

# A traceability framework to facilitate model evaluation

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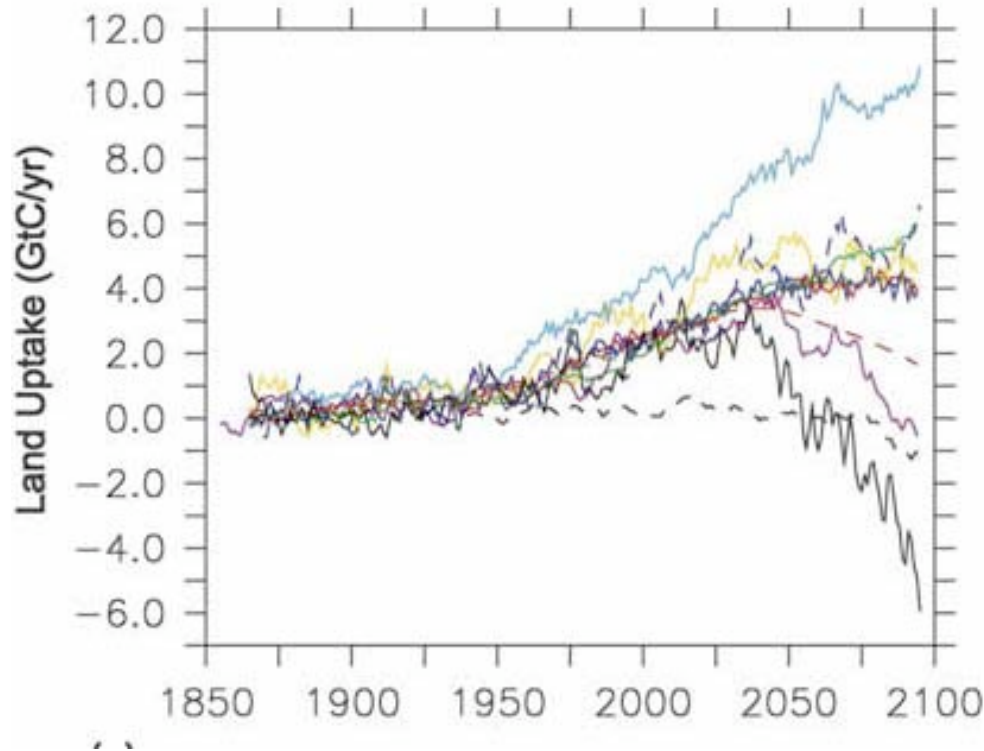


# Model Tractability

“There is a danger that we shall replace a world we do not understand by a model of the world we do not understand”

-----John Maynard Smith 1992 *Nature*

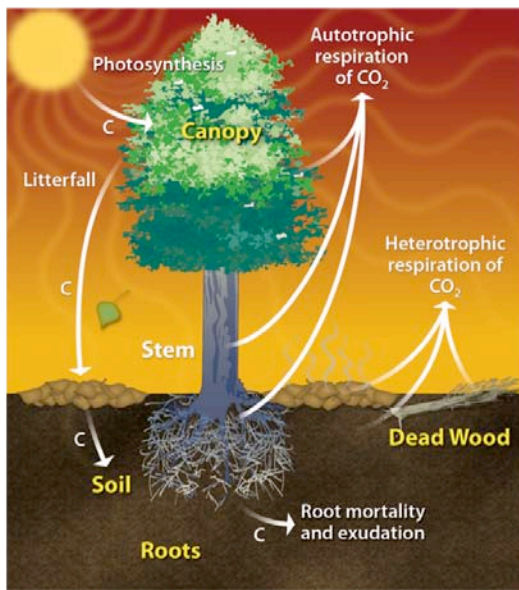
# Challenges



- Models behave so differently;
- Does the uncertainty reflect natural variability or mainly result from artifacts in models? ;
- It's essential to eliminate model artifacts as much as possible.
- How to identify them?

“Metrics/diagnostics for component model assessment”

--- Brian O’Neill  
CESM guidance



A: Basic processes

# Theoretical analysis

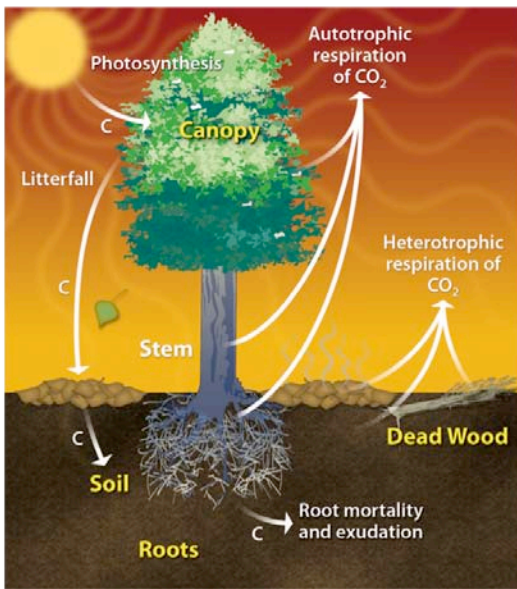
1. Photosynthesis as the primary C influx pathway
2. Compartmentalization,
3. Partitioning among pools
4. Donor-pool dominated carbon transfers
5. 1st-order kinetic transfers from the donor pools

Luo et al. 2003 GBC

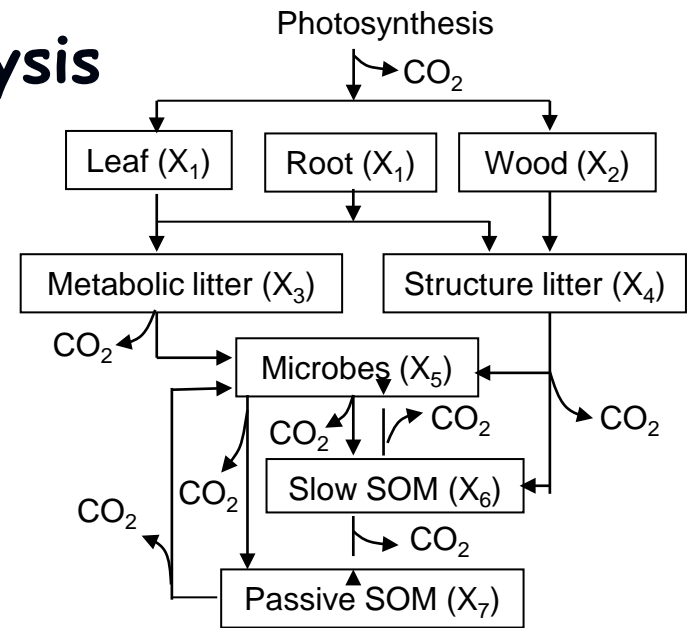
Luo and Weng 2011 TREE

Luo et al. 2012

# Theoretical analysis



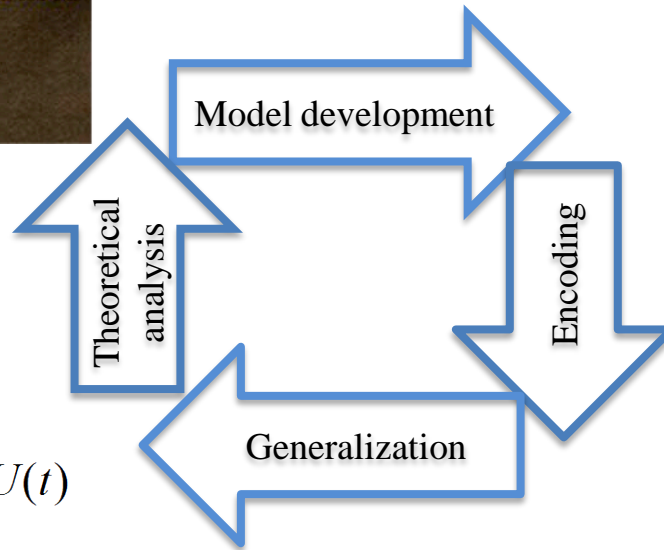
A: Basic processes



B: Shared model structure

D: General model

$$\begin{cases} \frac{dX(t)}{dt} = \xi ACX(t) + BU(t) \\ X(t=0) = X_0 \end{cases}$$



C: Similar algorithm

$$\text{Plant} \begin{cases} dX_1(t)/dt = b_1U(t) - \xi c_1X_1(t) \end{cases}$$

- Luo et al. 2003 GBC
- Luo and Weng 2011 TREE
- Luo et al. 2012

$$\begin{aligned} & a_{75}x_5(t) + c_6a_{76}x_6(t) - c_7X_7(t)] \\ dX_8(t)/dt = \xi & [c_6a_{86}x_6(t) + c_7a_{87}x_7(t) - c_8X_8(t)] \end{aligned}$$

# System equations

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Empirical evidence

1. First-order decay of litter decomposition (Zhang et al. 2008)
2. Carbon release from soil incubation data (Schaedel et al. 2012)
3. Ecosystem recovery after disturbance (Yang et al. 2011)
4. General behavior of CMIP5 models (Todd-Brown et al. 2013)

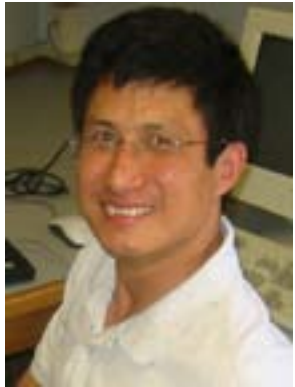
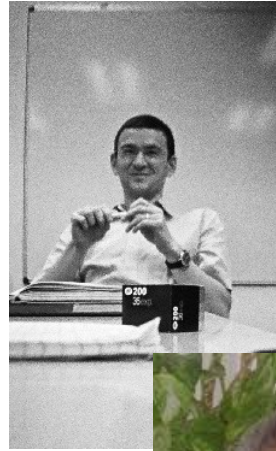
$$\begin{cases} \frac{dX(t)}{dt} = \xi(t)AX(t) + bU(t) \\ X(0) = X_0 \end{cases}$$

Mathematical and ecological properties (Luo et al. 2012)

Dynamic disequilibrium (Luo and Weng 2011)



# working group





# Applications

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$$\begin{cases} \frac{dX(t)}{dt} = \xi(t)AX(t) + bU(t) \\ X(0) = X_0 \end{cases}$$

1. Predictability of the terrestrial carbon cycle (Luo et al. in prep.)
2. Computational efficiency of spinup (Xia et al. 2012)
3. Traceability for model analysis (Xia et al. 2013)
  - a. Impacts of additional modules
  - b. Attribution of uncertainty to its Sources
  - c. Model intercomparison
4. Facilitating data assimilation (Hararuk et al. To be submitted)

The “**traceability**” of terrestrial carbon cycle is mathematically solved as:

$$\frac{dX(t)}{dt} = BU(t) - \xi(t)ACX(t) \quad (1)$$

According to equation (1), when an ecosystem at steady state, the steady-state ecosystem carbon pool size (i.e., ecosystem carbon storage capacity;  $X_{ss}$ ) is:

$$X_{ss} = \xi^{-1}(AC)^{-1}BU_{ss} = \xi^{-1}\tau_E'U_{ss} = \tau_E U_{ss} \quad (2)$$

where  $\tau_E'$  represents the baseline residence times of different carbon pools which are determined by the partitioning and transfer coefficients in equation 1 as:

$$\tau_E' = (AC)^{-1}B \quad (3)$$

The actual residence time ( $\tau_E$ ) of an ecosystem in the equation 2 is modified from  $\tau_E'$  by the environmental scalar ( $\xi$ ) as:

