

# Physics Parameterizations in Global Atmospheric Models

CESM Tutorial 2018

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# Outline

- What are “AGCM Physics”?
- Resolution, subgrid variability
- Parameterizations
- Examples
  - Mass-flux Convection scheme
  - CLUBB
  - More cloud issues
- Future directions

# Equations of Motion – explicitly resolved dynamics

Where do the “physics” appear?

$$d\bar{\mathbf{V}}/dt + f\mathbf{k} \times \bar{\mathbf{V}} + \nabla\bar{\phi} = \mathbf{F}, \quad (\text{horizontal momentum})$$

$$d\bar{T}/dt - \kappa\bar{T}\omega/p = Q/c_p, \quad (\text{thermodynamic energy})$$

$$\nabla \cdot \bar{\mathbf{V}} + \partial\bar{\omega}/\partial p = 0, \quad (\text{mass continuity})$$

$$\partial\bar{\phi}/\partial p + R\bar{T}/p = 0, \quad (\text{hydrostatic equilibrium})$$

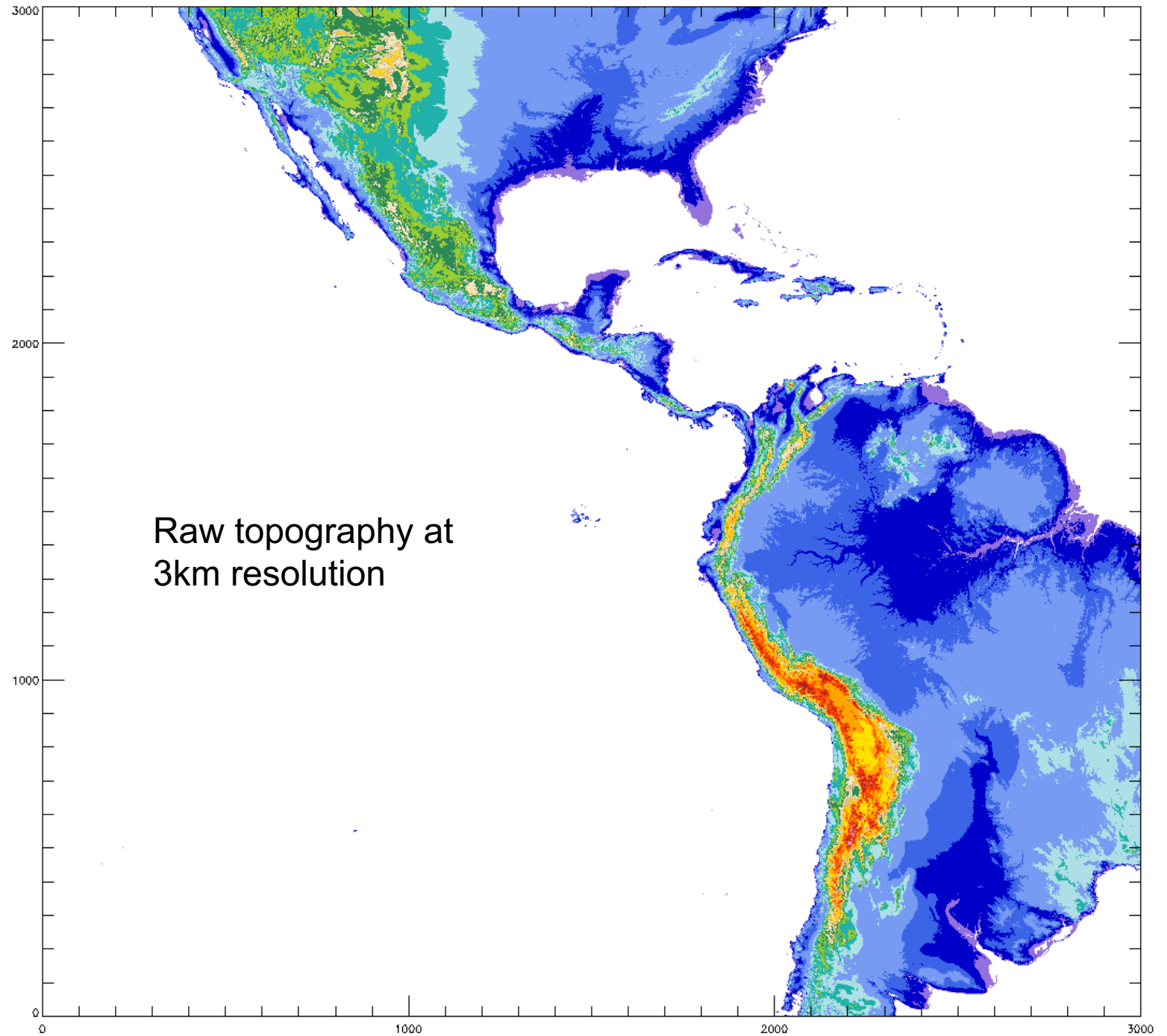
$$d\bar{q}/dt = S_q. \quad (\text{water vapor mass continuity})$$

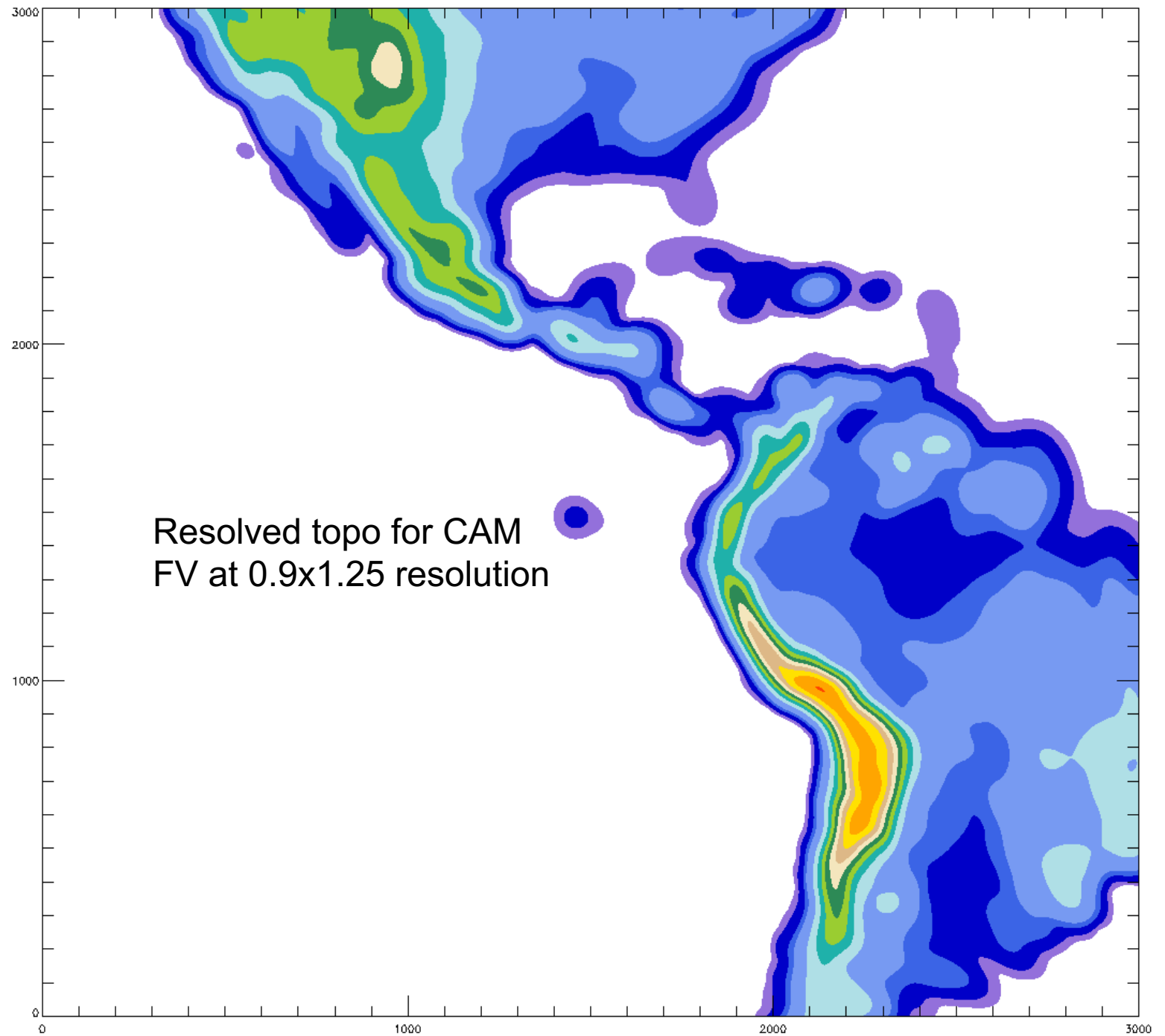
$$dq_{\{l,i,r,\dots\}}/dt =$$

$F_{QV}, F_{QL}, F_{QI} \dots?$  (water substance evolution equations, chemistry ...)

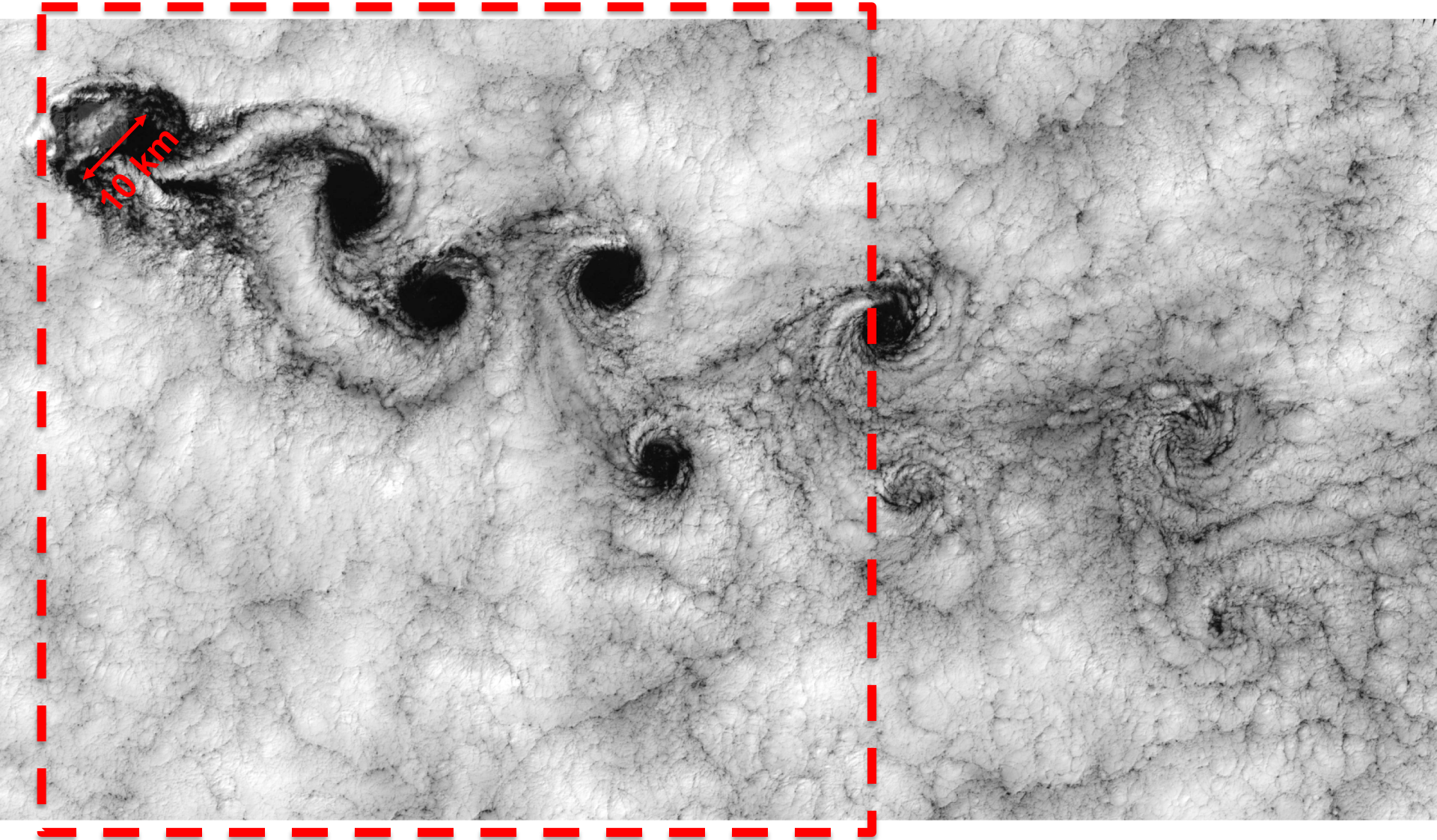
What are the “physics” trying to represent?

Unresolved motions, sub-grid  
variability, ... Photons ...





