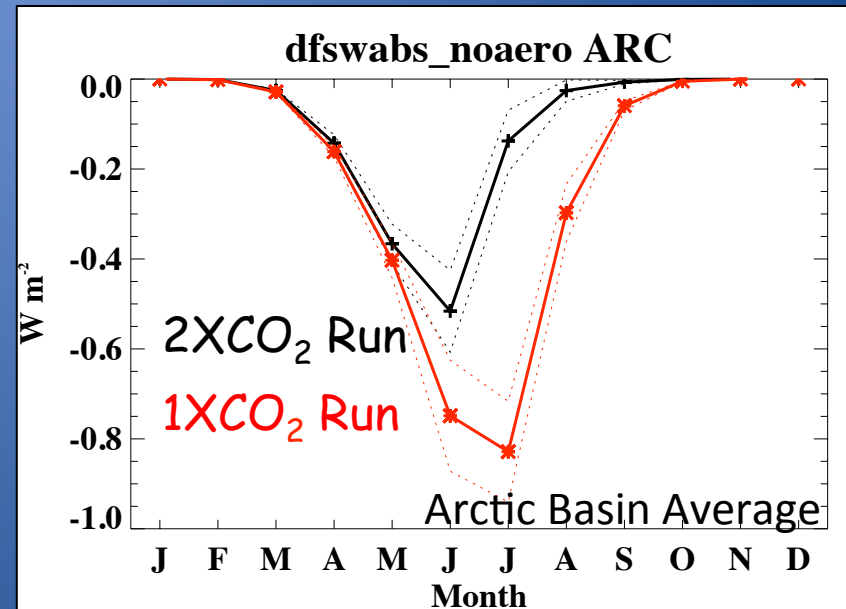
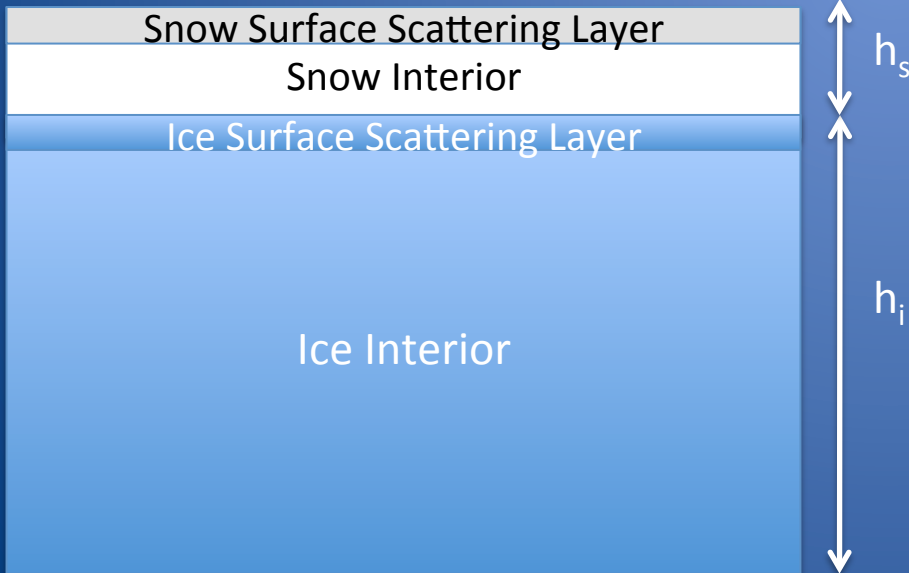
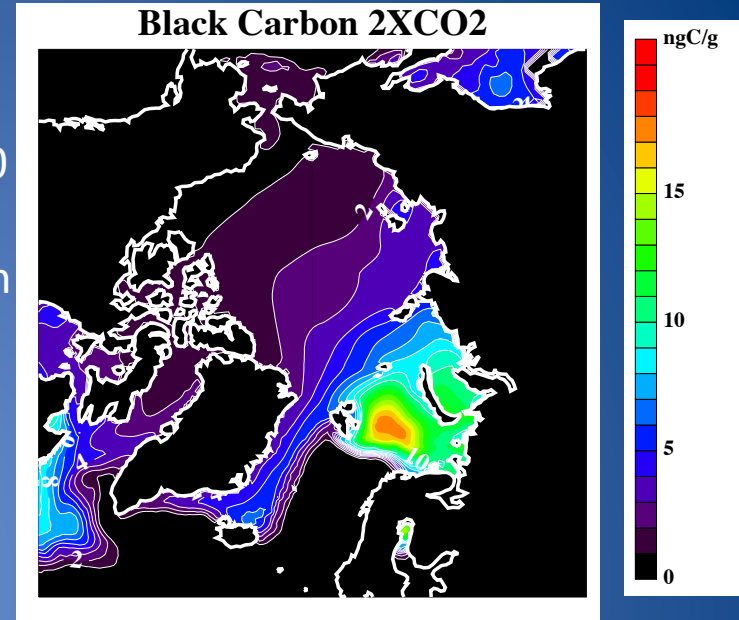


Holland, M. M., D. A. Bailey, B. P. Briegleb, B. Light, and E. C. Hunke, 2012: Improved sea ice shortwave radiation physics in CCSM4: The impact of melt ponds and black carbon. *J. Climate*, 25, 1413-1430.

Aerosol deposition and cycling

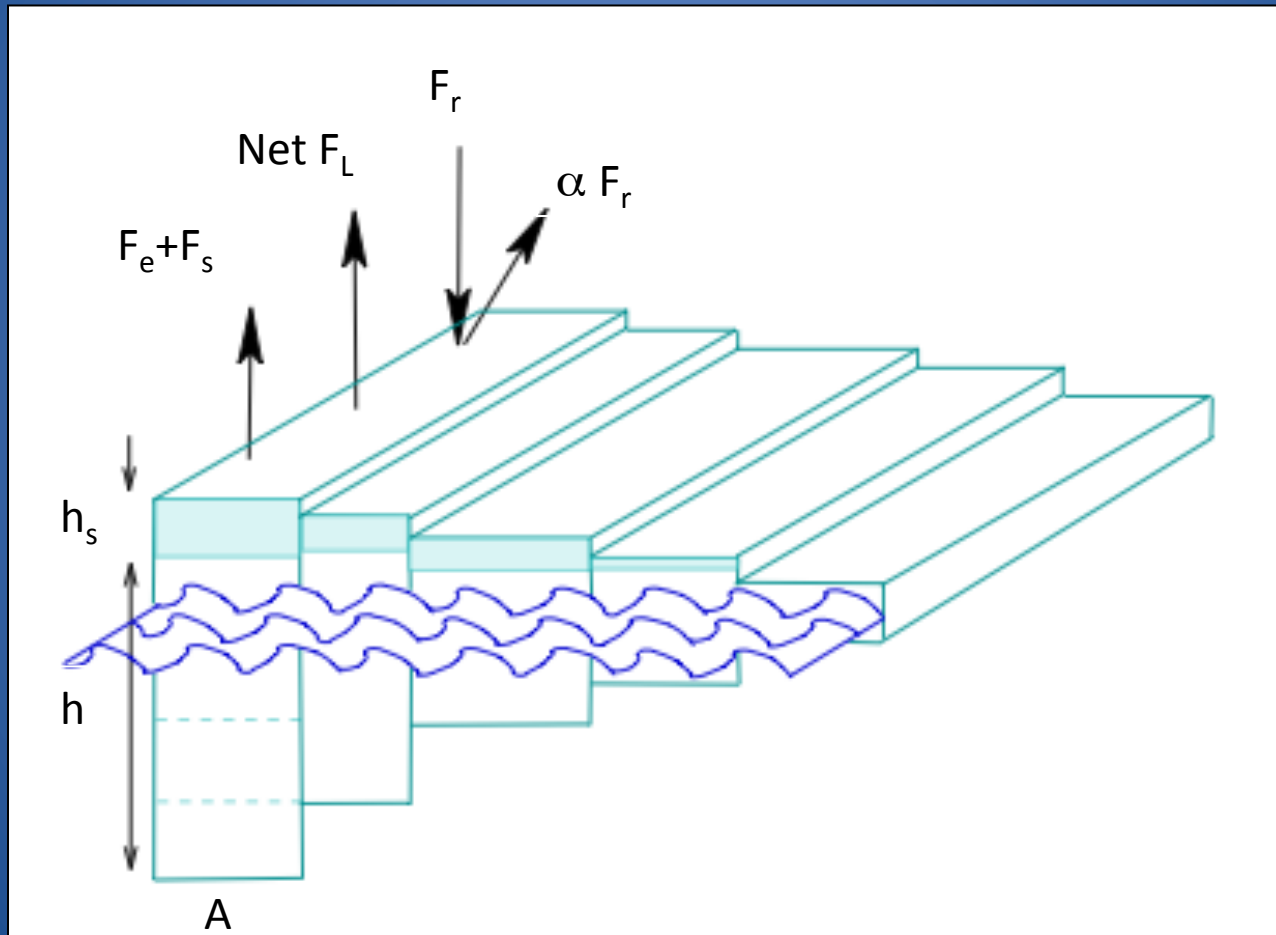
- Aerosol deposition and cycling now included.
- Account for black carbon and dust aerosols
- These are deposited from the atmosphere and modified by melt and transport

