

# A SPECTRAL VERTICAL REPRESENTATION IN CAM-SE



**David M. Hall**

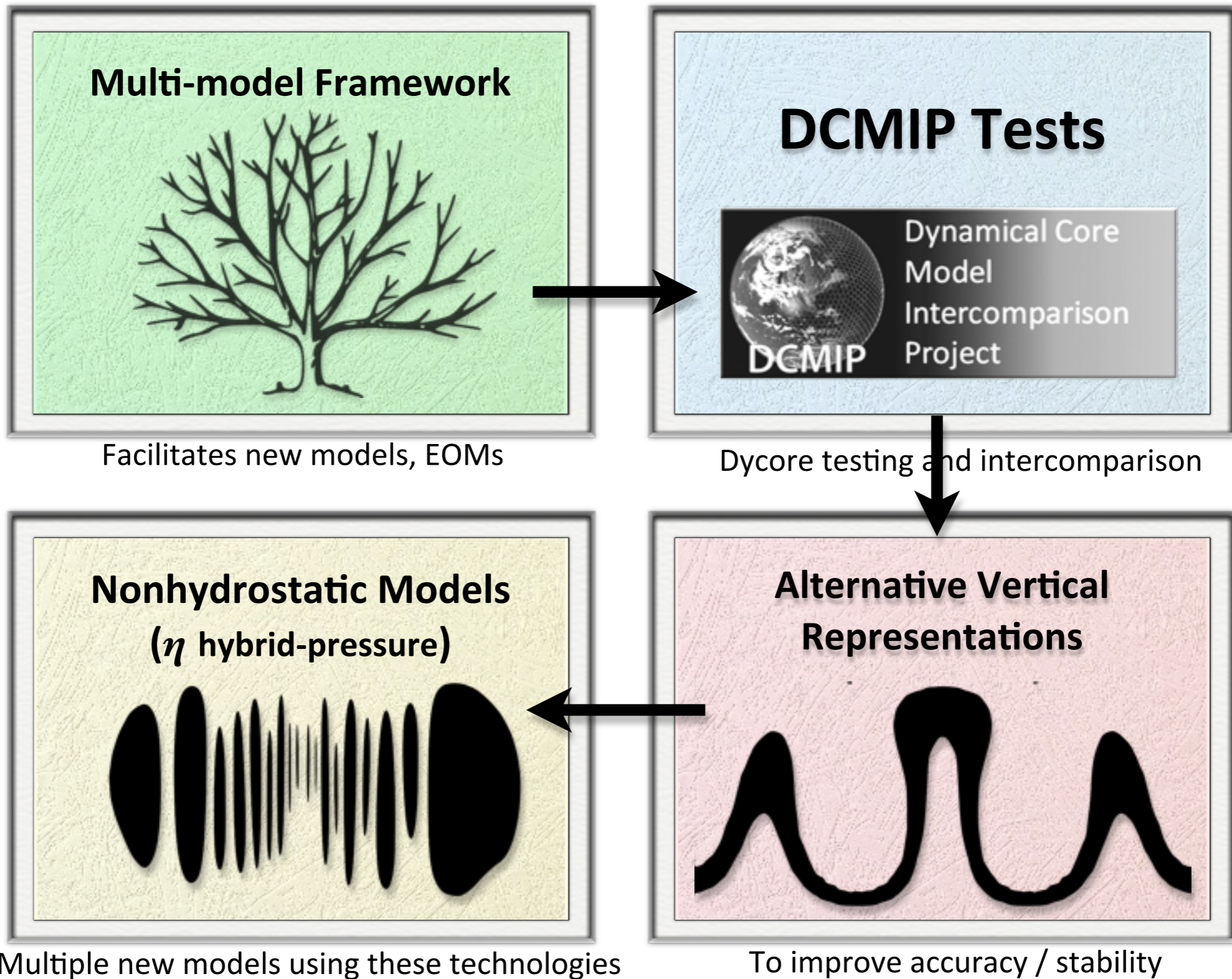
*Department of Computer Science  
University of Colorado at Boulder*

**CESM Atmospheric Working Group Meeting 2015, Boulder, CO**



# NEW TECHNOLOGIES IN HOMME

- Main thrust of project is nonhydrostatic model in  $\eta$  (hybrid-pressure)
- Enabling technologies: Multi-model framework, DCMIP, alternate vertical rep



# NEW TECHNOLOGIES IN HOMME

- Focus today: alternative vertical representations
- (Nonhydrostatic update at the end)

## Multi-model Framework



Facilitates new models, EOMs

## DCMIP Tests



Dycore testing and intercomparison

## Nonhydrostatic Models ( $\eta$ hybrid-pressure)



Multiple new models using these technologies

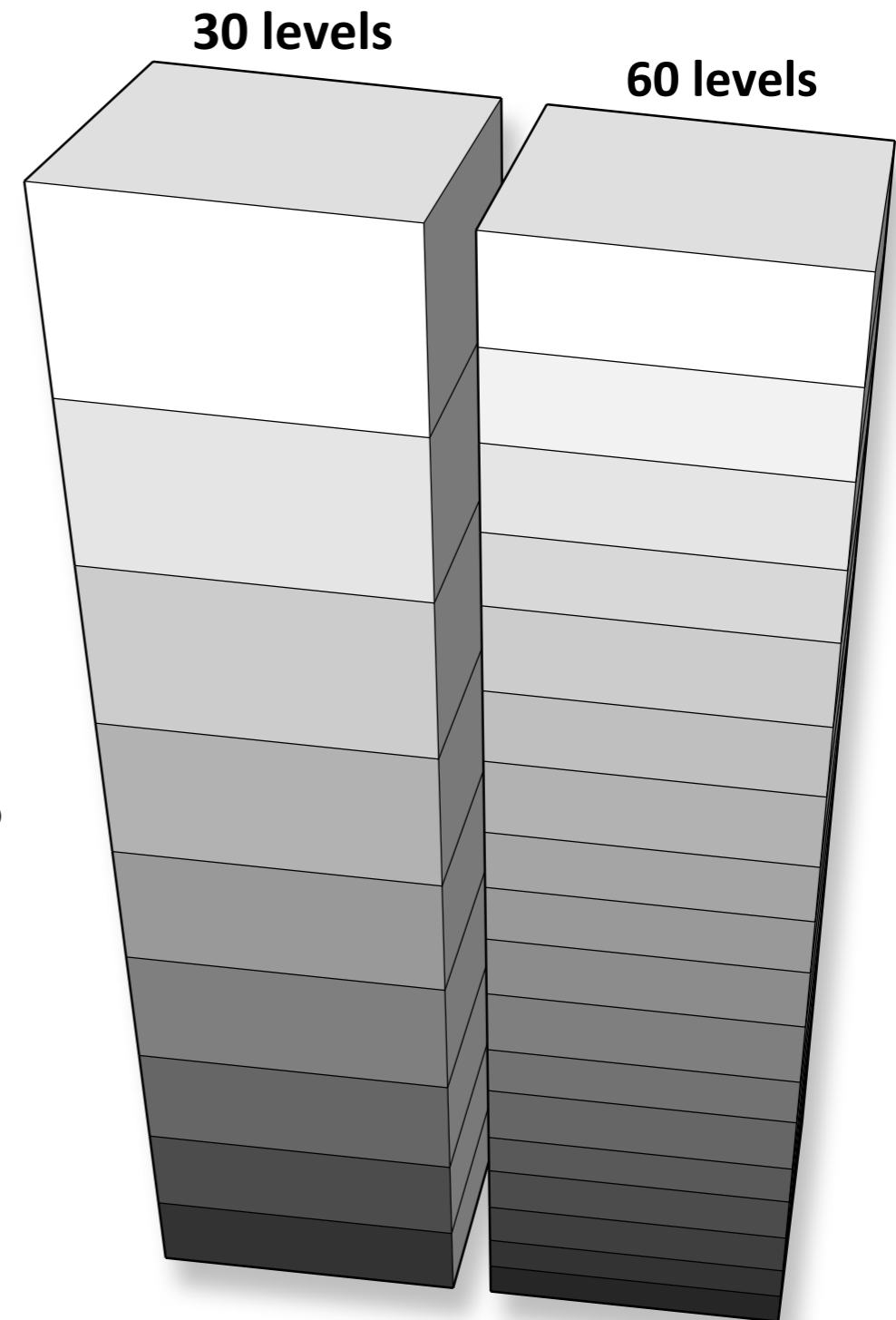
## Alternative Vertical Representations



To improve accuracy / stability

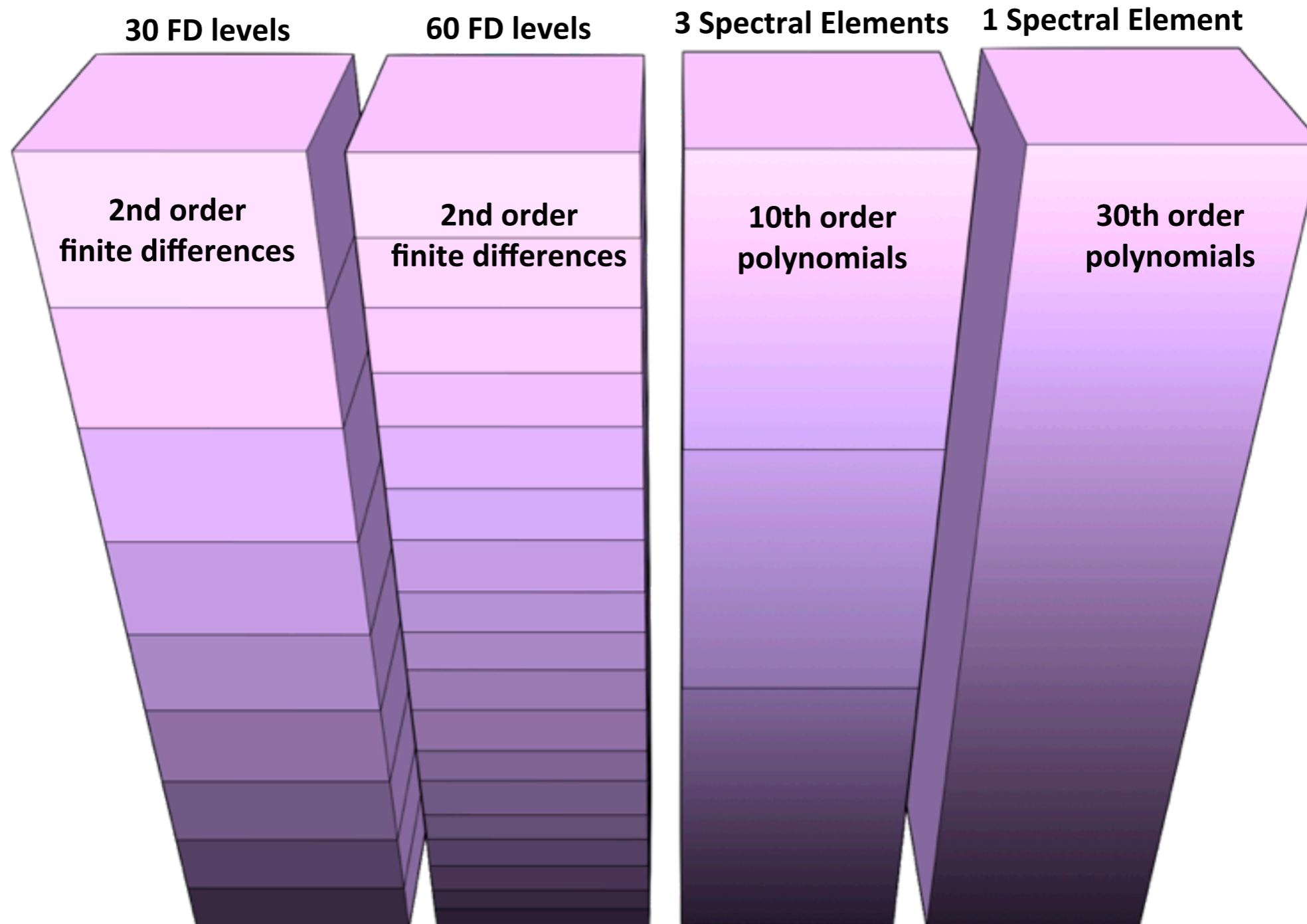
# AMWG 2014: PROPOSED INCREASE IN VERTICAL RESOLUTION

- **Currently 30 vertical levels in CAM**
- **Upgrade to 60 levels?**
  - Increases accuracy
  - Increases detail
  - Doubles cost of all simulations
- **Alt: Replace it with spectral representation?**
  - Increases vertical accuracy
  - No additional communication costs
  - No additional memory demands
  - Makes optimal use of vertical DOFs



# MANY POSSIBLE VERTICAL DISCRETIZATIONS

- 30 levels, 2nd order finite differences
- 60 levels, 2nd order finite differences (2x cost)
- 3 spectral elements, 10th order (1x cost)
- 1 spectral element, 30th order (1x cost)



# SPECTRAL TRANSPORT AND DYNAMICS

- Both **transport** and **dynamics** models developed using **vertical-spectral** routines
- Will show some **DCMIP test results** to evaluate their performance