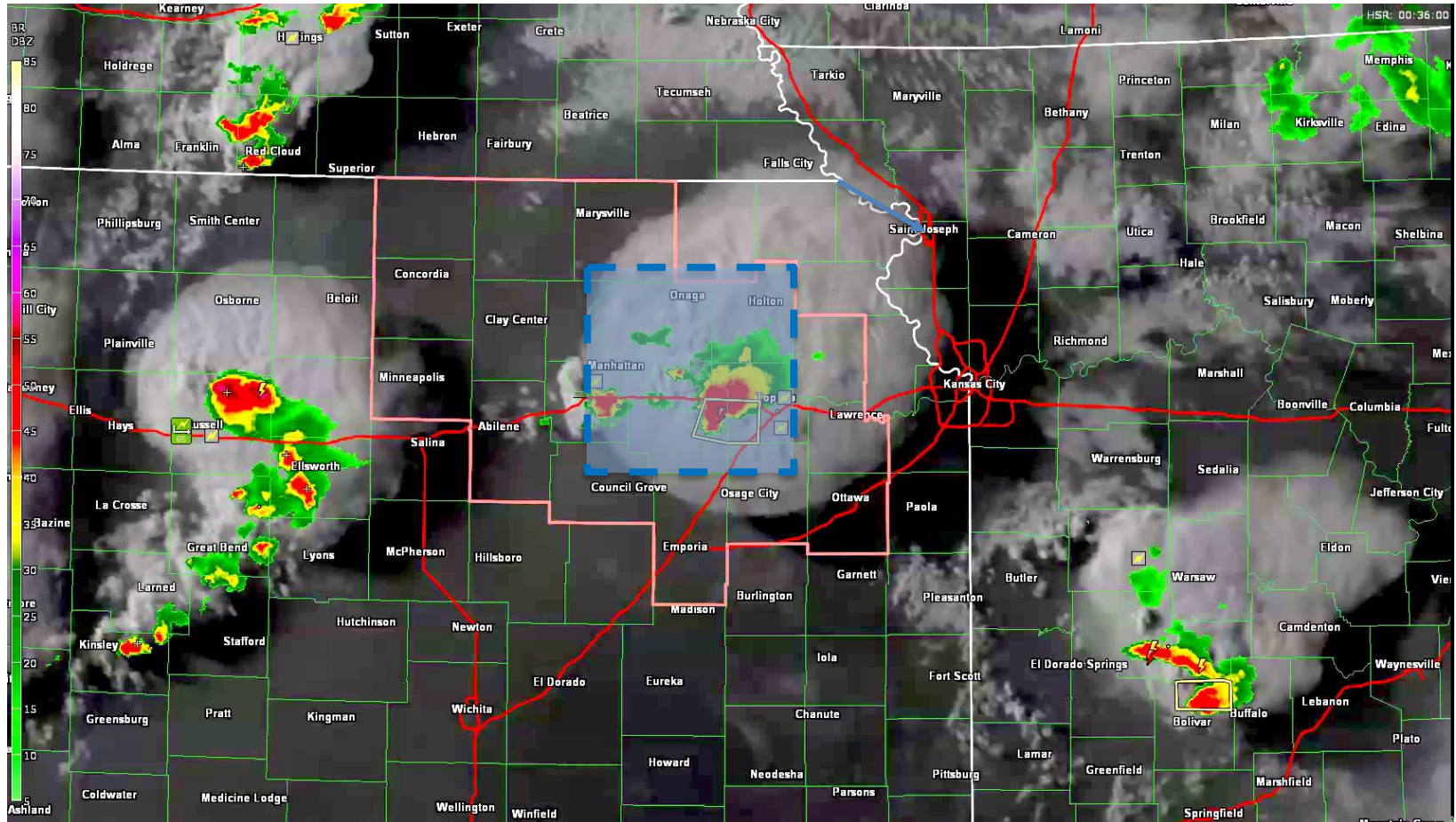
# Boundary layer clouds



Alejandro Selkirk Island (33S 80W)



# Deep Convection



July 15, 2015

OK, so atmospheric models with  
large grid boxes miss a lot of  
interesting stuff

....

So What??

# Nonlinearity

5 Values of “x” = 1,1,1,2,10

$$M(p) = \left[ \frac{1}{5} \sum x^p \right]^{\frac{1}{p}}$$

p=1

$$M(p) = 3.00000$$

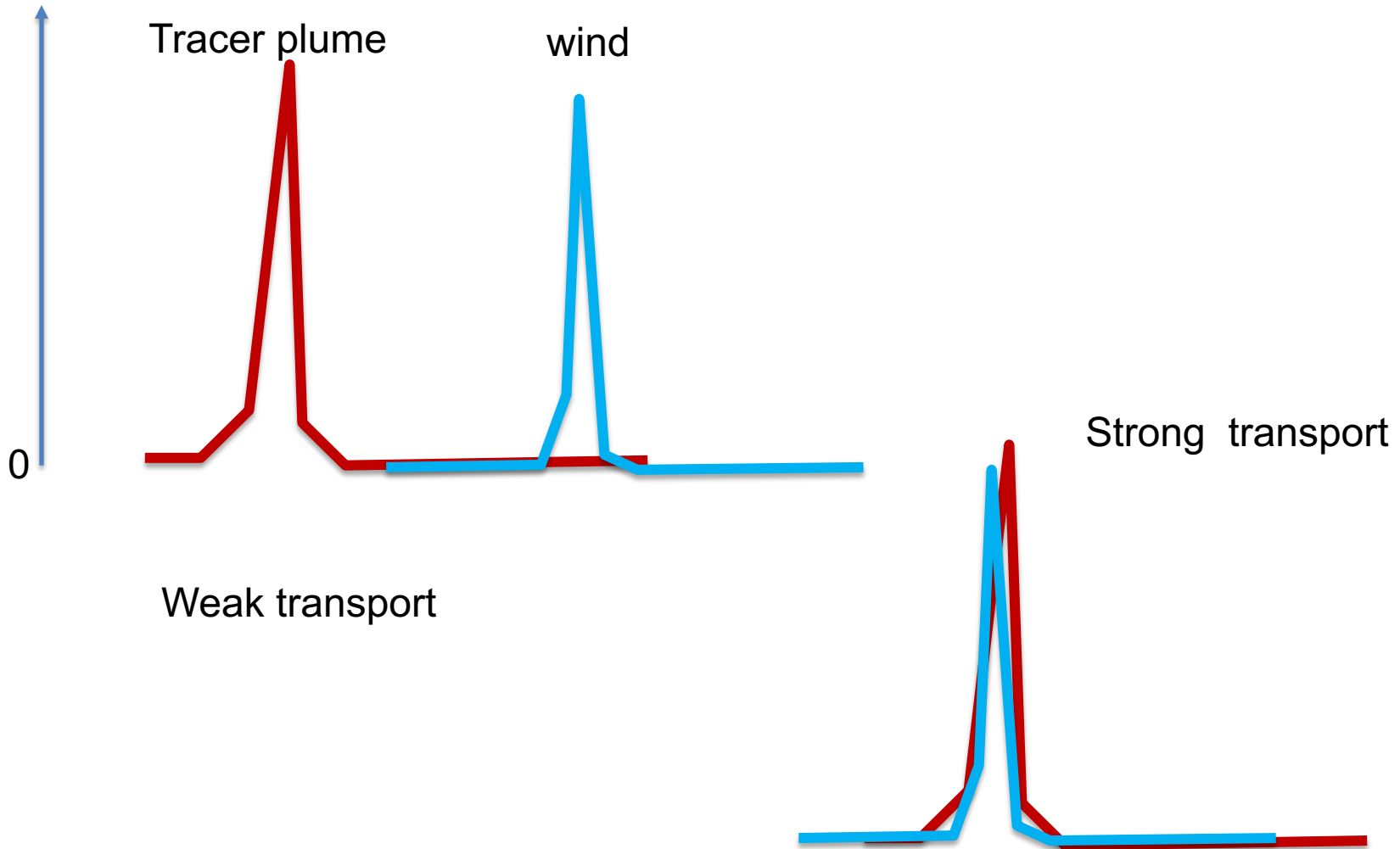
p=2

$$M(p) = 4.62601$$

p=10

$$M(p) = 8.51340$$

# Nonlinearity



# How do nonlinearities arise?

e.g., Cloud microphysics:

Autoconversion of cloud  
water to rain

$$P_{l \rightarrow r} = k q_l^a N_l^b$$

$a$  ranges from 2 to 4;

$b$  from around  $-1$  to  $-2$

Condensation at  $RH=1$

# How do nonlinearities arise?

Fluxes:

$$\partial_t(\rho s) + \partial_x(\rho u s) + \partial_y(\rho v s) + \partial_z(\rho w s) = P_s$$

$$\begin{aligned} \partial_t(\rho \bar{s}) + \partial_x(\rho \bar{u} \bar{s}) + \partial_y(\rho \bar{v} \bar{s}) + \partial_z(\rho \bar{w} \bar{s}) = \\ \bar{P}_s - \partial_x \rho \overline{u' s'} - \partial_y \rho \overline{v' s'} - \partial_z \rho \overline{w' s'} \end{aligned}$$

$\bar{(\ )}$  large-scale horiz. average;  $(\ )'$  deviation from avg.

# “Column physics”

Subgrid horizontal fluxes are typically ignored in atmospheric models

$$\partial_t(\rho\bar{s}) + \partial_x(\rho\bar{u}\bar{s}) + \partial_y(\rho\bar{v}\bar{s}) + \partial_z(\rho\bar{w}s) = \bar{P}_s - \cancel{\partial_x\rho\overline{u's'}} - \cancel{\partial_y\rho\overline{v's'}} - \partial_z\rho\overline{w's'}$$

$$\partial_t(\rho\bar{s}) + \partial_x(\rho\bar{u}\bar{s}) + \partial_y(\rho\bar{v}\bar{s}) + \partial_z(\rho\bar{w}s) = \bar{P}_s - \partial_z\rho\overline{w's'}$$

Column physics don't need to communicate with neighboring grid columns → “embarrassingly parallel”

# Summary

- Physics schemes - “*parameterizations*” - need to return tendencies as functions of model grid mean variables
- Tendency calculations may include representation of subgrid variability



# How are parameterizations built?

- Basic physics
- Empirical formulations from observations or high-resolution calculations (e.g. LES, CRMs)
- Some simple conceptual model – “cartoon”

# Physics Parameterizations needed by an AGCM

- Radiation
  - Clear sky (typically no subgrid variability used)
  - Cloudy
- Surface exchanges
- Boundary Layer Turbulence
- Shallow convection
- Cloud “macrophysics”
- Deep Convection
- Cloud microphysics
- PBL form drag
- Gravity wave drag

# Physics Parameterizations in CAM6

- Radiation **RRTMG**
  - Clear sky (typically no subgrid variability used)
  - Cloudy
- Surface exchanges **Similarity theory (Monin-Obukhov ...)**
- Boundary Layer Turbulence
- Shallow convection **CLUBB prognostic moments**
- Cloud “macrophysics”
- Deep Convection **Zhang & McFarlane mass flux scheme**
- Cloud microphysics **Morrison Gettelman 2-moment**
- PBL form drag **Beljaars et al neutral shear flow over obstacles**
- Gravity wave drag **Lindzen-type schemes for various sources**
- **Complex prognostic aerosol model**

# Mass flux convection schemes in atmospheric models



# Convective cloud conceptualized as simple entraining/detraining plume(s)

## Thermodynamic Equation

$$\partial_t \rho s + \nabla \cdot \rho \mathbf{u} s + \partial_z \rho w s = \overline{Q} + \dots$$

↑  
Latent heating

## Plume/cloud cont. equation

$$\partial_t \rho a + \partial_z \rho a w_c = E - D$$

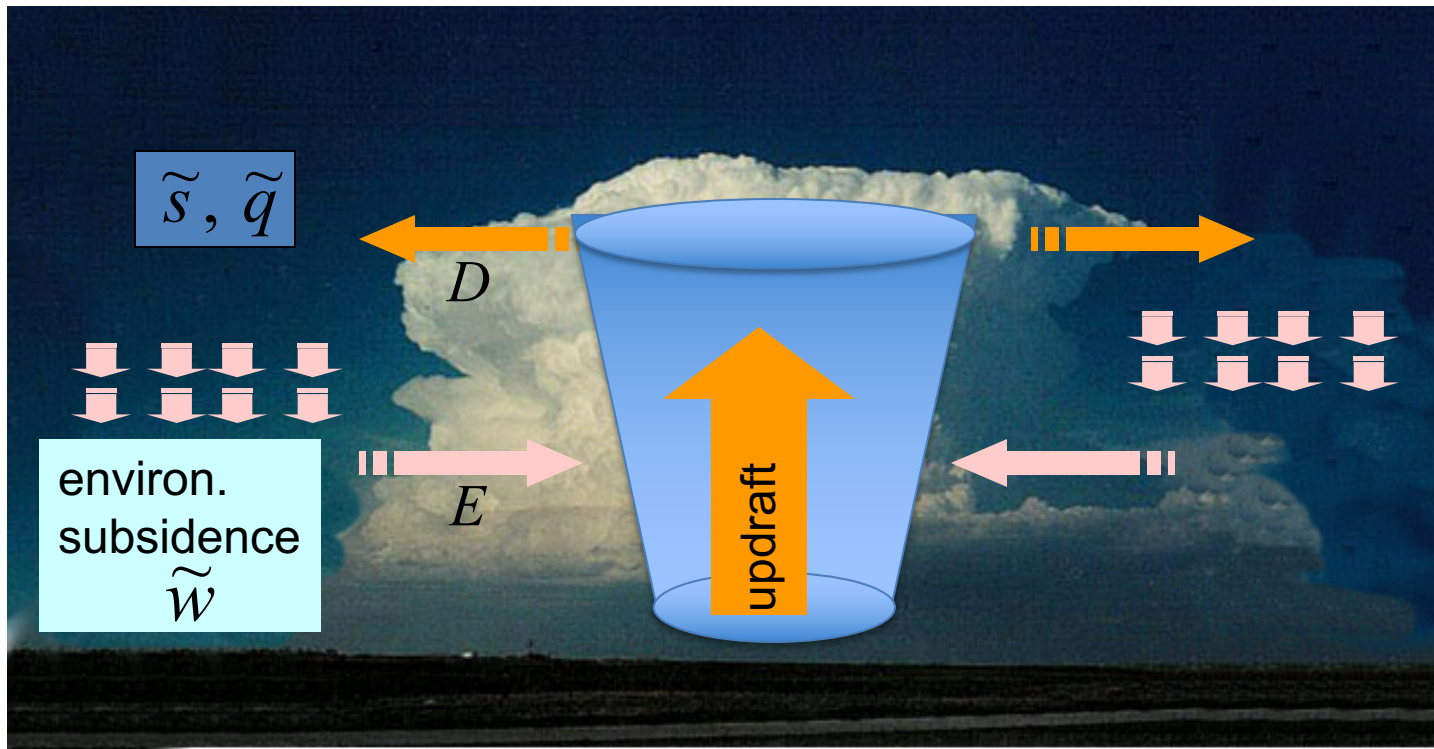
↑ Cloud areal fraction
↑ Entrainment
↑ Detrainment

## Grid box average therm. equation

$$\partial_t \overline{\rho s} + \overline{\nabla \cdot \rho \mathbf{u} s} + \partial_z \overline{\rho w s} = \overline{Q} - \partial_z \overline{\rho w' s'} + \dots$$

## Plume therm. equation

$$\partial_t \rho a s_c + \partial_z \rho a w_c s_c = E \tilde{s} - D s_c + a Q_c$$



## Grid box average therm. equation

$$\partial_t \overline{\rho s} + \overline{\nabla \cdot \rho \mathbf{u} s} + \partial_z \overline{\rho w s} = a Q_c - \partial_z \overline{\rho w' s'} + \dots$$

## Sub-grid fluxes re-written

$$\partial_z \overline{\rho w' s'} = \partial_z \rho a w_c s_c + \partial_z \rho (1-a) \tilde{w} \tilde{s}$$

## compensating subsidence\*

$$\Leftrightarrow \rho a w_c = -\rho (1-a) \tilde{w}$$

$$\partial_t \overline{\rho s} + \overline{\nabla \cdot \rho \mathbf{u} s} + \partial_z \overline{\rho w s} = a Q_c - \partial_z \rho a w_c s_c - \partial_z \rho (1-a) \tilde{w} \tilde{s} + \dots$$

$$\partial_z \rho a w_c s_c = E \tilde{s} - D s_c + a Q_c - \partial_t \rho a s_c$$