With 1850
Aerosol
Deposition



Ice Thickness Distribution

To represent high spatial heterogeneity of sea ice
Schematic of model representation with five ice "categories"



A =fractional coverage of a category

Ice Thickness Distribution

Ice thickness distribution $g(x,y,h,t)$ evolution equation from Thorndike et al. (1975)

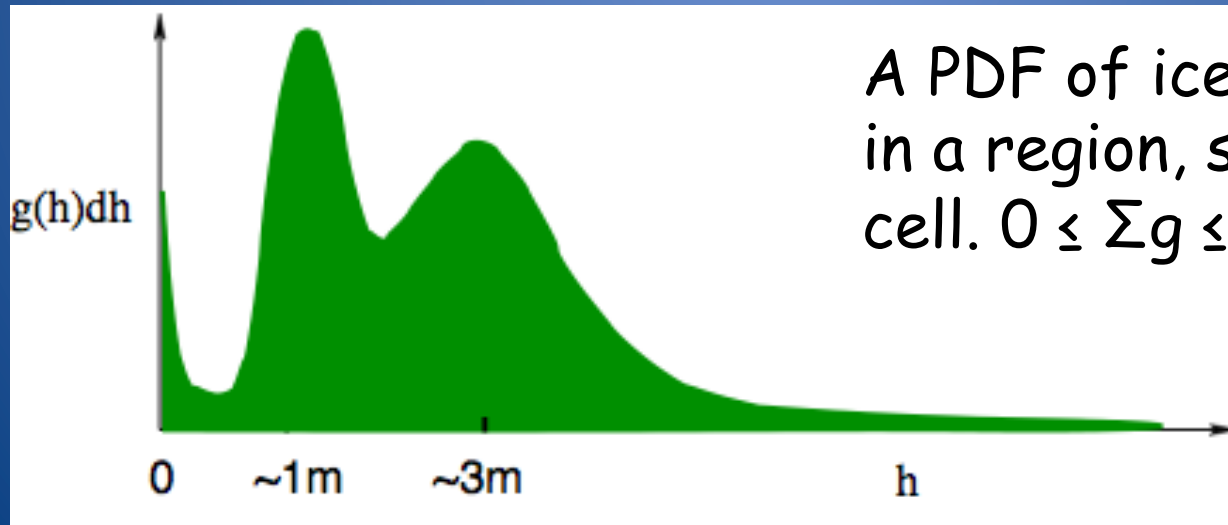
$$\frac{\partial g}{\partial t} = -\frac{\partial}{\partial h}(fg) + L(g) - \nabla \cdot (\vec{v}g) + \Psi(h,g,\vec{v})$$

↑
Ice Growth

↑
Lateral Melt

↑
Convergence

↑
Mechanical
Redistribution



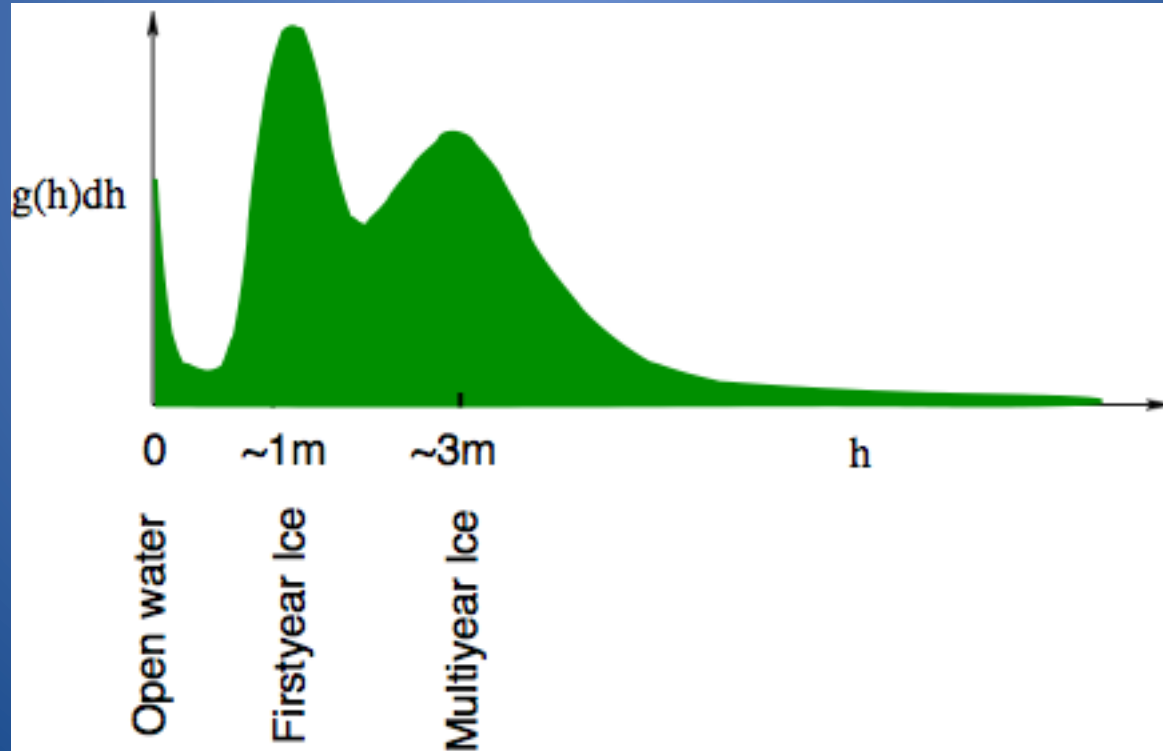
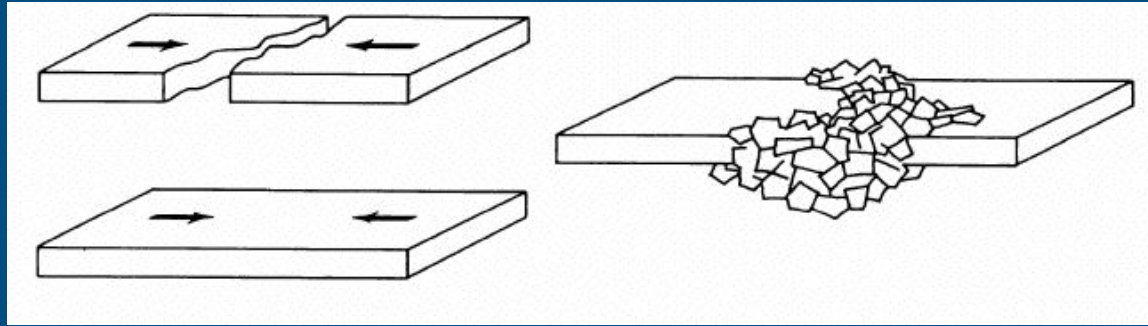
A PDF of ice thickness h in a region, such as a grid cell. $0 \leq \Sigma g \leq 1$

