

# *Wave Modeling and Langmuir Mixing*

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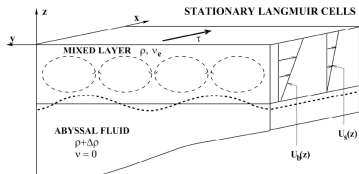
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## *Inverse Turbulent Langmuir Mixing Number*



The inverse turbulent Langmuir mixing number accounts for nonaligned wind and wave fields.

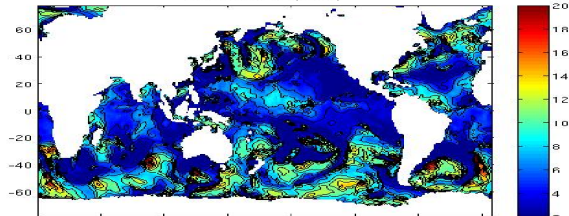
It is defined as

$$La_i = \begin{cases} \left( \frac{U_{stokes} \cdot u^*}{|u^*|^2} \right)^{1/2}, & |\theta| < \pi/2; \\ 0, & |\theta| \geq \pi/2. \end{cases}$$

where  $\theta$  is the difference in wind and wave directions

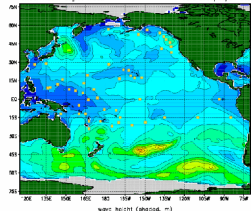
# Previous Work: A Simple Climatology

$1/La^2 - \text{Sec}/\text{Int} (U5/21)$



- Used output from NWW3 to estimate areas of Langmuir mixing and derive a simple climatology

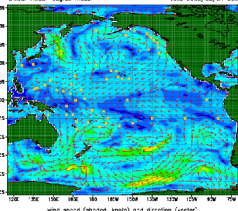
Global 1.25x1 degree model hindcast valid 2005/05/21 06z



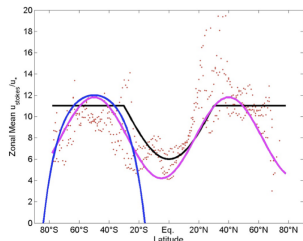
NOAA/NWS/NCEP Marine Modeling and Analysis Branch, 2005/05/21



Global 1.25x1 degree model hindcast valid 2008/05/21 06z



NOAA/NWS/NCEP Marine Modeling and Analysis Branch, 2008/05/21



# A Simple Scaling for Langmuir Depth/Entrainment: (Li & Garrett, 1997)

related to  
CAM  $u^*$  by  
WW3  
Climatology

$$Fr = \frac{\omega}{NH} \approx 0.6 \quad \omega \approx \frac{V}{1.5} \approx \frac{\sqrt{u^* u_s}}{1.5}$$

## The Algorithm

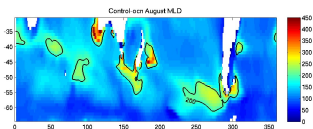
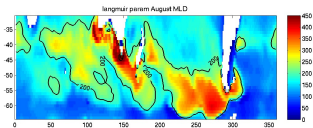
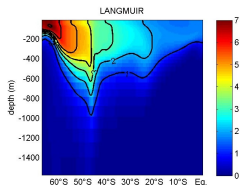
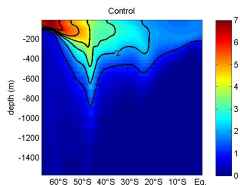
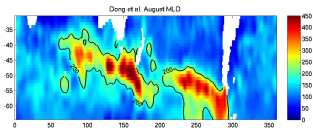
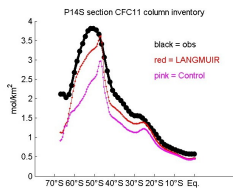
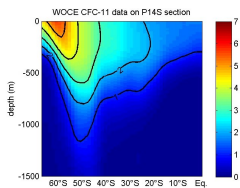
Use  $Fr$  to determine  $H$

If  $H$  is deeper than KPP Boundary Layer depth, use  $H$

Large came up with clever choices for  $N$ ,  $H$  that  
lead to a robust implementation in KPP

With these choices,  $H$  and BLD converge over time.