vertical  
**finite  
difference  
operators**

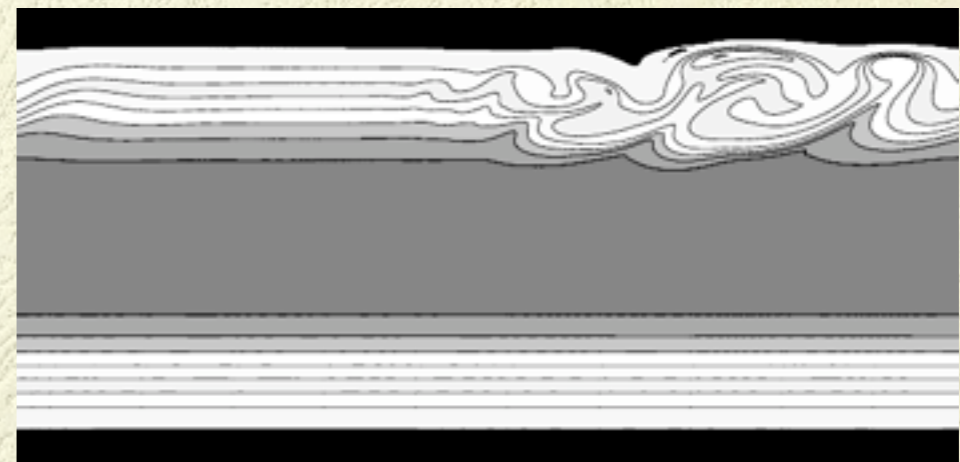
vertical  
**spectral  
operators**

vertical  
**spectral  
element  
operators**

**Vertical Spectral  
Tracer Transport**

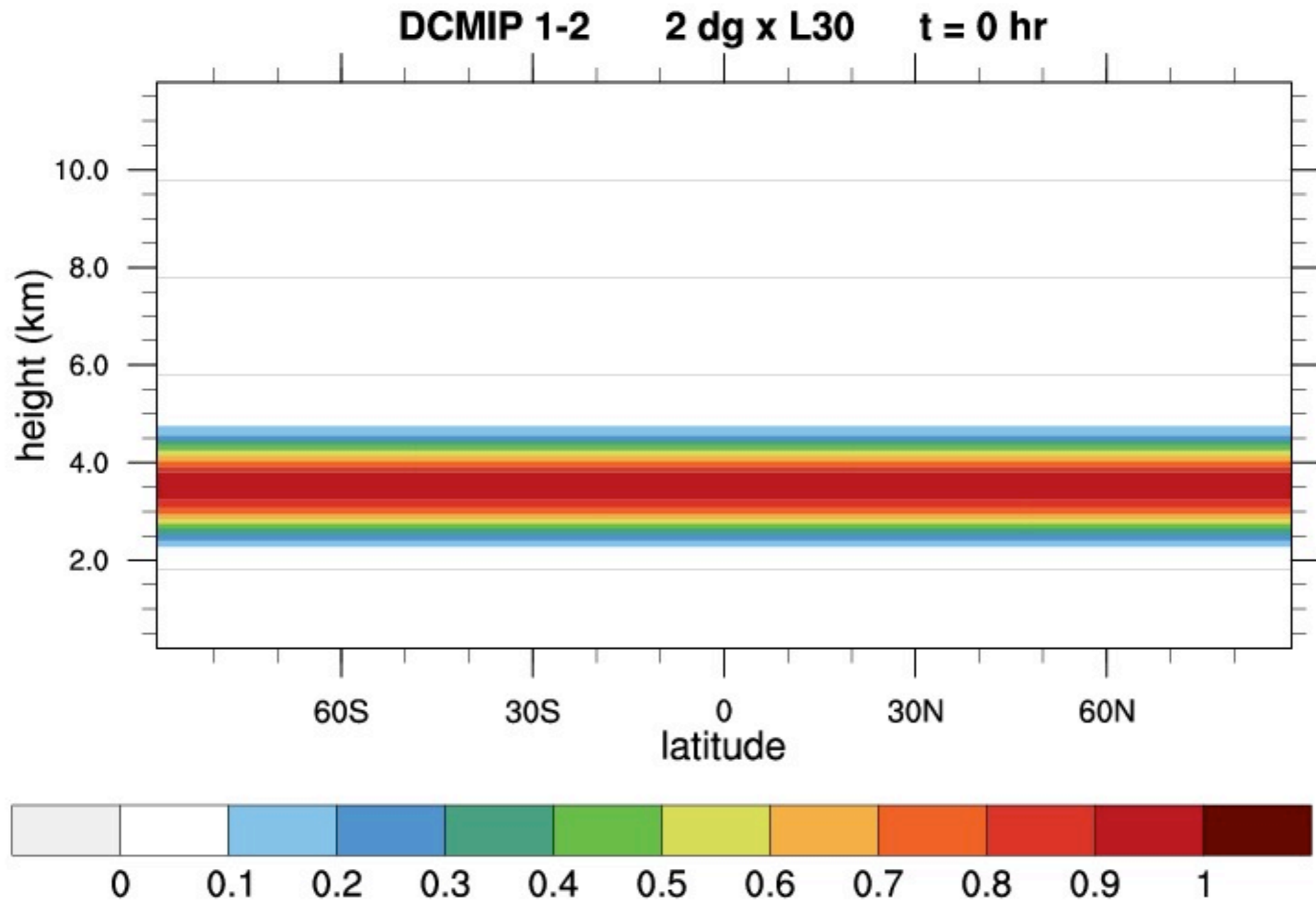


**Vertical Spectral  
Primitive Equations Dynamics**



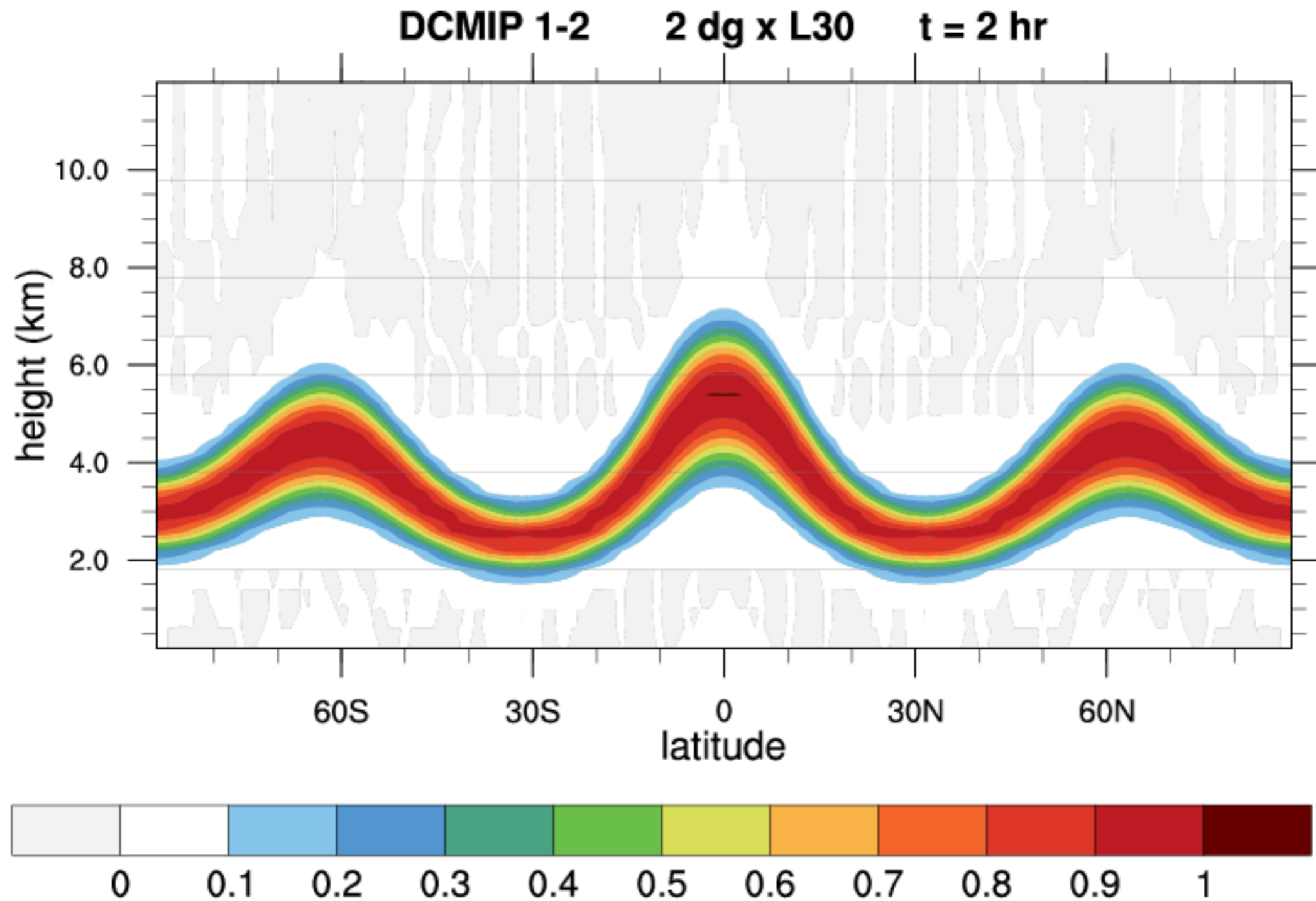
# DCMIP 1-2: DESCRIPTION

- Prescribed tracer transport, Hadley-like flow
- Examines impact of vertical representation on tracer transport routines
- No limiters, filters, or hyperviscosity