## Plume therm. equation

Grid box average therm. equation

$$\partial_t \overline{\rho s} + \overline{\nabla \cdot \rho \mathbf{u} s} + \partial_z \overline{\rho w s} = a Q_c - \partial_z \overline{\rho w' s'} + \dots$$

Sub-grid fluxes re-written

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$$\partial_t \overline{\rho s} + \overline{\nabla \cdot \rho \mathbf{u} s} + \partial_z \overline{\rho w s} = \cancel{a Q_c} - \partial_z \rho a w_c s_c - \partial_z \rho (1-a) \tilde{w} \tilde{s} + \dots$$

$$\partial_z \rho a w_c s_c = E \tilde{s} - D s_c + \cancel{a Q_c} - \partial_t \rho a s_c$$

Plume therm. equation

**Explicit in-cloud latent heating term drops out**

Grid box average therm. equation

$$\partial_t \overline{\rho s} + \overline{\nabla \cdot \rho \mathbf{u} s} + \partial_z \overline{\rho w s} = -E \tilde{s} + D s_c + \partial_t \rho a s_c - \partial_z \rho (1-a) \tilde{w} \tilde{s} + \dots$$

## Grid box average therm. equation

$$\partial_t \overline{\rho s} + \overline{\nabla \cdot \rho \mathbf{u} s} + \partial_z \overline{\rho w s} = -E \tilde{s} + D s_c + \partial_t \rho a s_c - \partial_z \rho (1-a) \tilde{w} \tilde{s} + \dots$$

$$-\rho(1-a)\tilde{w} = \rho a w_c \equiv M_c$$

$$a \rightarrow 0 \Leftrightarrow \tilde{s} \rightarrow \bar{s}$$

## Grid box average therm. equation

$$\partial_t \overline{\rho s} + \overline{\nabla \cdot \rho \mathbf{u} s} + \partial_z \overline{\rho w s} = \underbrace{-E \bar{s} + D s_c + \partial_z M_c \bar{s}}_{\text{cumulus forcing}} + \dots$$

In final form, cumulus forcing is determined entirely by profiles of  $E$ ,  $D$ , and  $M_c$ . Key assumptions up to here:

$$-\rho(1-a)\tilde{w} = \rho a w_c \quad (\text{compensating subsidence});$$

$$a \rightarrow 0 \quad (\text{small areal fraction/negligible storage})$$

Mass-flux convective parameterizations determine profiles  $E$ ,  $D$ , and  $M_c$  based on grid mean quantities and ***assumed plume models***.

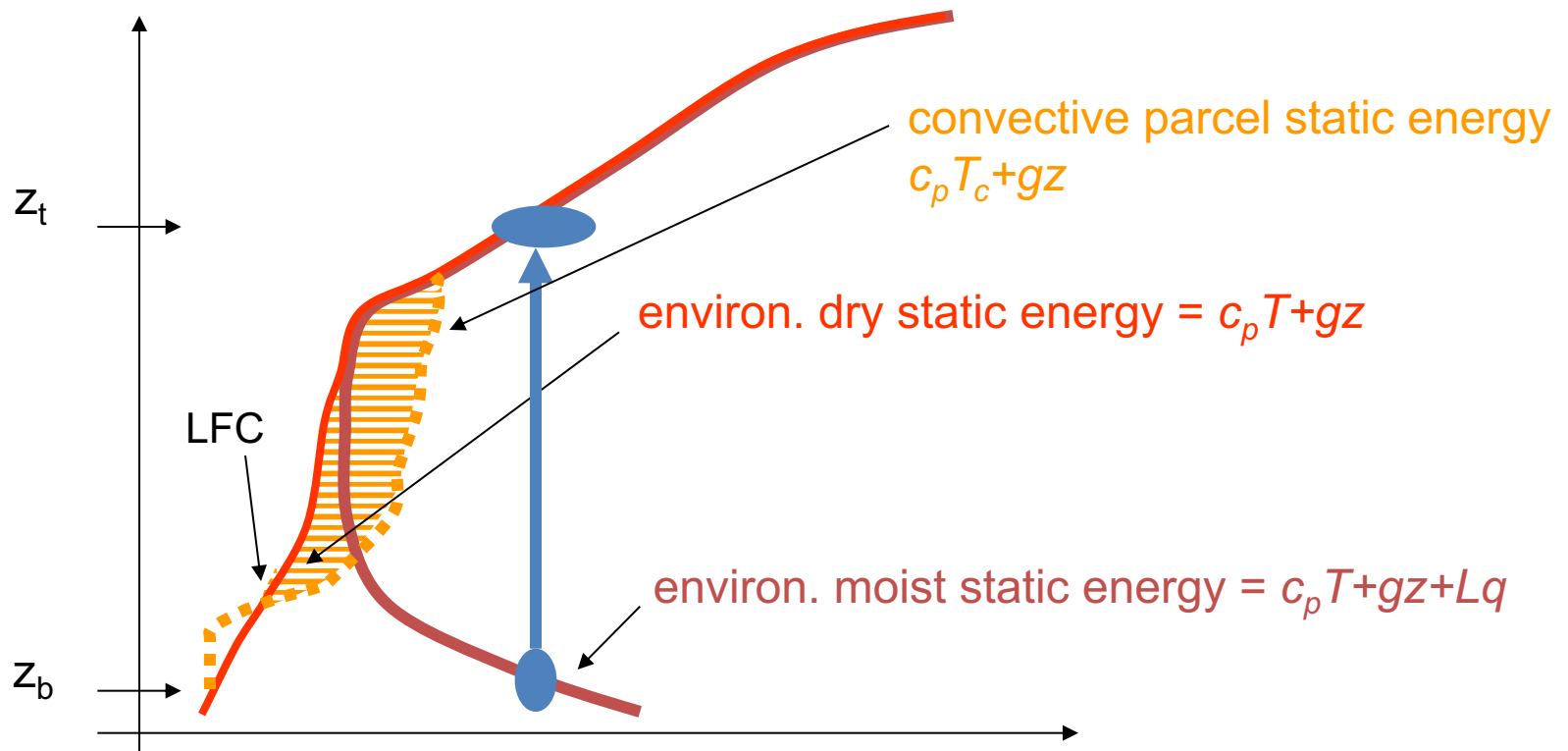


Convective Available Potential Energy is a common control for parameterized convective mass flux in climate models

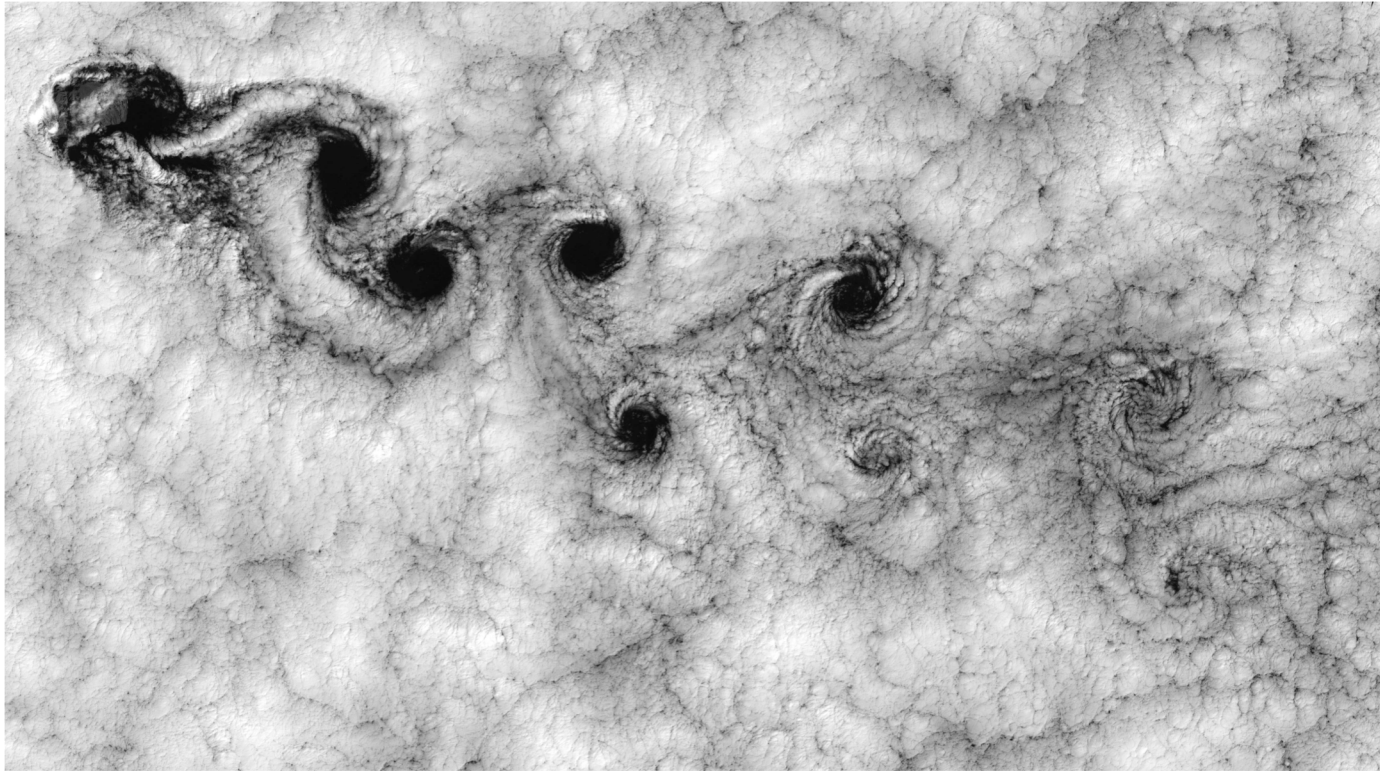


$$\sim CAPE = g \int_{z_B}^{z_T} \frac{T_c - T}{T} dz$$

$$M_c(z_b) \sim f(CAPE, \partial_t CAPE)$$



# Prognostic higher-order moments for turbulence and shallow convection – Cloud Layers Unified by Bi-normals (CLUBB)



# Overview of CLUBB's solution procedure

**Advance 10 prognostic equations**

$$\overline{w}, \overline{\theta_l}, \overline{q_t}, \overline{w'^2}, \overline{w'^3}, \overline{q_t'^2}, \overline{\theta_l'^2}, \overline{q_t'\theta_l'}, \overline{w'q_t'}, \overline{w'\theta_l'}$$

**Note:**

**No equations for**

$$\overline{u'w'}$$

$$\overline{v'w'}$$

Close dissipation terms

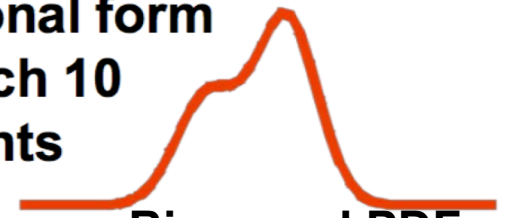
$\Delta t$

**Use PDF to close higher-order moments, buoyancy terms**

$$\overline{w'q_t'^2}, \overline{w'\theta_l'^2}, \overline{w'q_t'\theta_l'}, \overline{w'^2q_t'}, \overline{w'^2\theta_l'}, \overline{w'^4},$$

$$\overline{q_t'\theta_v'}, \overline{\theta_l'\theta_v'}, \overline{w'\theta_v'}, \overline{w'^2\theta_v'}$$