# Previous Work: Shown Sensitivity to Inclusion

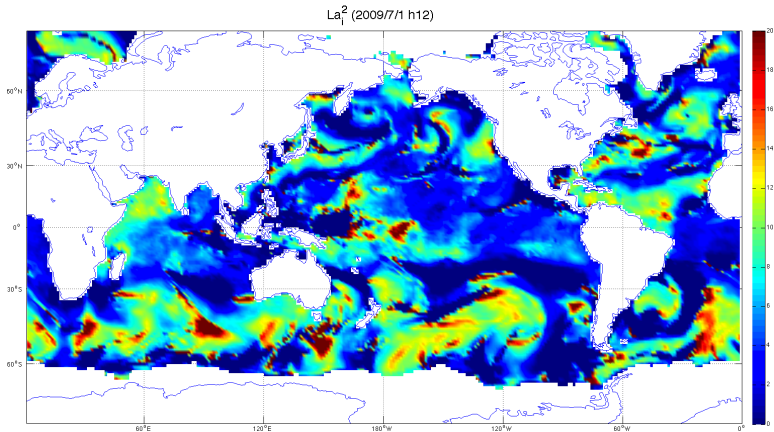


(a) CFC in CCSM 3.5 & P14S WOCE obs

(b) August mixed layer depths

# *Problem 1: Calculating the Surface Friction Velocity*

- Installed WW3 on bluefire (details later)
- Obtained similar calculations of  $La_i$  using WW3's  $u^*$  with COREv2 forcings



## *Problem 2: Estimating Stokes Drift*

For monochromatic waves, it can be shown that at the surface

$$U_{stokes} = \frac{\pi^3 Hs^2}{gTm^3}$$

where  $Hs = 4\sqrt{m_0}$  and  $m_0$  is the zeroth moment of the variance.

*However, this is not true for anything other than monochromatic waves.*

### *Problem 3: Different Definitions of Mean Wave Period*

WaveWatch:  $Tm_0 = \overline{(f^{-1})}$

ERA40:  $Tm_1 = 1/(\overline{f})$

TOPEX:  $Tm_2 = 1/\sqrt{\overline{(f^2)}}$

$$m_n = \int_0^{2\pi} \int_0^\infty f^n S(f, \theta) df d\theta$$

$$Tm_0 = \frac{m_{-1}}{m_0}, \quad Tm_1 = \frac{m_0}{m_1}, \quad Tm_2 = \left( \frac{m_0}{m_2} \right)^{1/2}$$



## *A Quick Example*

### *Pierson-Moskowitz Spectrum*

$$S(f, \theta) = S(f) = \frac{\alpha g^2}{(2\pi)^4} f^{-5} \text{Exp} \left[ -\frac{5}{4} \left( \frac{f_p}{f} \right)^4 \right]$$

where  $\alpha$  is the Phillips constant and  $f_p$  the peak frequency

$$(Tm_0/Tm_1)^3 = 1.37, \quad (Tm_0/Tm_2)^3 = 1.76$$

$$(Tm_1/Tm_2)^3 = 1.28$$

## Calculating Stokes Drift Using 2-D Spectrum

From previous work by Kenyon (1969) and McWilliams & Restrepo (1999), we can reformulate Stokes drift using the 2-D spectrum as

$$\begin{aligned}U_{stokes} &= \frac{16\pi^3}{g} \int_0^{2\pi} \int_0^\infty f^3 S(f, \theta) df d\theta \hat{\mathbf{e}}_d \\ &= \frac{16\pi^3}{g} m_3 \hat{\mathbf{e}}_d\end{aligned}$$

where  $\hat{\mathbf{e}}_d$  is the dominant direction of wave propagation.