$g(h)dh$ is the fractional area covered by ice of thickness h to $h+dh$

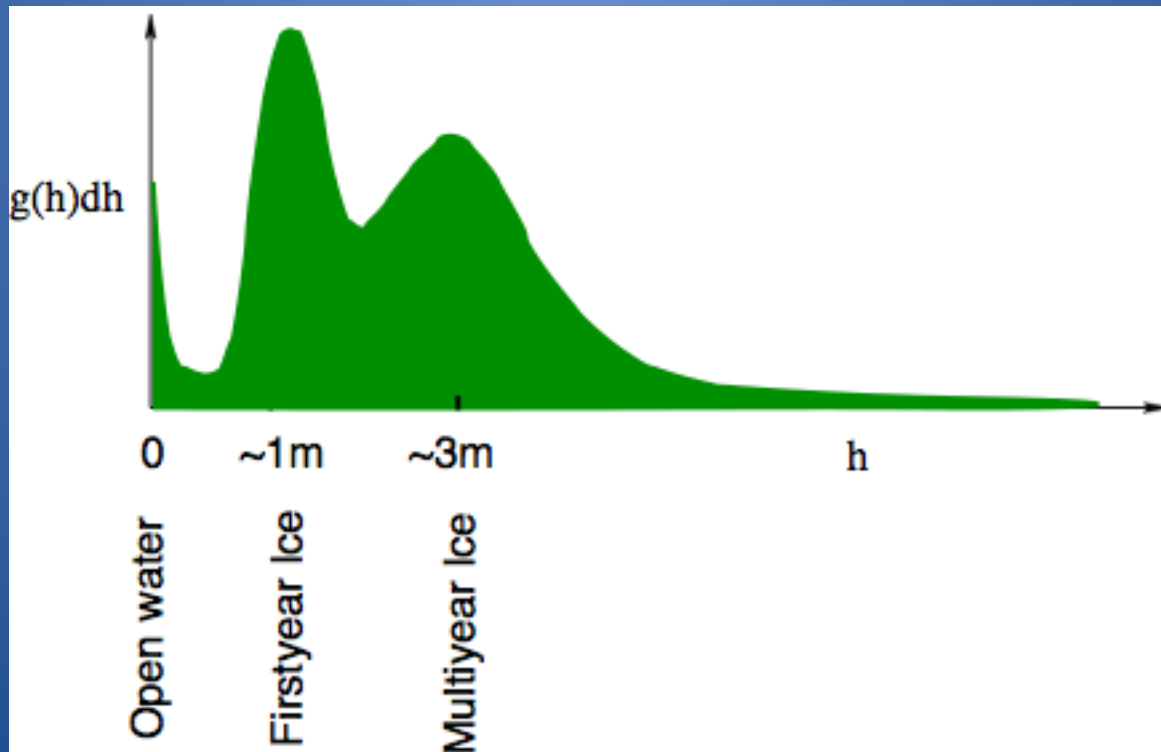
Ψ = Mechanical redistribution

Transfers ice from thin part of distribution to thicker categories

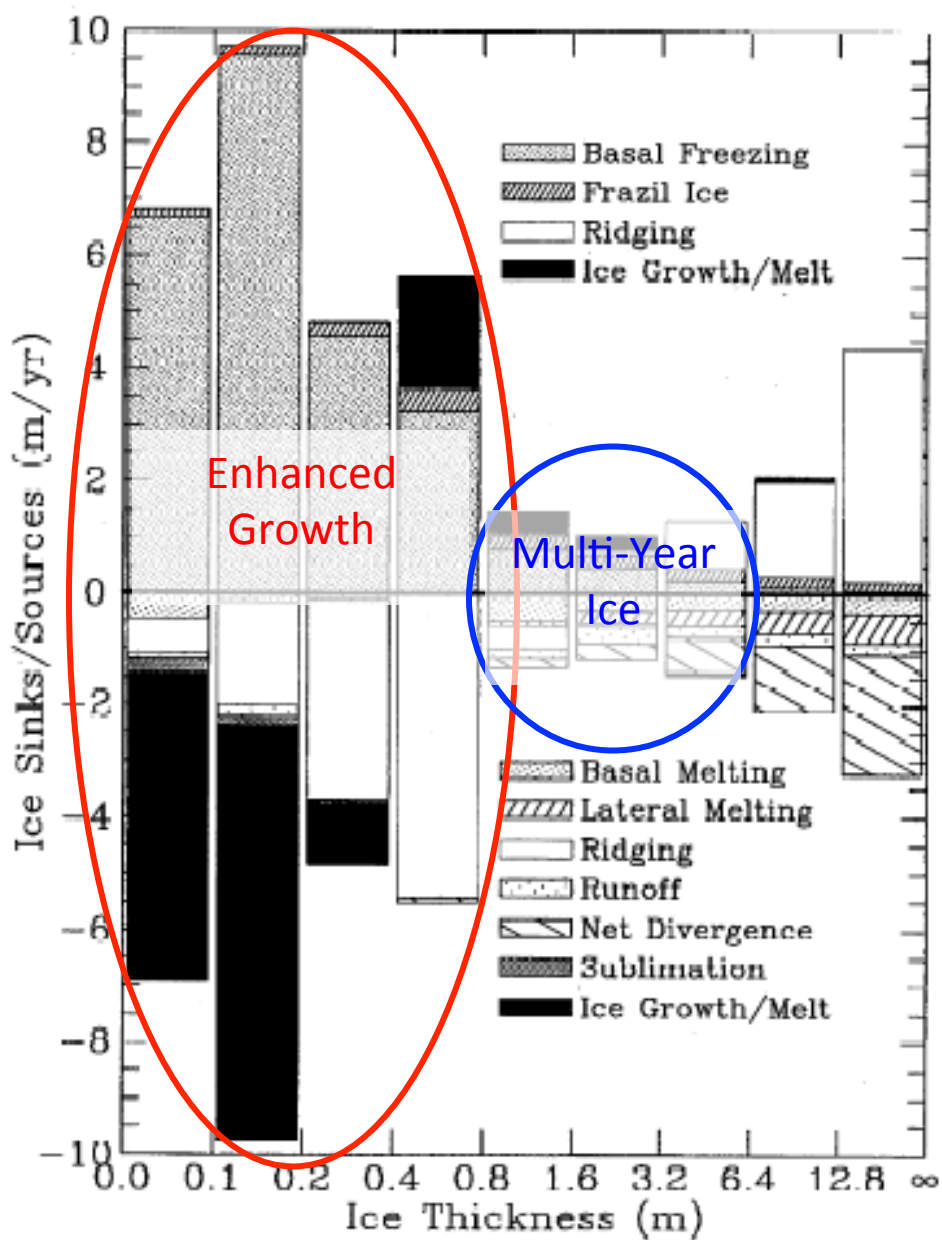
Converging hypothetical floes



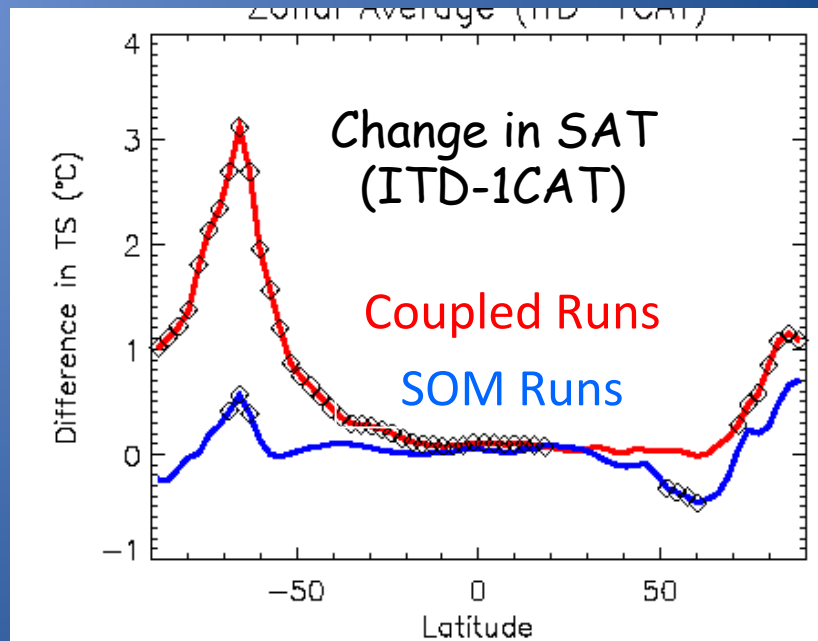
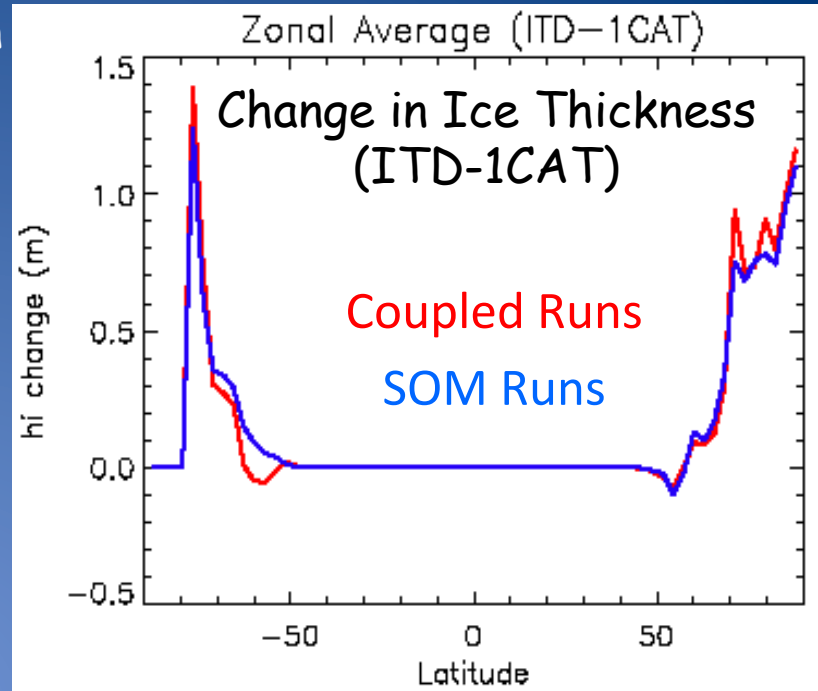
Ice growth:



Influence of including an Ice Thickness Distribution



Schramm et al., 1997



(Holland et al., 2006)

State variables for each category:

A , V_i , V_s , $E_i(z)$, $E_s(z)$, T_{surf} , melt pond state, aerosol contents (z), etc.

A = category area per unit gridcell area (or fractional coverage)

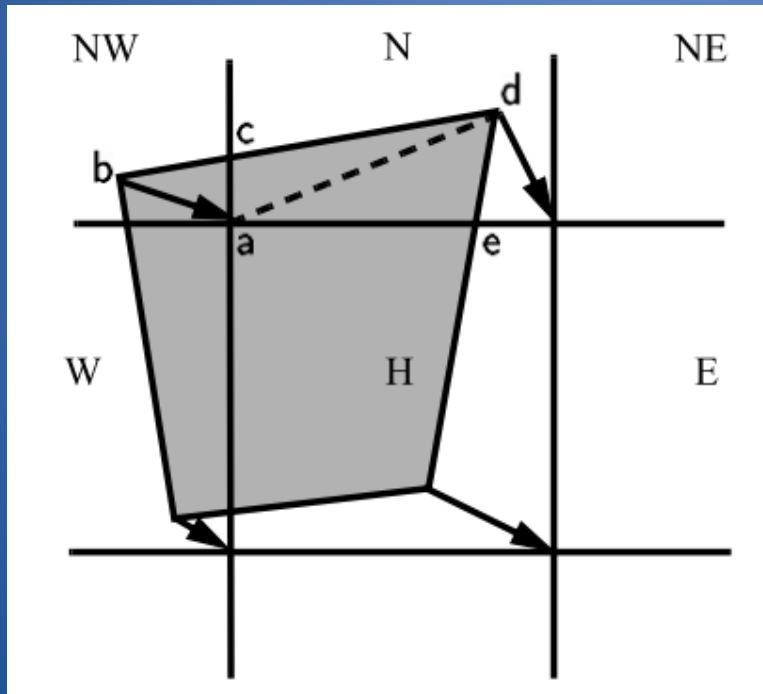
$V = hA$ is the category volume per unit gridcell area

$E = Vq$ is the category enthalpy per unit gridcell area

V and E are preferred as state variables because they are conserved quantities (rather than T).