**Select PDF from given functional form to match 10 moments**



Bi-normal PDFs

**Diagnose cloud fraction, liquid water from PDF**

# More on Clouds

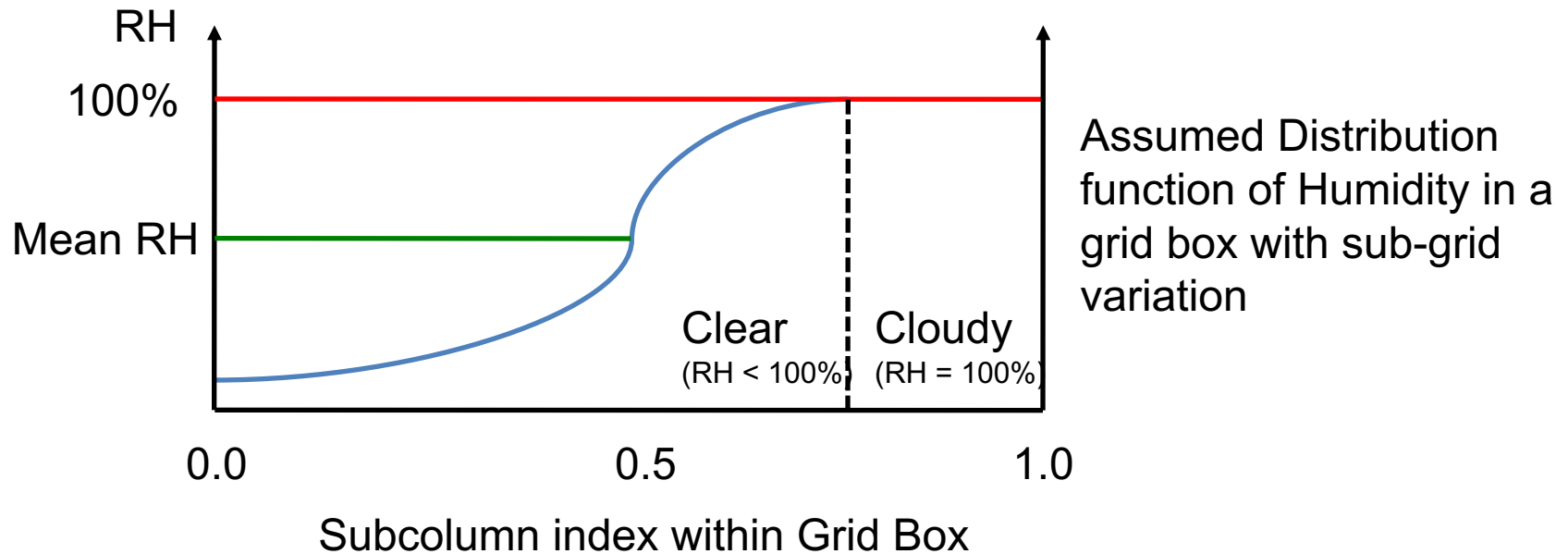


# Stratiform Clouds

## Sub-Grid Humidity and Clouds

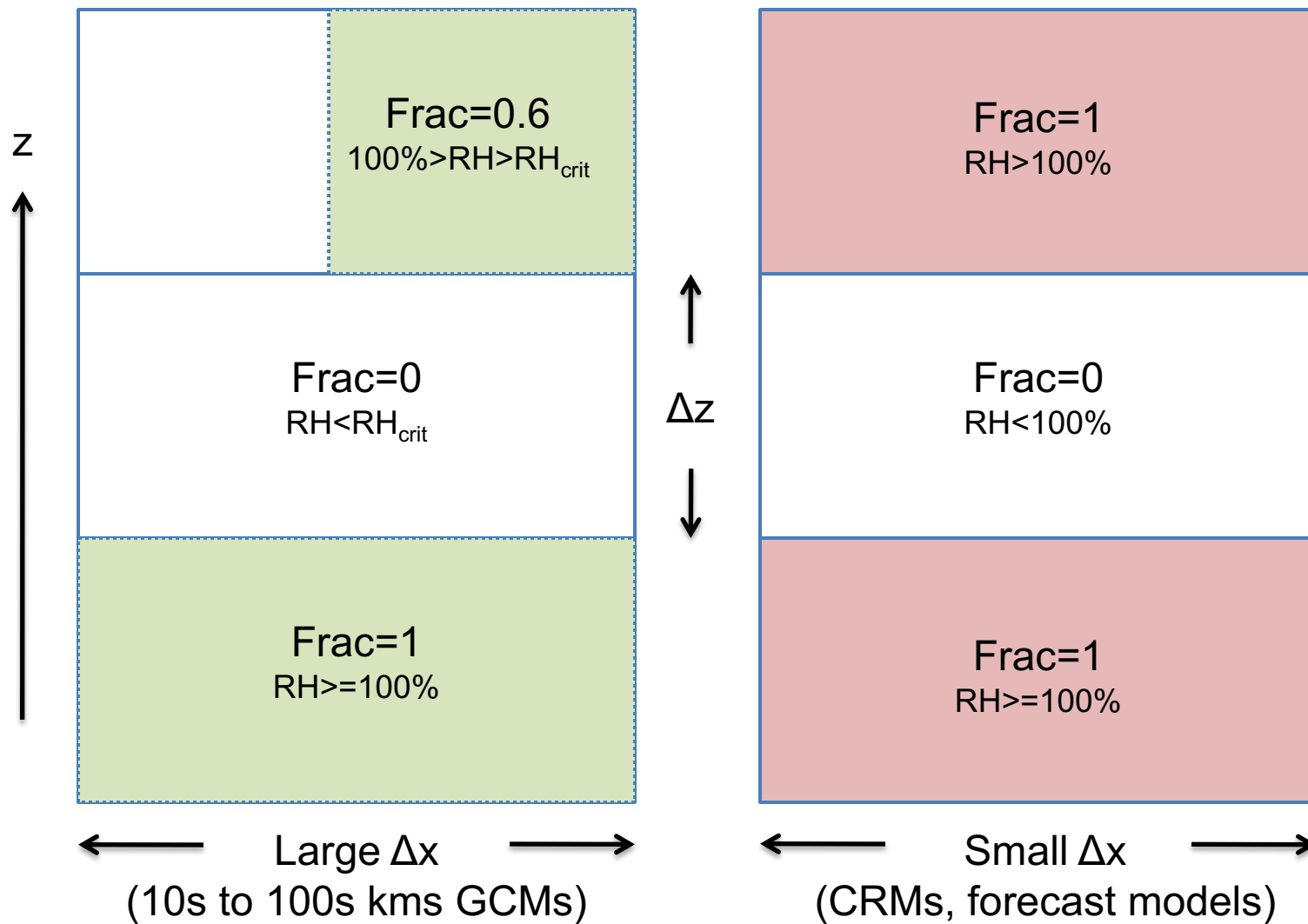
Liquid clouds form when  $RH = 100\%$  ( $q=q_{sat}$ )

But if there is variation in RH in space, some clouds will form before *mean*  $RH = 100\%$



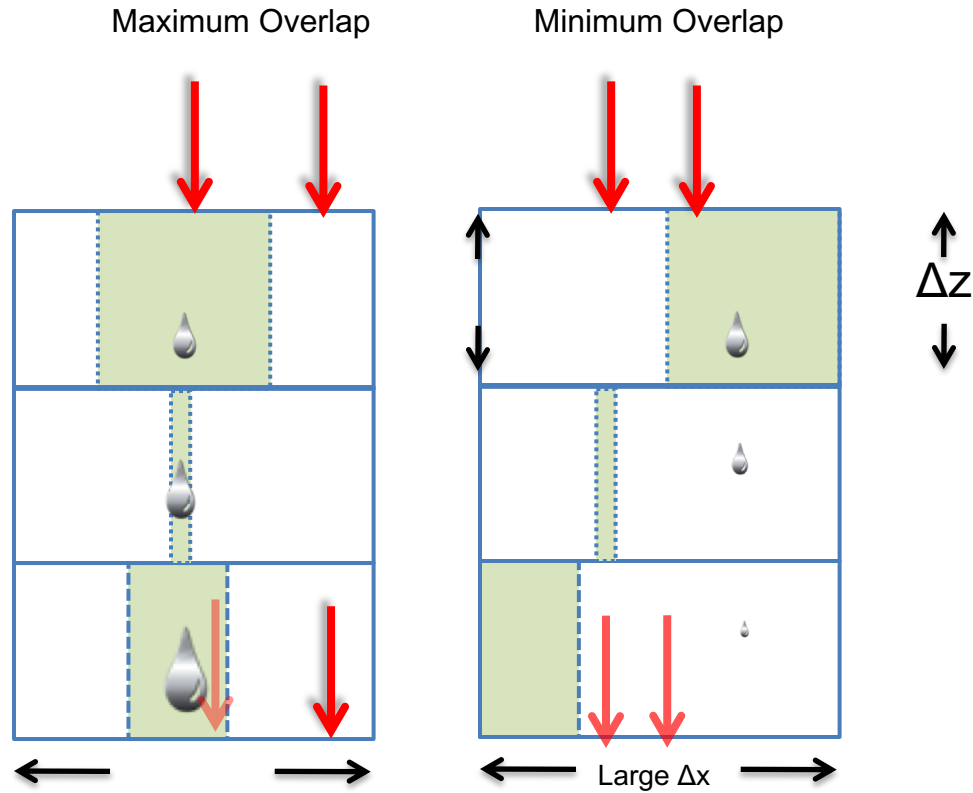
# Fractional Cloud Cover

$$\text{Cloud\_Frac} = f(\text{RH}, w, \text{water}, \text{aerosols}, \text{time}, \dots)$$



# The Cloud Overlap Challenge

Radiation and micro/macro-physics impact



- Contiguous cloudy layers maximally overlapped in CAM
- Non-contiguous layers randomly overlapped

# Parameterizations

## High level design

1. Inputs and effects totally contained within single columns

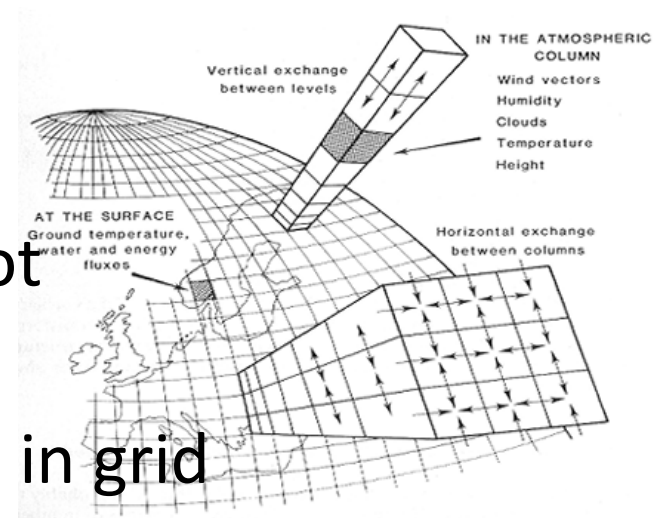
– Single grid point structures are believed

2. Most (many common) schemes do not possess a “memory”

3. Assume sufficient space-time volume in grid means for “good” statistics

4. For climate should be mass, momentum and energy conserving (limiters and fixers)

*1,2 and 3 begin to cause trouble as resolution increases and time-steps decrease*





# Parameterizations

## High level design

Process splitting versus time splitting (CAM)

Process splitting:

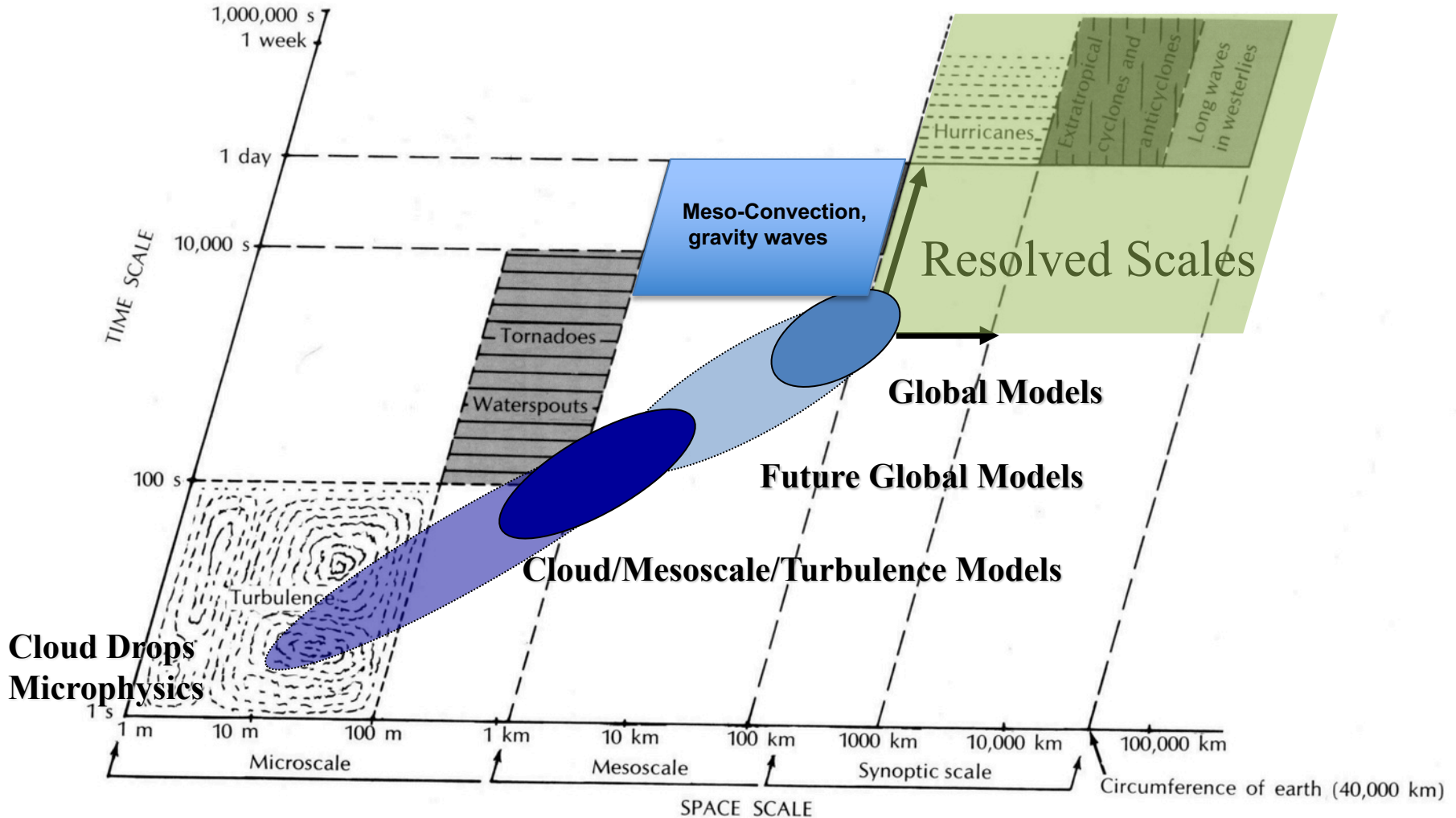
- All parameterizations work on same state.  
Provide tendencies for unified update

Time splitting

- Parameterizations update state as they work  
and pass updated state to next param.

# Scales of Atmospheric Processes

Determines the formulation of the model



# Future Directions for Physics in Models?

What do we need to consider?

As grid-sizes and time steps decrease, parameterizations may need to communicate across space and time

As grid-sizes and time steps decrease, resolved scales may not contain enough information to close parameterizations

- Stochastic elements?
- Life-cycles of processes?

At any resolution, better sub-grid representations are needed

- Subcolumns?

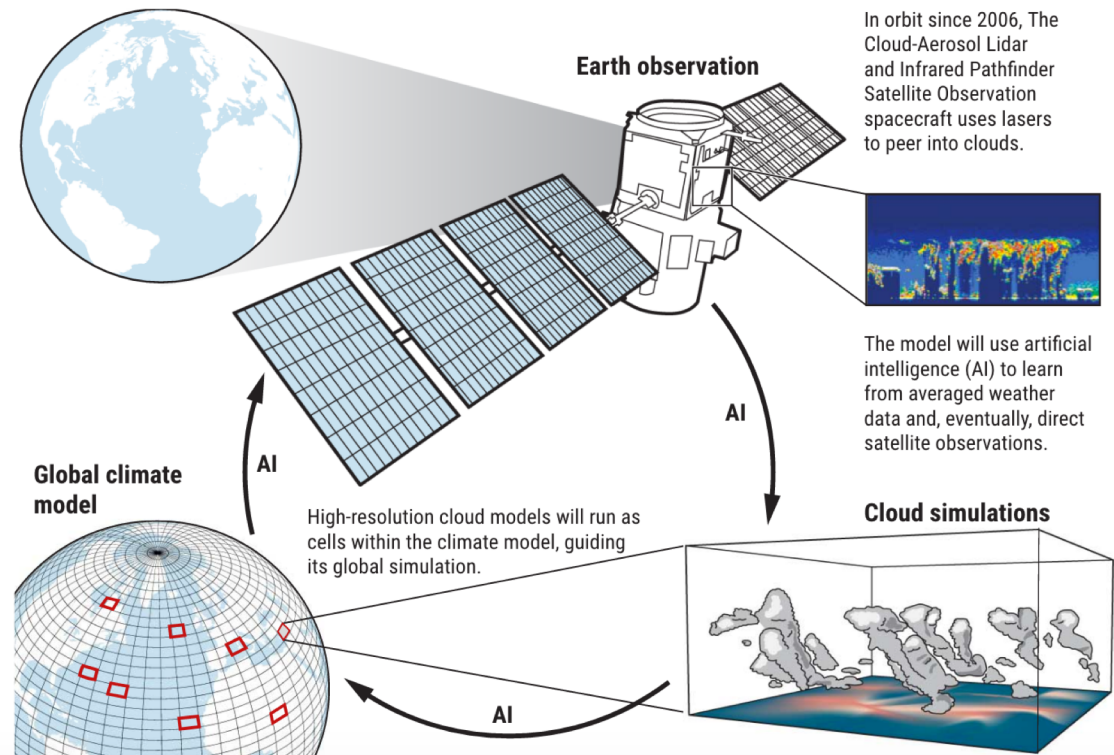
# Future Directions for Physics in Models?