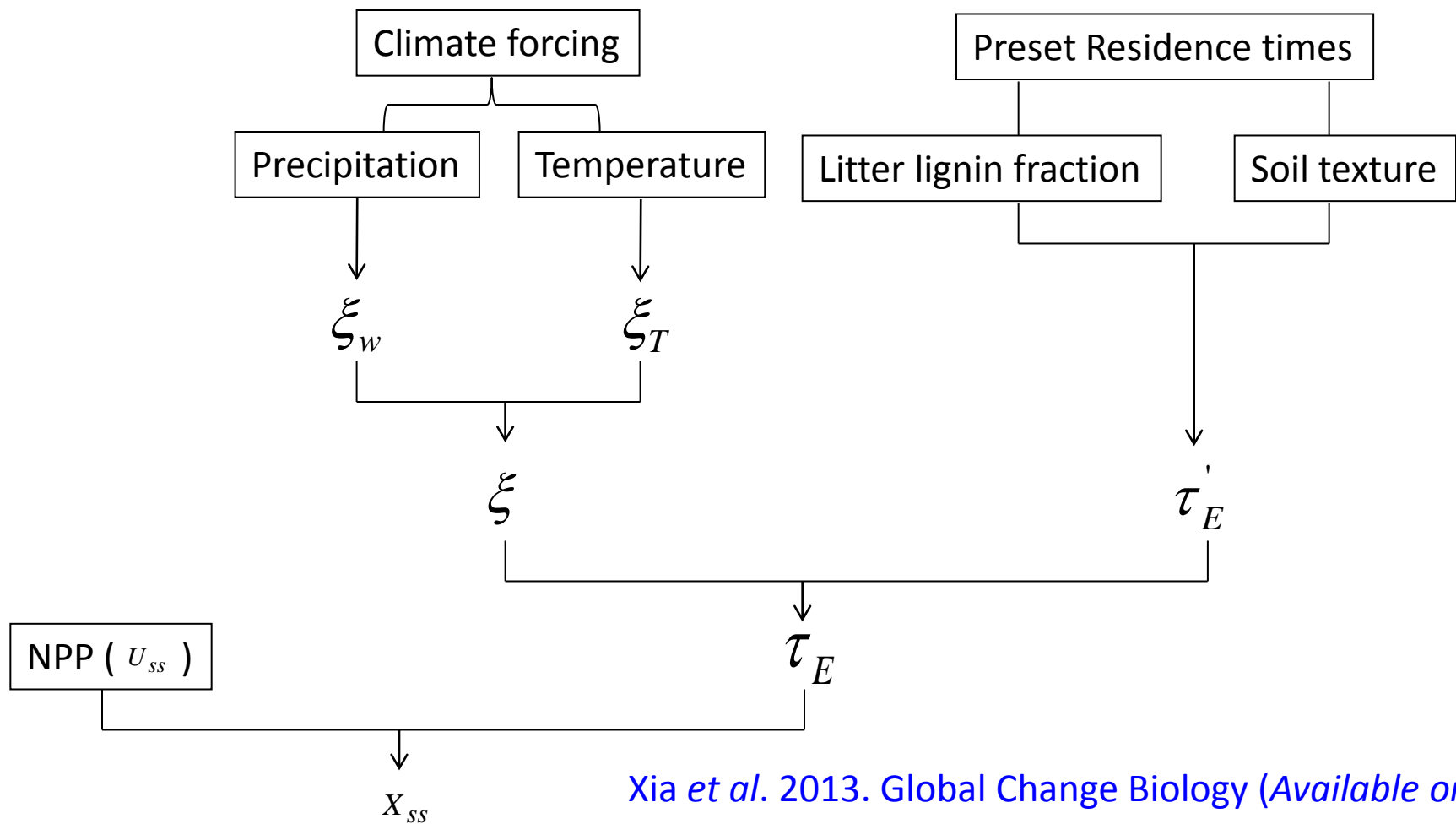
$$\tau_E = \xi^{-1}\tau_E' \quad (4)$$

For litter and soil carbon pools,  $\xi$  usually is calculated from temperature  $\xi_T$  and water  $\xi_W$  as:

$$\xi = \xi_T \xi_W \quad (5)$$

*Xia et al. 2013. Global Change Biology (Available online)*

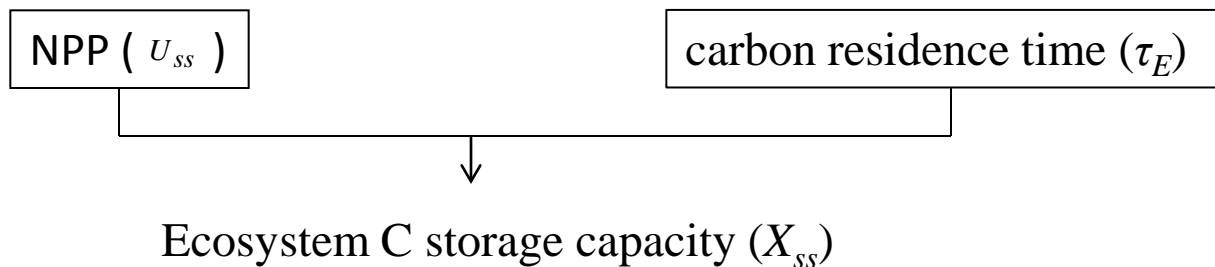
# The traceability framework



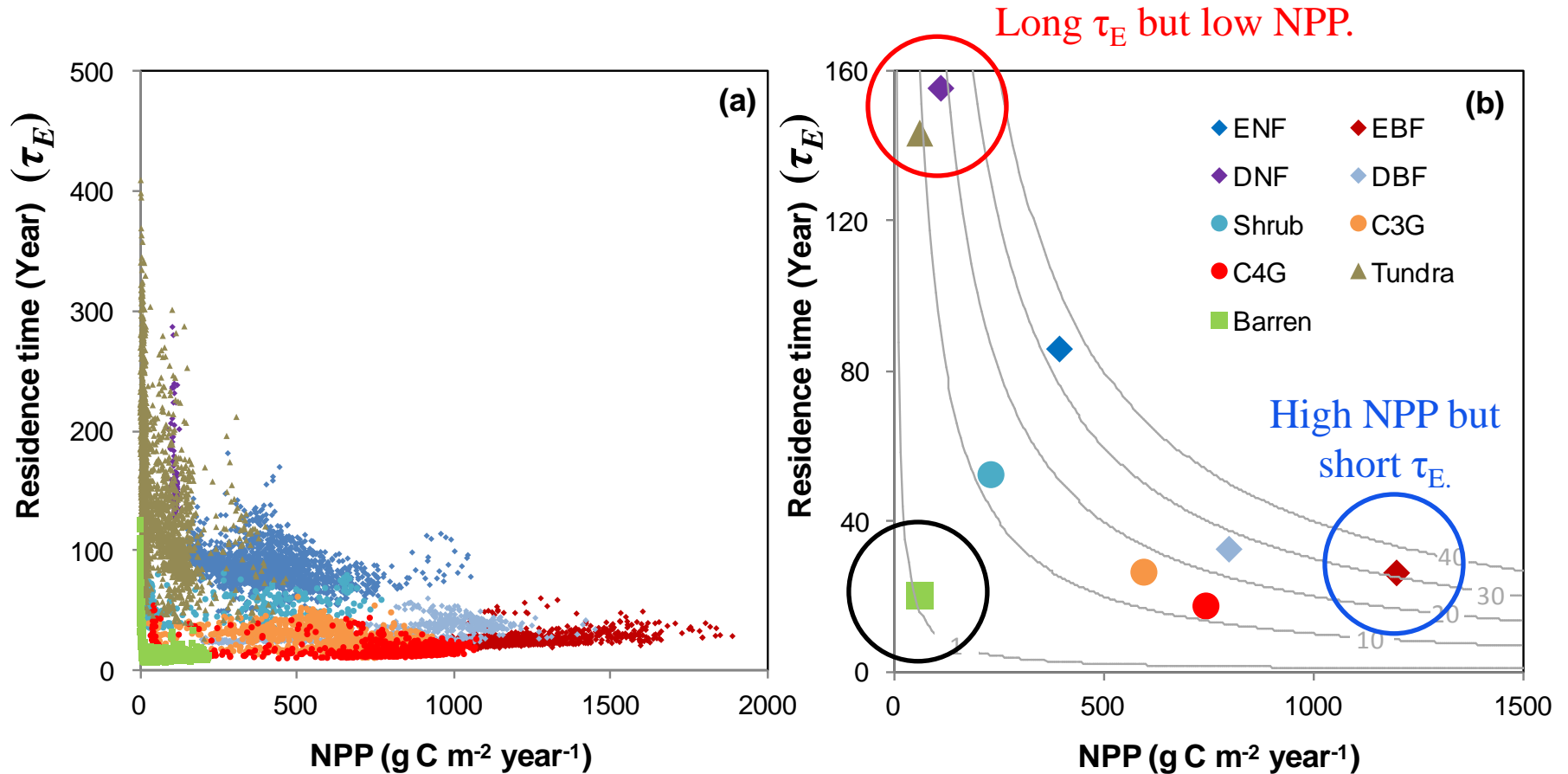
Xia et al. 2013. Global Change Biology (Available online)

Ecosystem carbon storage capacity ( $X_{ss}$ ) is determined by ecosystem carbon influx (i.e., NPP;  $U_{ss}$ ) and ecosystem carbon residence time ( $\tau_E$ ).

Luo et al, 2003. GBC

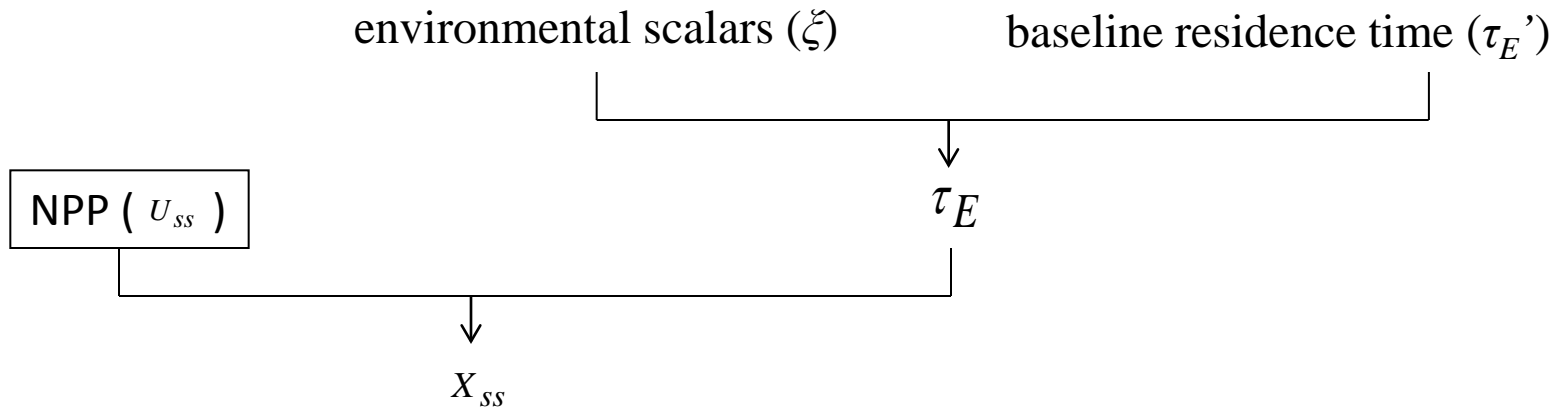


# Differential determinants on carbon storage capacity among biomes



Based on spin-up results from CABLE with 1990 forcings.