Advection

Would make so many state variables prohibitive, if it weren't for remapping by Lipscomb and Hunke 2004.

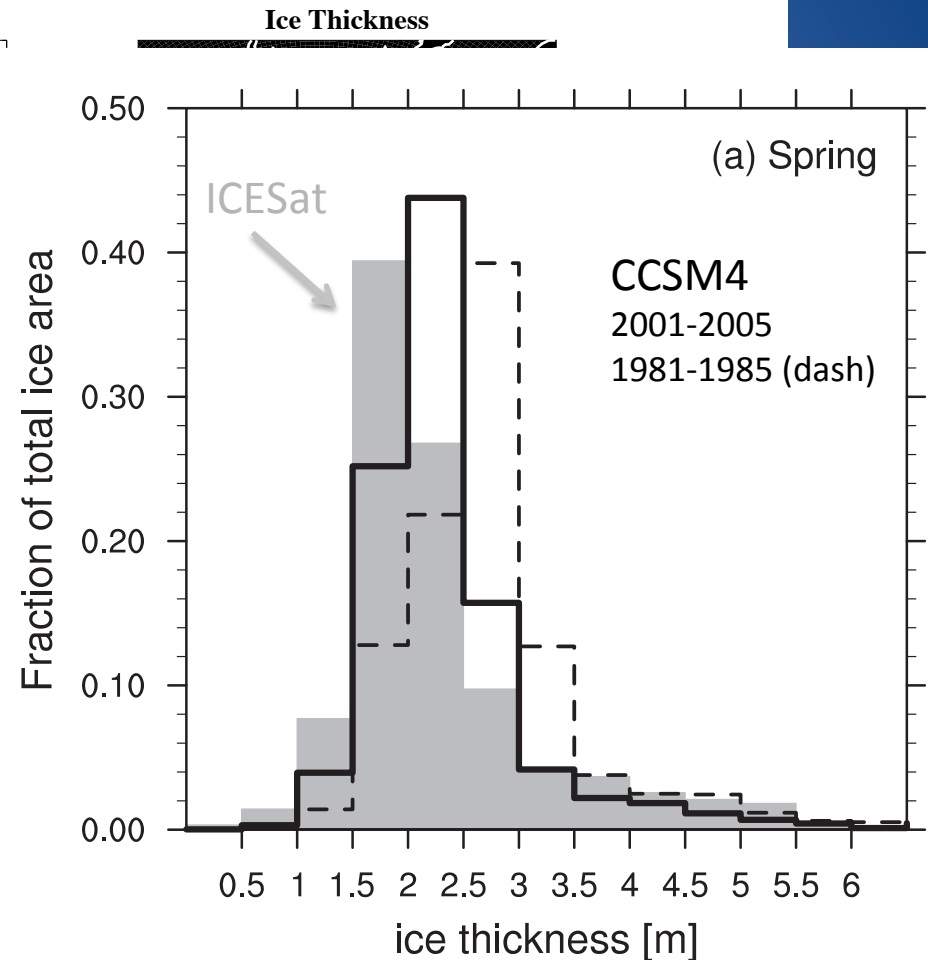
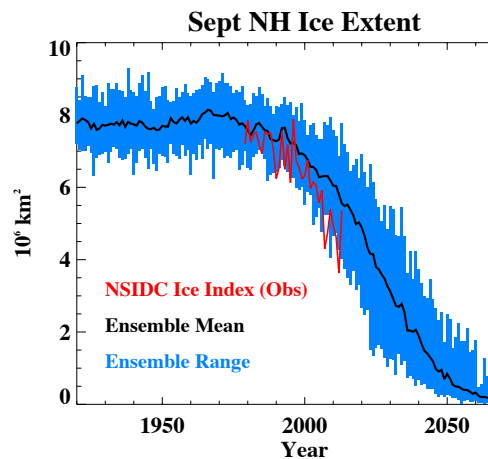
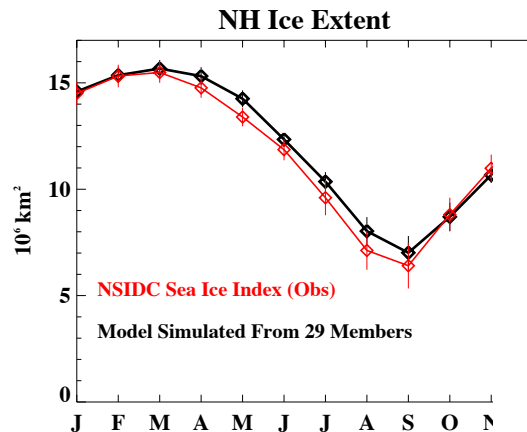


Conserved quantities are remapped from the shaded "departure region", which is computed from backward trajectories of the ice motion field.

Science Highlights

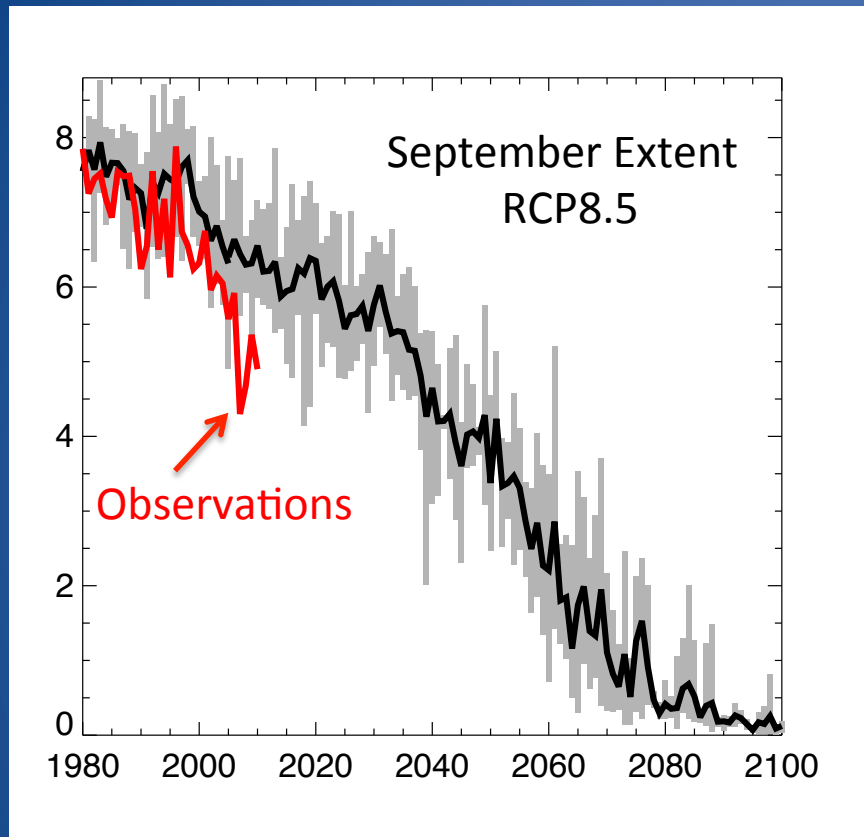
- How well does the model actually simulate the sea ice cover?
- What does the model say about the future of sea ice?
- Northern versus Southern Hemisphere?