## Science insurgents plot a climate model driven by artificial intelligence

By [Paul Voosen](#) Jul. 26, 2018 , 2:00 PM

<http://www.sciencemag.org/news/2018/07/science-insurgents-plot-climate-model-driven-artificial-intelligence> **Learning the climate**

A new data-driven climate model will use satellite observations and high-resolution simulations to learn how best to render its clouds. Similar methods will also be applied to other, small-scale phenomena, such as sea ice and ocean eddies.





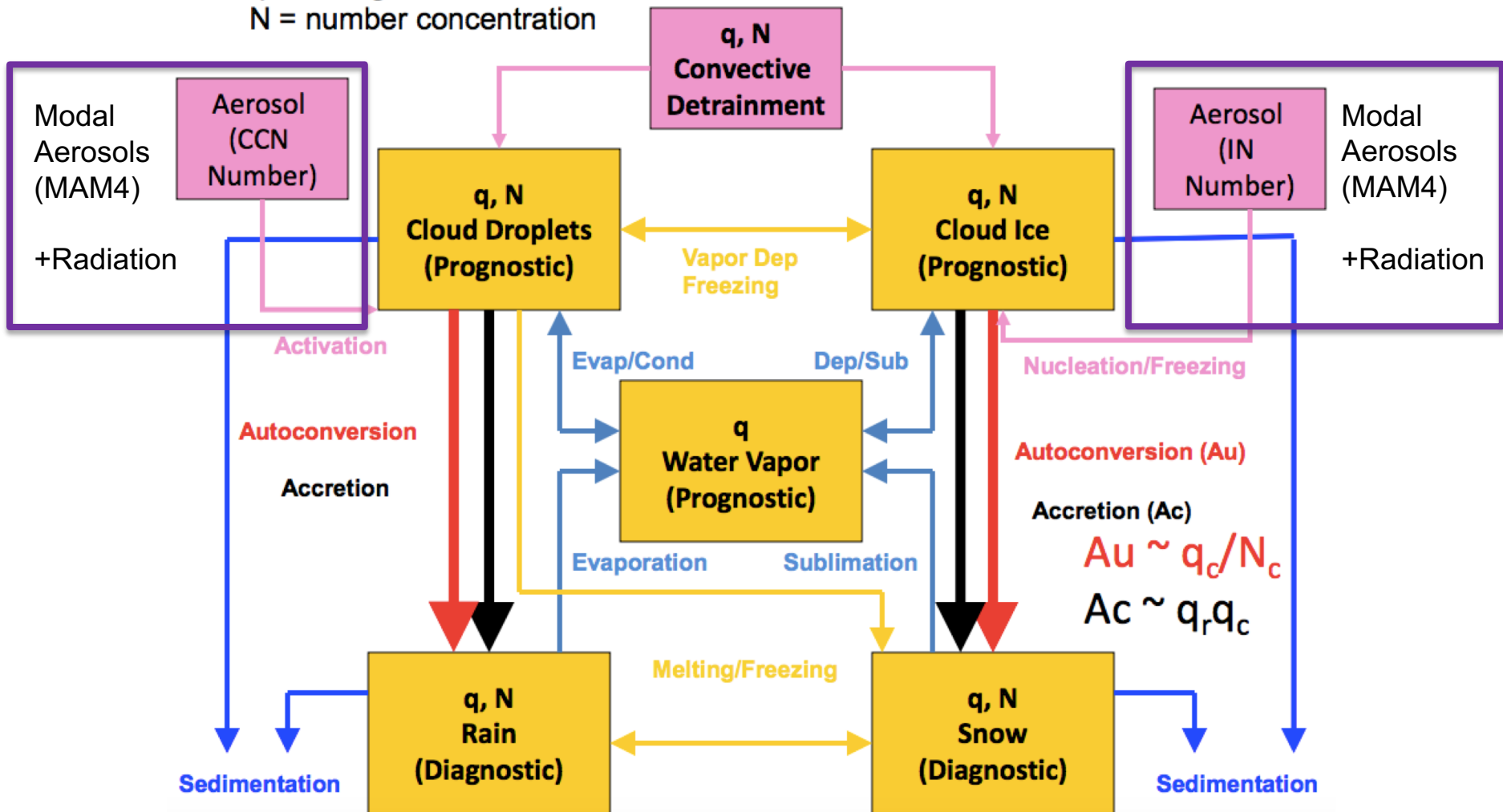
Questions?

**EXTRA SLIDES**

# CAM5 Microphysics

q = mixing ratio  
N = number concentration

Morrison & Gettelman 2008

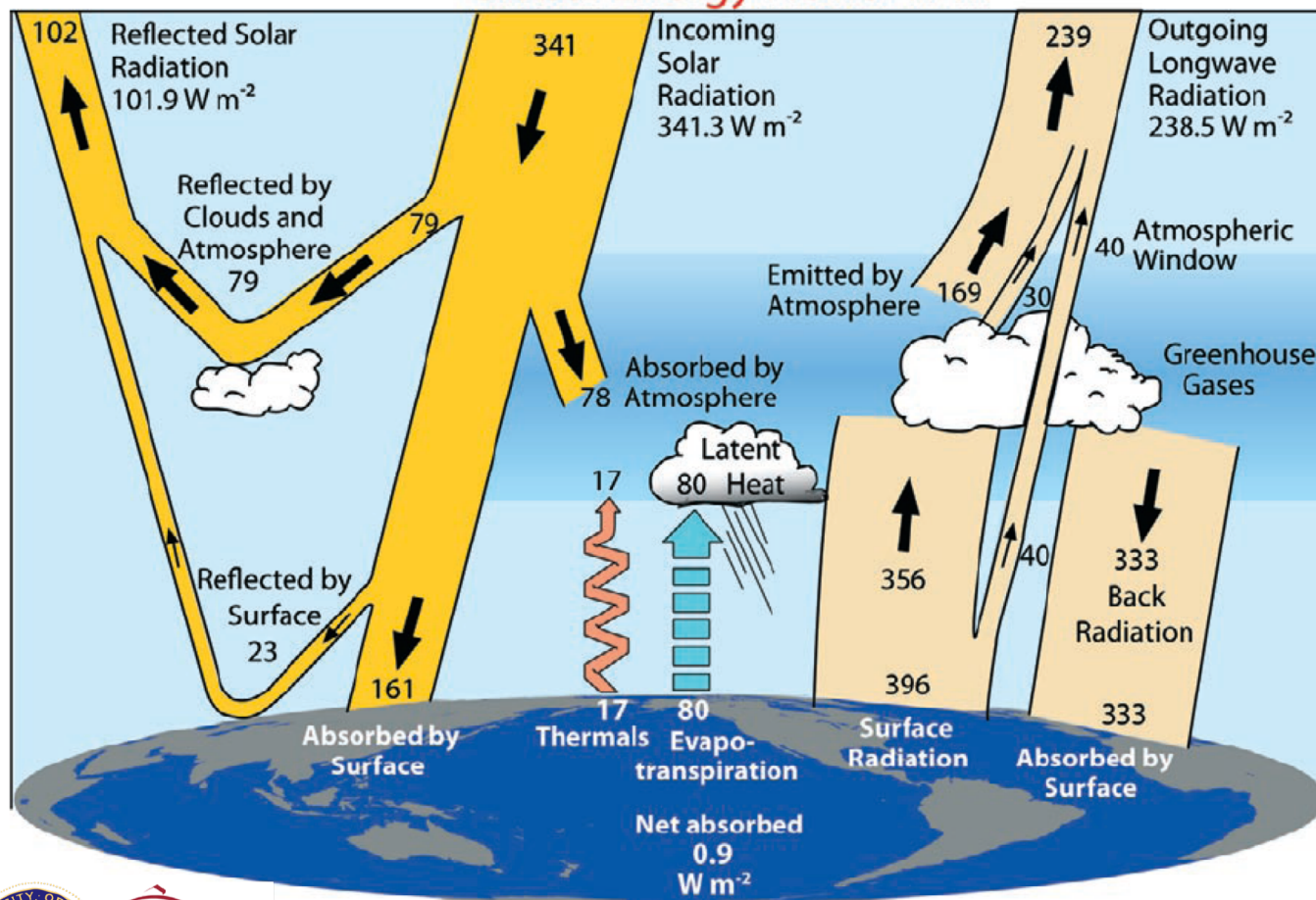


# Radiation

## The Earth's Energy Budget

Trenberth & Fasullo, 2008

Global Energy Flows  $W m^{-2}$



Gas	SW Absorption ( $W m^{-2}$ )
CO <sub>2</sub>	1
O <sub>2</sub>	2
O <sub>3</sub>	14
H <sub>2</sub> O	43