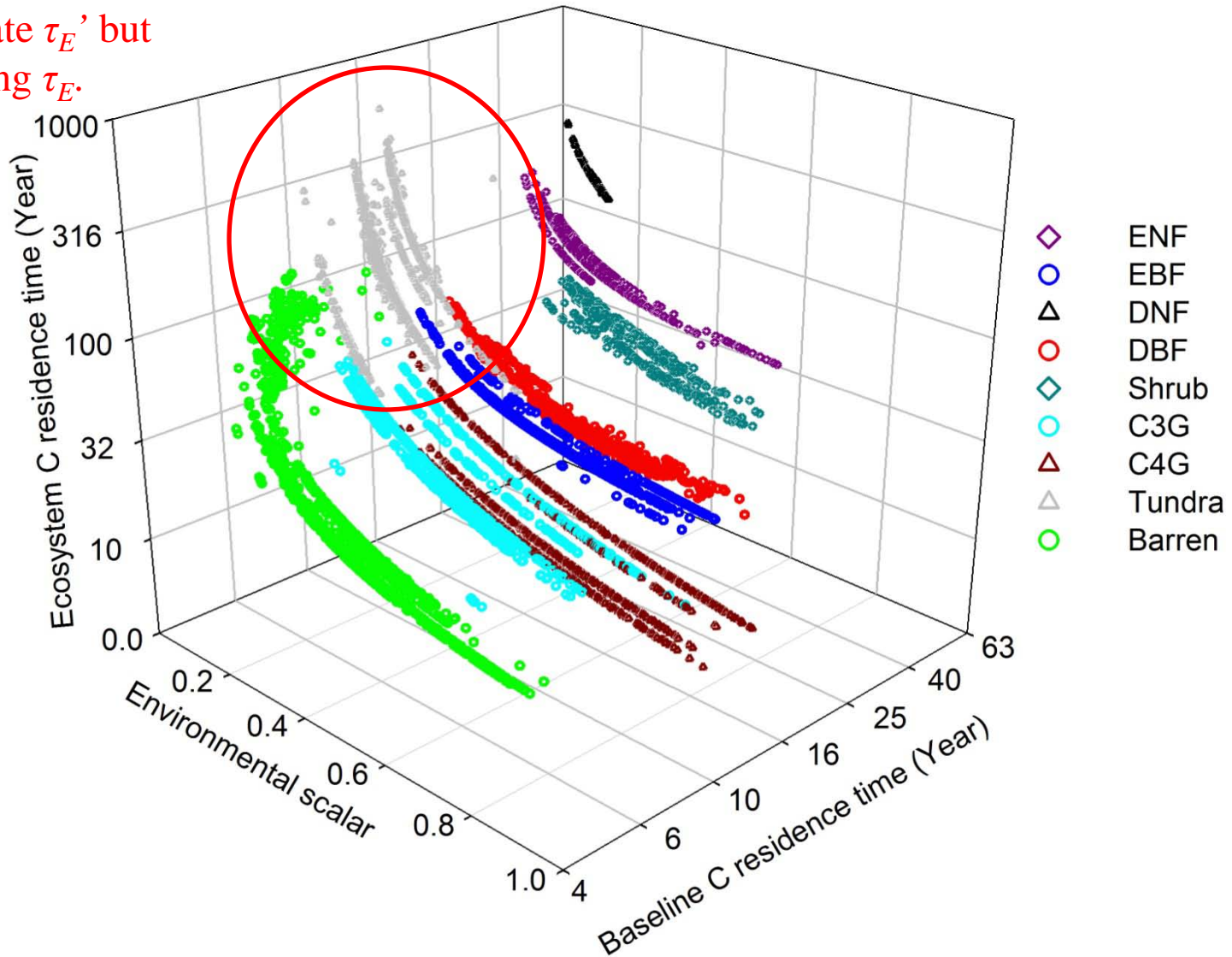
Ecosystem carbon residence time ( $\tau_E$ ) is modified from baseline residence time ( $\tau_E'$ ) by environmental scalars ( $\zeta$ ).



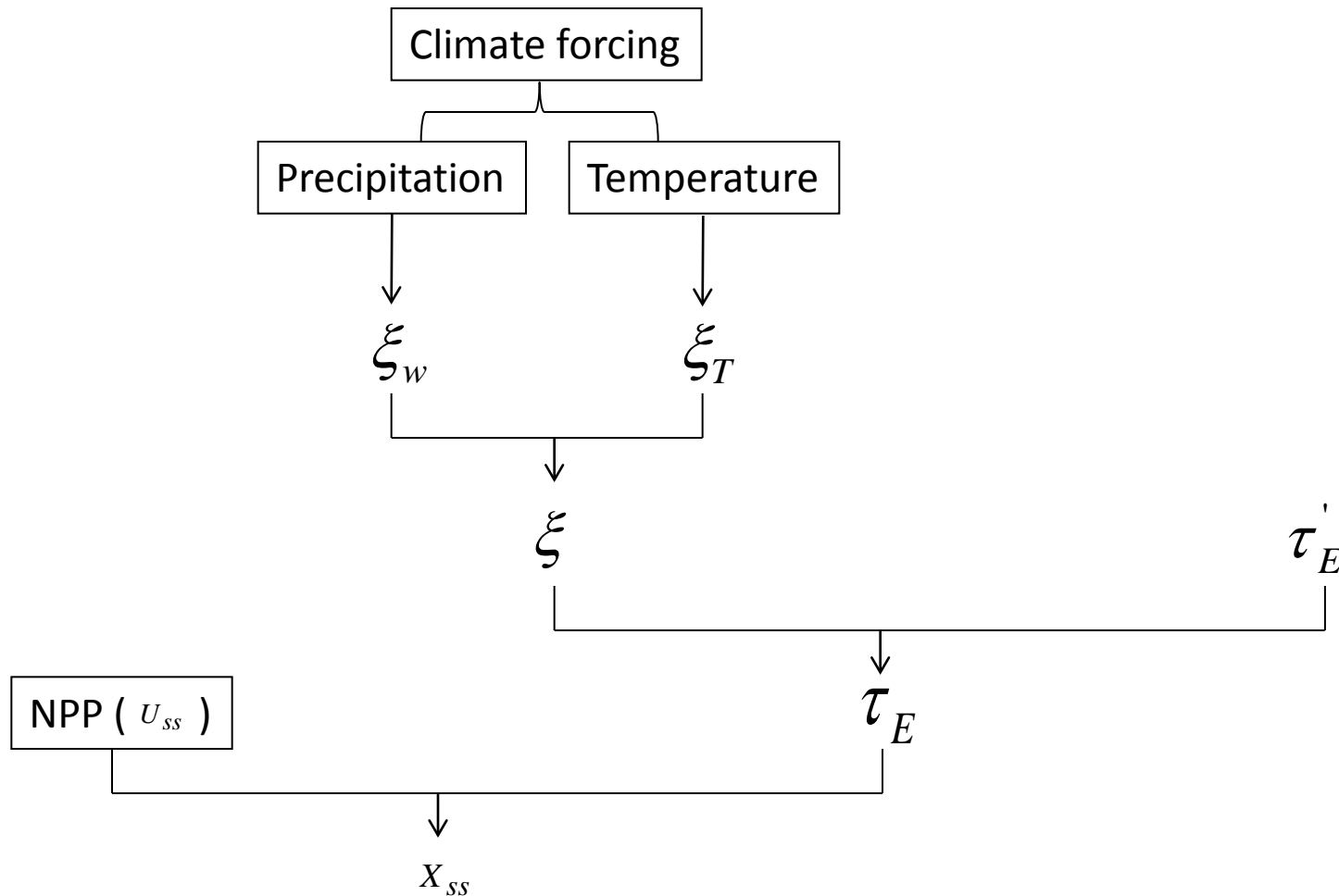
# Modification of environmental scalars on baseline carbon residence times

## Tundra:

Moderate  $\tau_E$ ' but very long  $\tau_E$ .

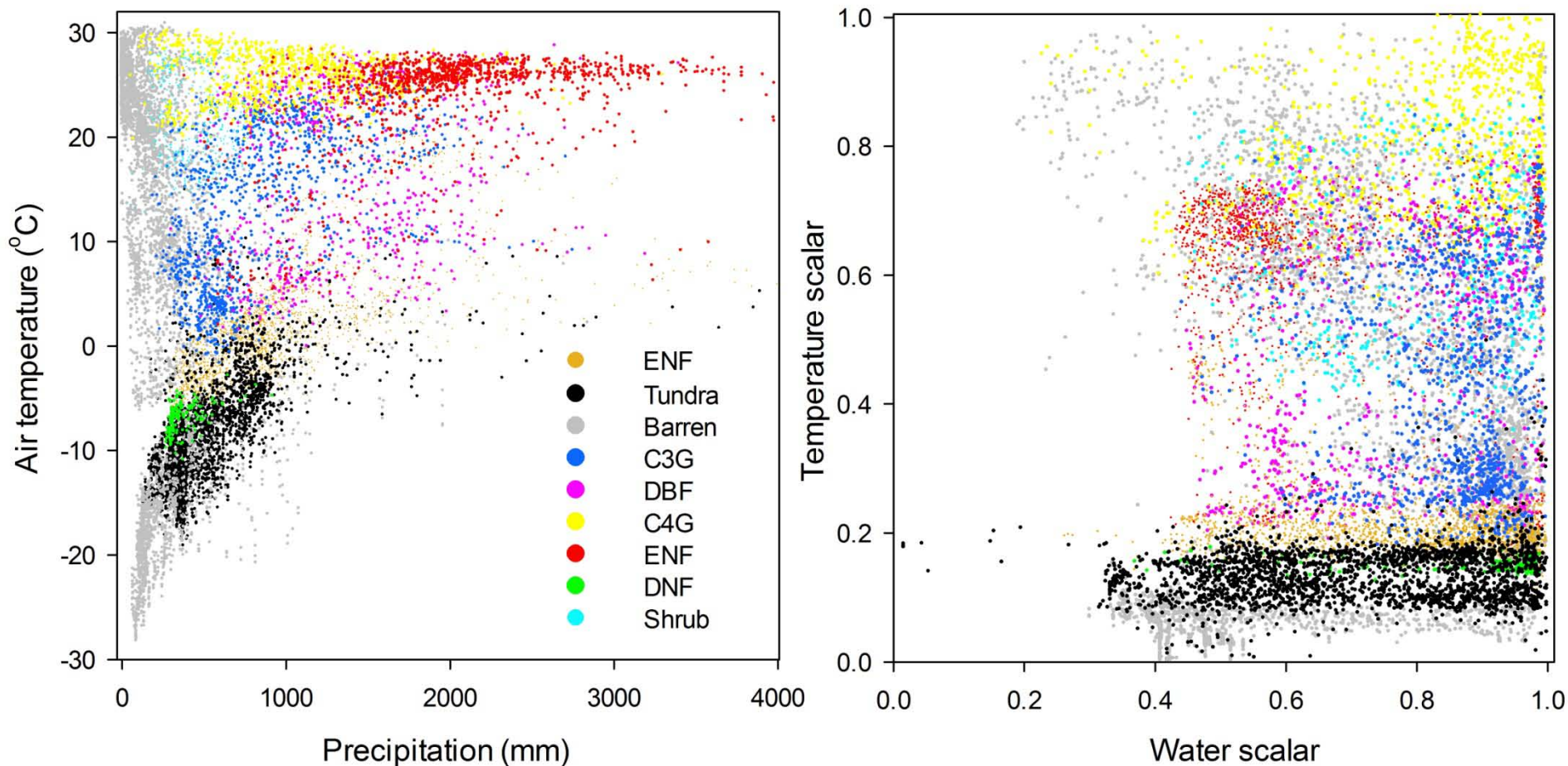


Temperature and water scalars link environmental space (air temperature and precipitation) into the C space.