CCSM4/CESM1 Simulation of Arctic sea ice cover

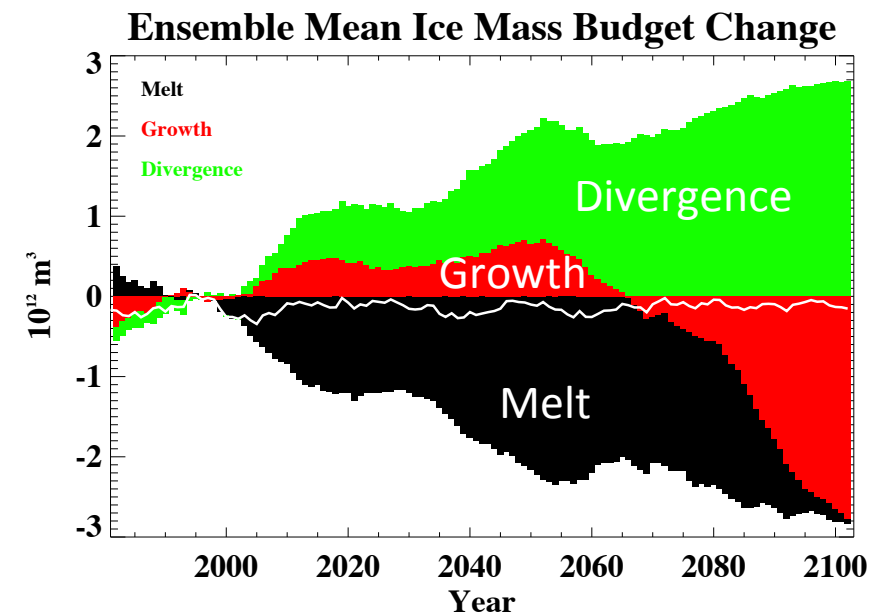
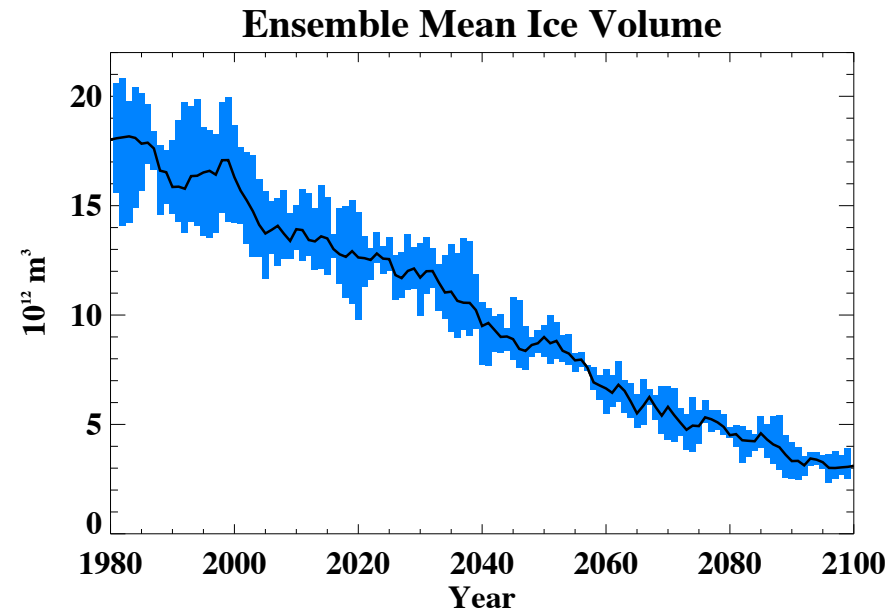


Jahn, A and Coauthors, 2012: Late-Twentieth-Century Simulation of Arctic Sea Ice and Ocean Properties in the CCSM4. *J. Climate*, 25, 1431–1452.

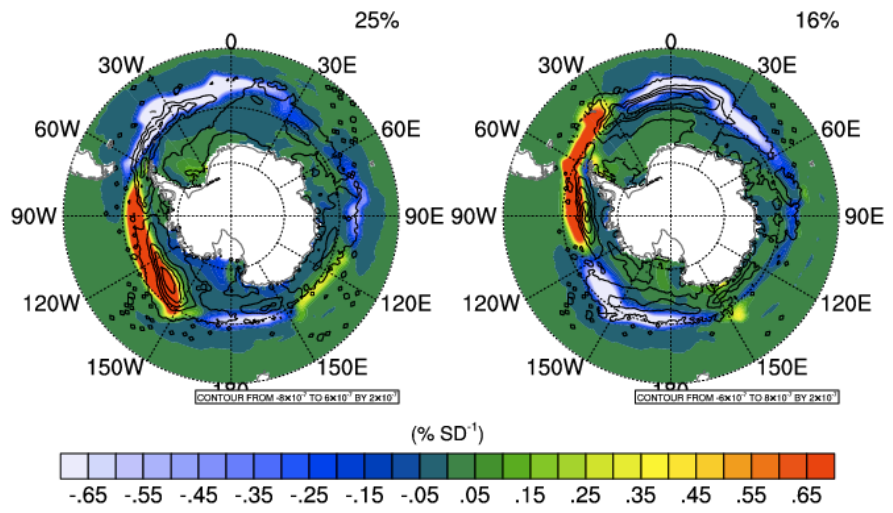
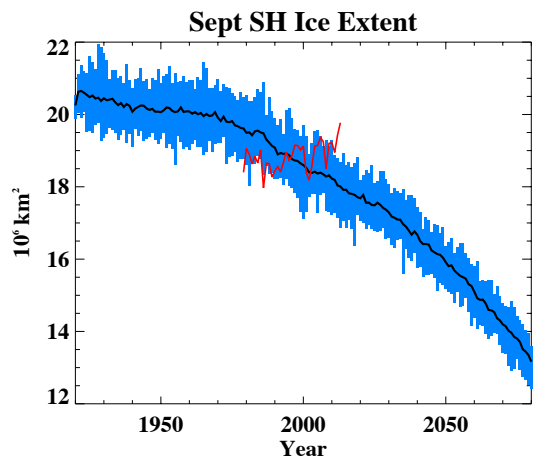
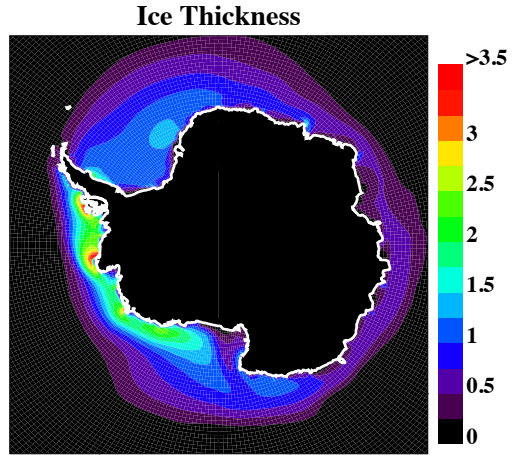
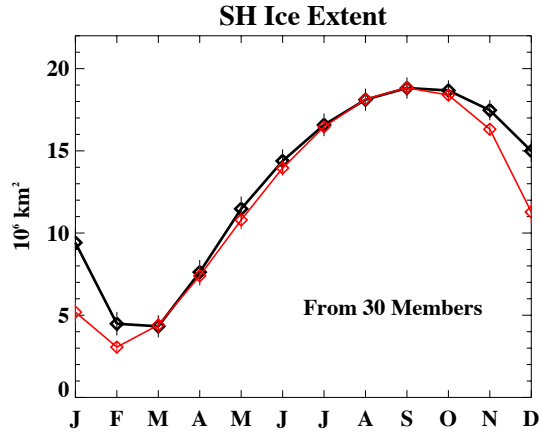
CCSM4 21st Arctic Ice Loss



Vavrus, SJ, MM Holland, A Jahn, DA Bailey, BA Blazey, 2012: Twenty-First-Century Arctic Climate Change in CCSM4. J. Climate, 25, 2696–2710.



CCSM4/CESM1 Simulation of Antarctic sea ice



Summary

- CESM1 uses the Los Alamos CICE model
- This includes:
 - EVP dynamics,
 - thermodynamics that account for brine inclusions,
 - and a subgridscale ice thickness distribution.
- CCSM4 and CESM1 simulate very good Arctic sea ice overall.
- CCSM4 Antarctic sea ice is too extensive but variability in ice concentration looks realistic. CESM1 Antarctic sea ice is greatly improved.

Where are we heading?