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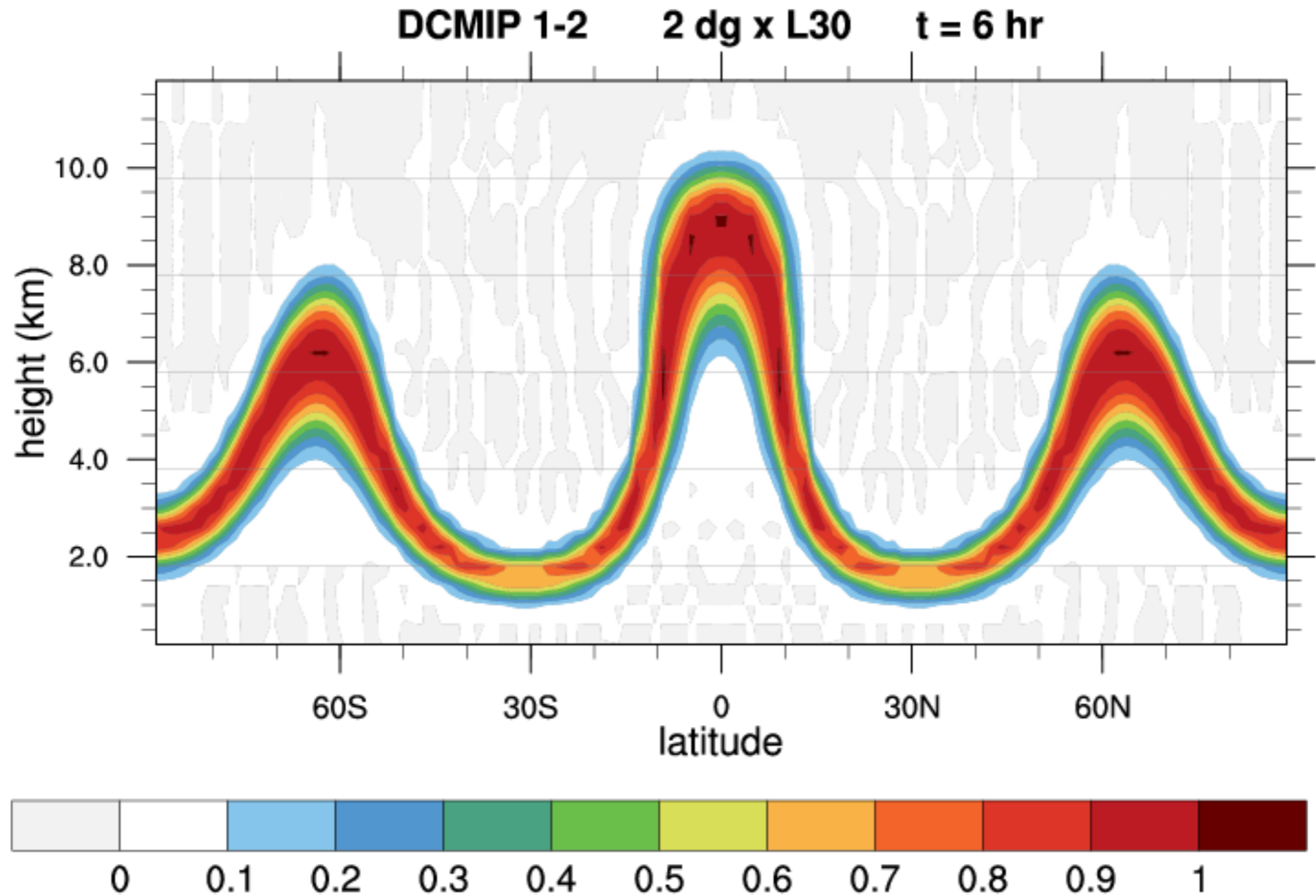
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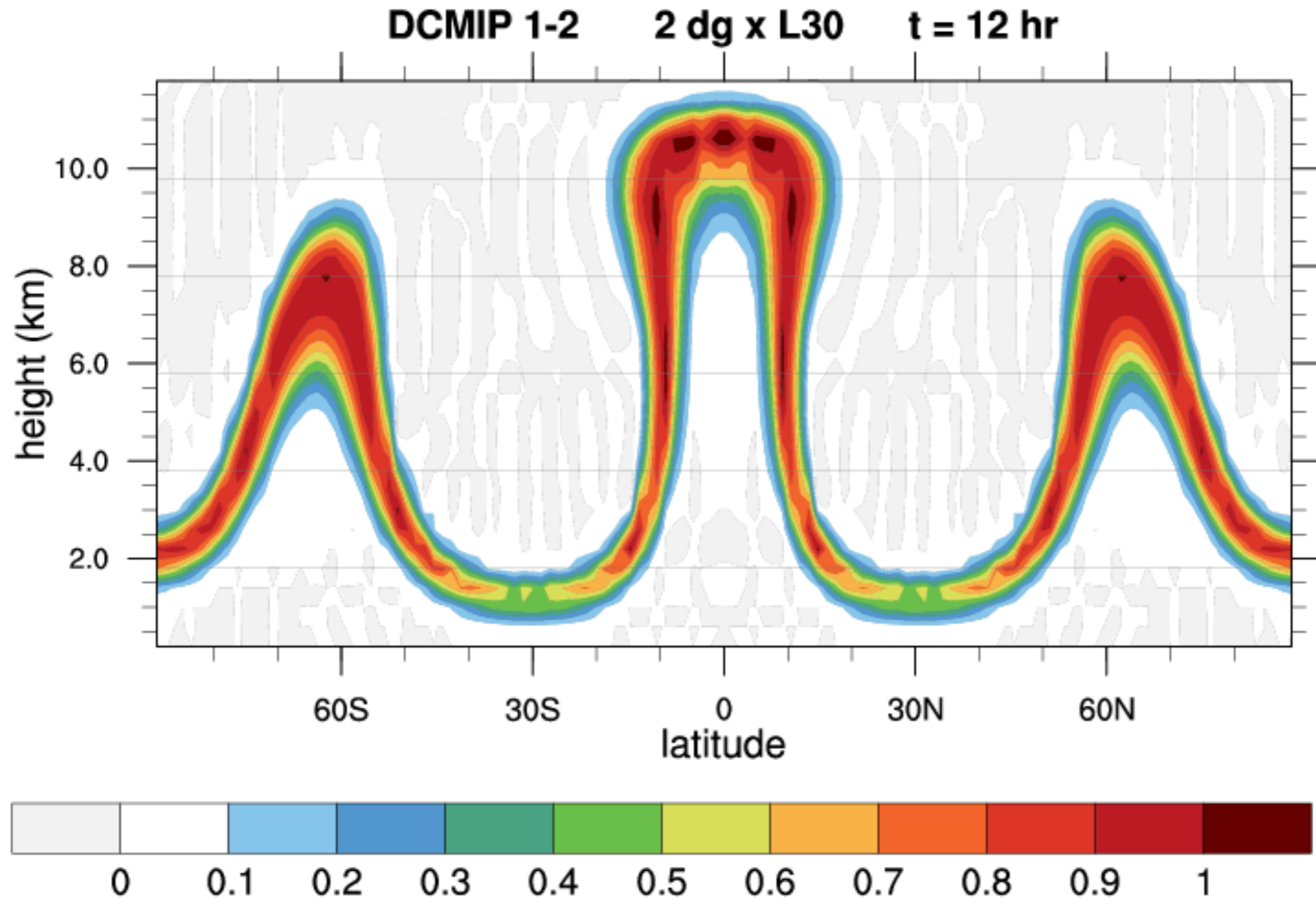
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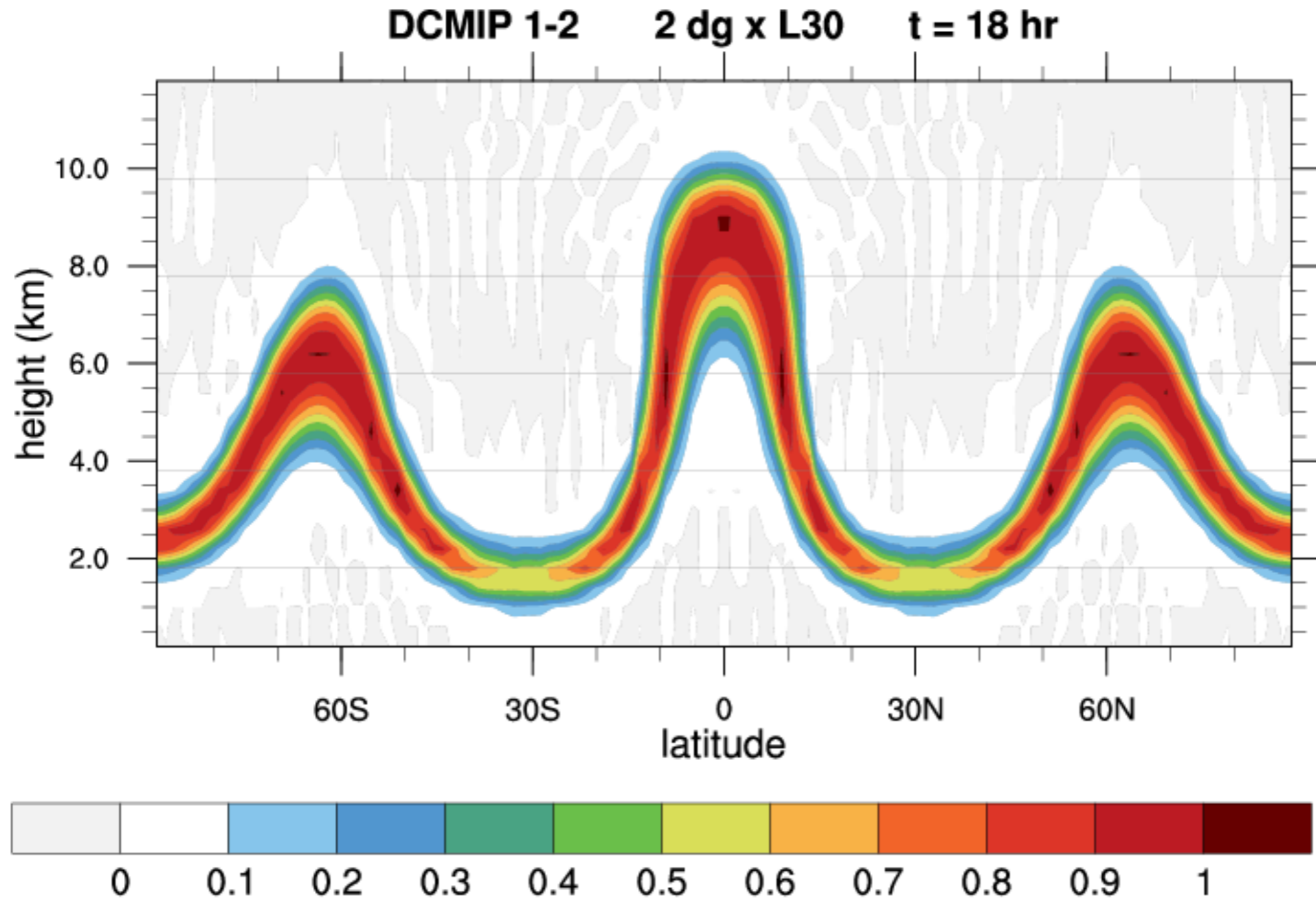
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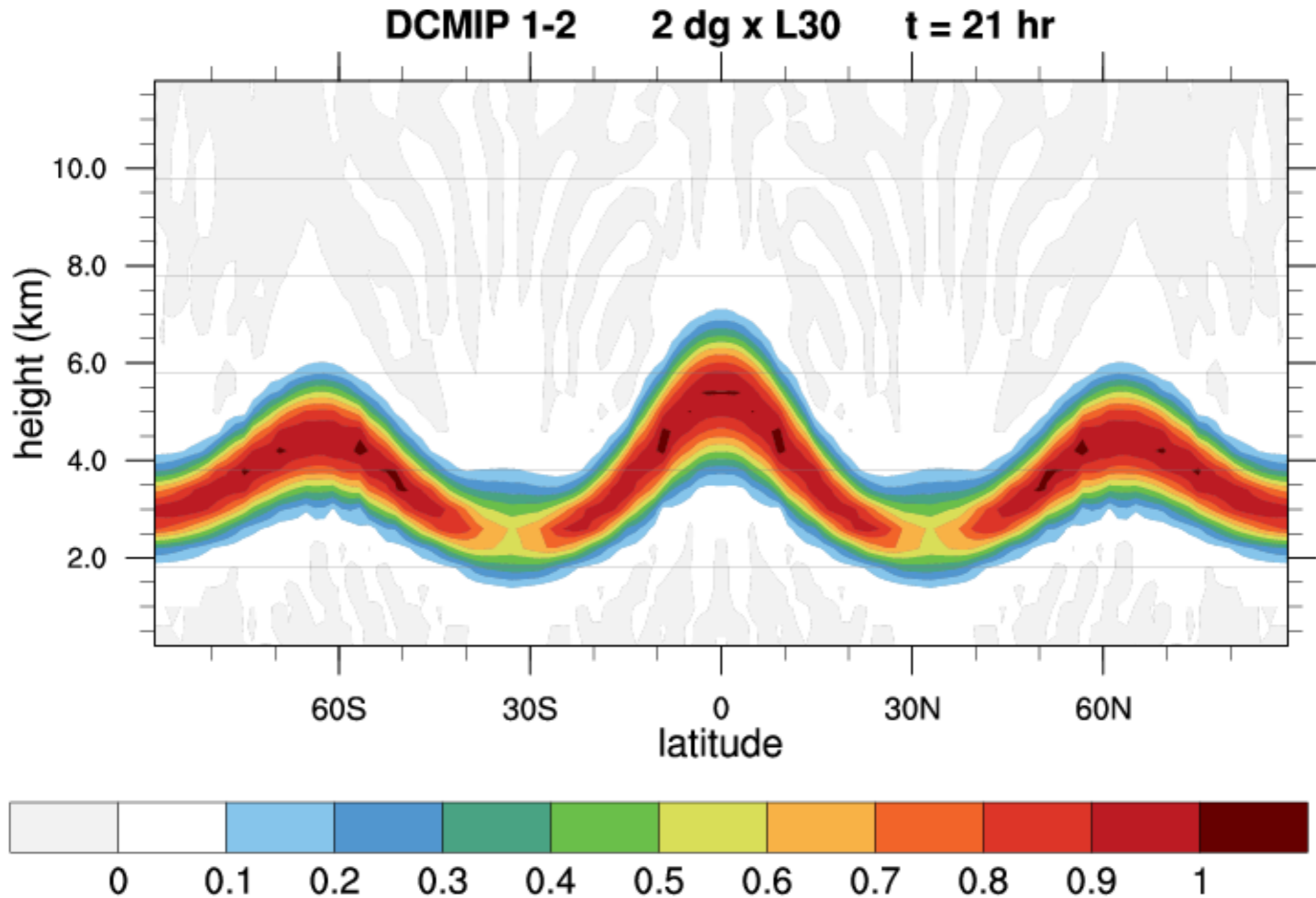
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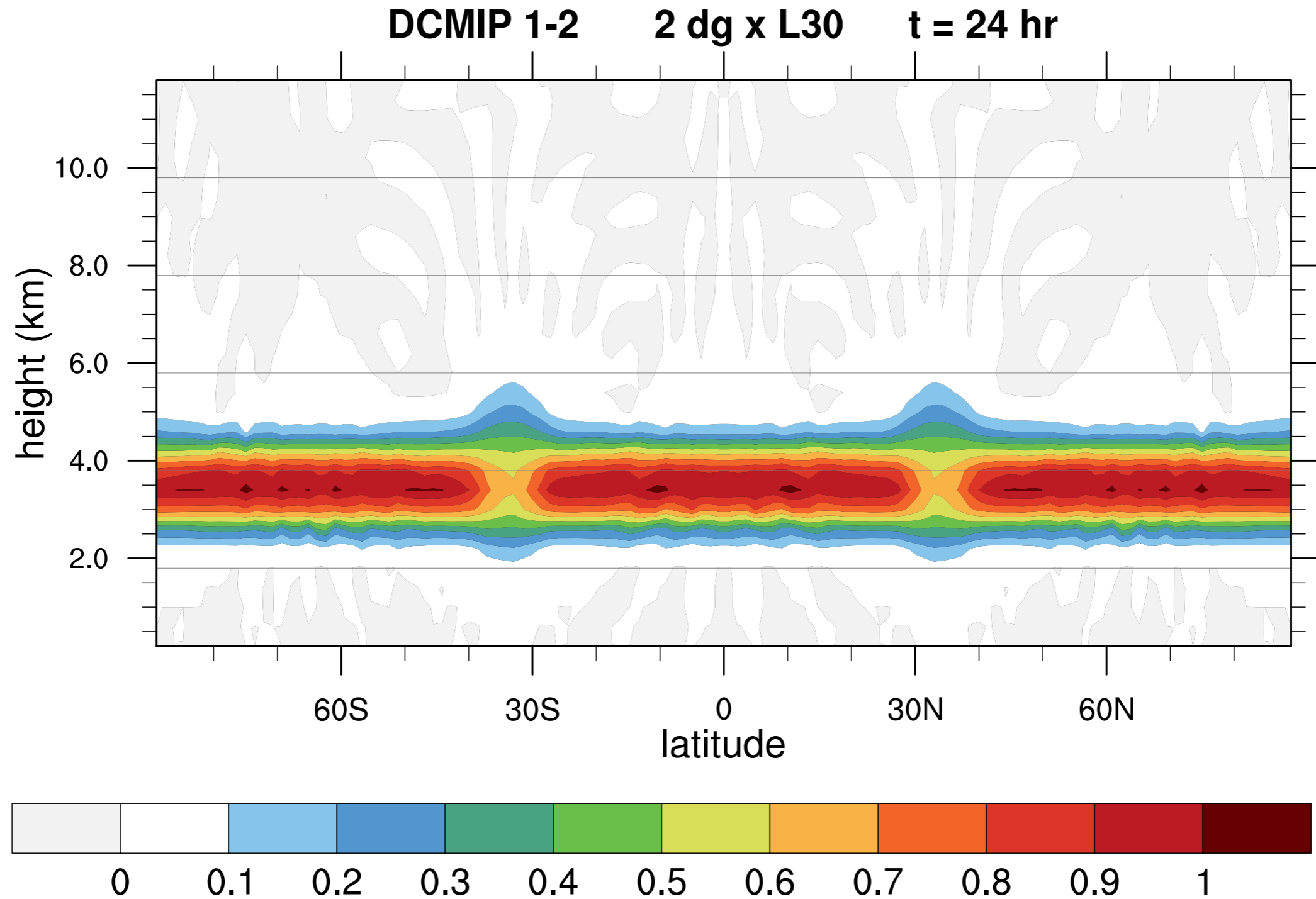
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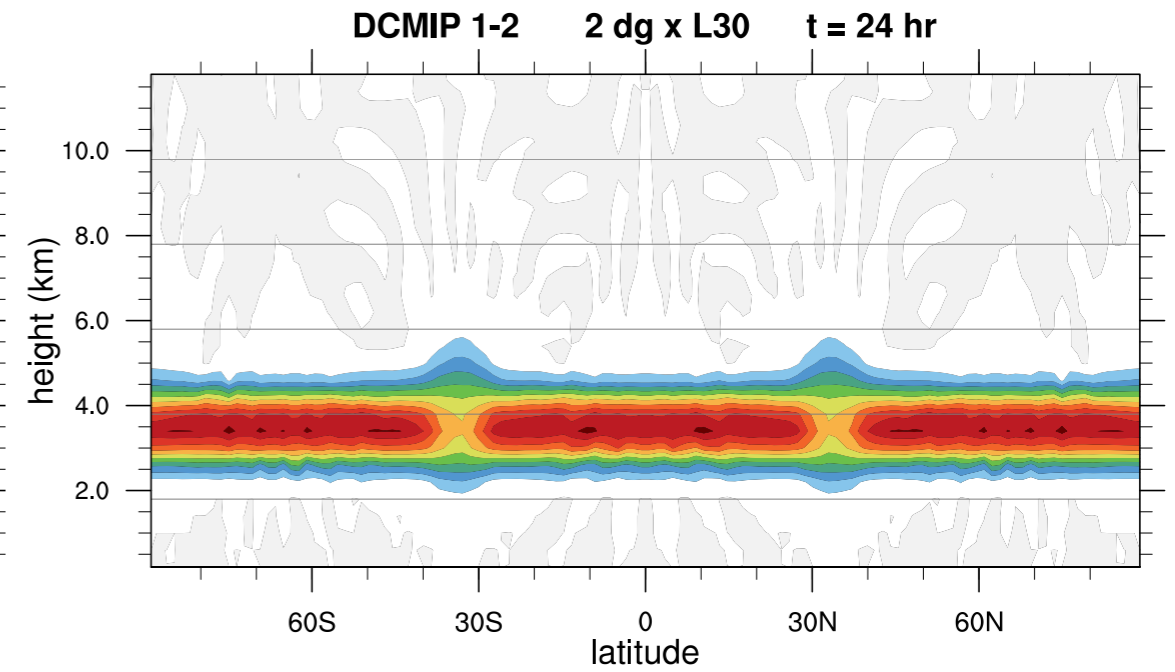
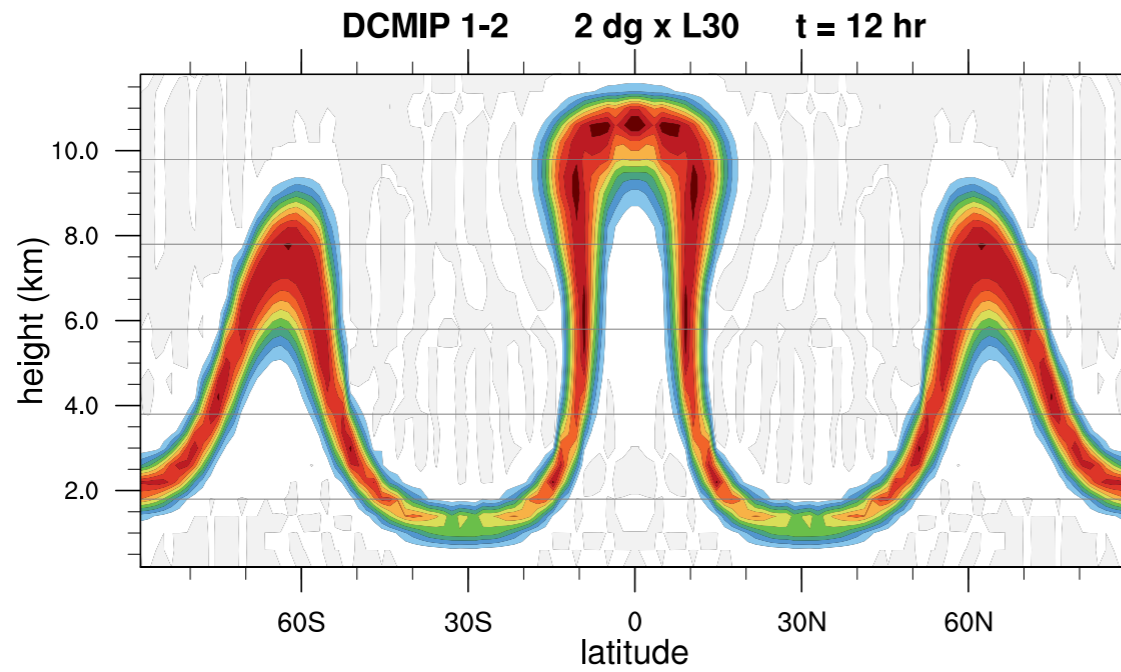
- Prescribed tracer transport, Hadley-like flow
- Examines impact of vertical representation on tracer transport routines
- No limiters, filters, or hyperviscosity ( $2^\circ$ ,  $1^\circ$ )



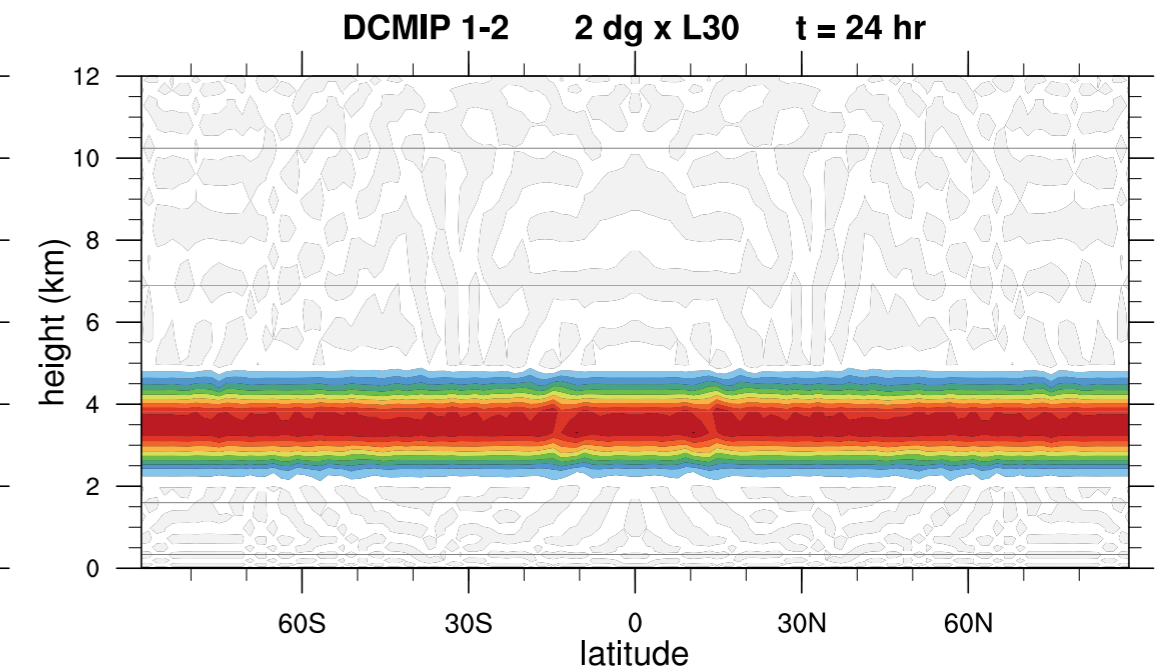
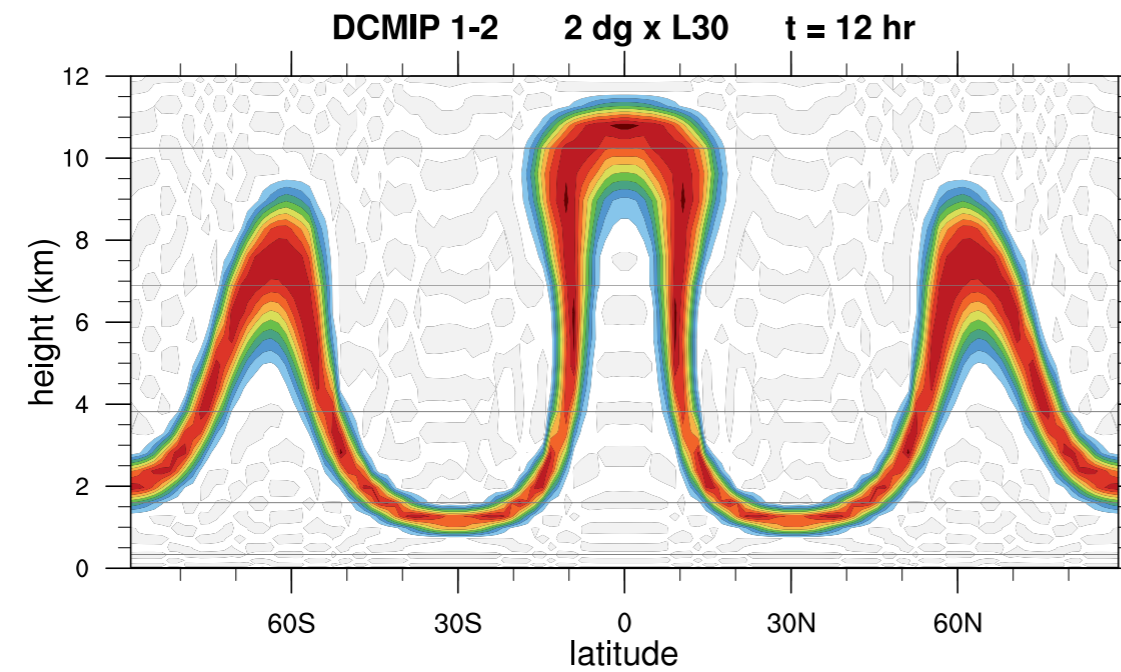
# DCMIP 1-2: HADLEY-LIKE TRANSPORT, 2°