*As a result, we no longer need the previous  $U_{stokes}$  approximation!*

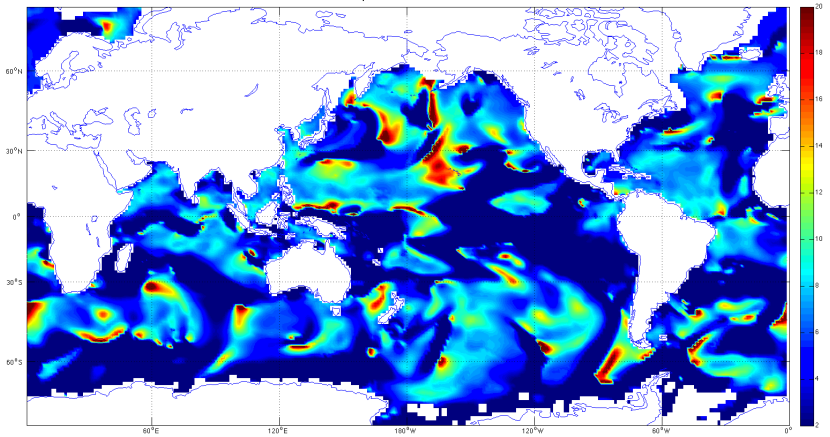
## *Refining our Stokes Drift Approximation*

- Would still like to be able to estimate Stokes drift using satellite and buoy data for comparison
- Currently examining if there is an empirical or mathematical relationship that we can use such as

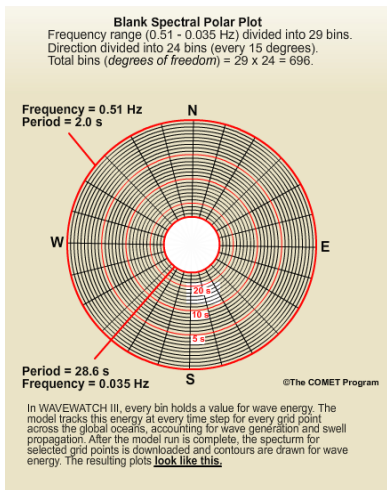
$$U_{stokes} \approx a(f) \frac{\pi^3 Hs^2}{gTm^3} \hat{\mathbf{e}}_d$$

# *Current Estimate of $La_i^2$*

$La_i^2$  (1993/2/8 h00)



## Problem 4: Numerical Cost



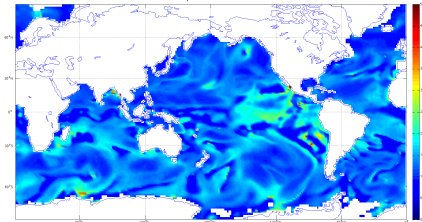
- 3<sup>rd</sup> generation wave model
- Solves the spectral action density balance equation
- 15-20 sec per time step (1 hr) for one processor ( $\approx 35\text{-}50$  hr/yr)
- Plan on scaling back the number of bins significantly and turning off some interactions
- Alternative 2<sup>nd</sup> generation model developed by George Mellor (Princeton) worth exploring

## *Applications of Coupling a Wave Model*

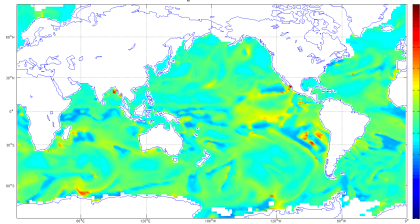
- Calculate Langmuir Mixing forcing prognostically
  - A coupled wave model will allow use of more sophisticated and validated parameterizations (e.g., Smyth et al, 04; Harcourt & D'Asaro, 08; Grant & Belcher, 09)
- Improve the air-sea momentum flux
- Improve the air-sea tracer flux
- Conduct climate change studies like erosion
- Others?

# Some Properties of $a(f)$

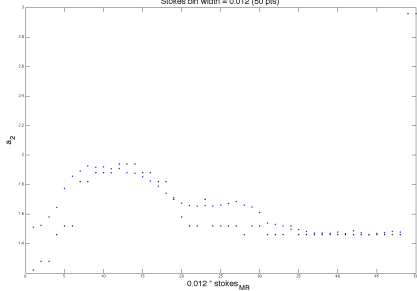
$a_1$  (1993/28 h00)



$a_2$  (1993/28 h00)



Stokes bin width = 0.012 (50 pts)



Stokes Comparison to M & R calculation