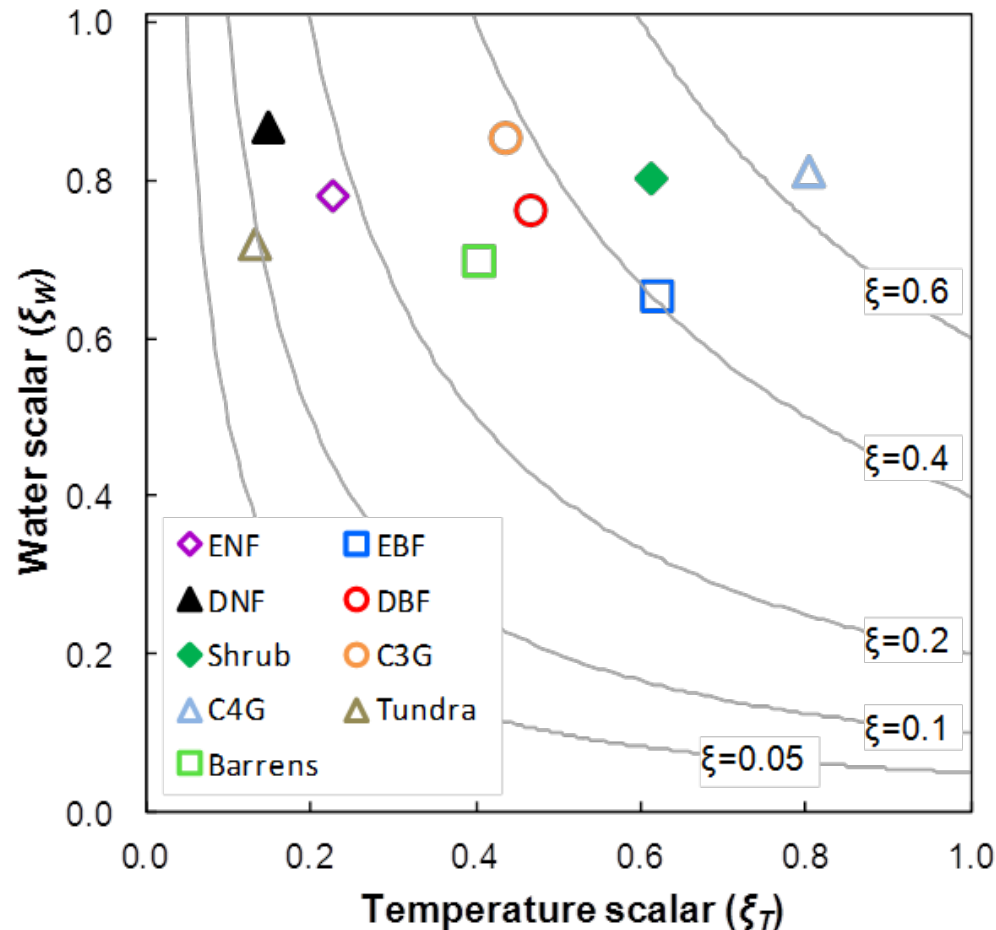


Temperature and water scalars link environmental space (air temperature and precipitation) into the C space.



Cropland is excluded in this study. Input forcing in 1990.

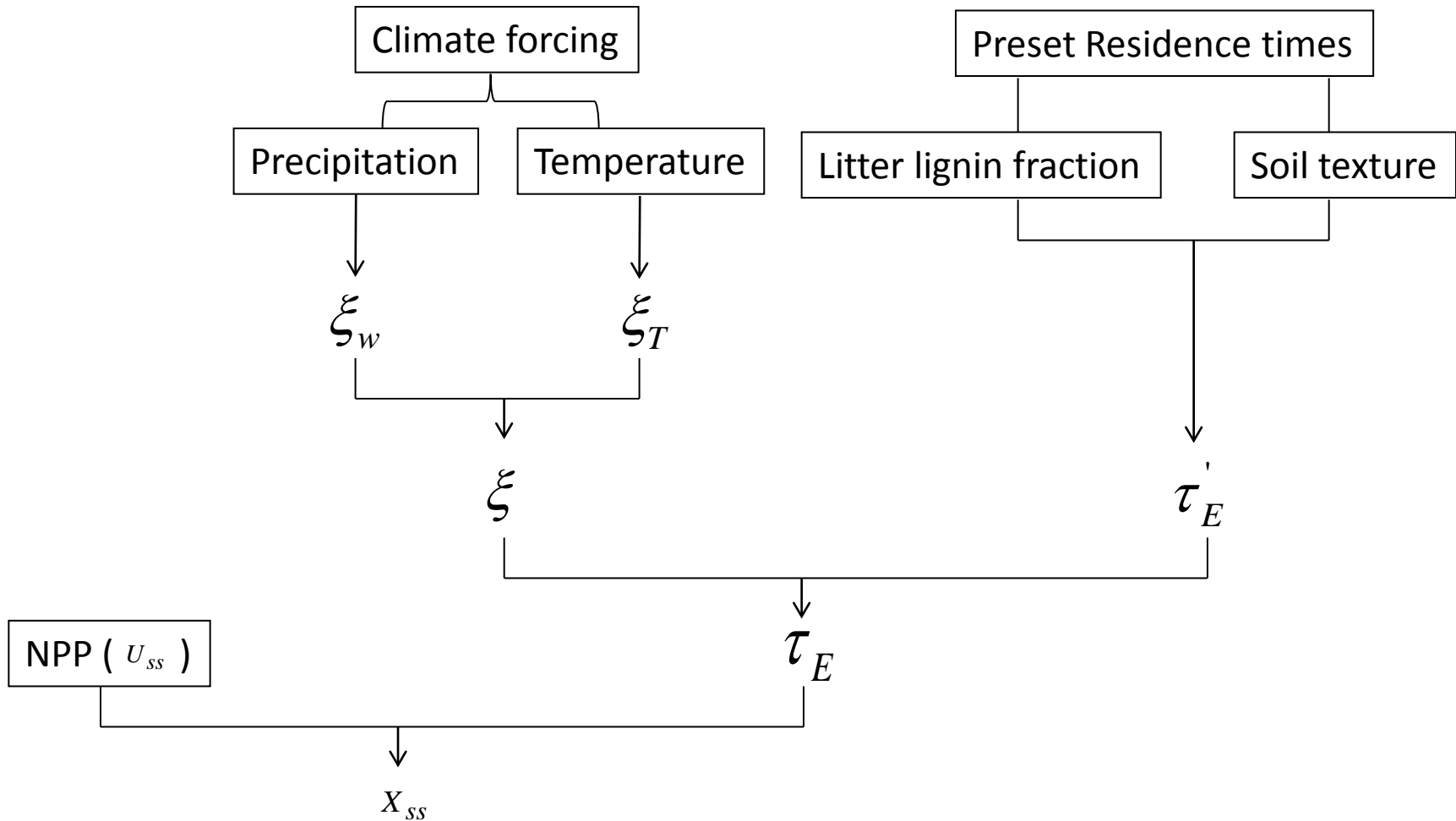
Temperature and water scalars link environmental space (air temperature and precipitation) into the C space.

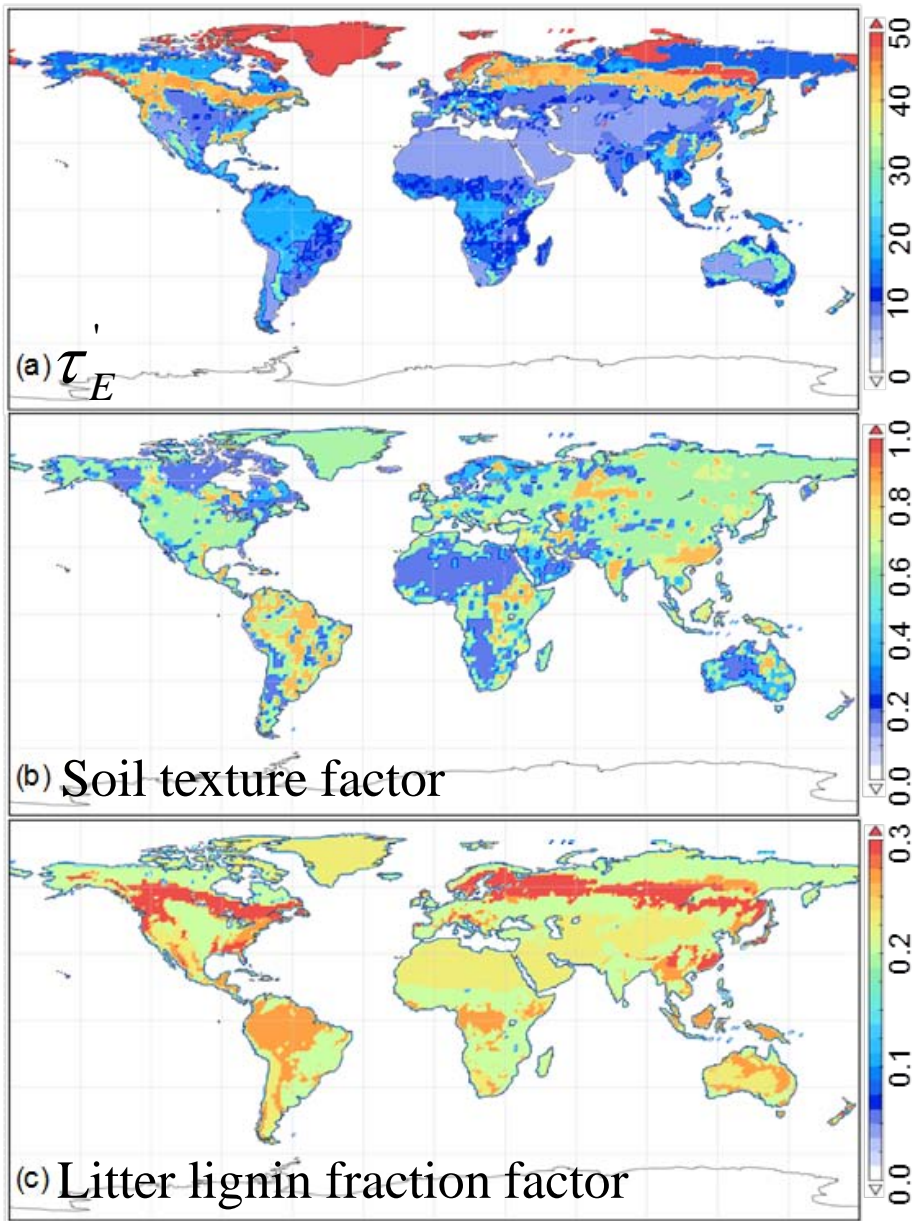


In CABLE model, the differences in environmental scalars among biomes are more determined by the temperature scalar.