## Vertical Cross-Sections at 12 and 24 hours

default  
method



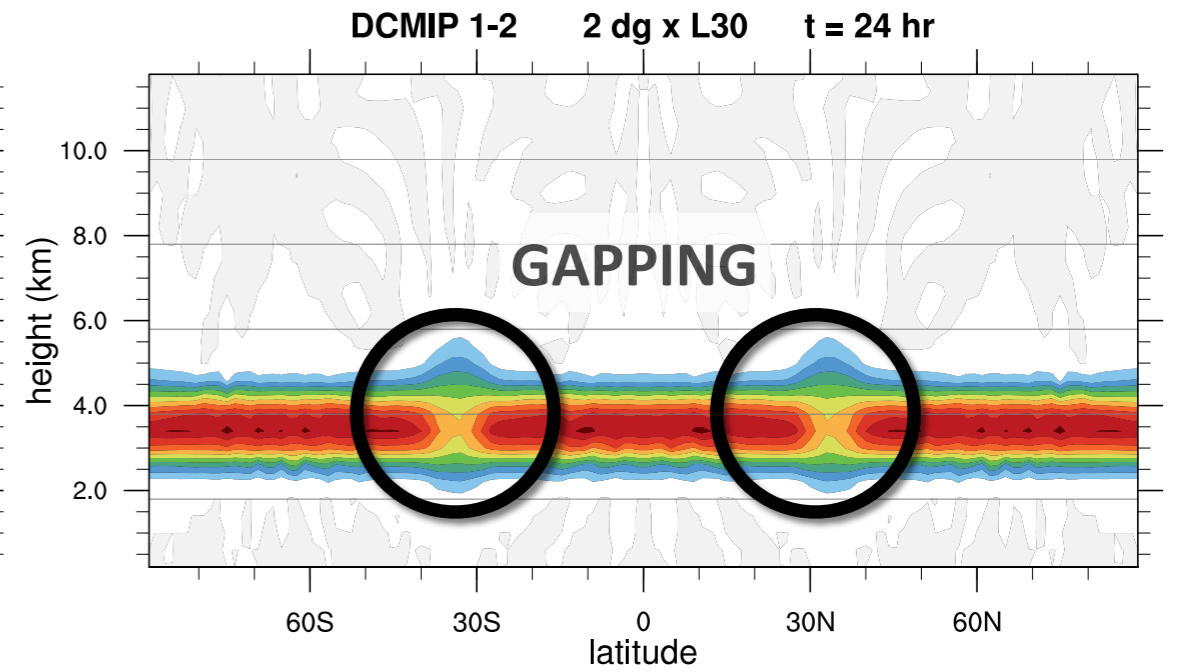
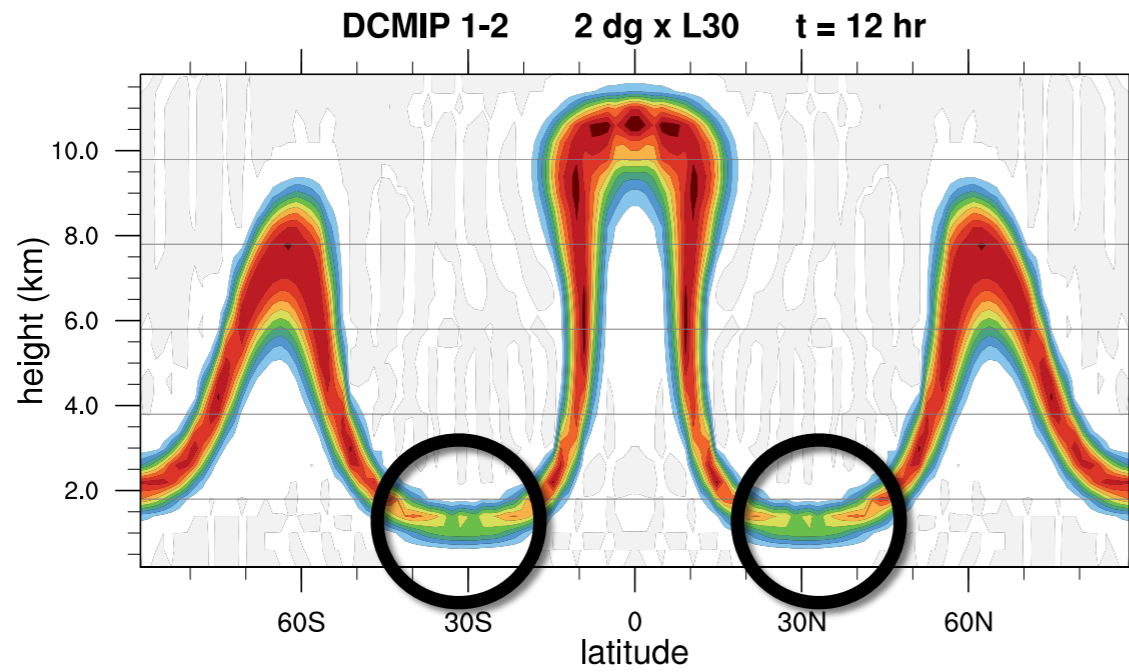
spectral  
vertical



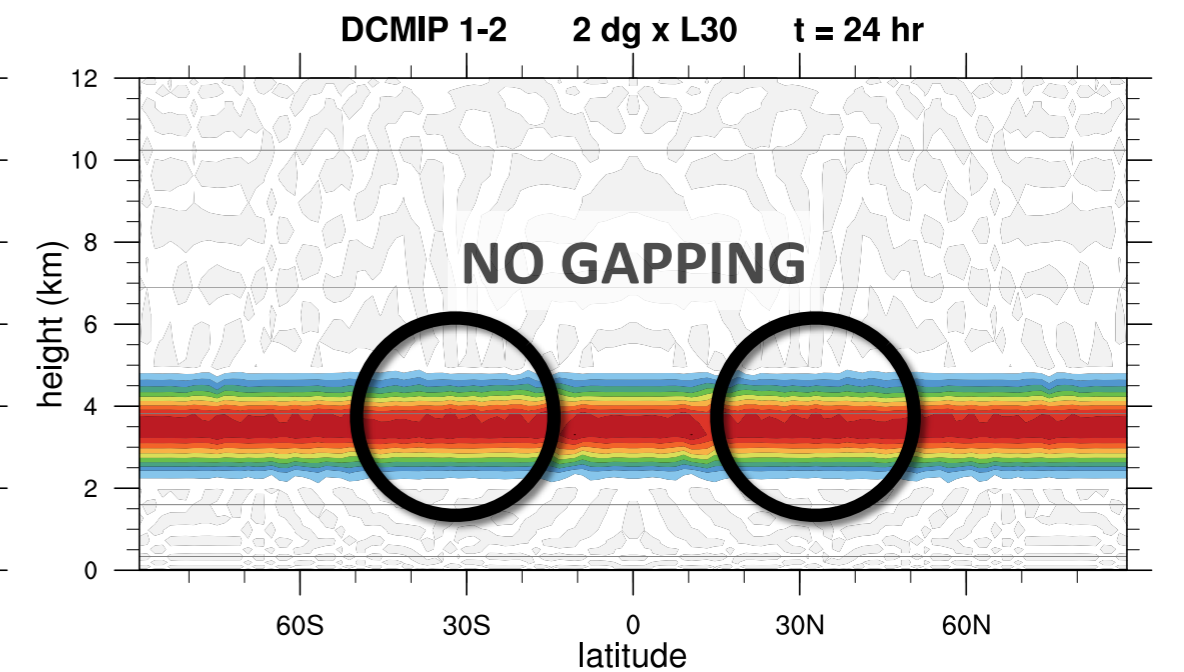
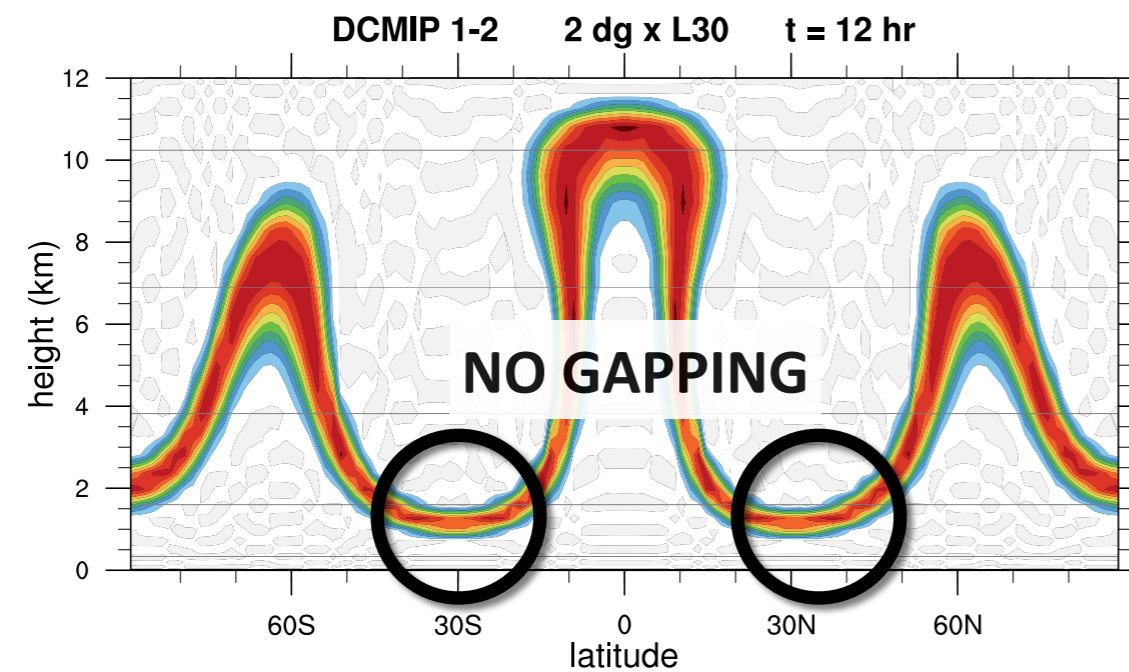
dt=5 sec, no limiter, no hyperviscosity

# DCMIP 1-2: HADLEY-LIKE TRANSPORT

default  
method



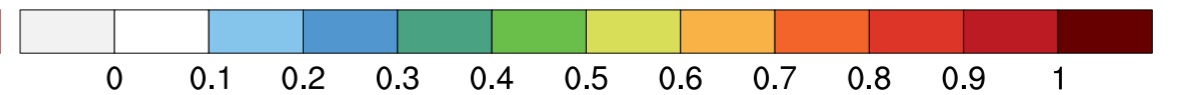
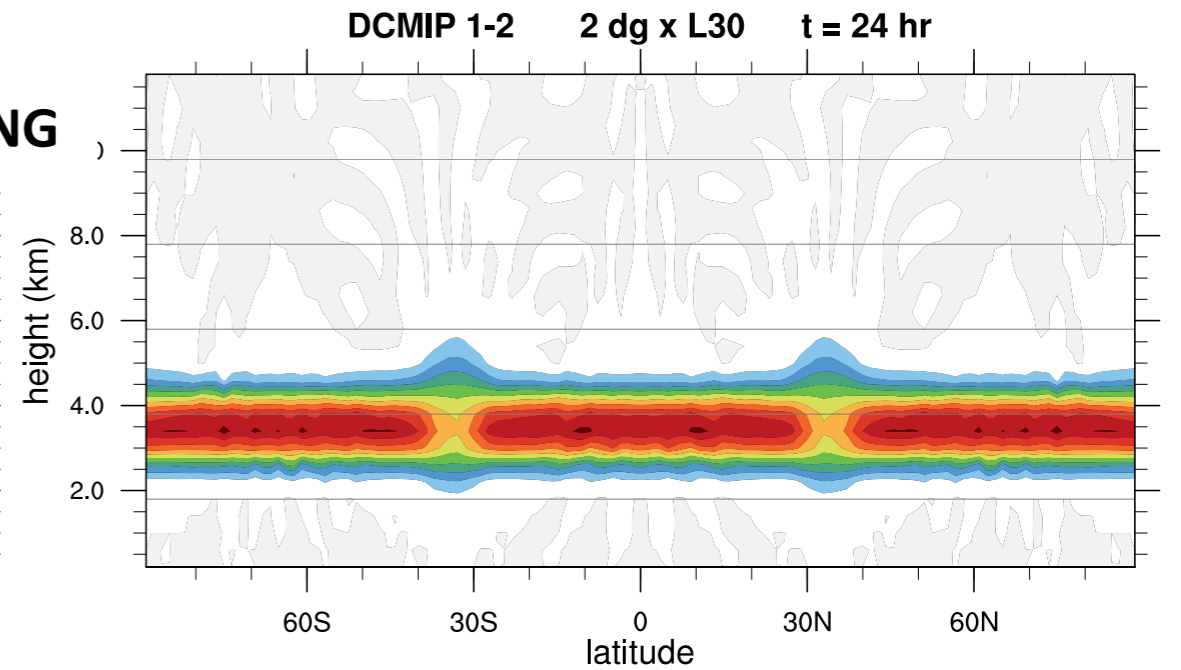
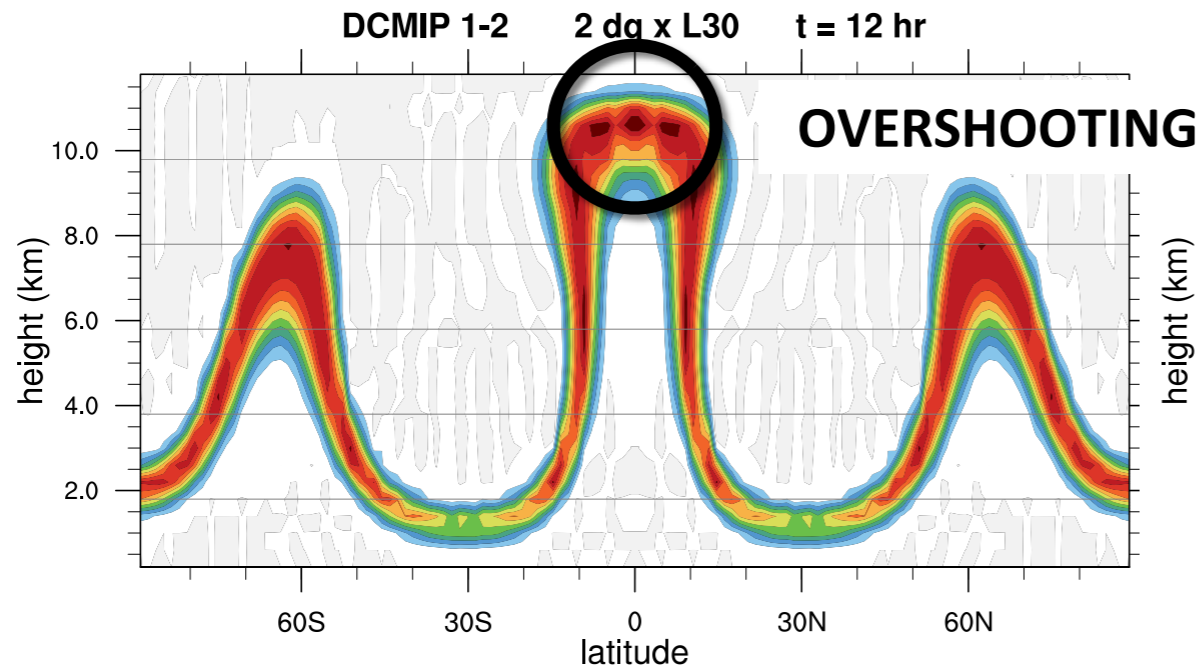
spectral  
vertical