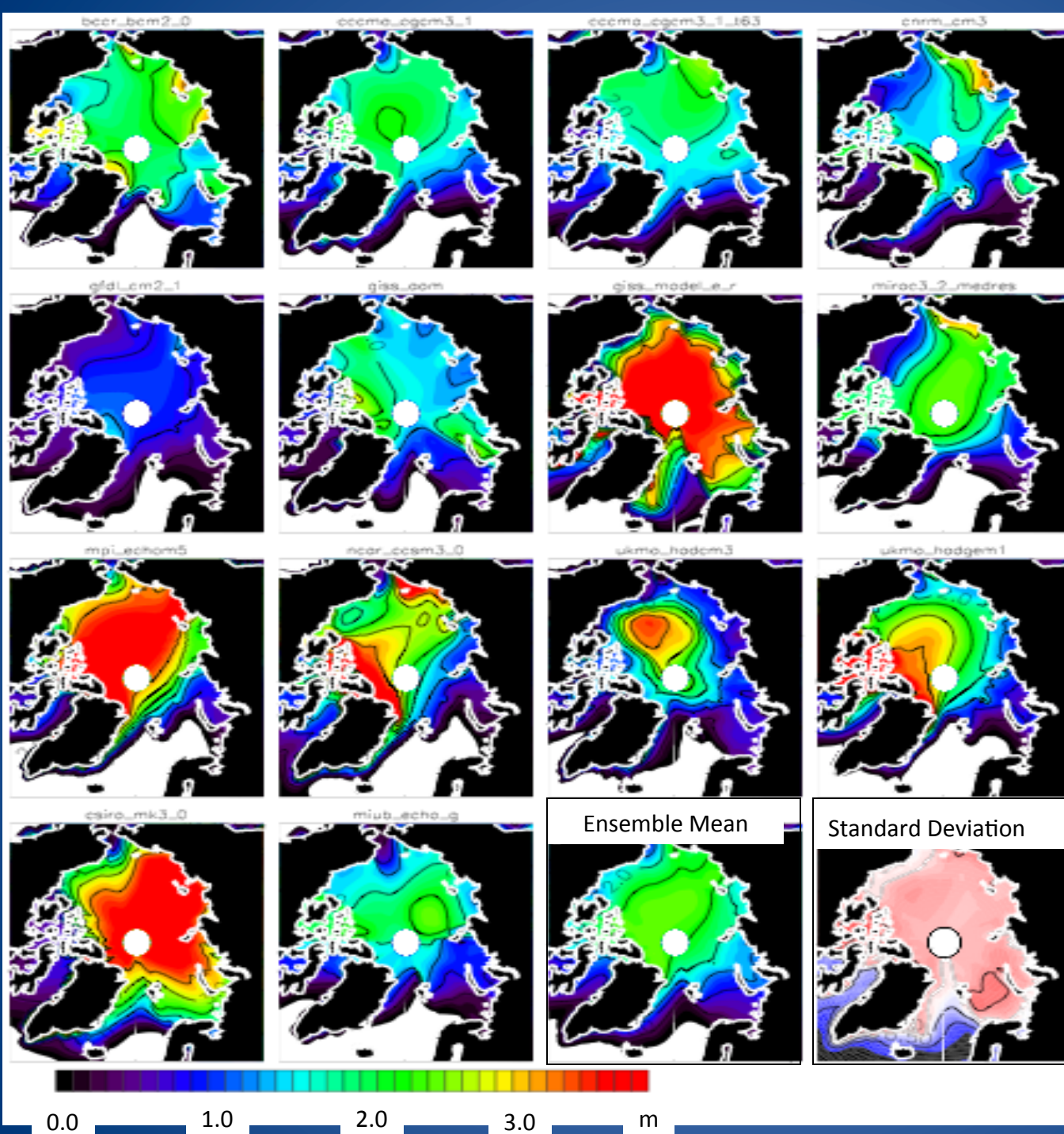
- Prognostic salinity
- Biogeochemistry (Iron, Isotopes, Algae)
- More sophisticated melt pond modeling
- Snow model improvements
- Improved ice-ocean coupling

Much of this work is being done by collaborators at DOE Labs (primarily LANL) and Universities.

Questions?



Simulated Ice Thickness Climatology 1980-1999



Thickness
varies
considerably
across models

Differences in
mean and
distribution

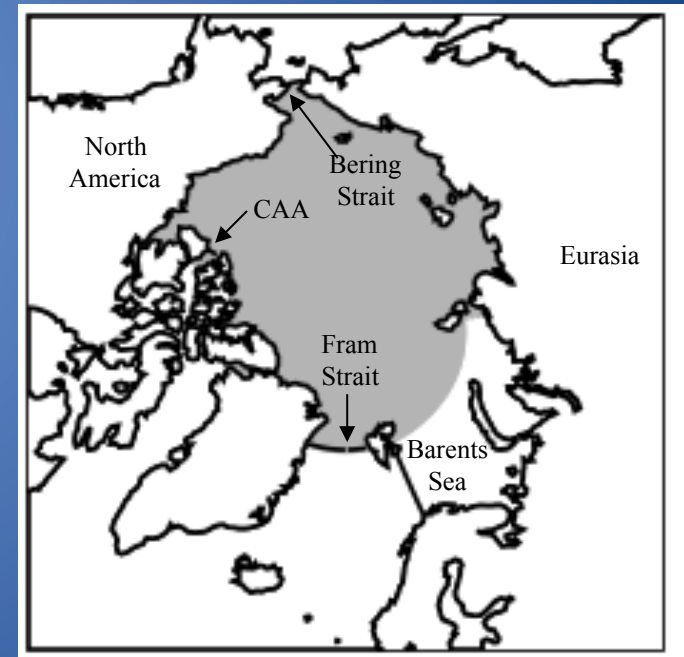
Largest inter-
model scatter
is in the
Barents Sea
region

Assessing Sea Ice Mass Budgets

- Equilibrium Ice Thickness Reached when
 - Ice growth is balanced by ice melt + ice divergence
 - Illustrative to consider how different models achieve this balance and how mass budgets change over time

$$\frac{d\bar{h}}{dt} = \Gamma_h - \nabla \cdot (\vec{u}h)$$

Ice volume change Thermodynamic source Divergence

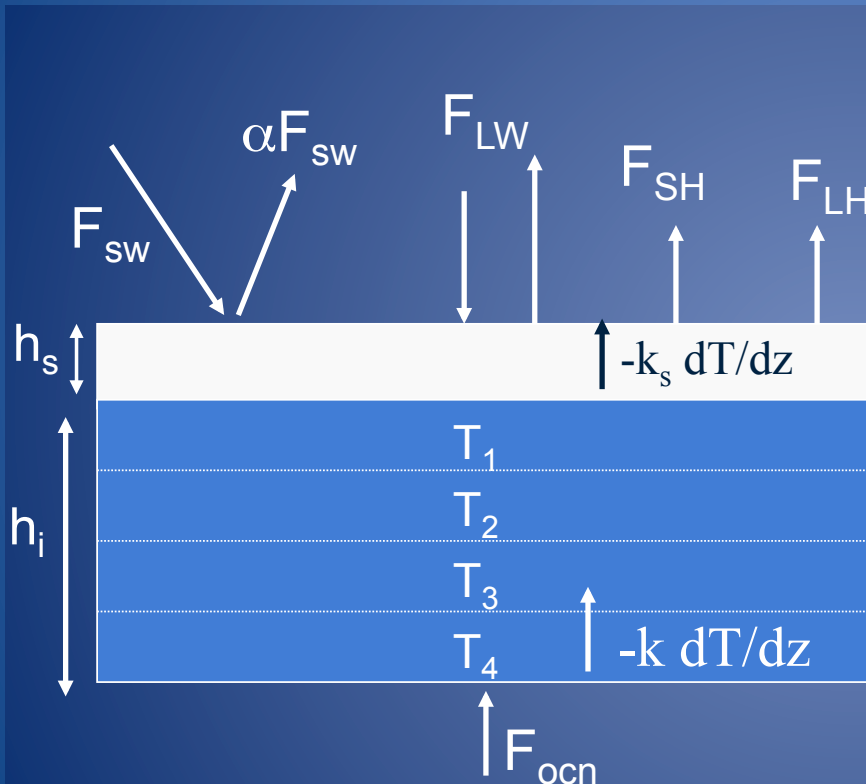


Climate model archive of monthly averaged ice thickness and velocity

Assess Arctic ice volume, transport through Arctic straits, and solve for ice growth/melt as residual

Sea ice loss is modified by climate feedbacks

- Fundamental sea ice thermodynamics gives rise to a number of important feedbacks



Balance of fluxes at surface

$$(1 - \alpha)F_{sw} + F_{LW} - \sigma T^4 + F_{SH} + F_{LH} + k \frac{\partial T}{\partial z} = -q \frac{dh}{dt}$$

Vertical heat transfer
(conduction, SW absorption)

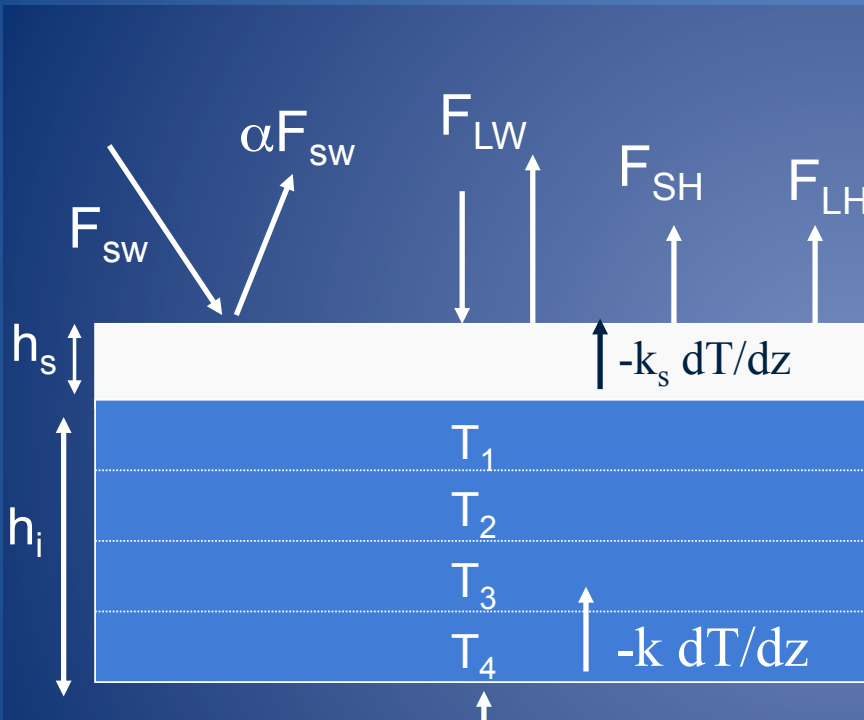
Balance of fluxes at ice base

$$F_{ocn} - k \frac{\partial T}{\partial z} = -q \frac{dh}{dt}$$

Surface albedo changes modify SW absorption in ice and ocean heat flux
Ice loss lowers albedo - positive feedback