The environmental limitation on  $\tau_E$ ' is largest in Tundra and needleleaf forests.

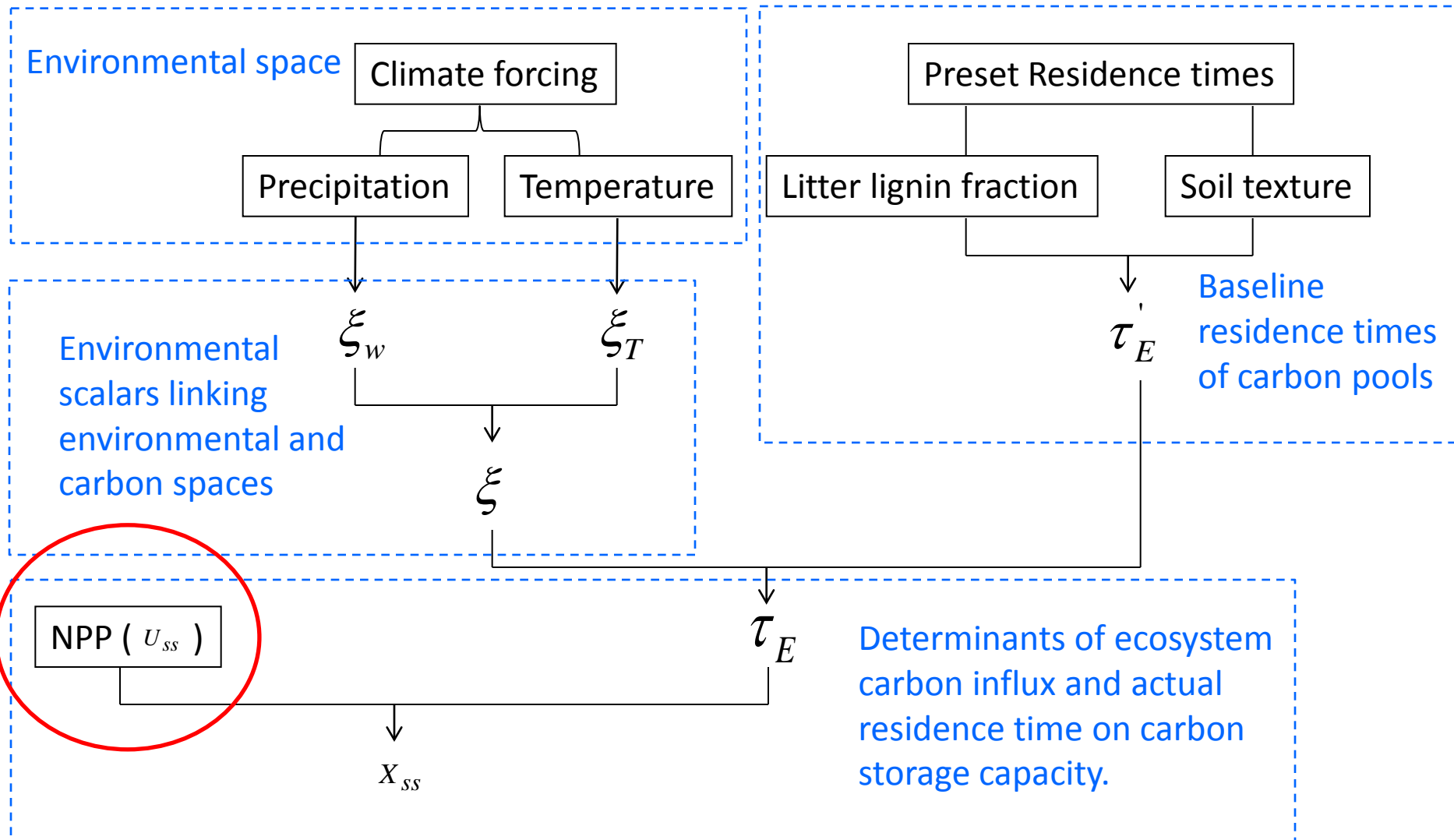
Litter lignin fraction and soil texture spatially modified the preset residence times into baseline carbon residence times in different grids.



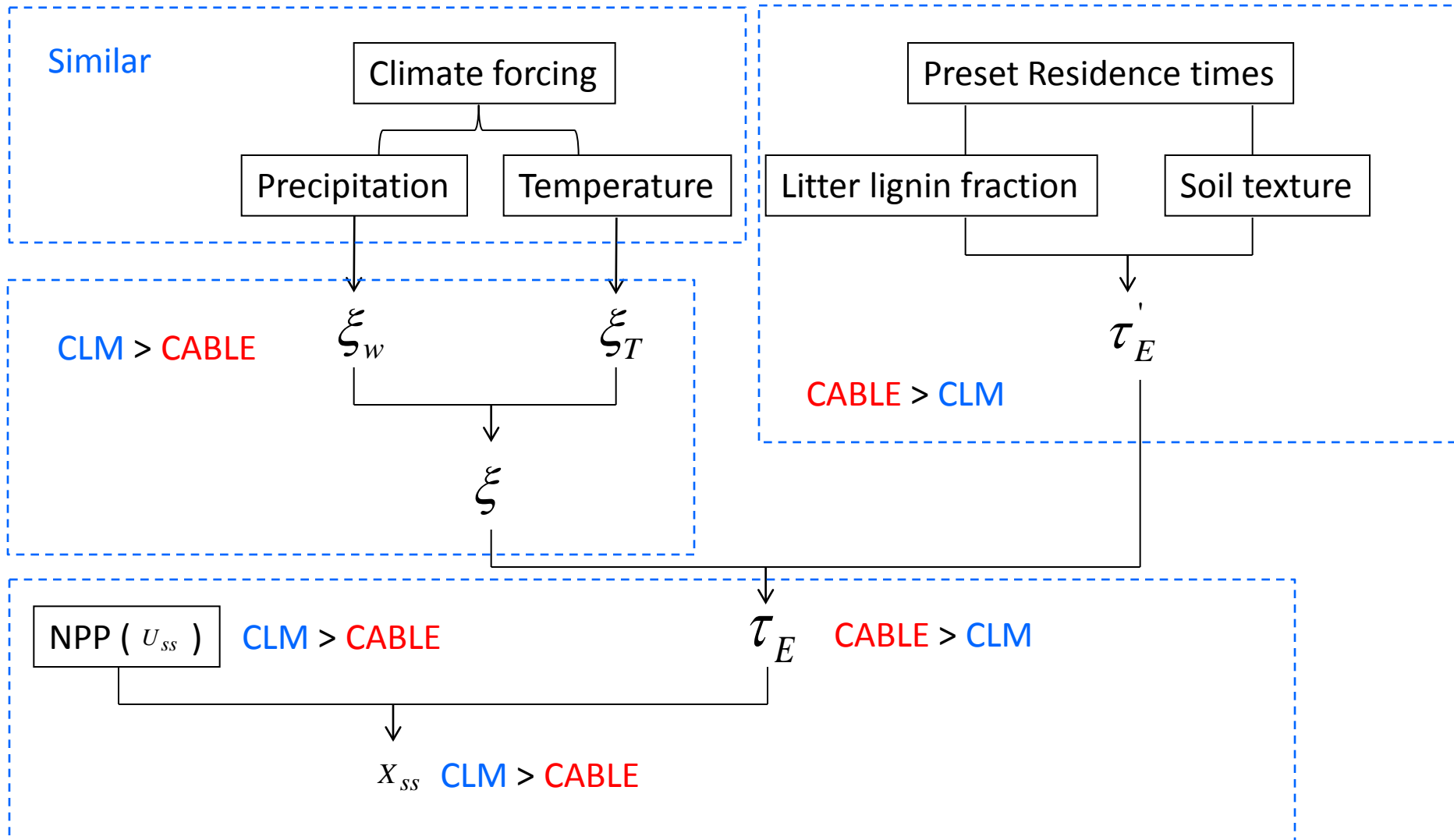


**Litter lignin fraction and soil texture influence spatially distribution of C turnover rates**

# A traceable framework for terrestrial C cycle

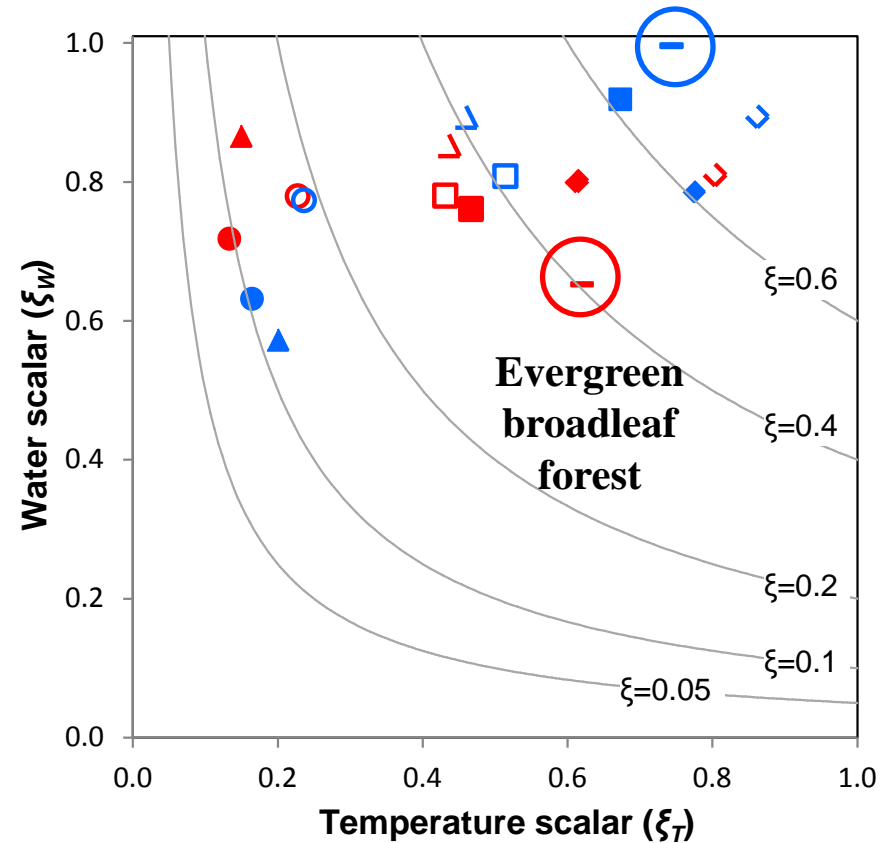
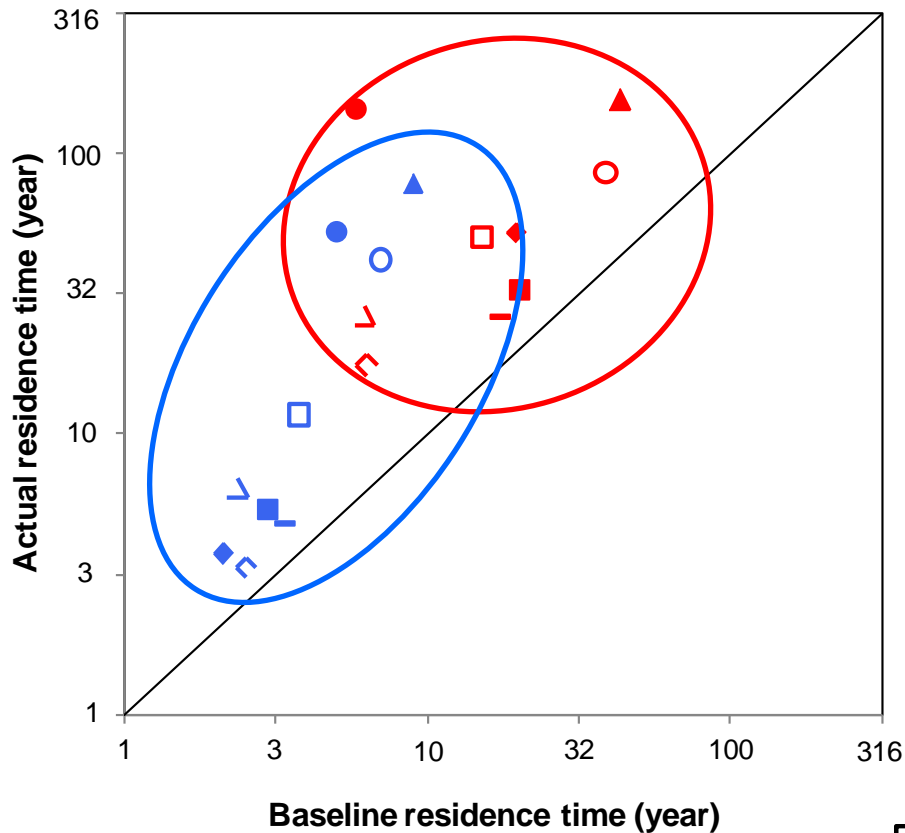