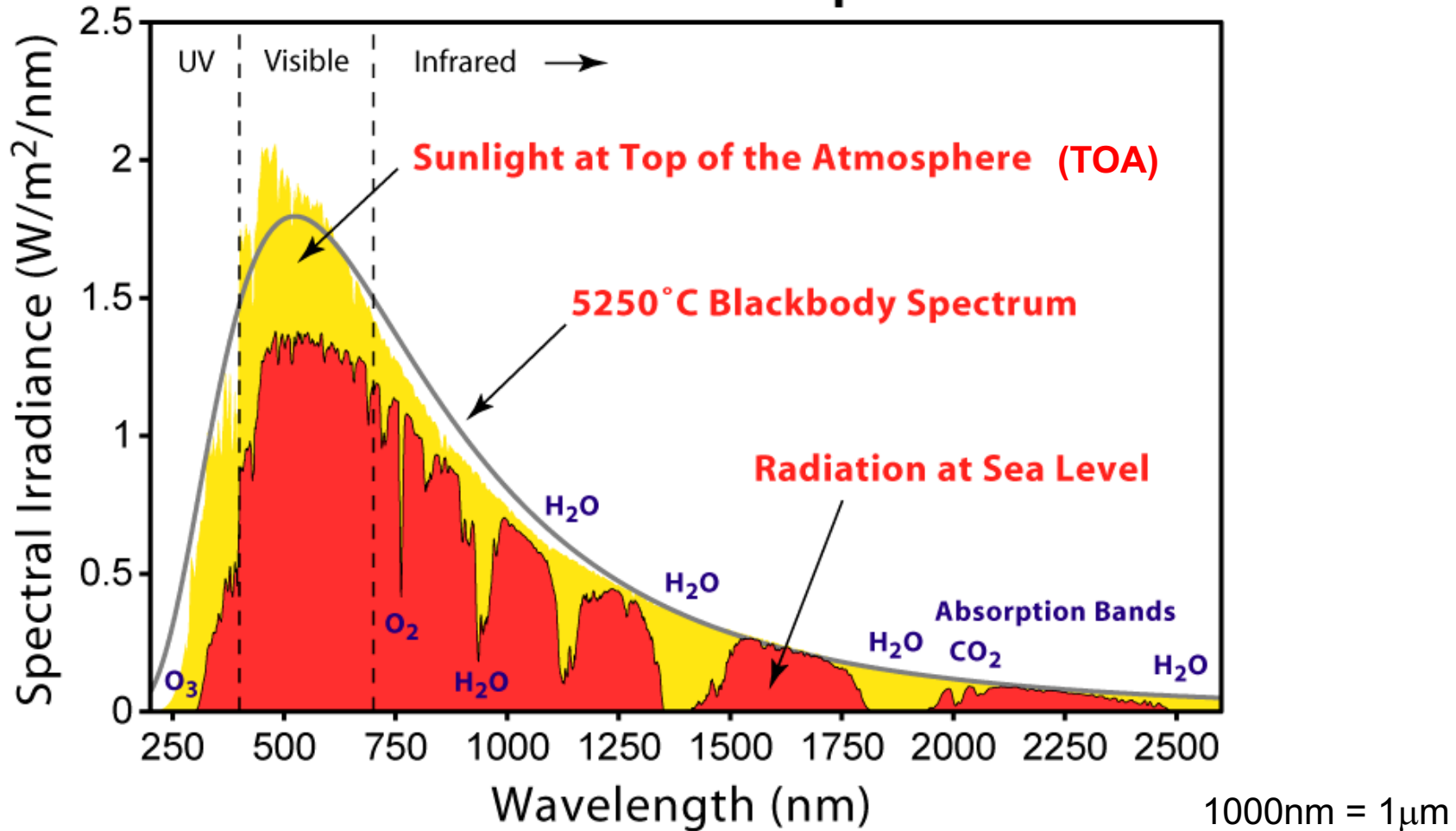
+Condensed species: Clouds & Aerosols



Bill Collins, Berkeley & LBL



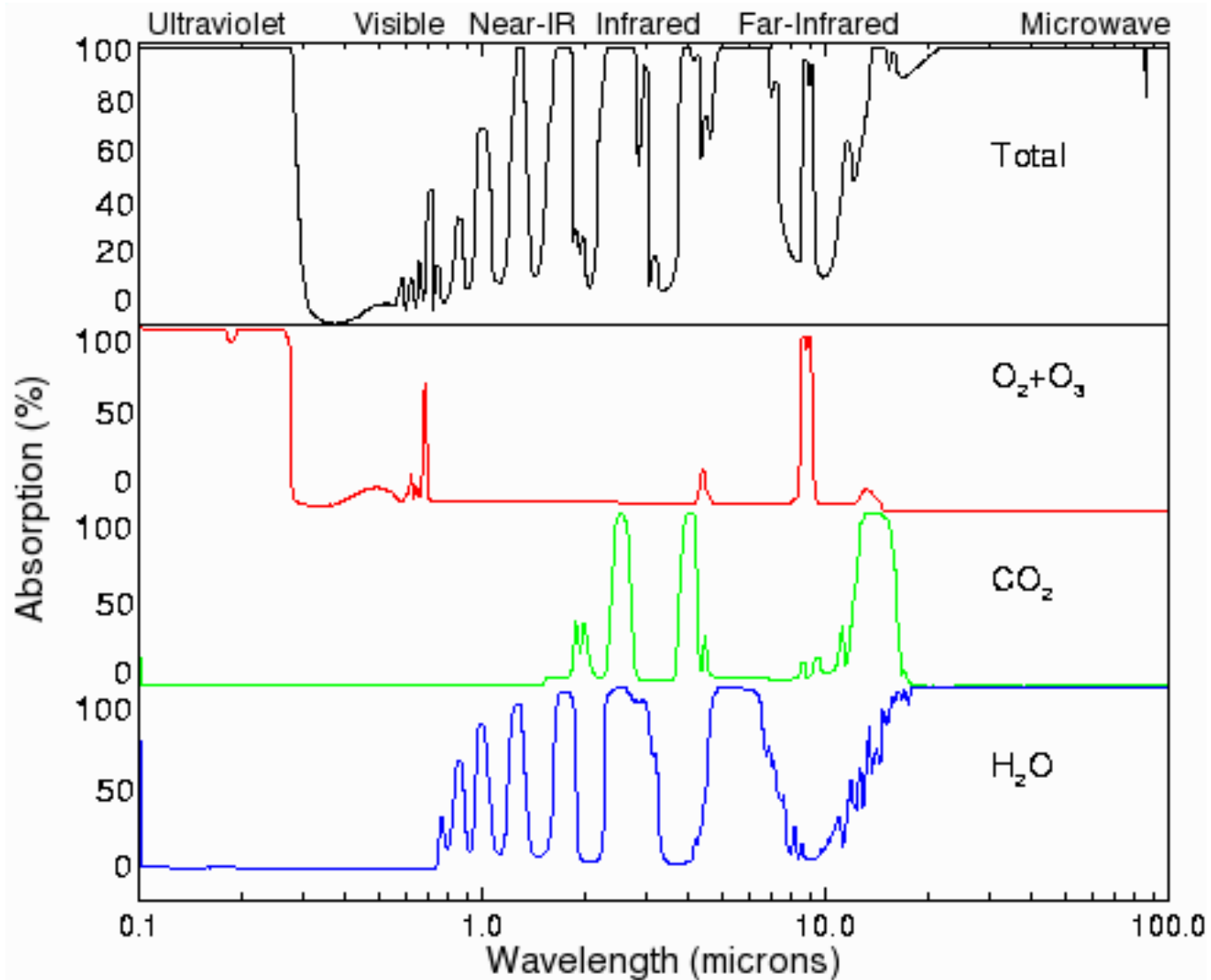
# Solar Radiation Spectrum



Input at TOA, Radiation at surface

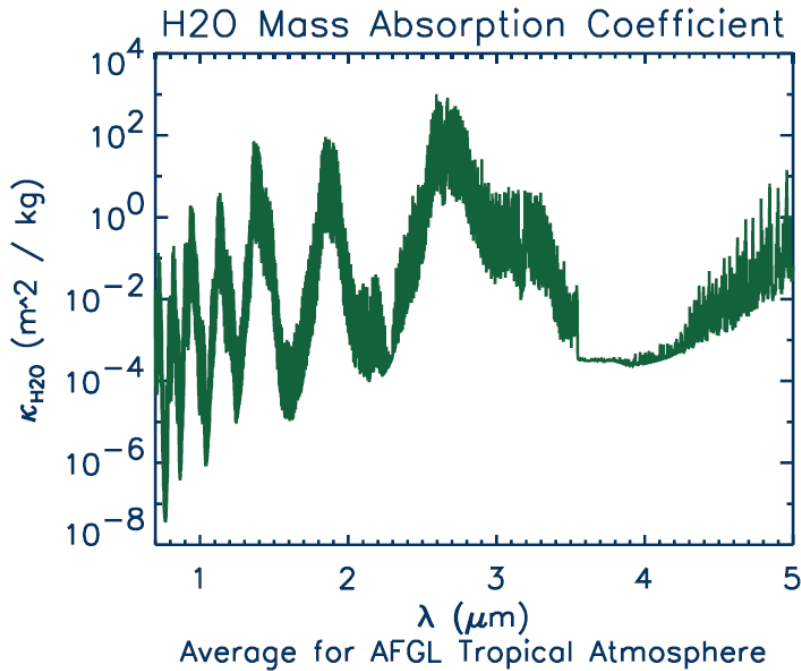
From: 'Sunlight', Wikipedia

# IR absorption

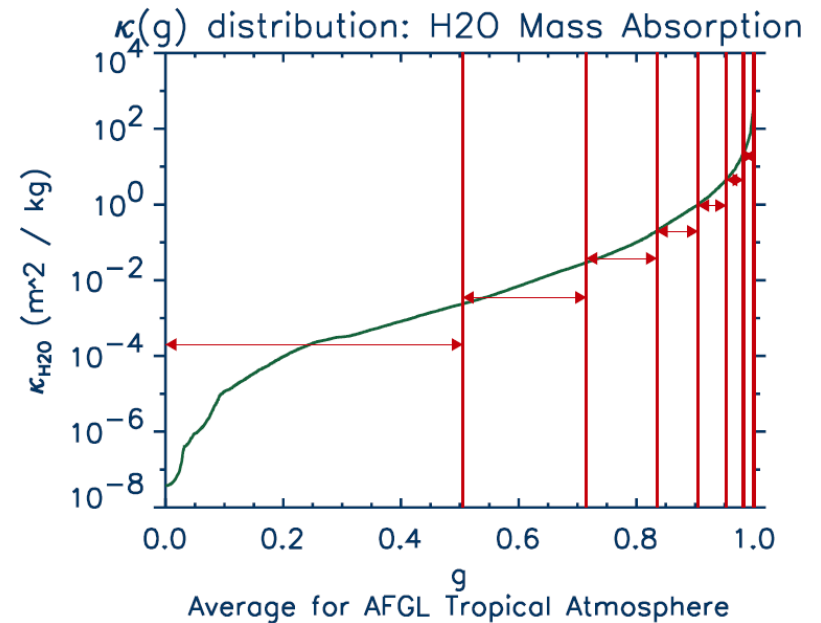


1000nm = 1 $\mu$ m

# k-distribution Band Models



Sort



- Line-by-line calculations
- **Very expensive/slow, accurate**

- k-distribution band model, sort absorption coefficients by magnitude
- **Cheaper/fast, less accurate**

# Planetary Boundary Layer (PBL)

## Regime dependent representations

- Vital for near-surface environment (humidity, temperature, chemistry)
- Exploit **thermodynamic conservation** (liquid virtual potential temperature  $\theta_{vl}$ )

- **Conserved** for rapidly well mixed PBL

- **Not conserved** for stable PBL

- Critical determinant is the presence of turbulence

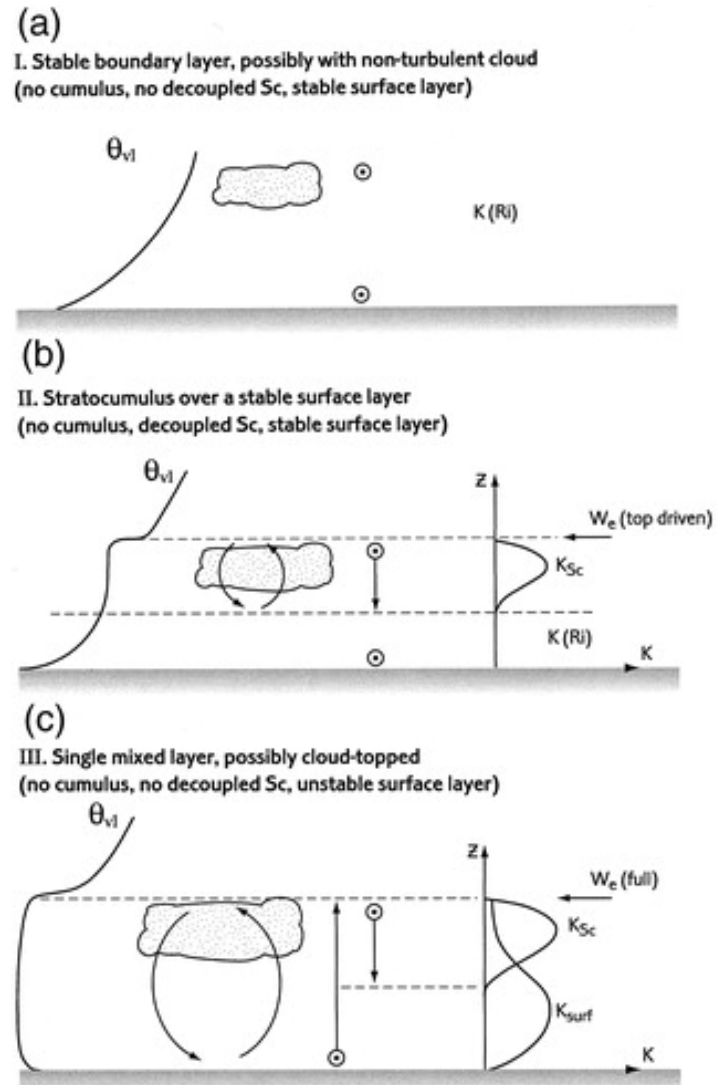
$$Ri = \frac{g\beta}{(\partial u / \partial z)^2},$$

- **Richardson number**

- $\ll 1$ , flow becomes turbulent

- **CAM4**: Gradient Ri # + non-local transport (Holtslag and Boville, 1993)

- **CAM5**: TKE-based Moist turbulence (Park and Bretherton, 2009)



How do we parameterize this  
menagerie of small-scale flows in a  
global model???

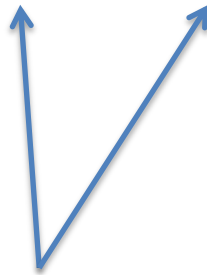
# Subgrid momentum fluxes

## Momentum Equation

$$\partial_t \rho \mathbf{u} + \dots + \partial_z \rho w \mathbf{u} = -\nabla p - \rho \nabla \phi + \mathbf{F} + \dots, \quad \rho \text{ is atmospheric density}$$

## Grid box average momentum equation

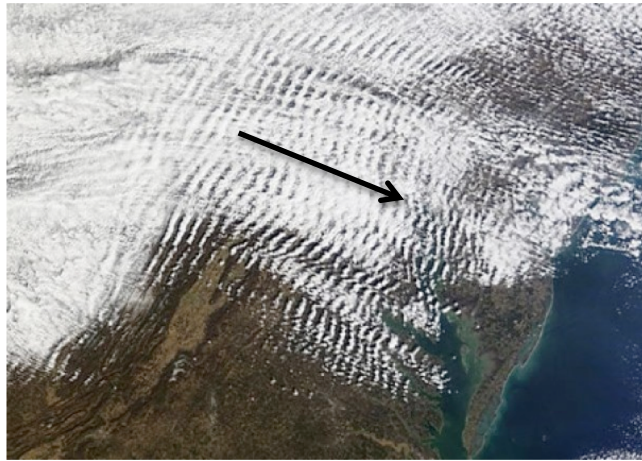
$$\partial_t \bar{\rho} \bar{\mathbf{u}} + \dots + \partial_z \bar{\rho} \bar{w} \bar{\mathbf{u}} = -\nabla \bar{p} - \bar{\rho} \nabla \bar{\phi} - \partial_z \bar{\rho} \overline{u'w'} \mathbf{i} - \partial_z \bar{\rho} \overline{v'w'} \mathbf{j} + \bar{\mathbf{F}}$$



Vertical derivatives of zonal and meridional subgrid vertical momentum fluxes produce drag forces

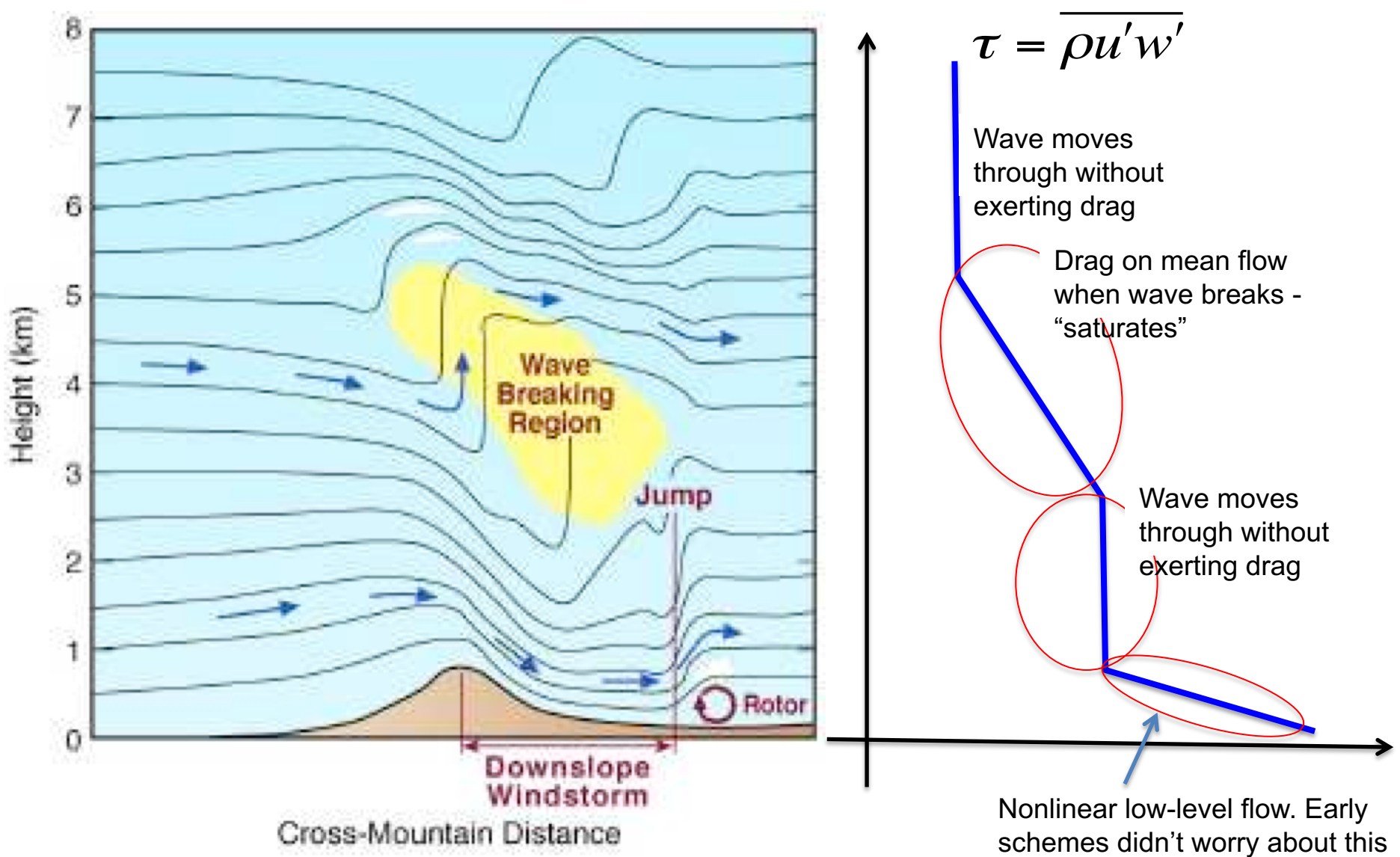
# Subgrid momentum fluxes

Let's turn into coordinates where "x" is perpendicular to wave crests



Our job is then to calculate

$$\tau = \overline{\rho u' w'}$$



Complex wave pattern conceptualized as 2D monochromatic wave controlled by "saturation"