Ice mass budgets affected by climate feedbacks

- Fundamental sea ice thermodynamics gives rise to a number of important feedbacks



Balance of fluxes at surface

$$(1 - \alpha)F_{sw} + F_{LW} - \sigma T^4 + F_{SH} + F_{LH} + k \frac{\partial T}{\partial z} = -q \frac{dh}{dt}$$

Vertical heat transfer (conduction, SW absorption)

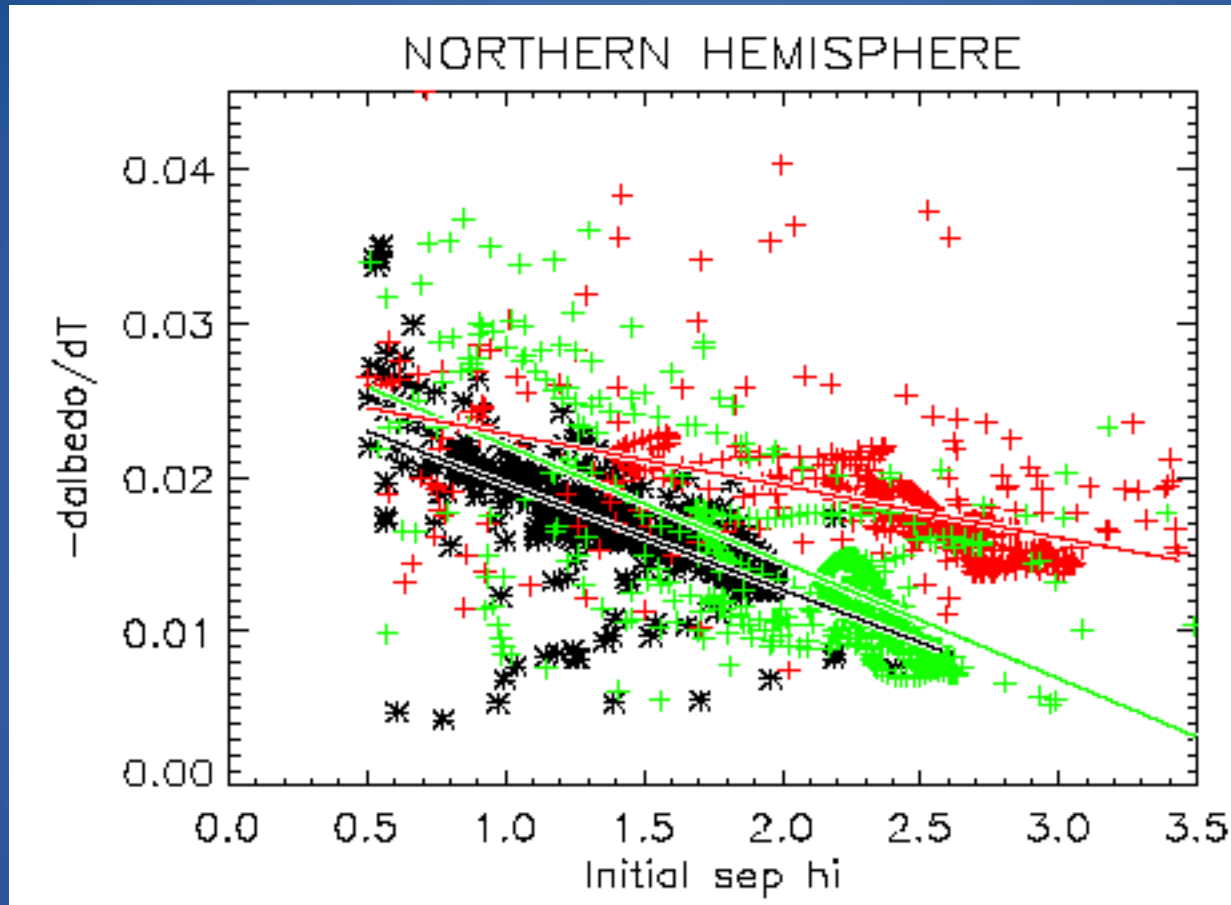
Balance of fluxes at ice base

$$F_{ocn} - k \frac{\partial T}{\partial z} = -q \frac{dh}{dt}$$

Heat conduction related to vertical temperature gradient
 Causes ice growth to vary as $1/h$
 Has a stabilizing effect on ice thickness since thin ice grows more rapidly

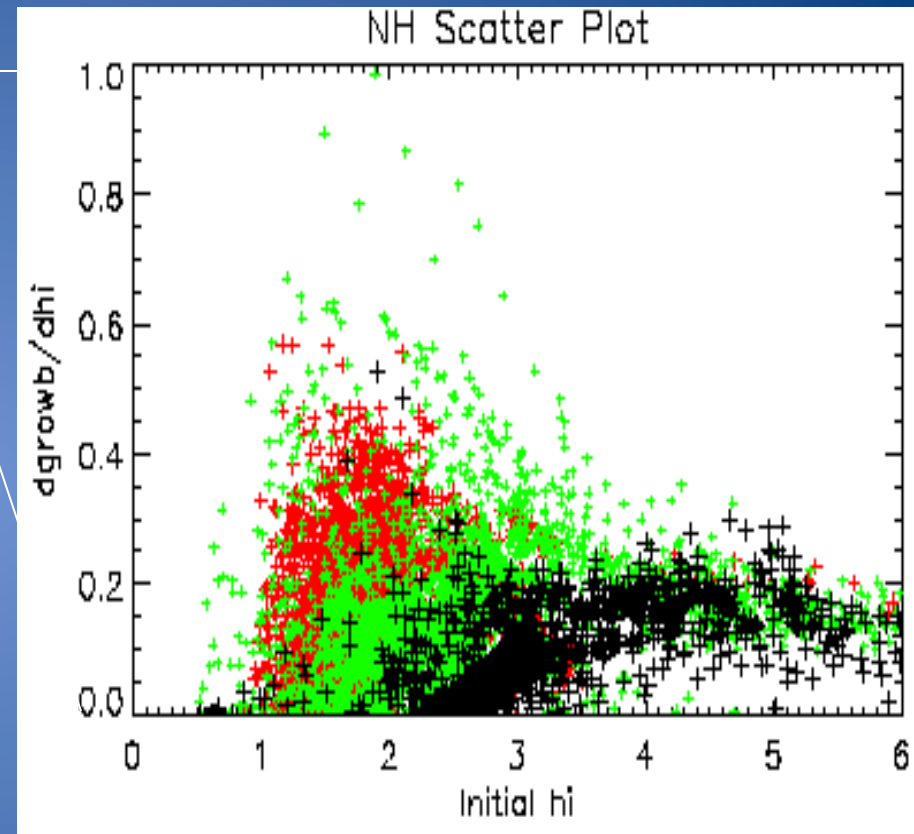
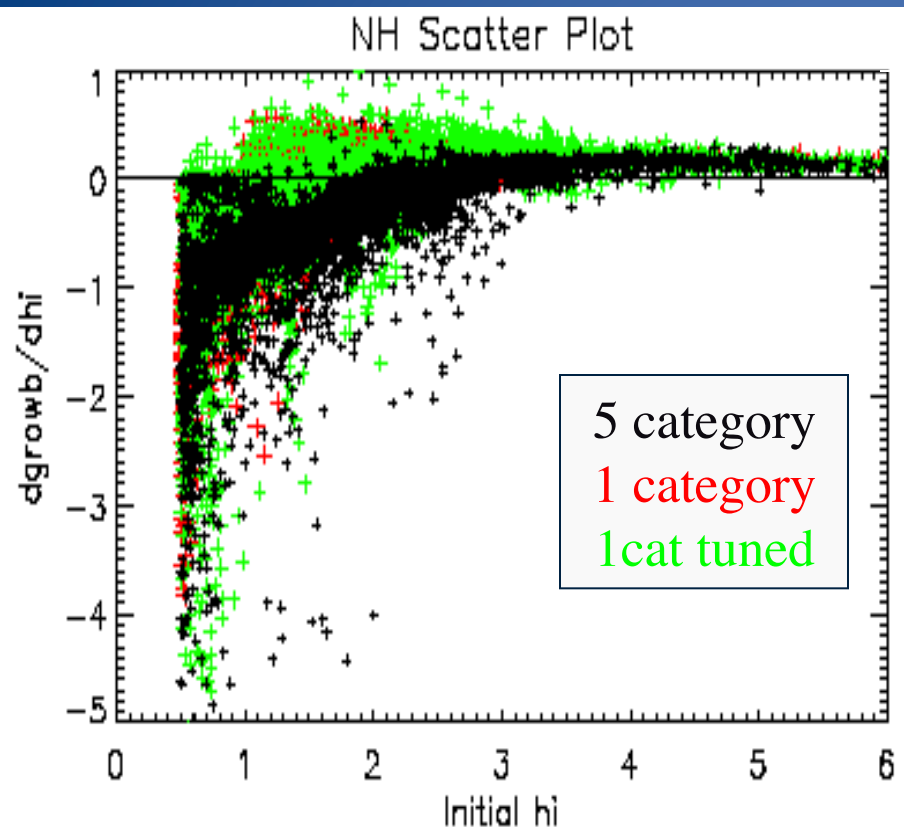
Evidence that model parameterizations influence feedback strength