# Model intercomparison



# Longer residence times in CABLE than CLM-CASA

$$\tau_E = \xi^{-1} \tau'_E$$

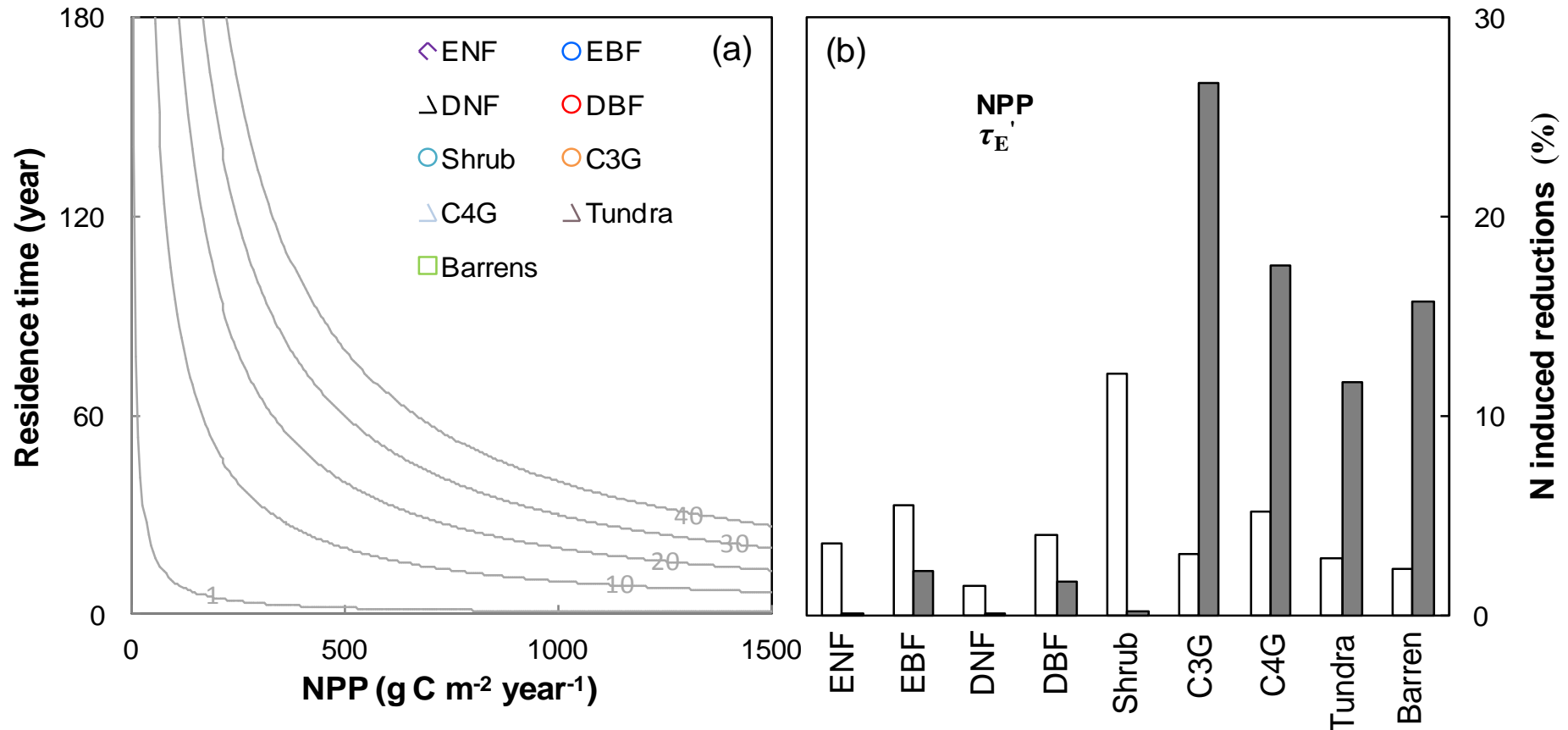


**CABLE**  
**CLM-CASA**

○ ENF	— EBF
▲ DNF	■ DBF
◆ Shrub	▲ C3G
◇ C4G	● Tundra

# Impacts of incorporating nitrogen cycle into CABLE model

Xia *et al.* 2013 *Global Change Biology*



- reduces  $X_{SS}$  in all biomes in comparison with that in the carbon-only model;
- mainly by decreasing NPP in woody biomass and via shortened  $\tau_E'$  in other biomes.



# Attribution of model uncertainty to its sources

$$\begin{cases} \frac{dX(t)}{dt} = \xi(t)AX(t) + bU(t) \\ X(0) = X_0 \end{cases}$$

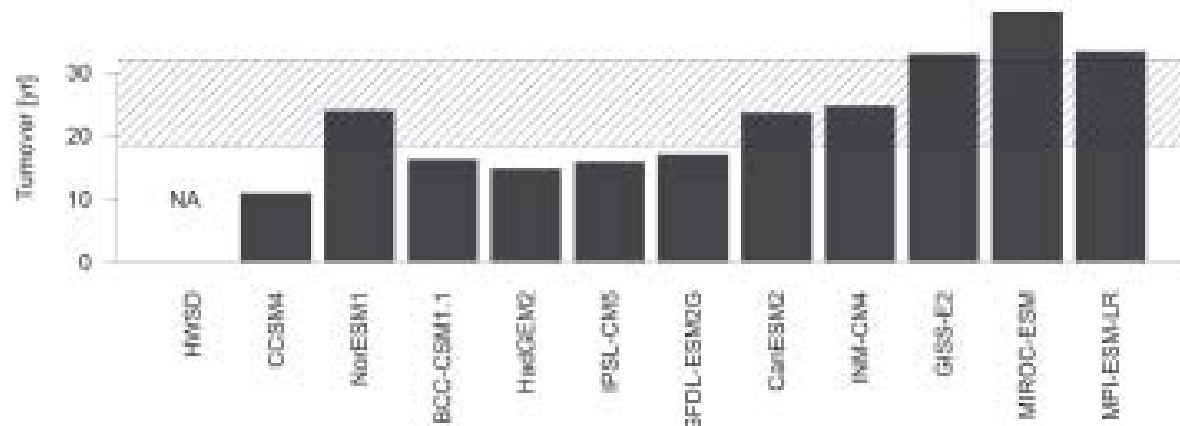
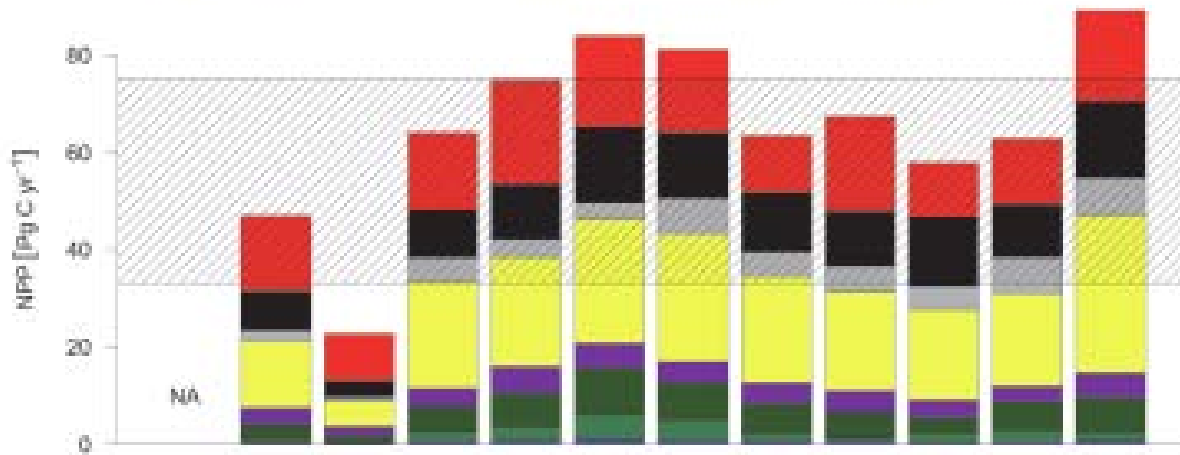
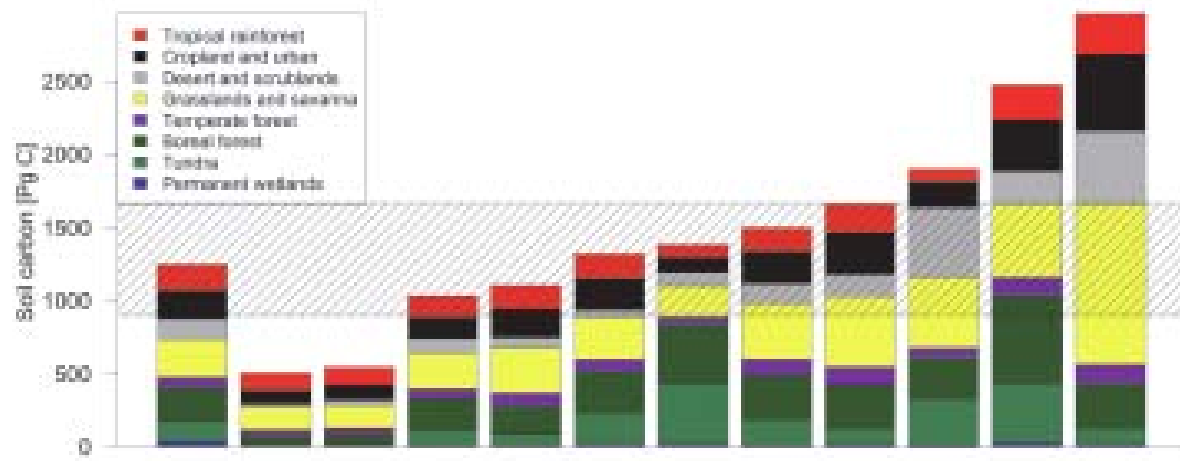
Environmental scalar  $\xi(t)$  (indicated by a downward arrow)  
 Transfer coefficient  $A$  (indicated by an arrow from the top)  
 Partitioning coefficient  $b$  (indicated by an arrow from the top right)  
 Carbon influx  $U(t)$  (indicated by an arrow from the right)  
 Initial values of carbon pools  $X_0$  (indicated by an arrow from the bottom left)