Lindzen, R. S. (1981). Turbulence and stress owing to gravity wave and tidal breakdown. *Journal of Geophysical Research*, 86(C10), 9707-9714.



$$\tau = \overline{\rho u' w'}$$

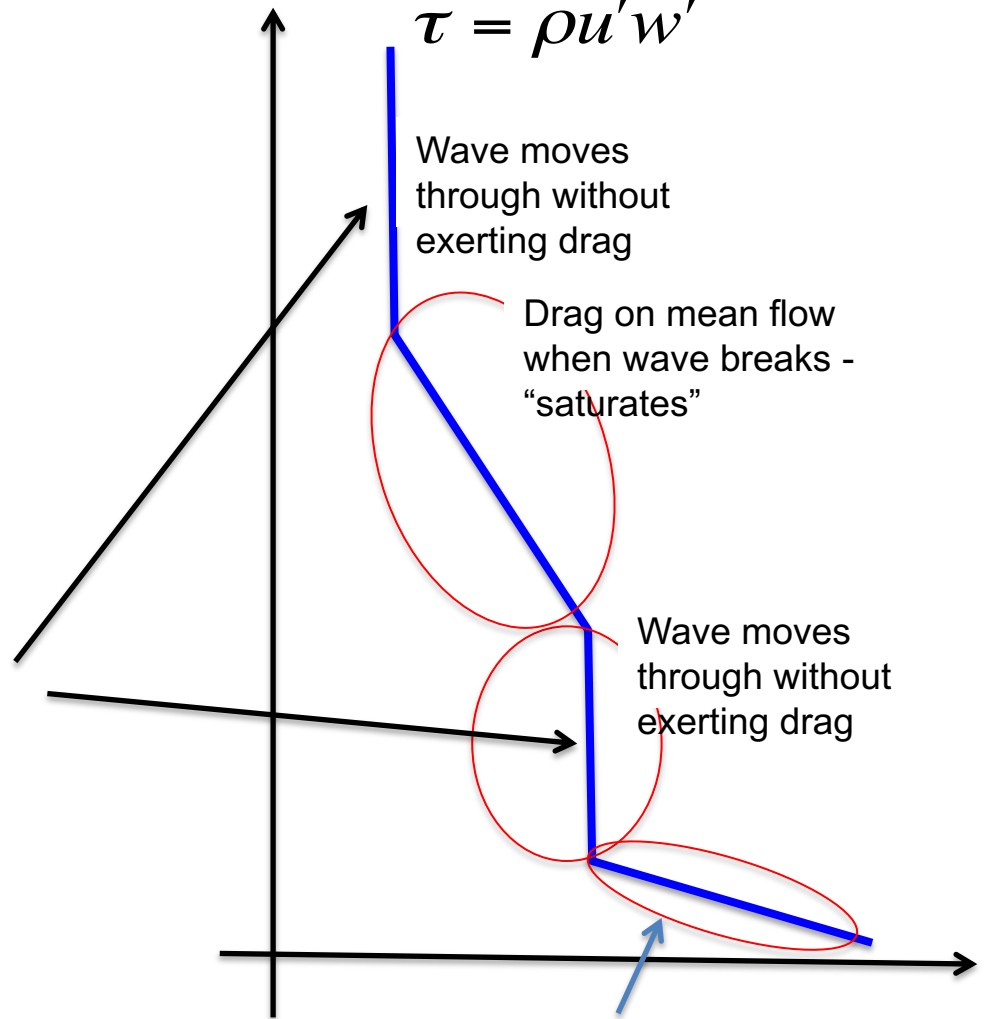
Wave moves through without exerting drag

Drag on mean flow when wave breaks - "saturates"

Wave moves through without exerting drag

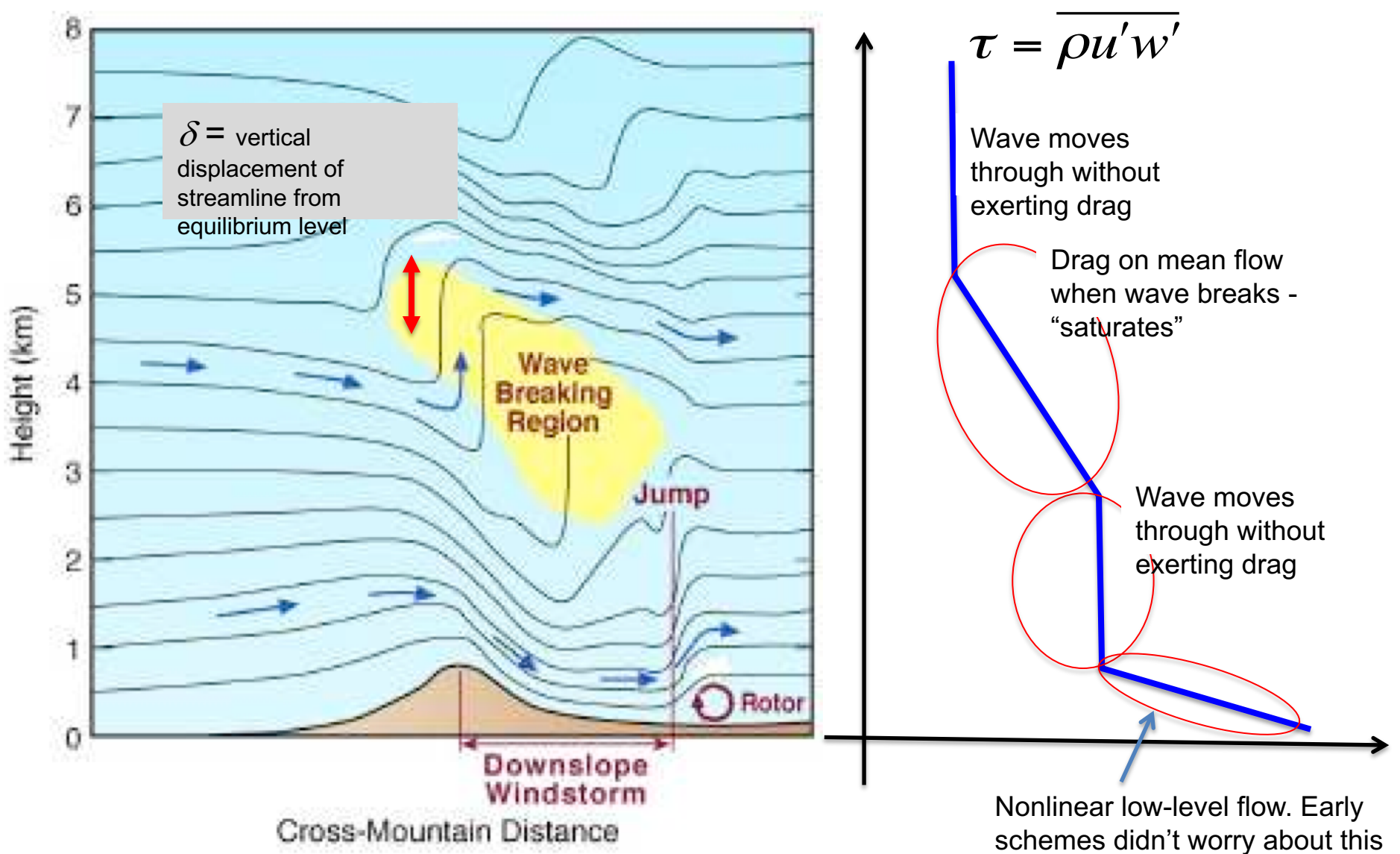
Nonlinear low-level flow. Early schemes didn't worry about this

**Eliassen-Palm theorem:**  
Non-dissipating waves have conserve  $\tau$  as they propagate vertically



Complex wave pattern conceptualized as 2D monochromatic wave controlled by "saturation"

Lindzen, R. S. (1981). Turbulence and stress owing to gravity wave and tidal breakdown. *Journal of Geophysical Research*, 86(C10), 9707-9714.



How do we calculate  $\tau$  based on topographic information?

Orographic gravity wave momentum flux based on  $\delta$  and gravity wave dispersion relationships

$$u' = N\delta$$

$$w' = k\bar{U}\delta$$

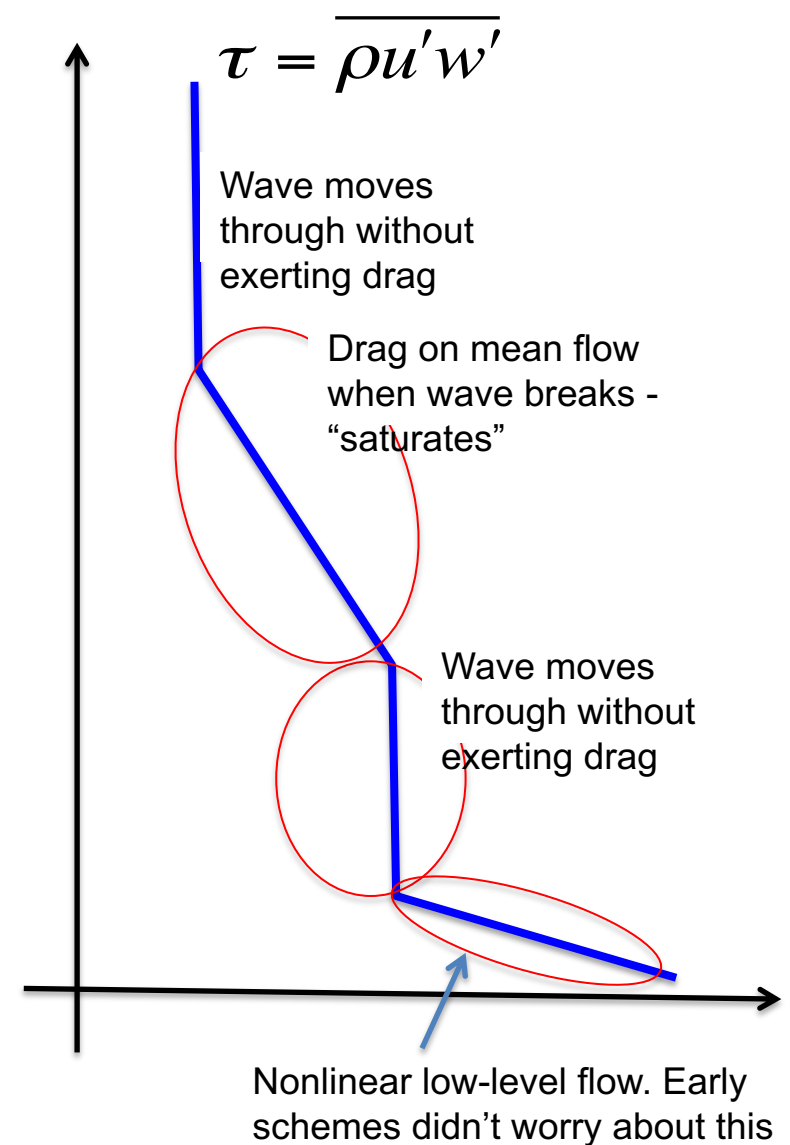
so momentum flux becomes

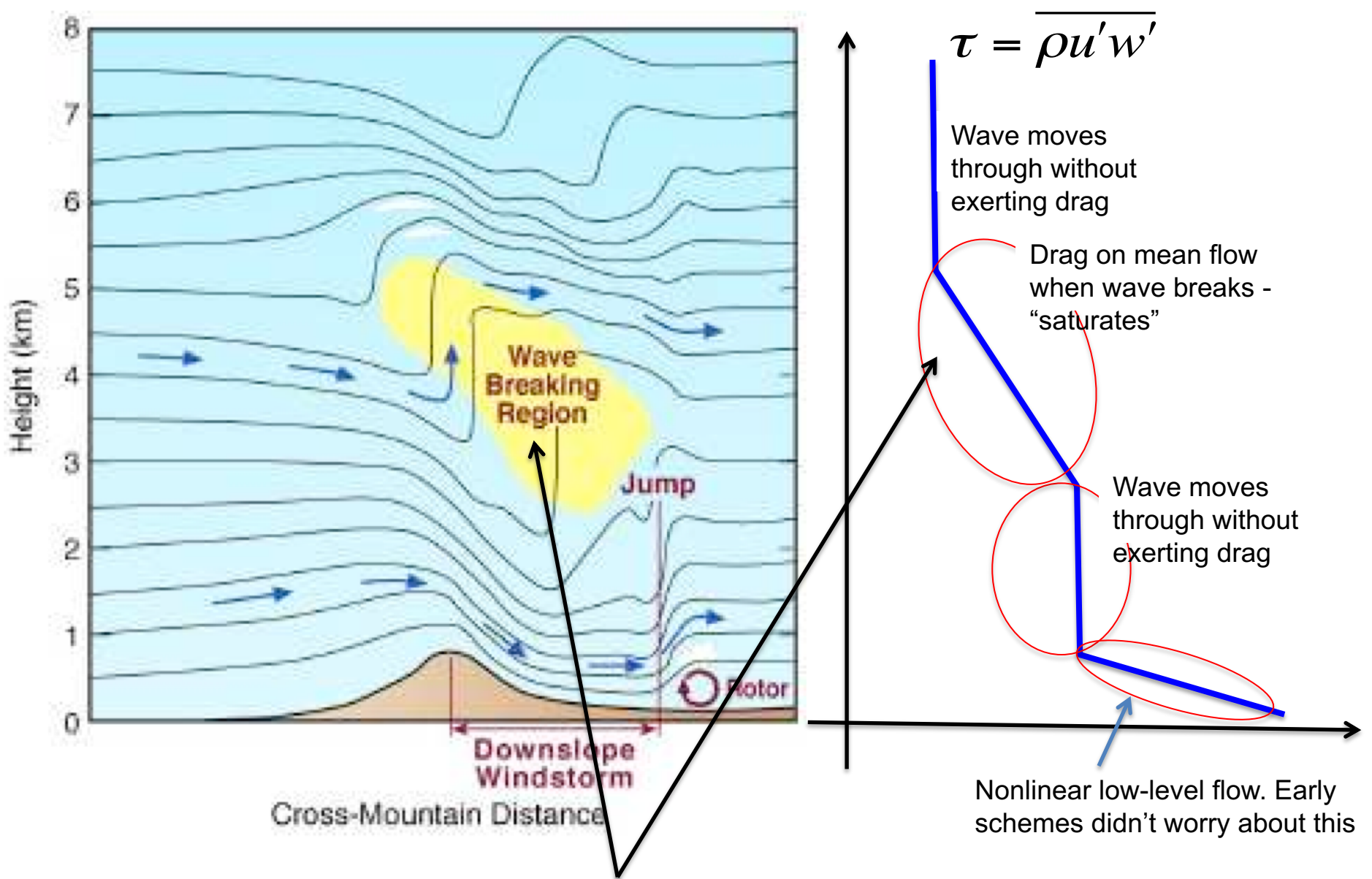
$$\tau \approx C\rho k\bar{U}N\delta^2$$