Enhanced albedo feedback in ITD run



Larger albedo change per temperature change for thinner initial ice
With ITD have larger a change for ice with same initial thickness
Suggests surface albedo feedback enhanced in ITD run

Model parameterizations modify ice growth rate feedback



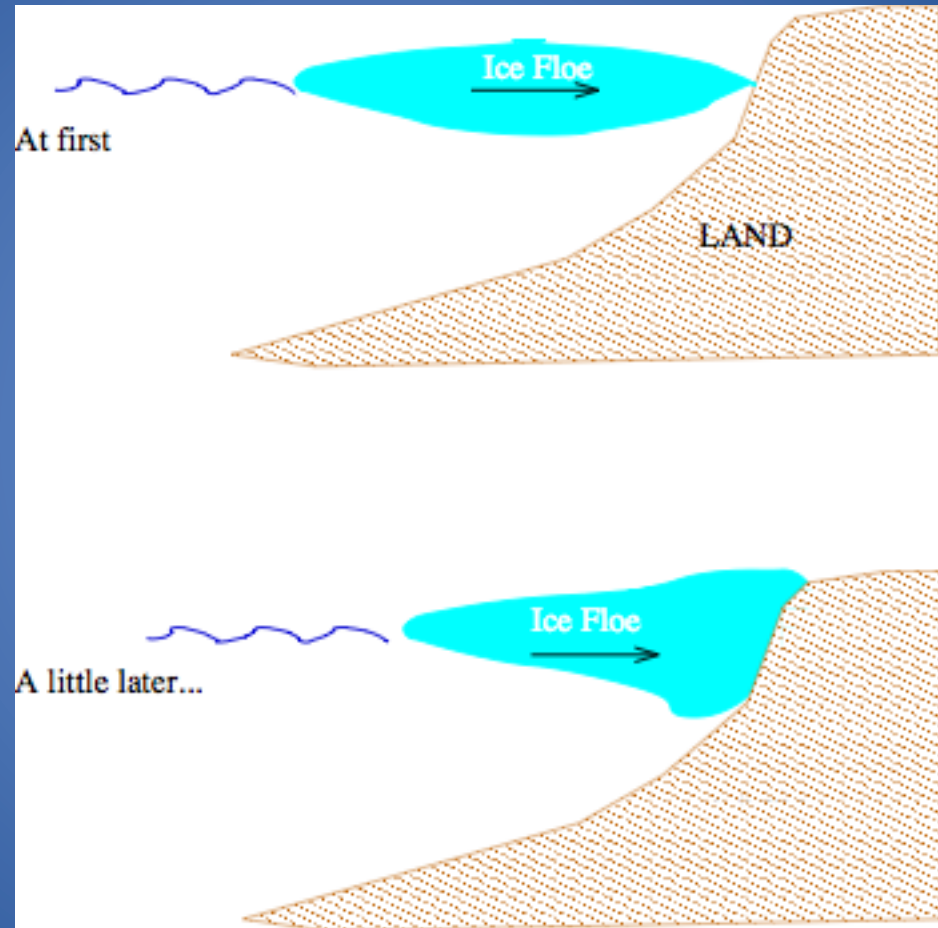
For ice of the same mean thickness,

- The ITD has fewer locations with increased ice growth.
- This suggests a reduced negative feedback on ice thickness

Challenges in Modeling Sea Ice in a Changing Environment

- So, is it all hopeless?
- Recent studies providing insight on what is needed if we are to accurately simulate sea ice change:
 - present day ice conditions, including extent and the spatial distribution of ice thickness;
 - the evolving surface energy budget
- To achieve this involves numerous and interacting factors across the coupled ice-ocean-atmosphere system
- Models are continuously improving and have provided considerable insight into the functioning of sea ice and its role in the climate system

Sea Ice Dynamics in climate models



Past ad hoc method was to stop ice from moving at a critical thickness, sometimes called stoppage.

$$\frac{Dg}{Dt} = -g \nabla \cdot \mathbf{u} + \Psi - \frac{\partial}{\partial h} (fg) + \mathcal{L}$$

1
2
3
4
5

1. Lagrangian time derivative of g following “parcel”
2. Convergence of parcel
3. Ψ = Mechanical redistribution
4. Ice growth/melt results in “advection of g in thickness space”
5. \mathcal{L} = Reduction of g from lateral melt

h = ice thickness

\mathbf{u} = ice velocity

f = growth rate

Heat Equation used to find temperature T

$$\rho c \frac{\partial T}{\partial t} = \frac{\partial}{\partial z} k \frac{\partial T}{\partial z} + \kappa I_0 e^{-\kappa z},$$

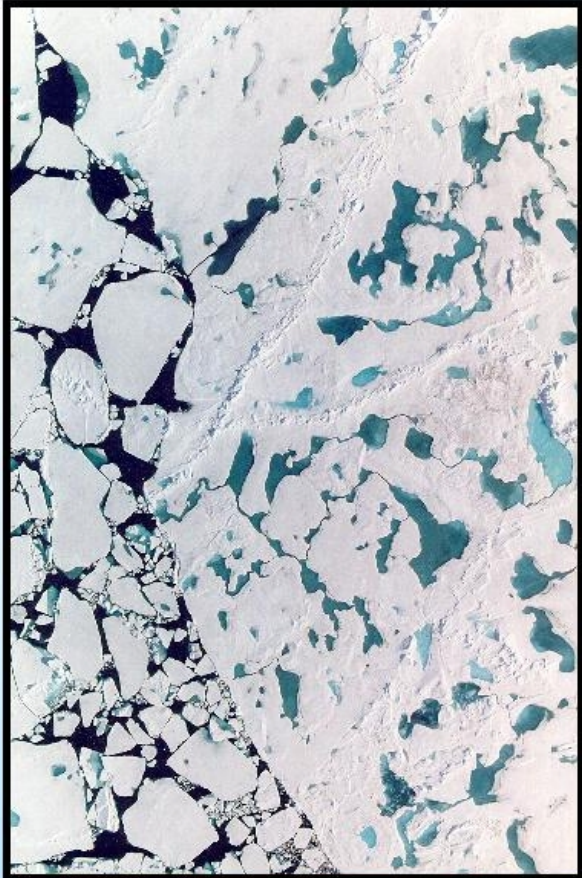
Untersteiner (1961) suggested the heat capacity of sea ice is

$$c(T, S) = c_0 + \frac{\gamma S}{T^2}$$

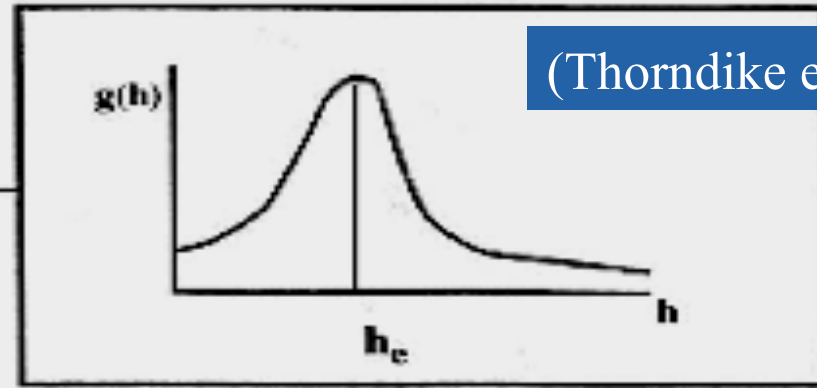
where T is in Celsius,

$$\gamma = L_0 \mu \quad \text{and} \quad T_m = -\mu S$$

Ice Thickness Distribution

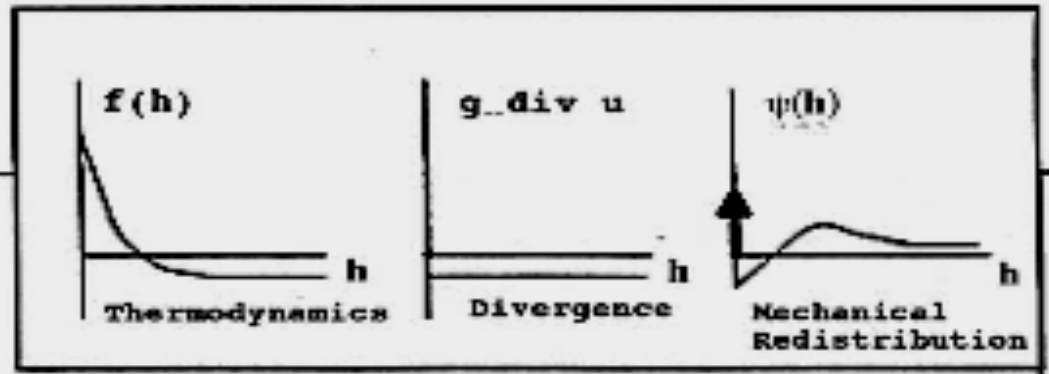


Sea ice thickness distribution



(Thorndike et al., 1975)

Processes that alter the thickness distribution



$$\frac{Dg}{Dt} = -\frac{\partial}{\partial h}(fg) + L(g) - \nabla \cdot (\vec{v}g) + \Psi(h, g, \vec{v})$$

Evolution depends on: Ice growth, lateral melt, ice divergence, and mechanical redistribution (riding/rafting)