$$X_{ss} = \xi^{-1} \tau'_E U_{ss} = \tau_E U_{ss}$$

Carbon influx  $U_{ss}$  (indicated by an arrow from the top right)  
 Residence time  $\tau_E$  (indicated by an arrow from the bottom right)

$$\tau_E = \xi^{-1} \tau'_E = (\xi_T \xi_W)^{-1} (A^{-1} B)$$

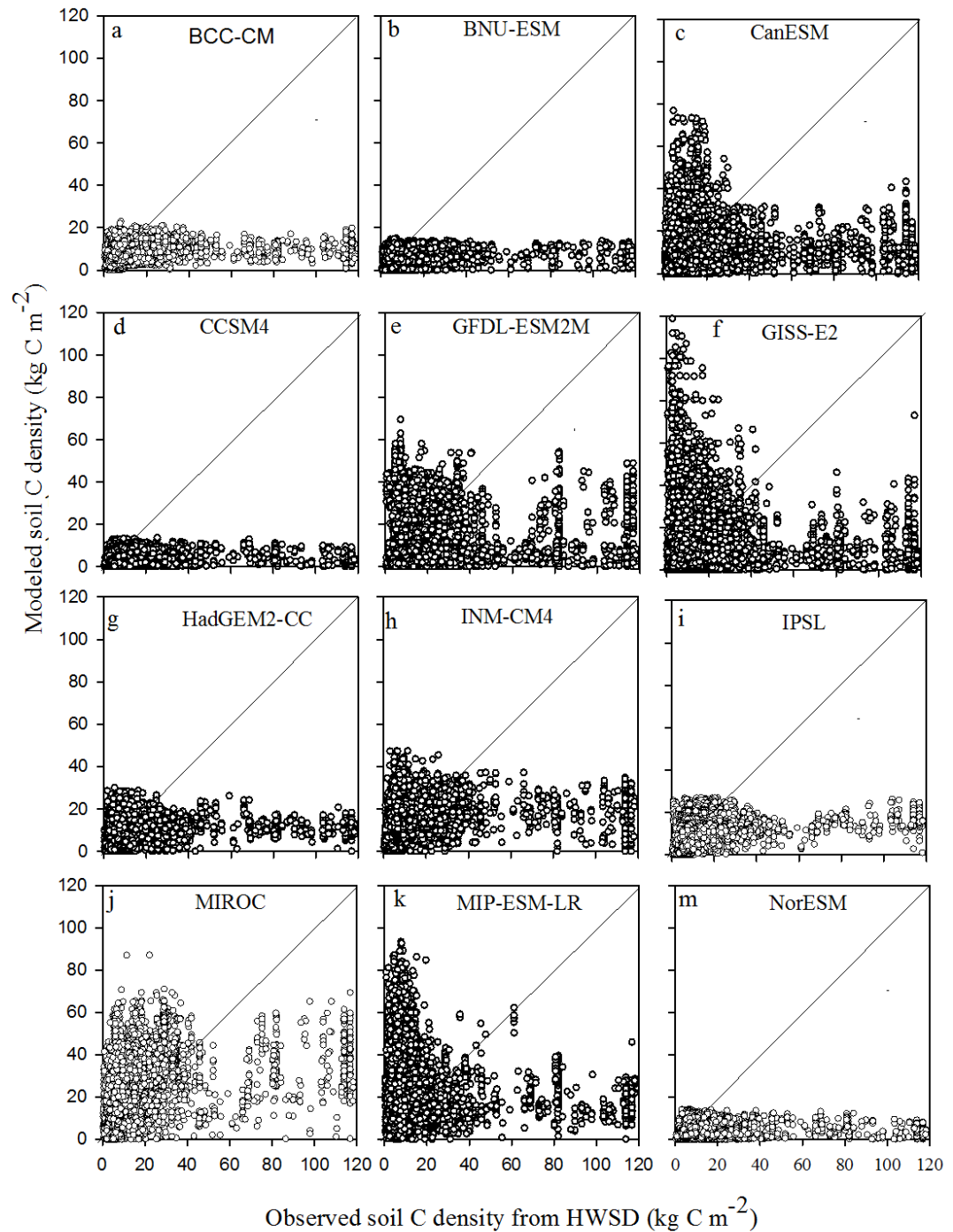
# Soil carbon modeled in CMIP5 vs. HWSD



Todd-Brown et al. 2012 BGD

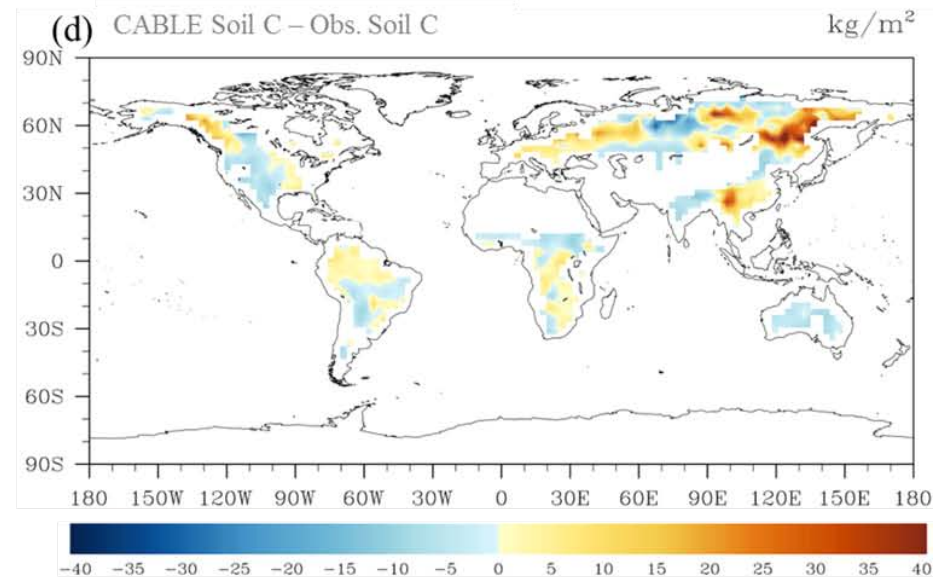
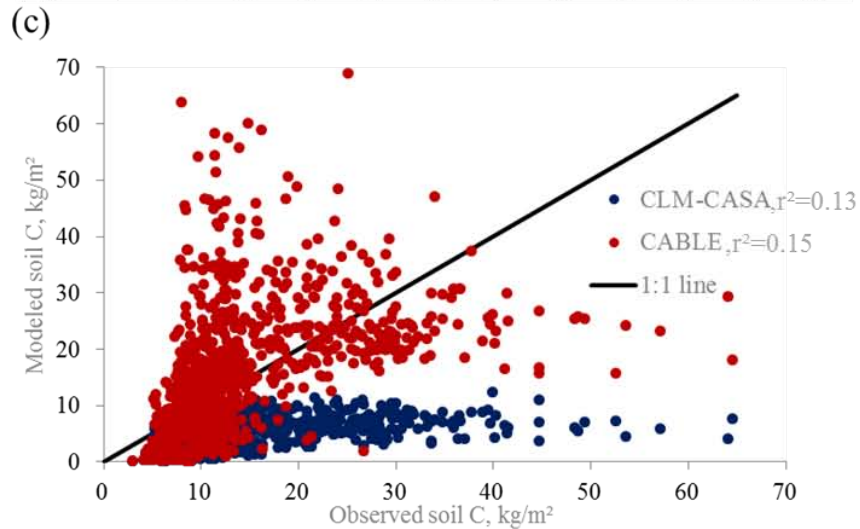
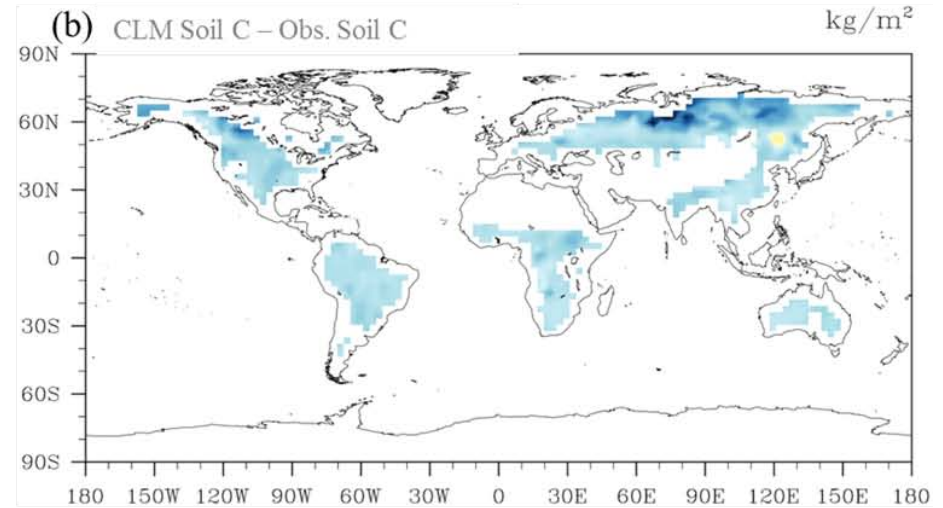
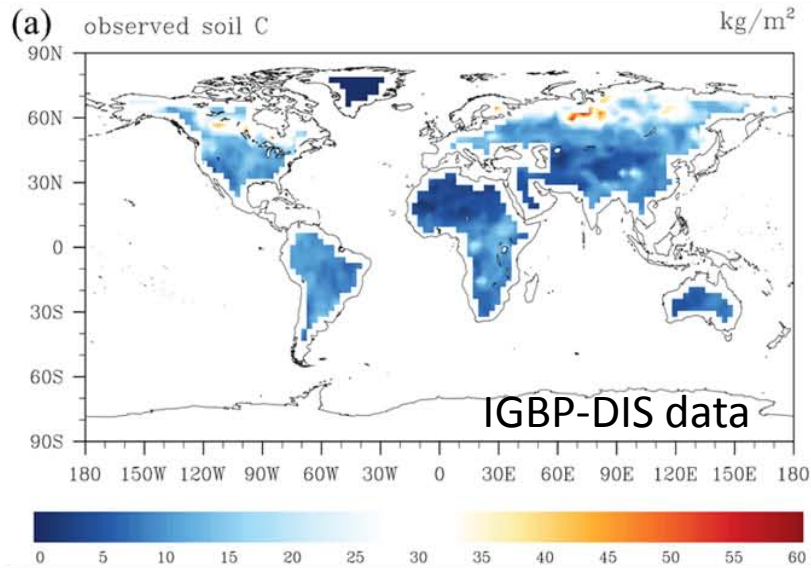
# Soil carbon modeled in CMIP5 vs. HWSD