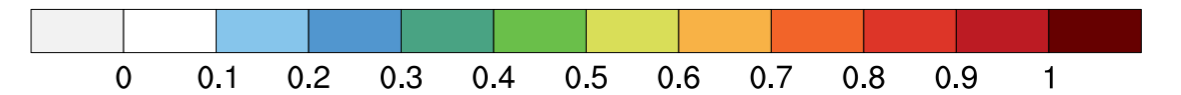
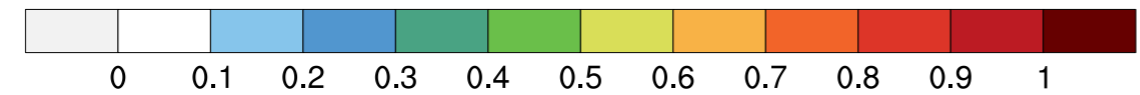
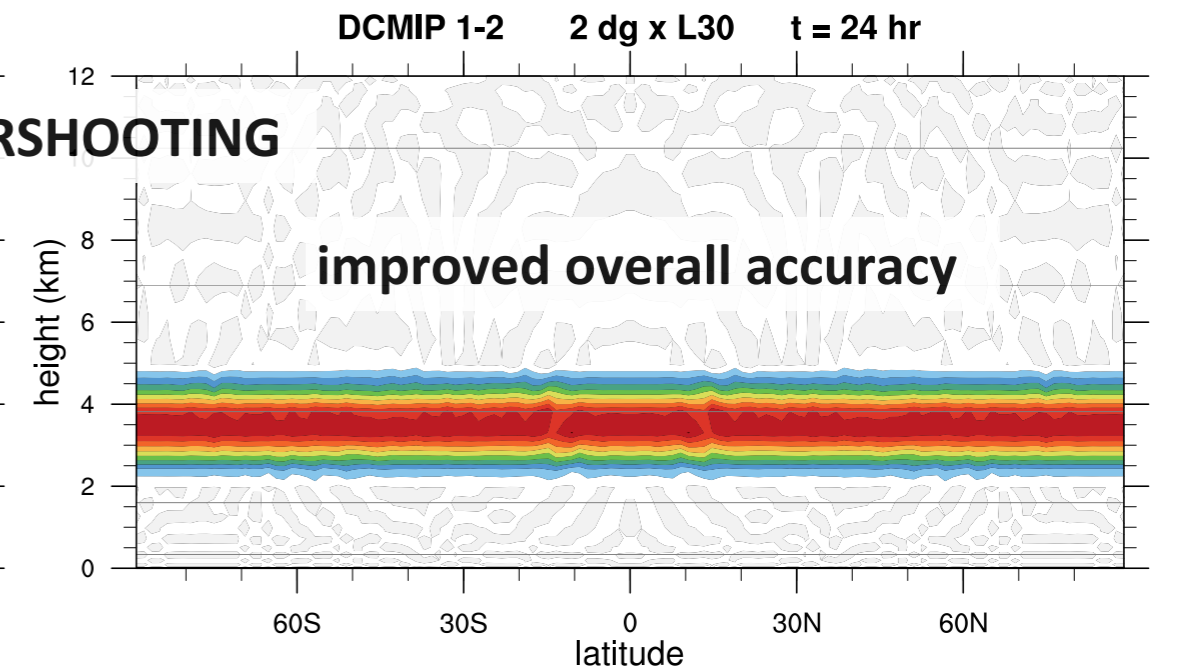
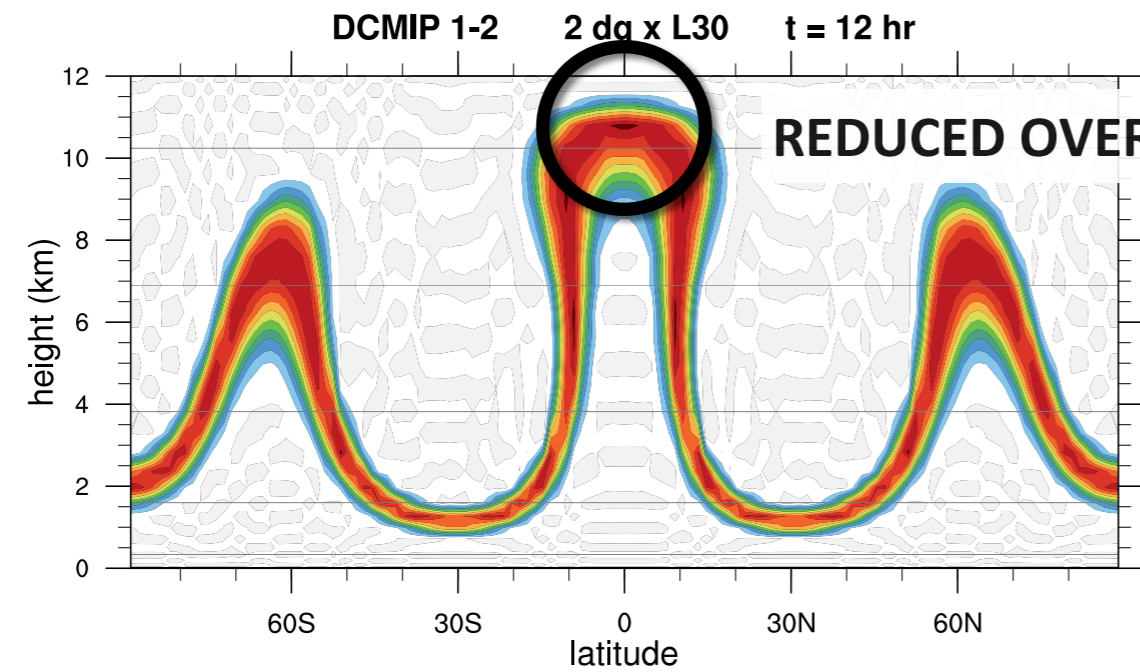
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default  
method



spectral  
vertical



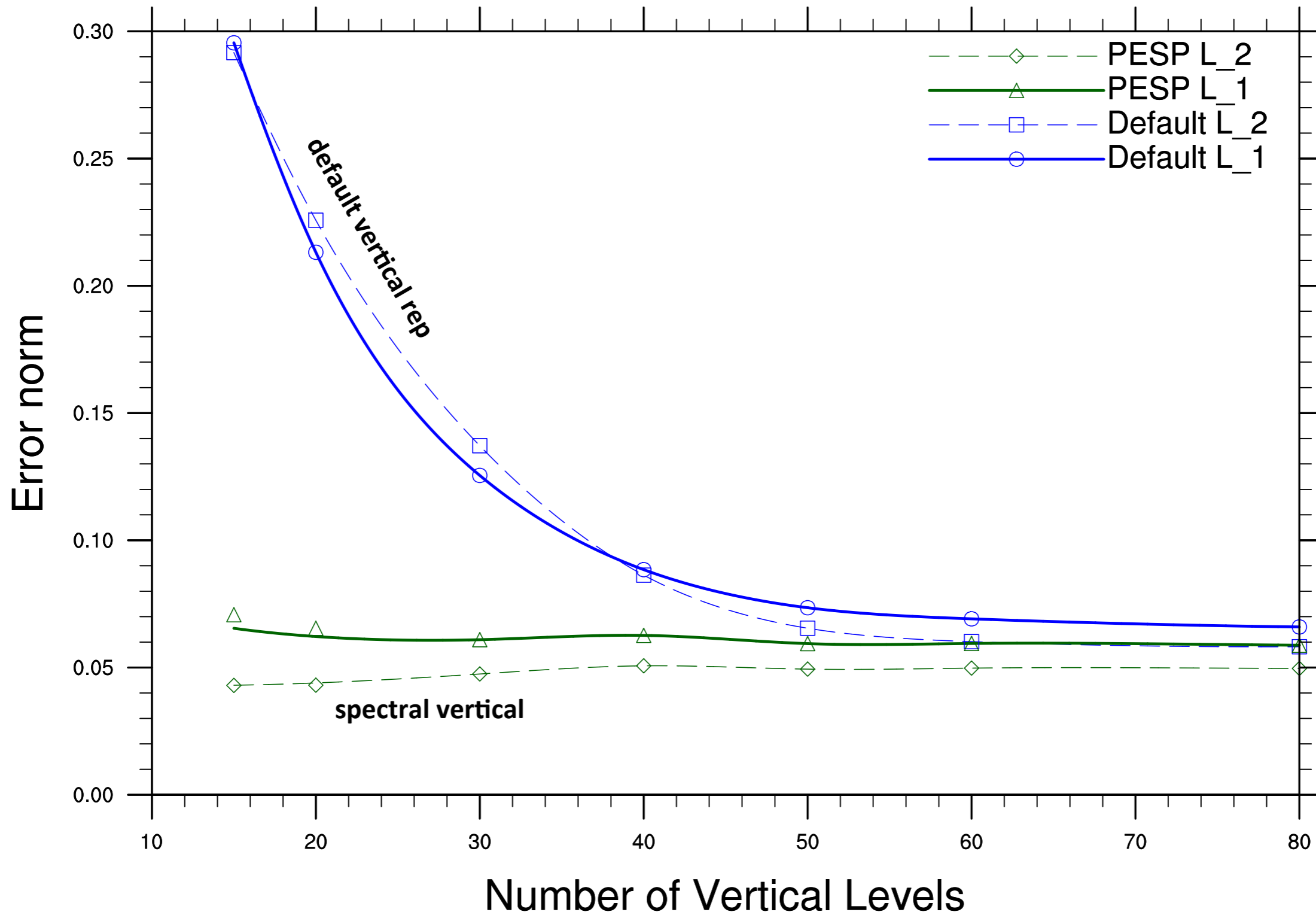
dt=5 sec, no limiter, no hyperviscosity



# DCMIP1-2: ERROR NORMS AT 2°

- L1, L2 error computed by comparing initial and final states
- Vertical SP more accurate at all resolutions

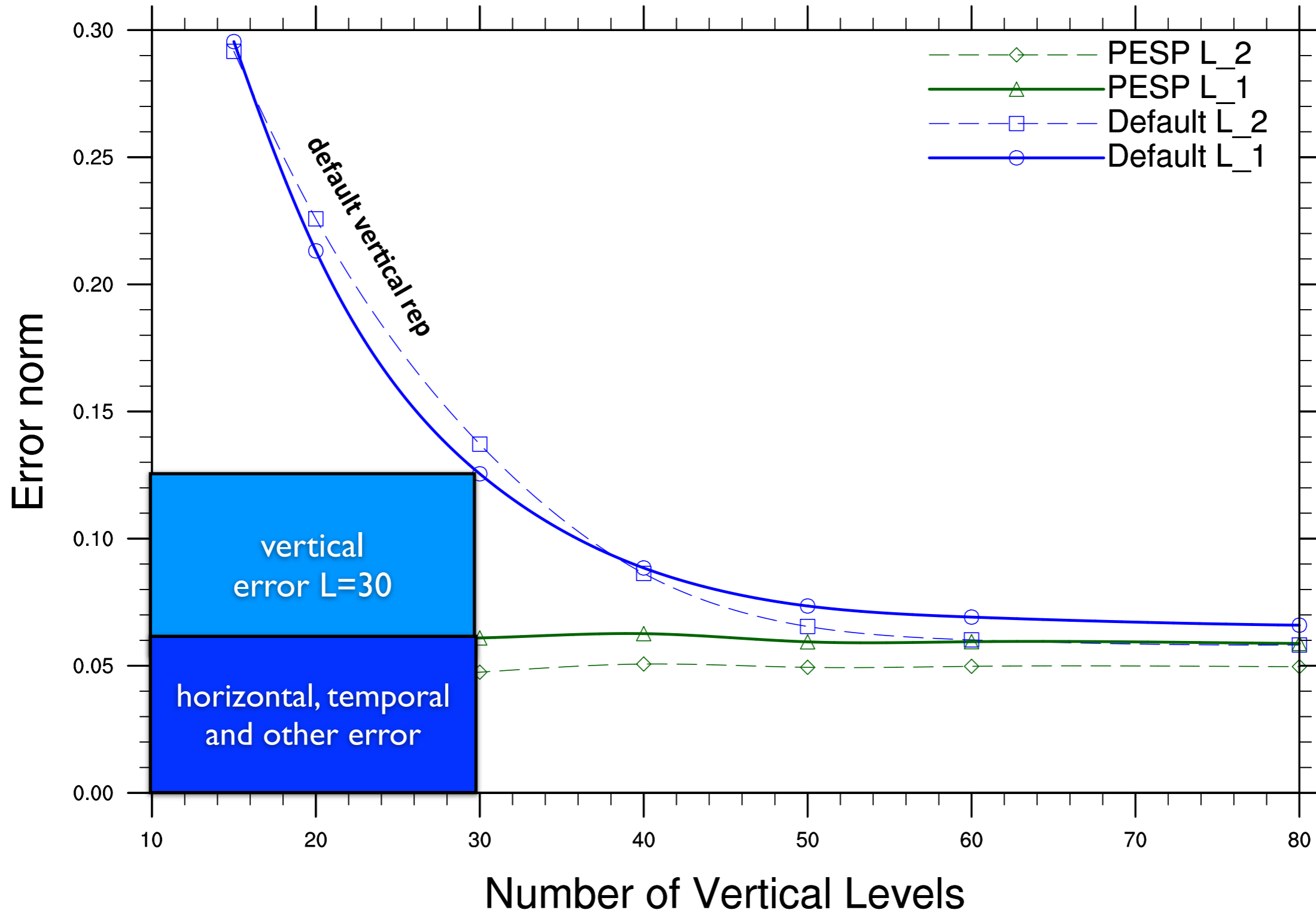
DCMIP 1-2 Error vs Vertical Resolution at 2dg



# DCMIP1-2: ERROR NORMS AT 2°

- total error = sum(vertical, temporal, horizontal, other err)
- vertical err is reduced with greater L

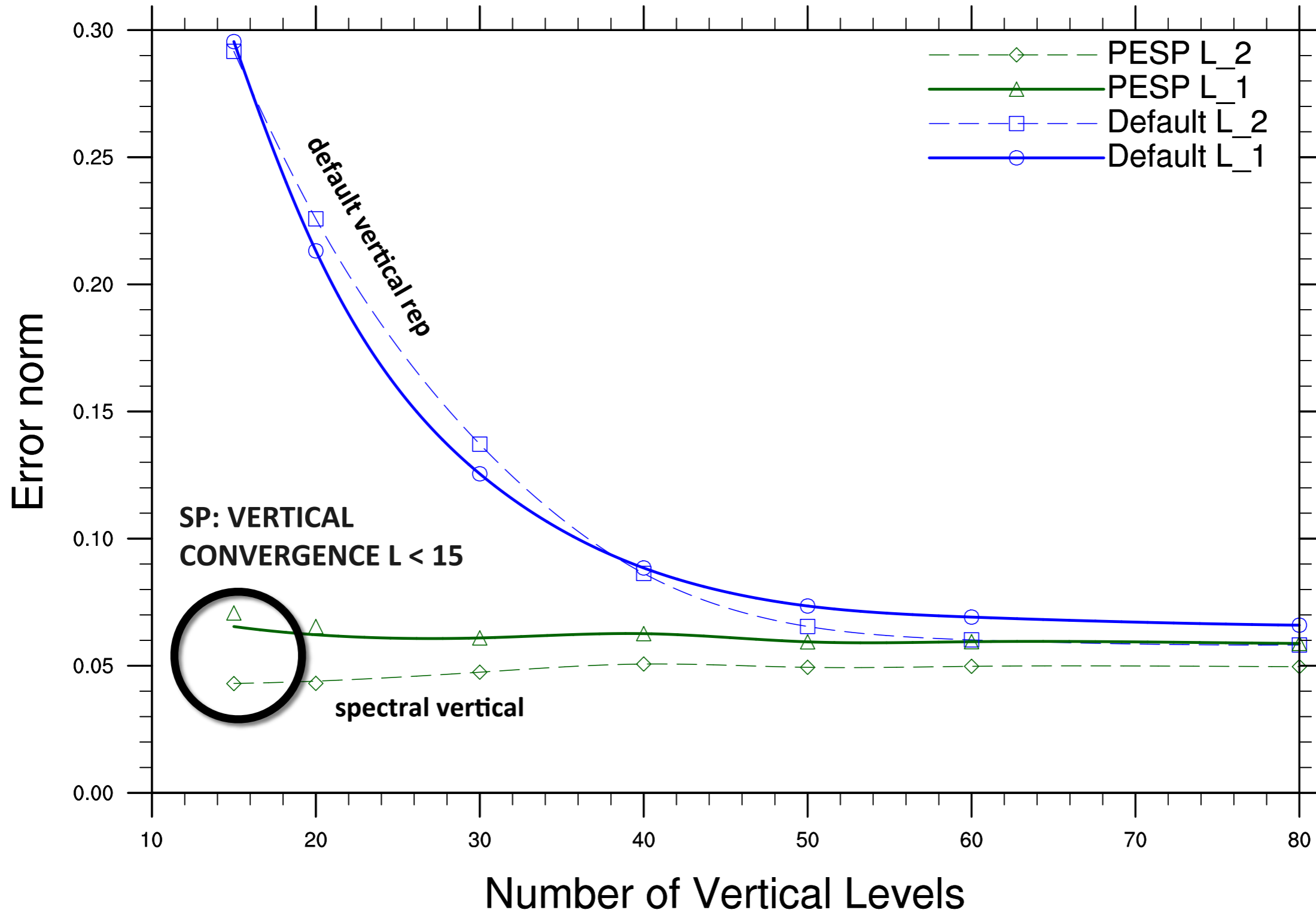
## DCMIP 1-2 Error vs Vertical Resolution at 2dg



# DCMIP1-2: ERROR NORMS AT 2°

● spectral vertical is converged L<15 (smaller than other error sources)