Intuitively obvious that  $\delta$  at source level is related to mountain heights

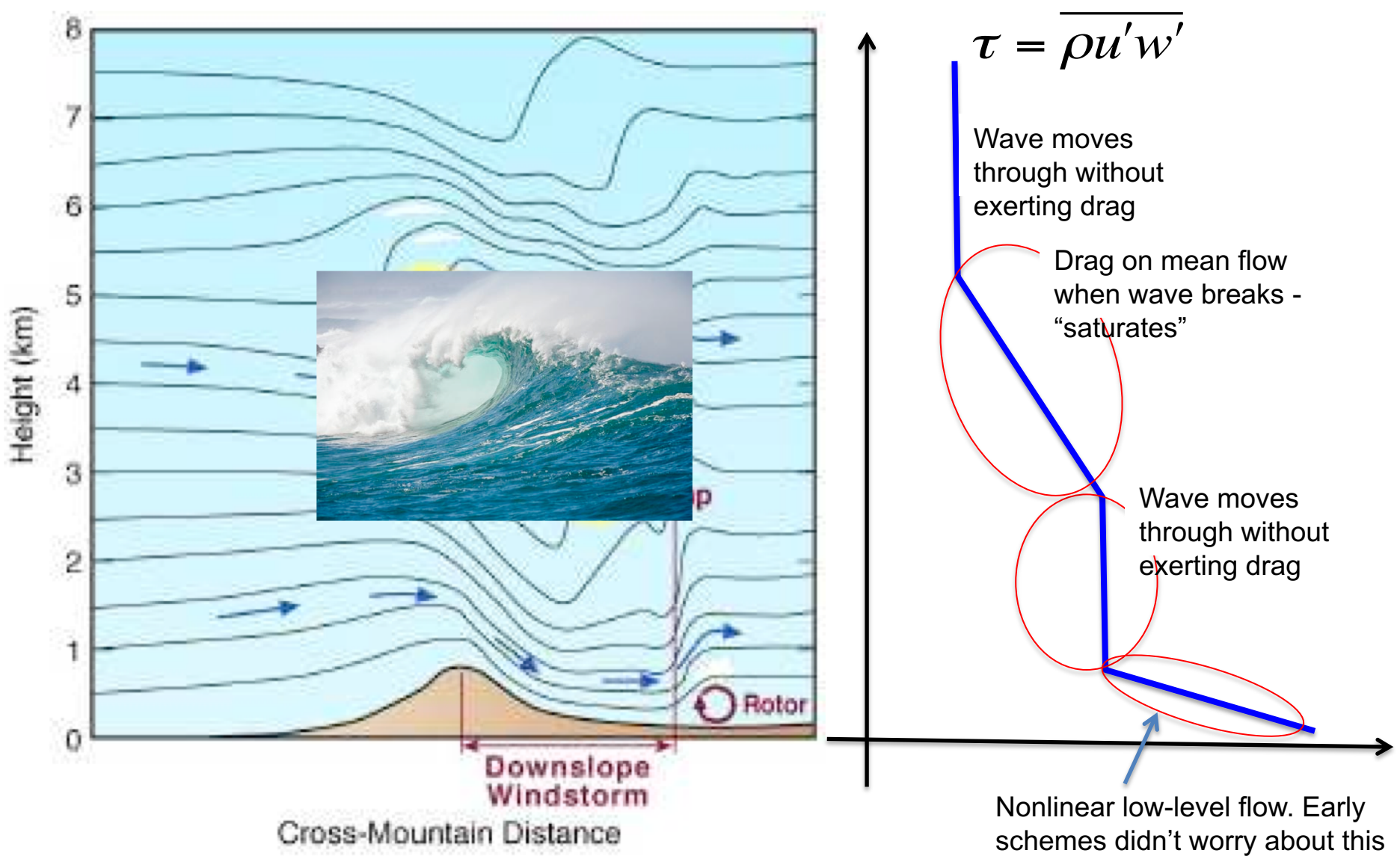
Not so obvious how to get  $\delta$  from topographic data:

- RMS of subgrid topo?
- Residuals left after smoothing ?





What about **“Saturation”**, i.e., wave breaking??



Gravity wave saturation/breaking occurs when streamlines are vertical or overturning → local convective instability

“Saturation hypothesis” holds that turbulence continually shaves off just enough energy to keep breaking wave exactly at edge of instability (vertical streamlines), i.e.,

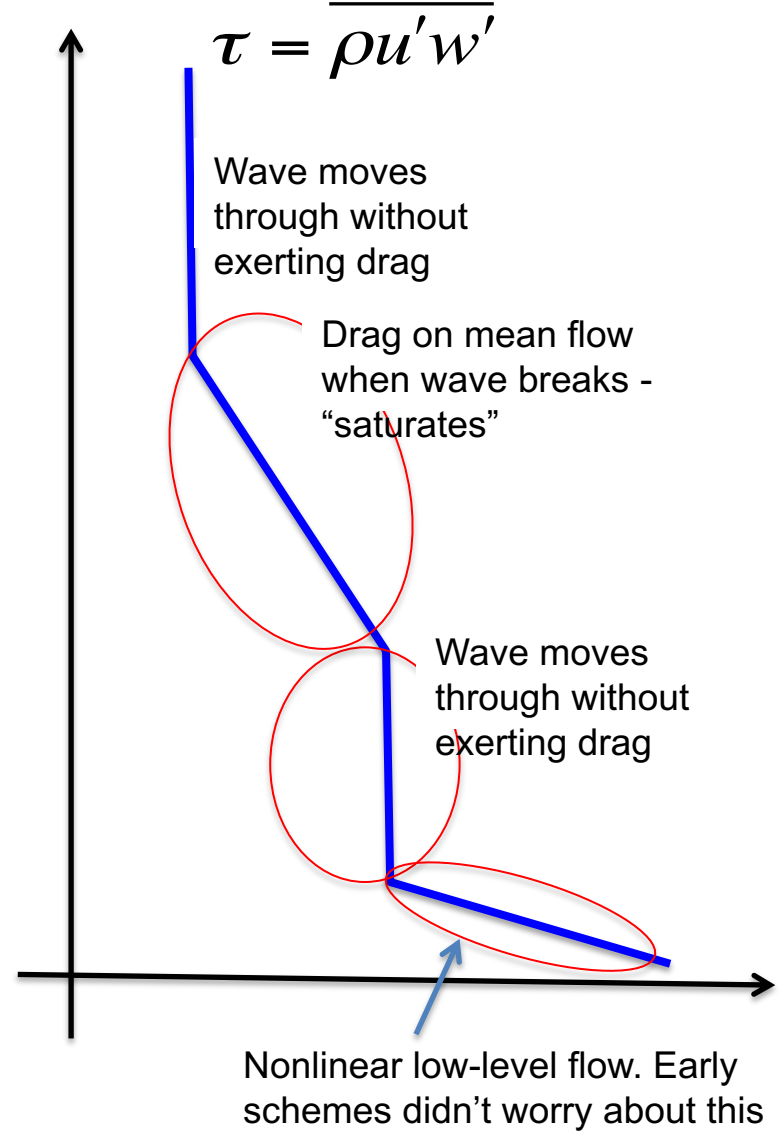


Spilling breaker

*NOT*

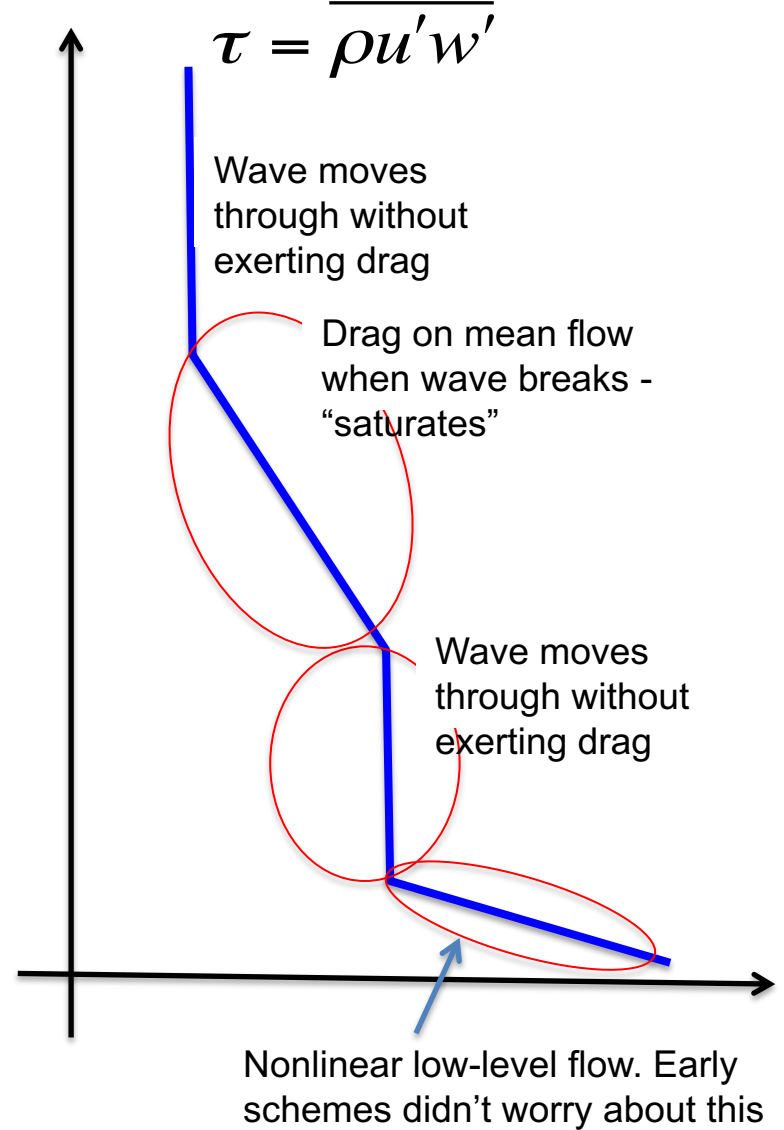


Plunging breaker



***Is saturation hypothesis actually true?*** Probably sometimes. Not bad first g

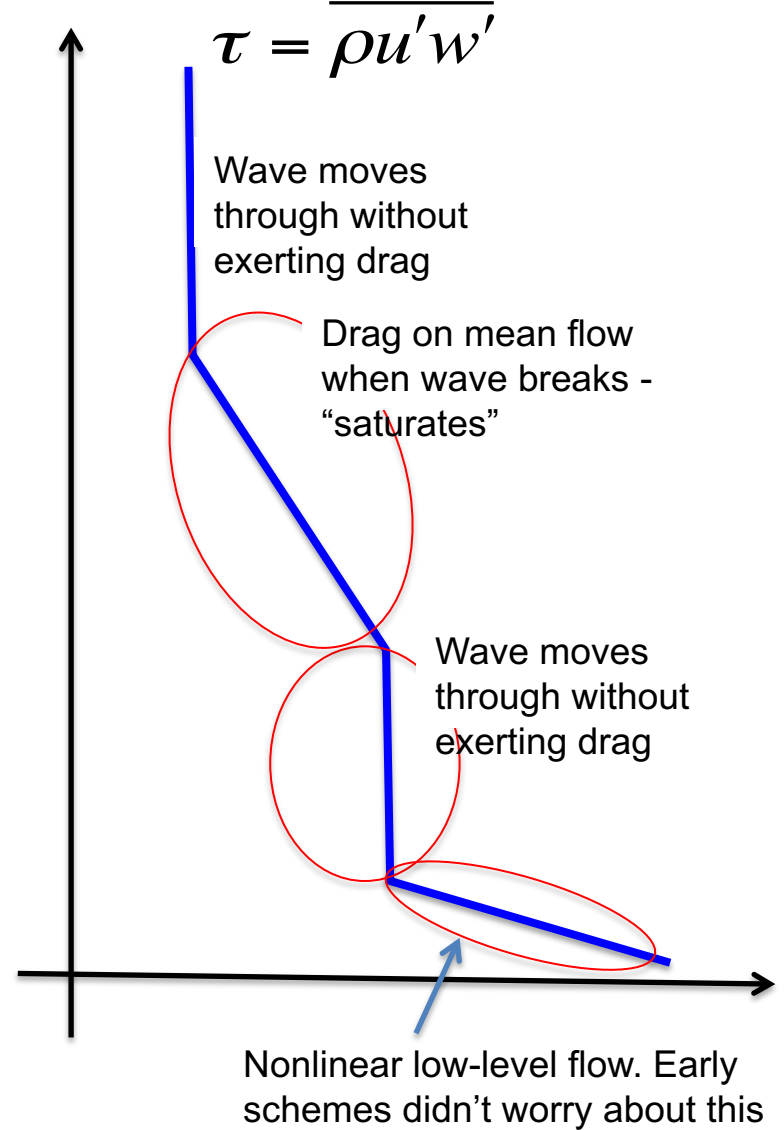
So when do gravity wave streamlines become vertical?



So when do gravity wave streamlines become vertical?

You guessed it. When

$$\delta = \frac{\bar{U}}{N}$$





At this point you have most of what you need to calculate wave momentum flux

Pseudocode:

1) Estimate  $\delta(LM)$  from topography dataset

2) Calculate  $\tau(LM) = \rho k U N \delta^2$

3) Advance to level above:  $\tau(L-1) = \tau(L)$

4) Infer  $\delta(L-1)$

5) Test for  $\delta(L-1) > U/N$

if **no** go to 3)

if **yes** set  $\delta(L-1) = U/N$  recalculate  $\tau(L-1)$  and go to 3)