Yan et al. unpublished

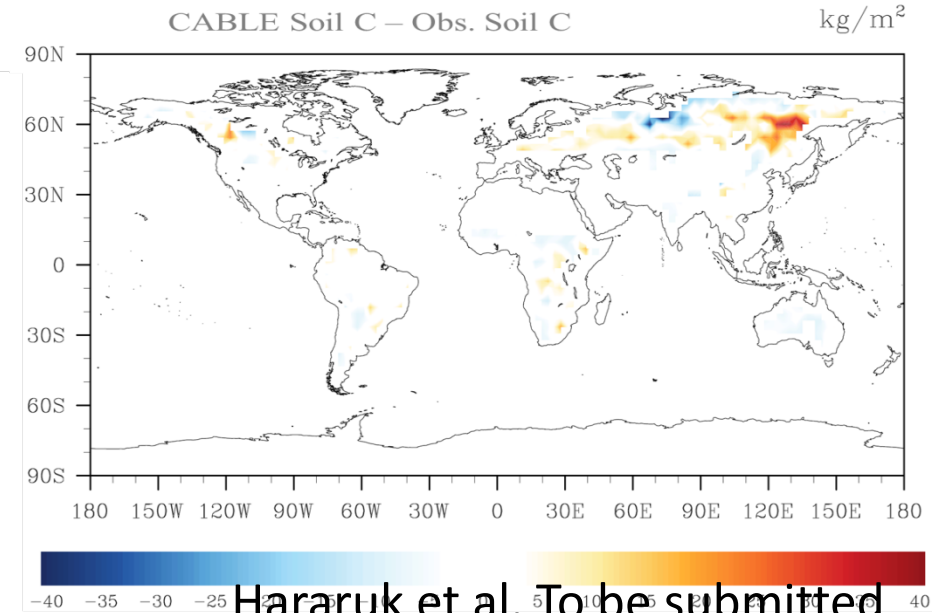
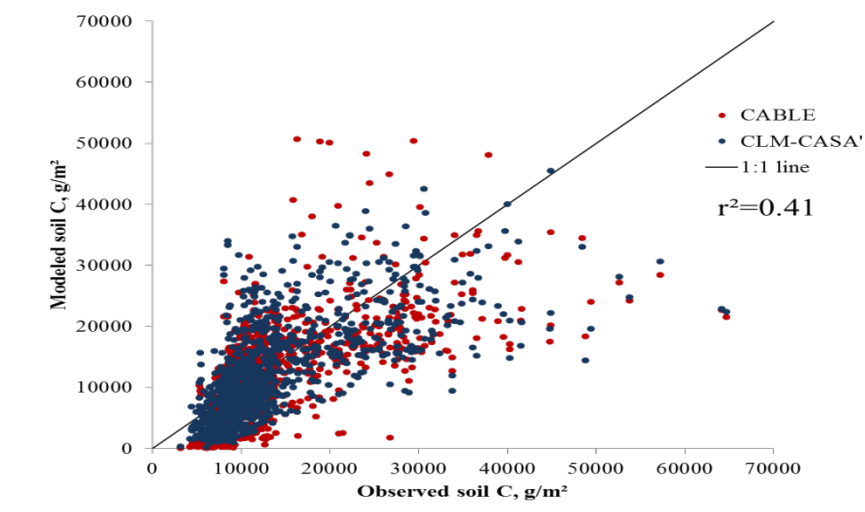
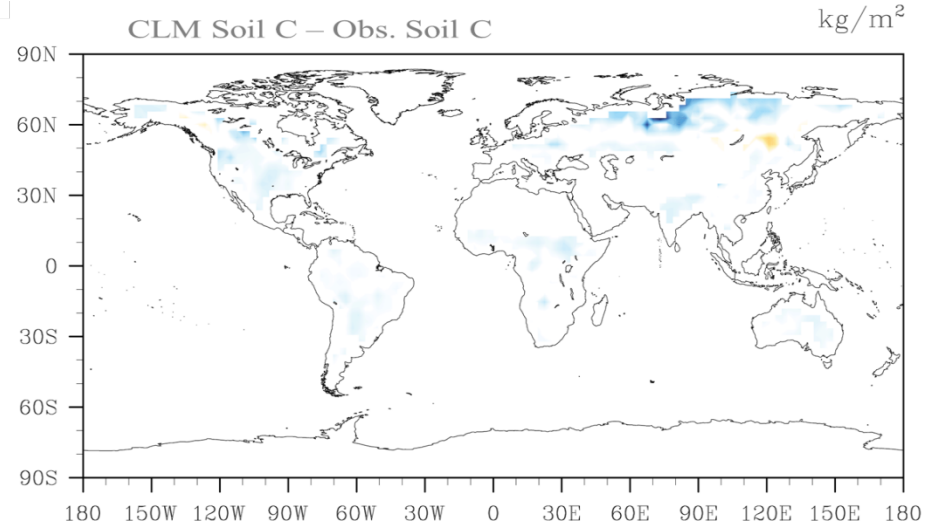
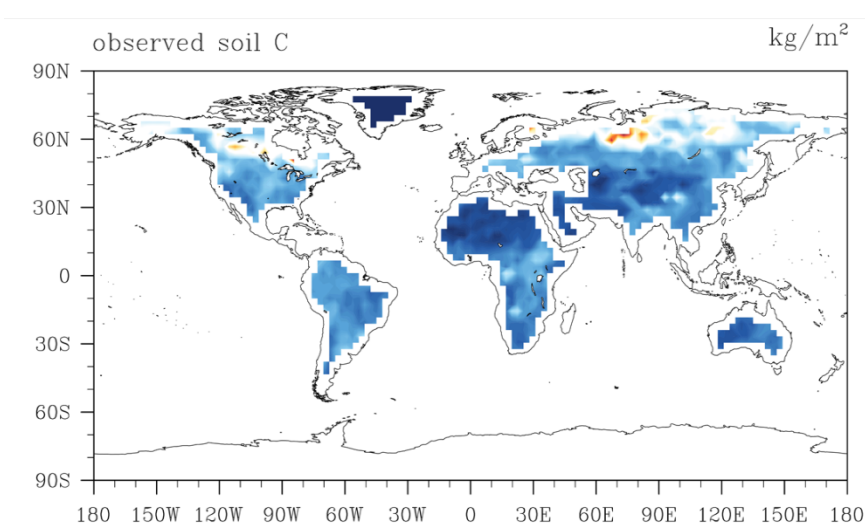


# How do CLM-CASA' and CABLE simulate Soil C?

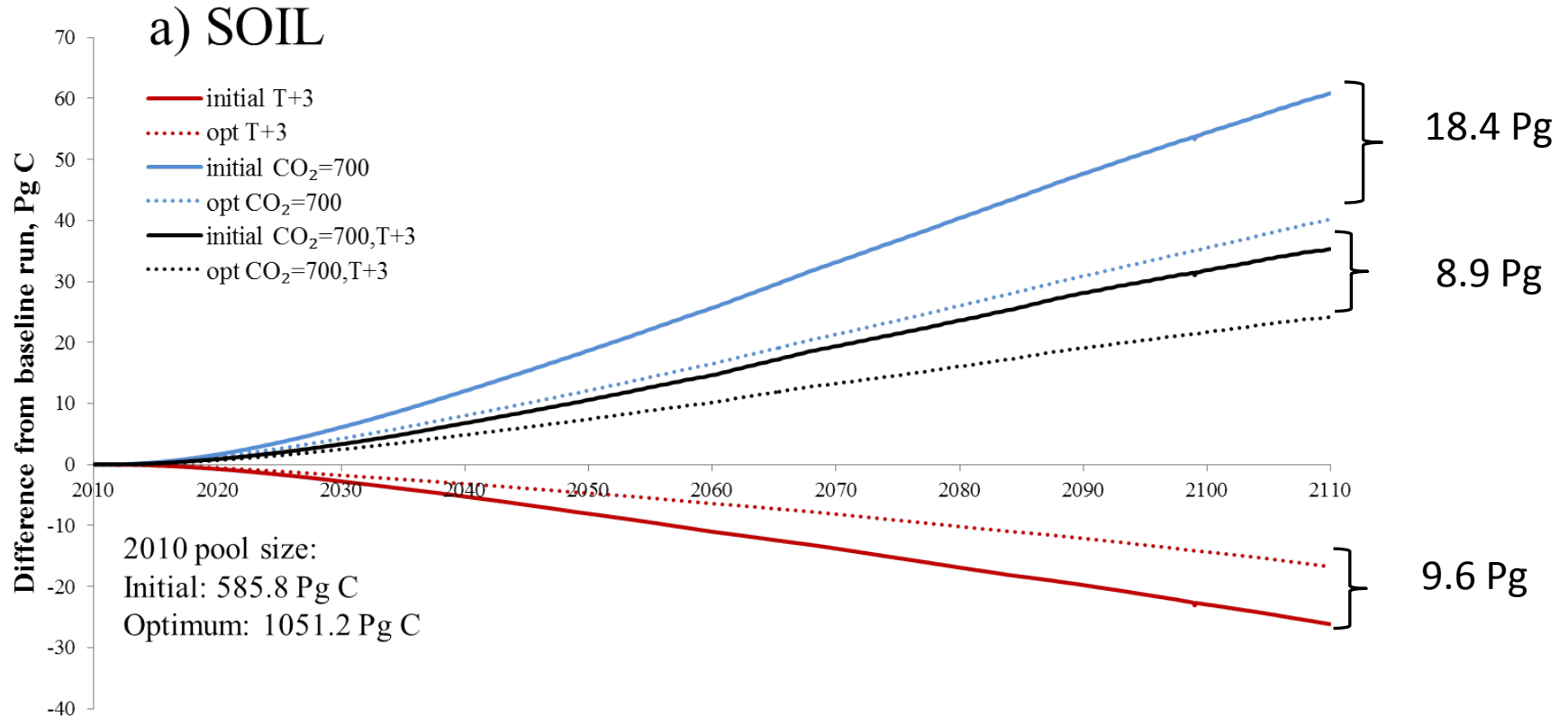
Hararuk et al. To be submitted



# Data assimilation to improve soil C simulation by two global models:



# Changes in temporal dynamics: CLM-CASA'



# Summary

- Improvement and applications of the traceability framework to make carbon cycle models more tractable. Procedure will be available at <http://ecolab.ou.edu>
- The traceability framework makes it possible evaluate impacts of adding components on model performance skills before we do so.
- It is urgent to correct the initial value problem of global carbon cycle models before they are used for CMIP6. It is also relatively easy to do so