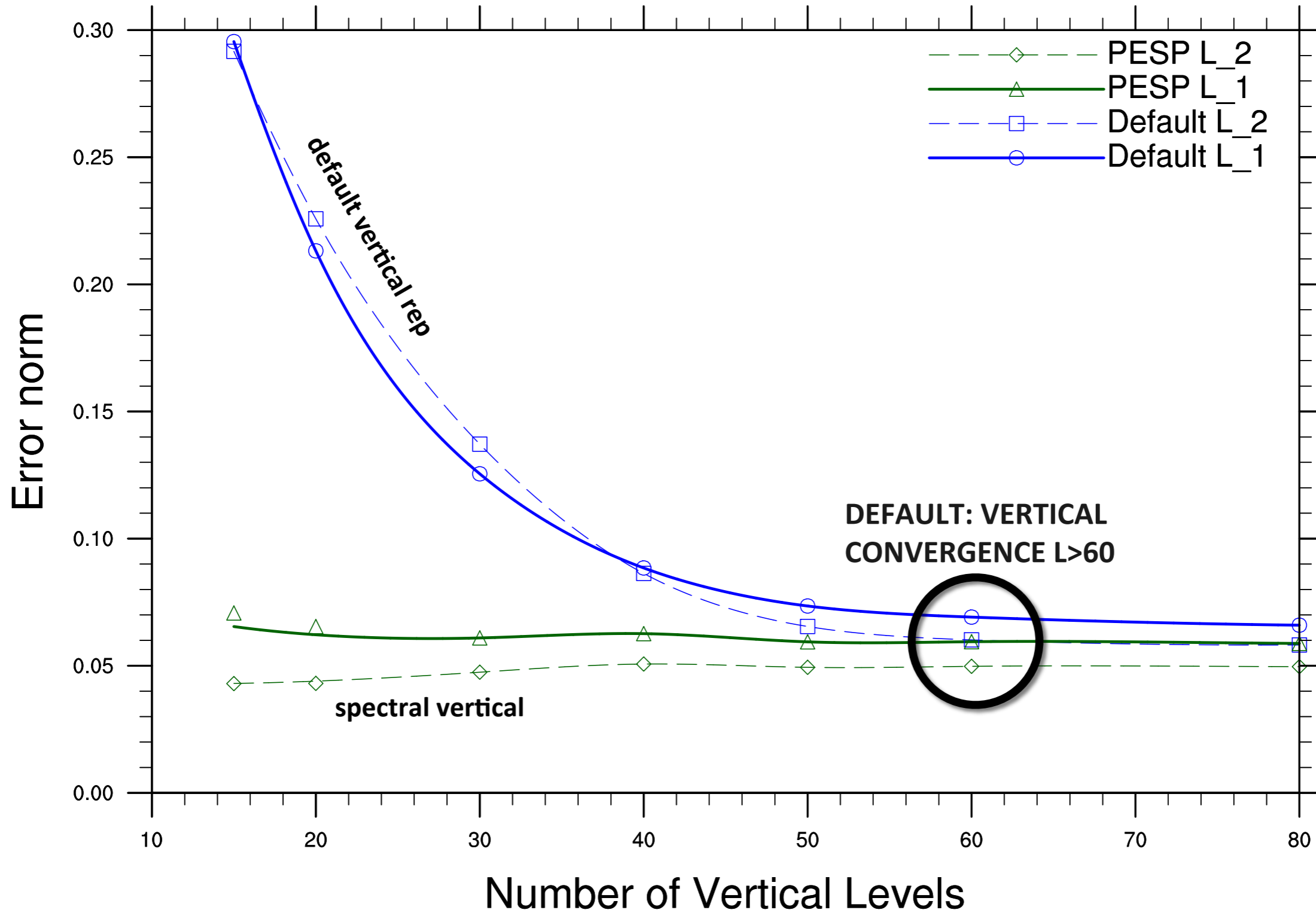
## DCMIP 1-2 Error vs Vertical Resolution at 2dg



# DCMIP1-2: ERROR NORMS AT 2°

- default converged at  $L > 60$
- asymptotic approach to vertical SP result

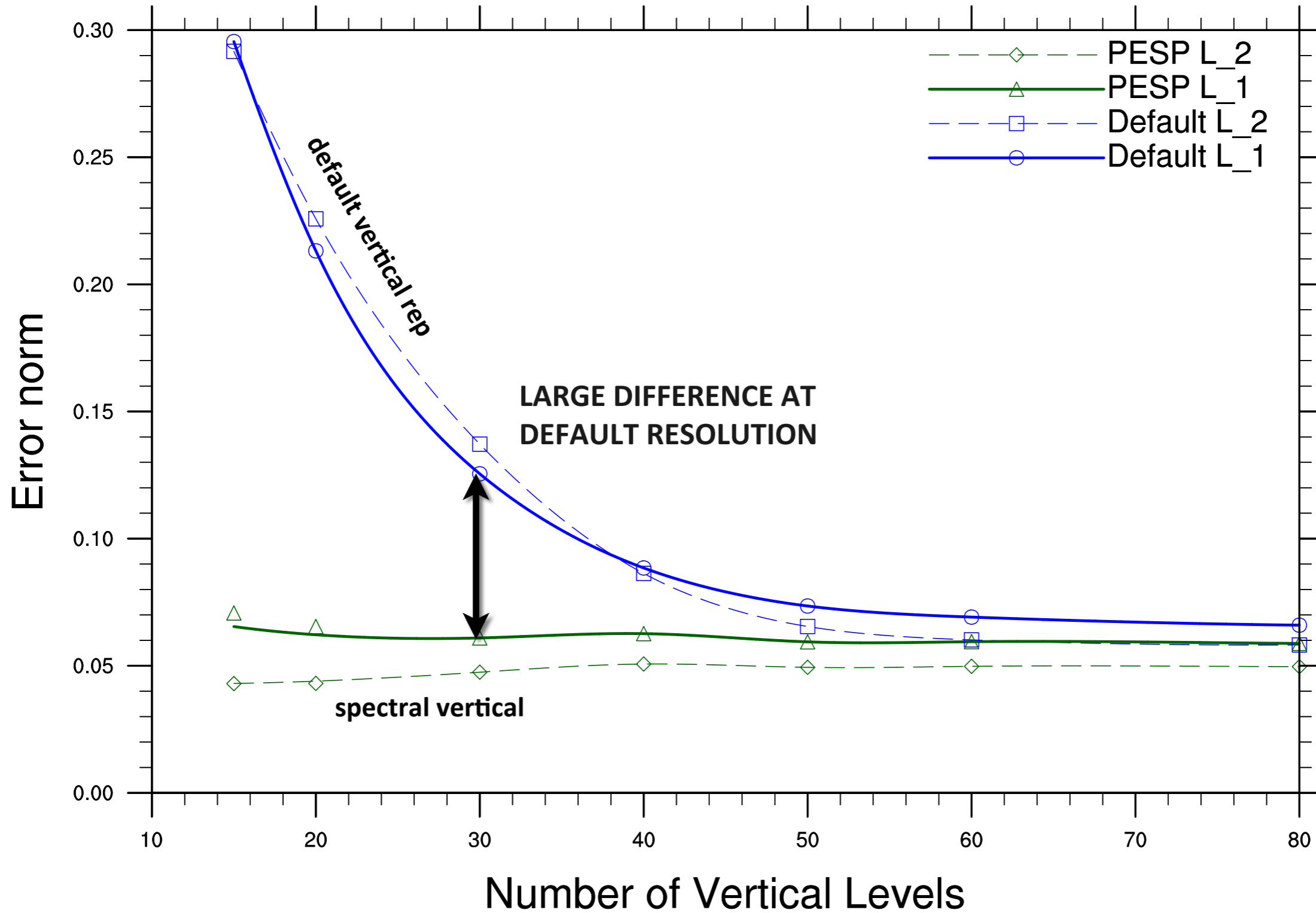
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# DCMIP1-2: ERROR NORMS AT 2°

● At default resolution, there is a large difference in vertical accuracy

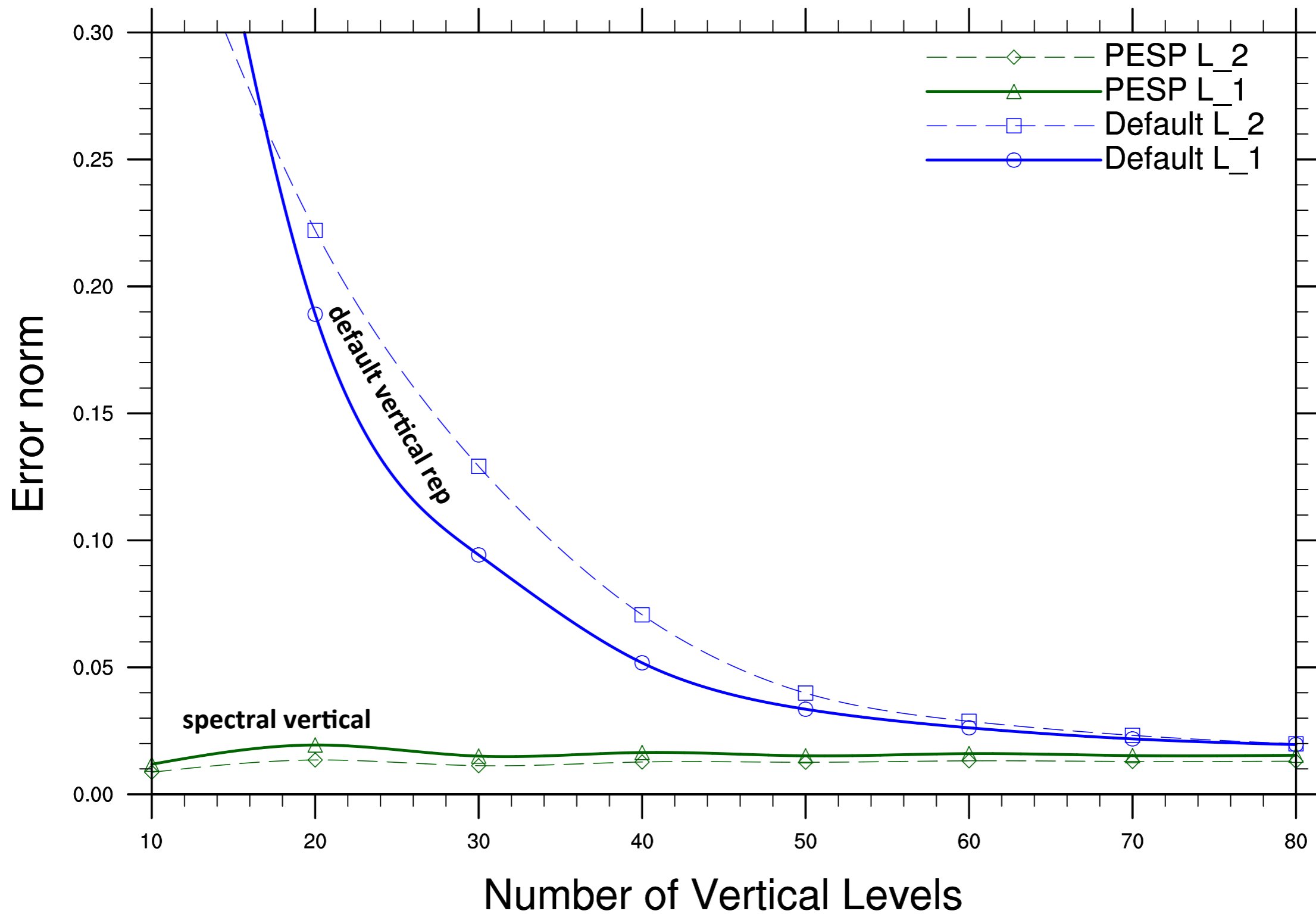
## DCMIP 1-2 Error vs Vertical Resolution at 2dg



# DCMIP1-2: ERROR NORMS AT 1°

- At 1° horizontal resolution, errors are shifted down
- Qualitatively the same relationship

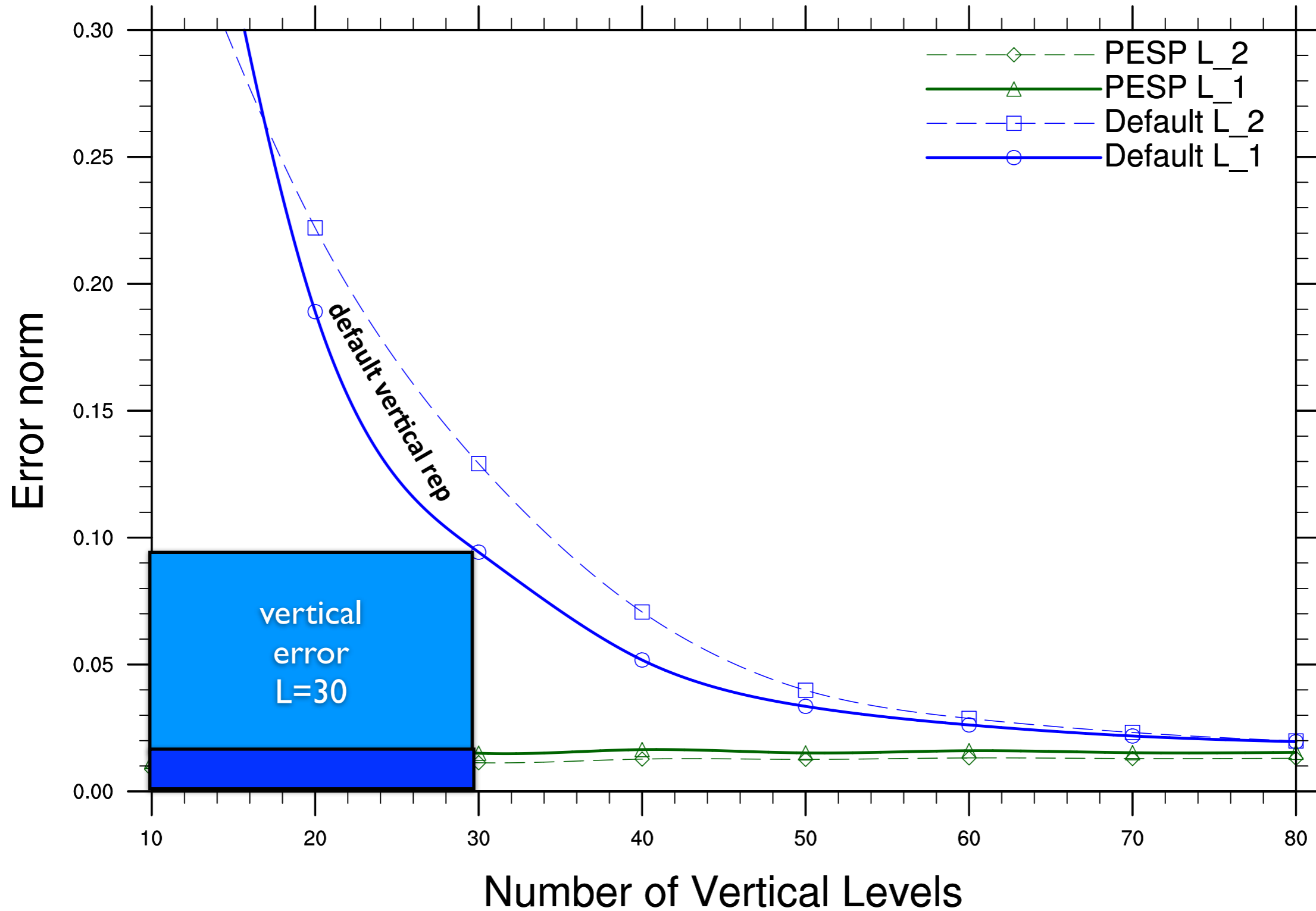
**DCMIP 1-2 Error vs Vertical Resolution at 1dg**



# DCMIP1-2: ERROR NORMS AT 1°

- Horizontal error is greatly reduced
- Vertical error stays about the same

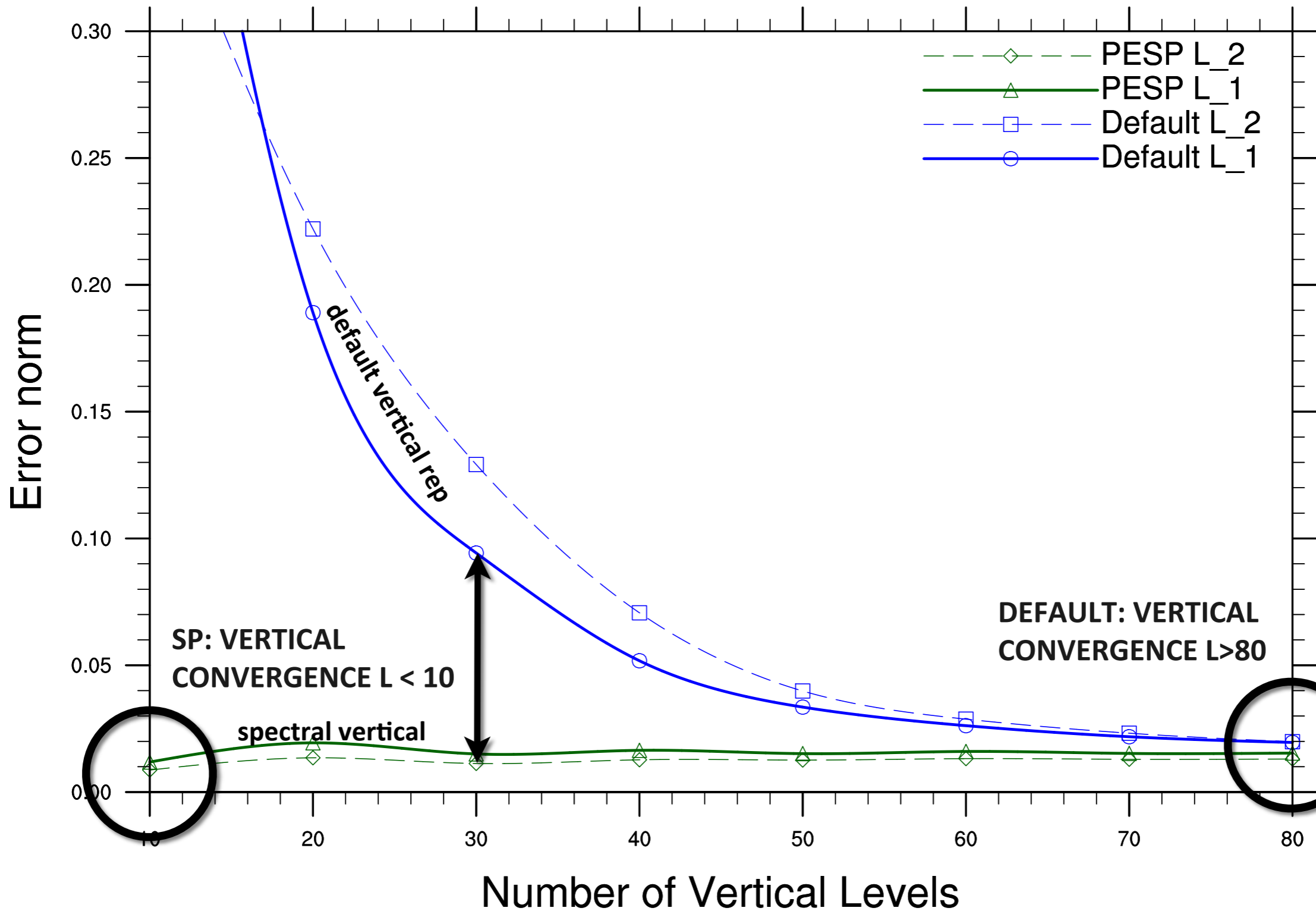
## DCMIP 1-2 Error vs Vertical Resolution at 1dg



# DCMIP1-2: ERROR NORMS AT 1°

● SP converged L<10    default L>80    large difference at L=30

## DCMIP 1-2 Error vs Vertical Resolution at 1dg





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- Extract **prim\_run walltotal**: isolates tracer and dynamic run time

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prim_run	256	256	4.423680e+06	<b>1.073763e+04</b>	42.070	41.068
prim_advance_exp	256	256	4.423680e+06	3.870625e+03	18.405	14.196
prim_advec_tracers_remap_rk2	256	256	4.423680e+06	3.936514e+03	17.003	10.629
vertical_remap	256	256	4.423680e+06	2.311321e+03	10.434	8.373
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prim_advance_exp	256	256	4.423680e+06	3.787254e+03	17.252	13.911

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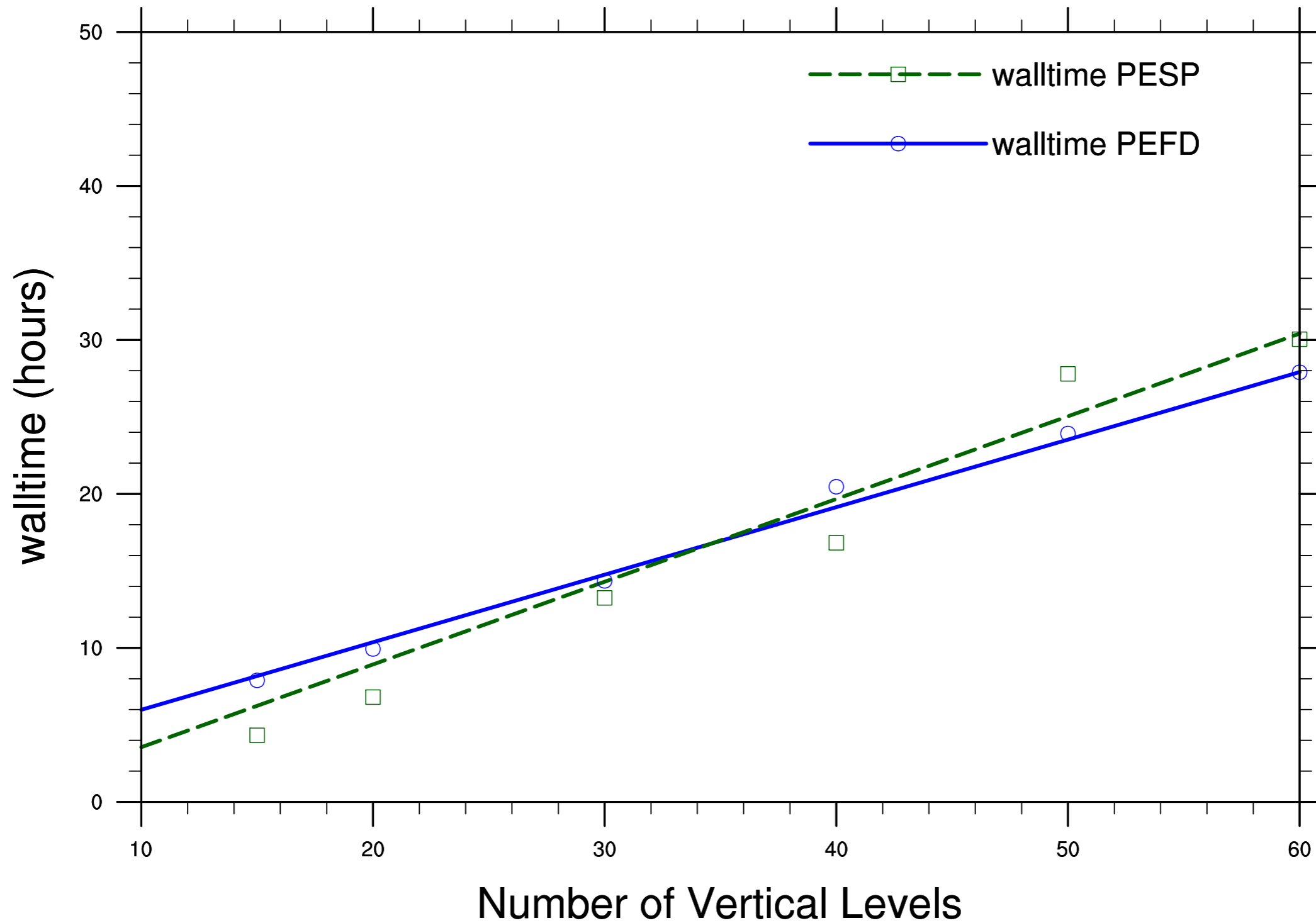
$$9929 \text{ s} / 10737 \text{ s} = 0.92$$

VERTICAL-SPECTRAL TRACER TRANSPORT IS **8% FASTER** AT **L=30**

# DCMIP1-2: PERFORMANCE VS VERTICAL RESOLUTION

- Look at wallclock time vs L
- Near optimal scaling for both, all data on one node

DCMIP 1-2: Total Wall-Clock Time vs Vertical Resolution at 2dg

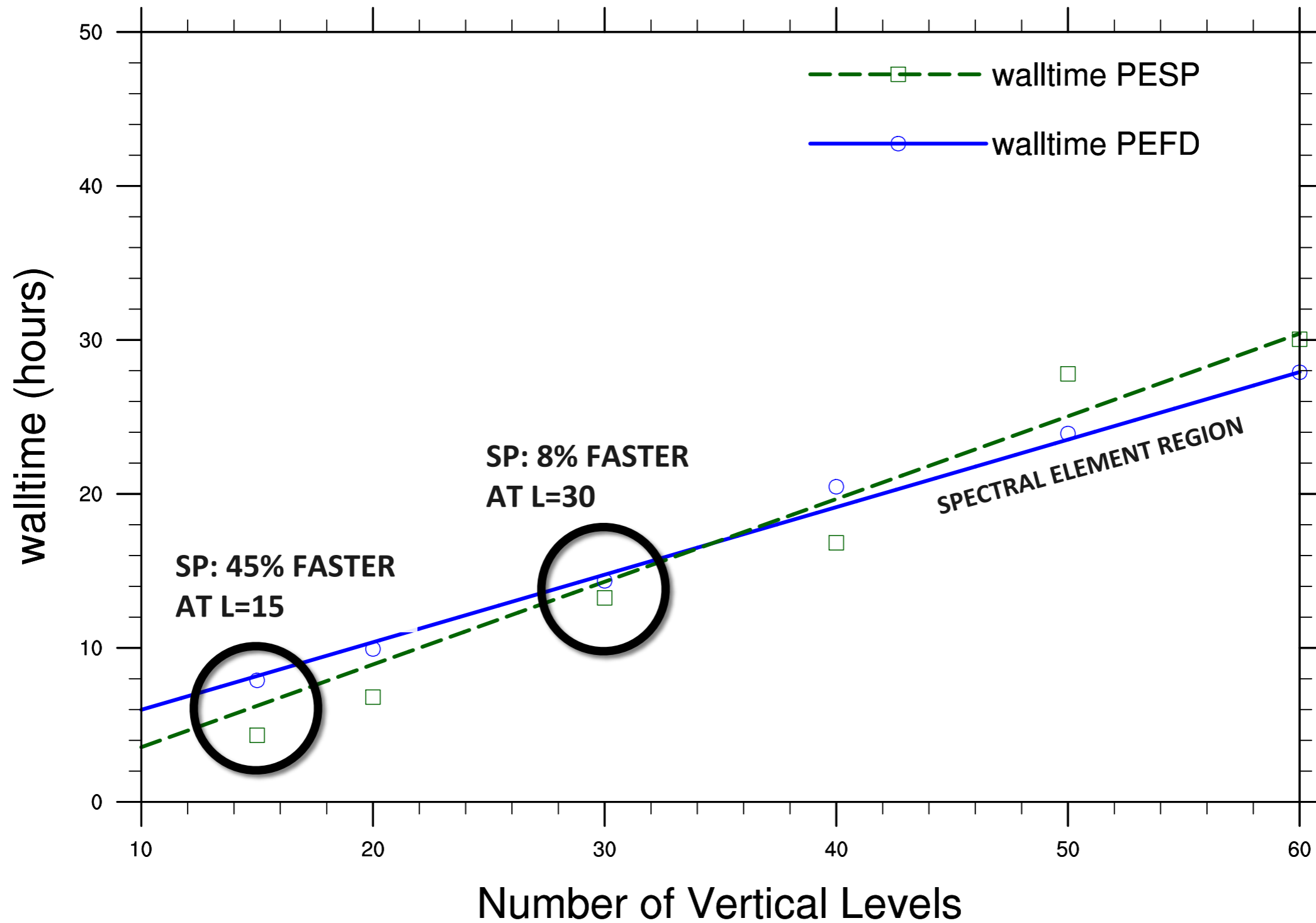


DOE XSEDE Stampede supercomputer, 256 cores

# DCMIP1-2: WALL-CLOCK TIME AT 2°

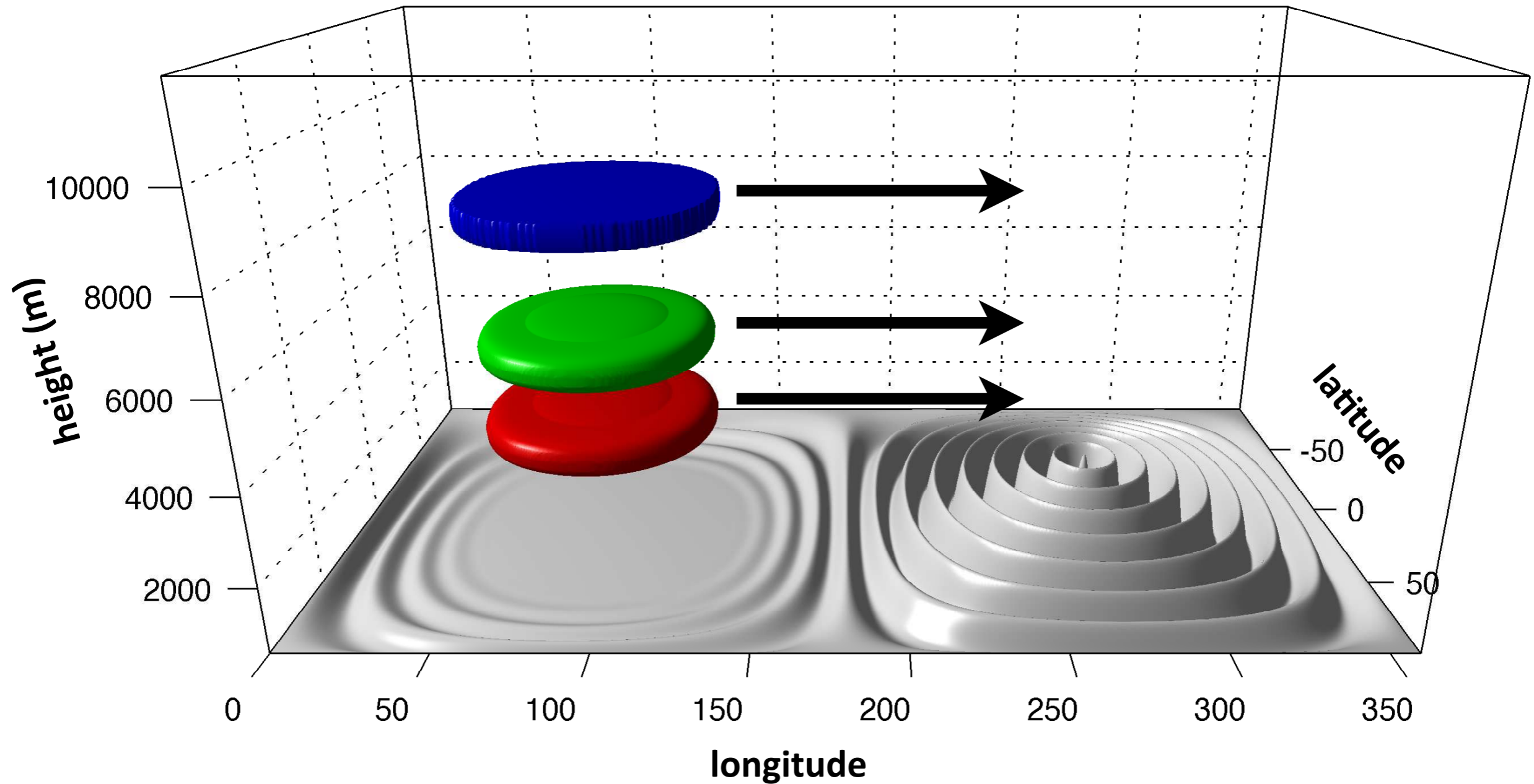
- SP much faster at low L. A bit faster at L=30
- SP is a bit slower at L=60, but here one would choose vertical spectral elements

## DCMIP 1-2: Total Wall-Clock Time vs Vertical Resolution at 2dg



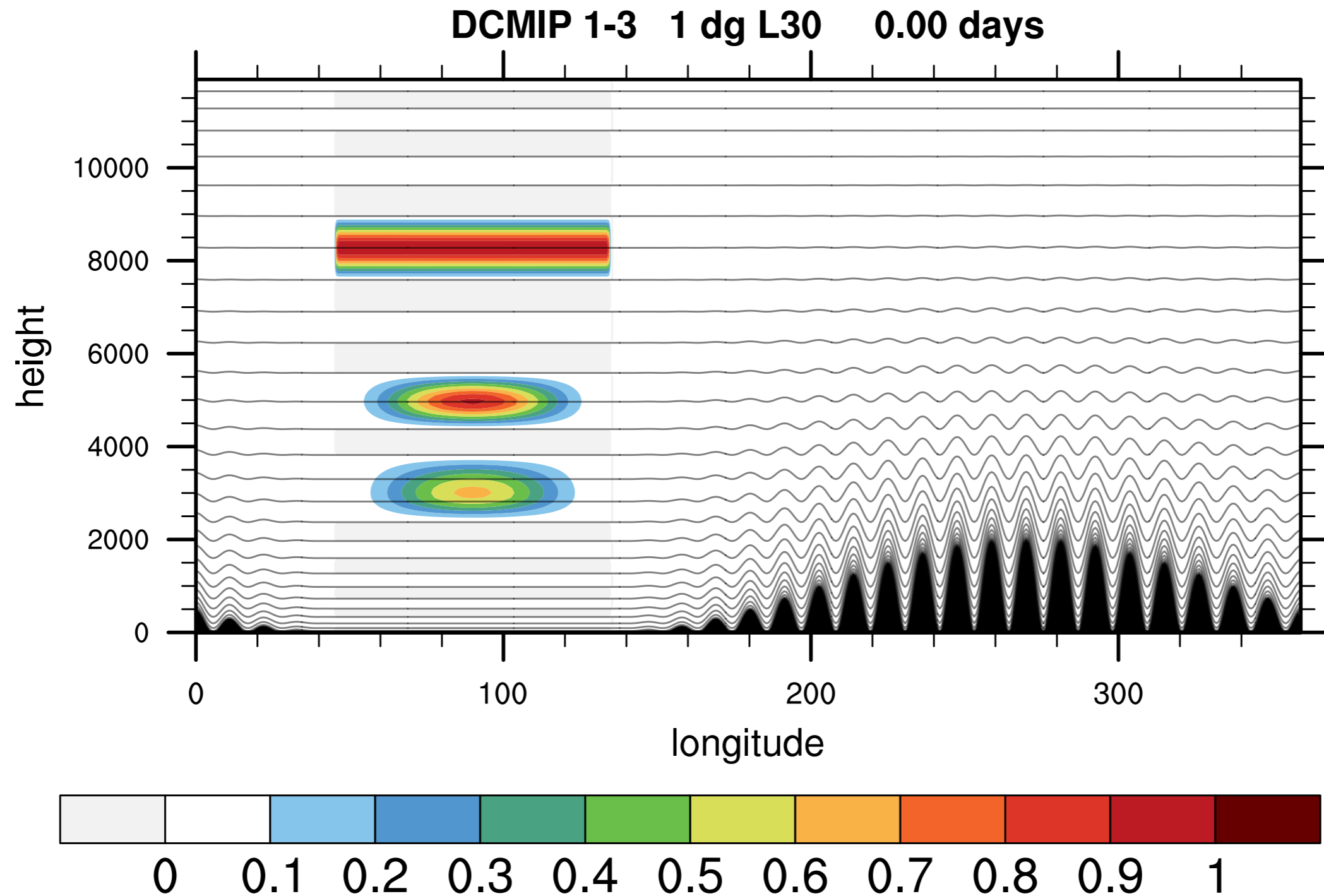
# DCMIP 1-3: DESCRIPTION

- Thin cloud tracer transport over Schär-type mountain range
- Tests impact of terrain following coordinates: numerical mixing, induced flux



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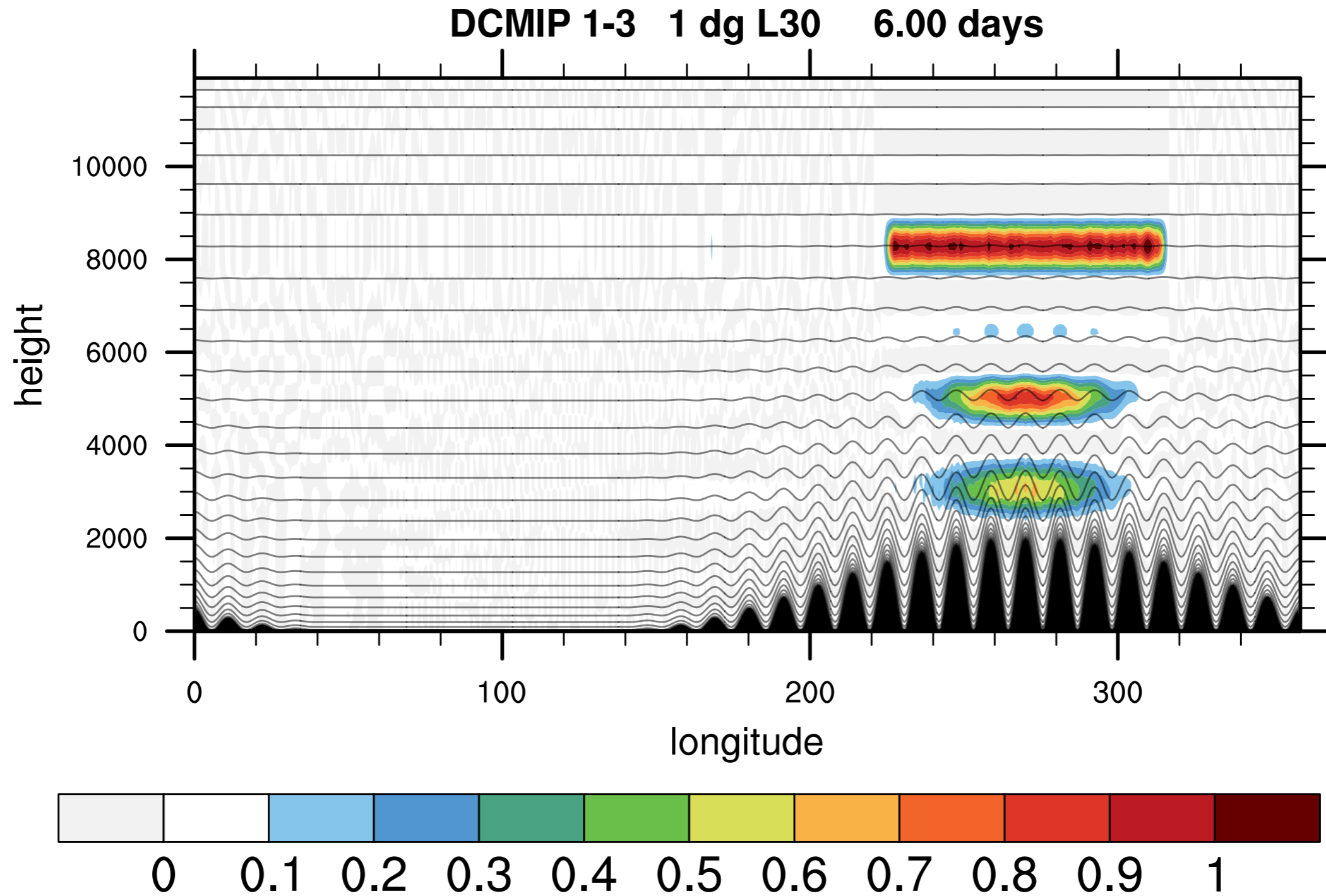
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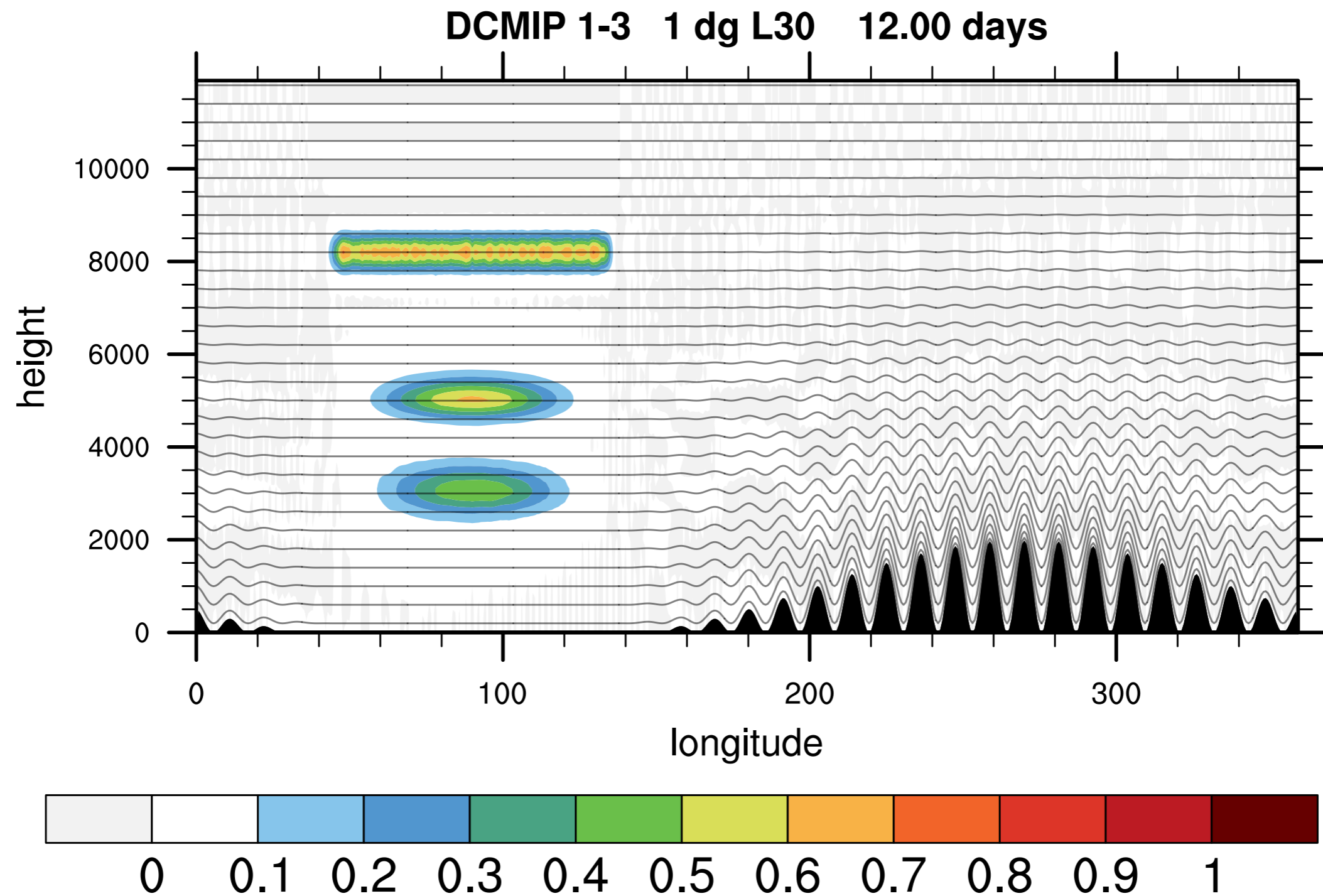
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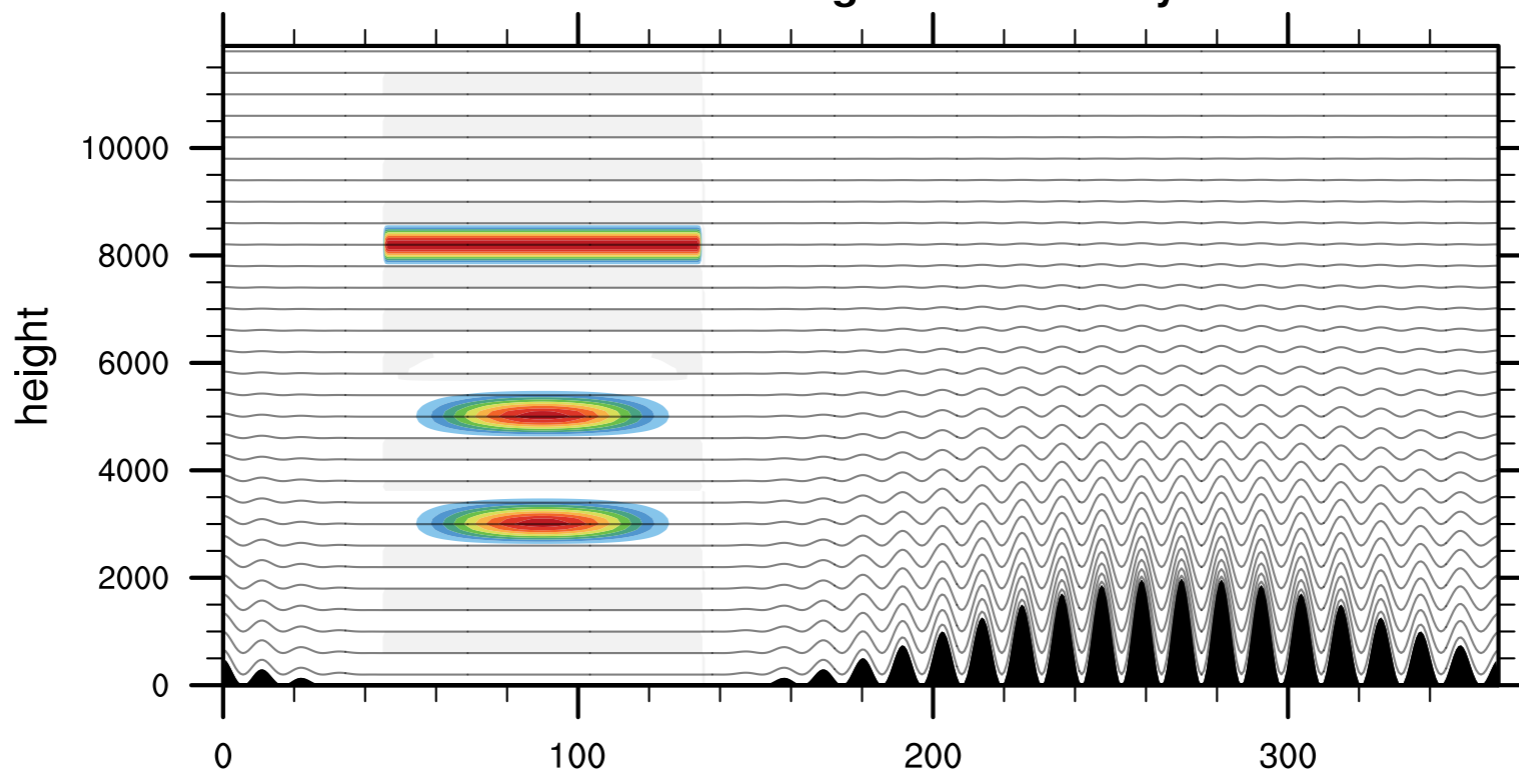
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# DCMIP 1-3: HORIZONTAL THIN CLOUD TRANSPORT

DCMIP 1-3 1 dg L30 0.00 days

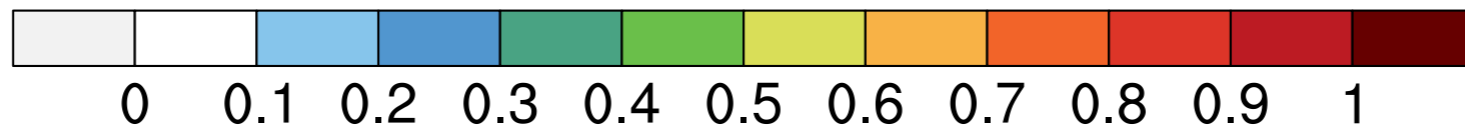
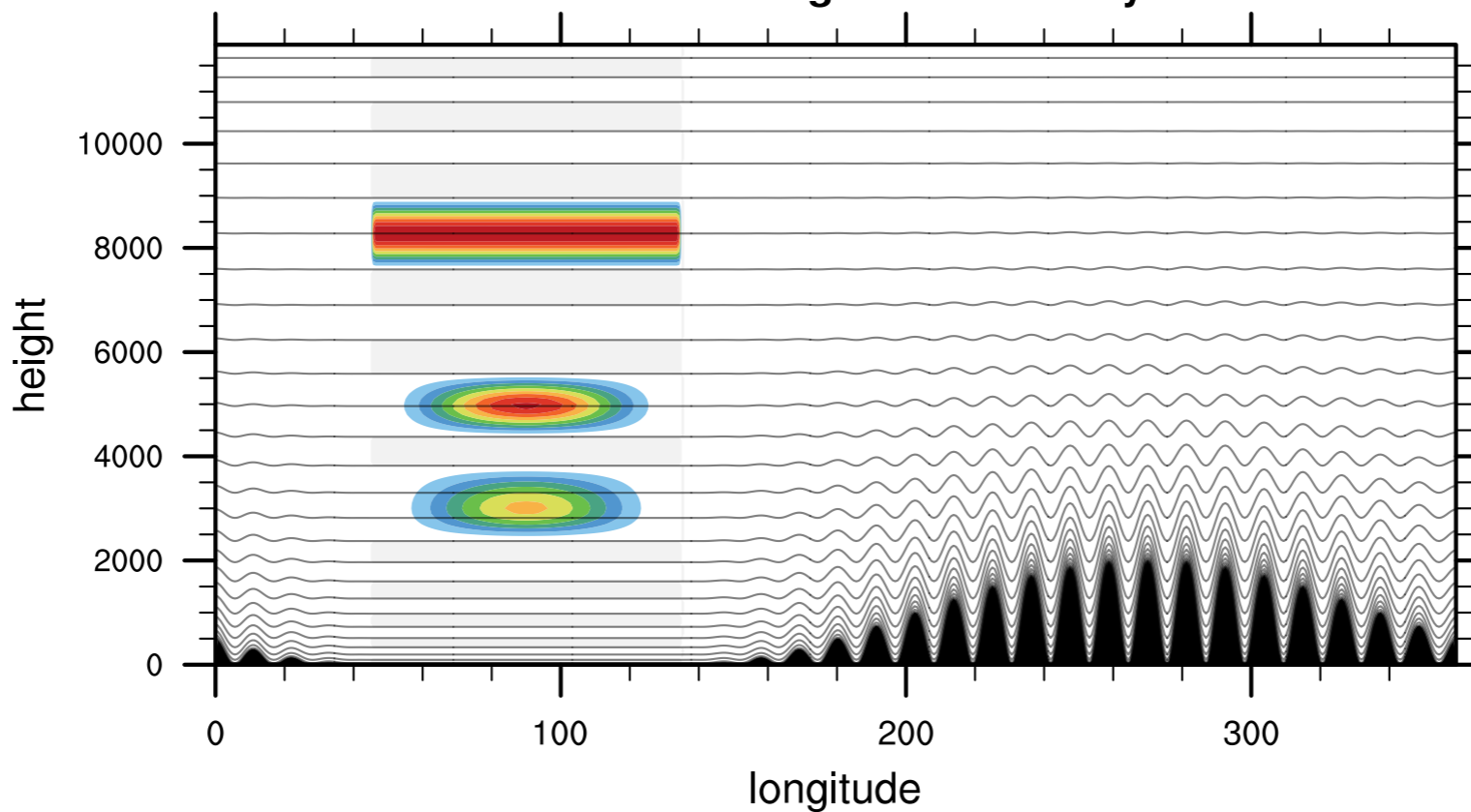
default  
method



INITIAL STATE

DCMIP 1-3 1 dg L30 0.00 days

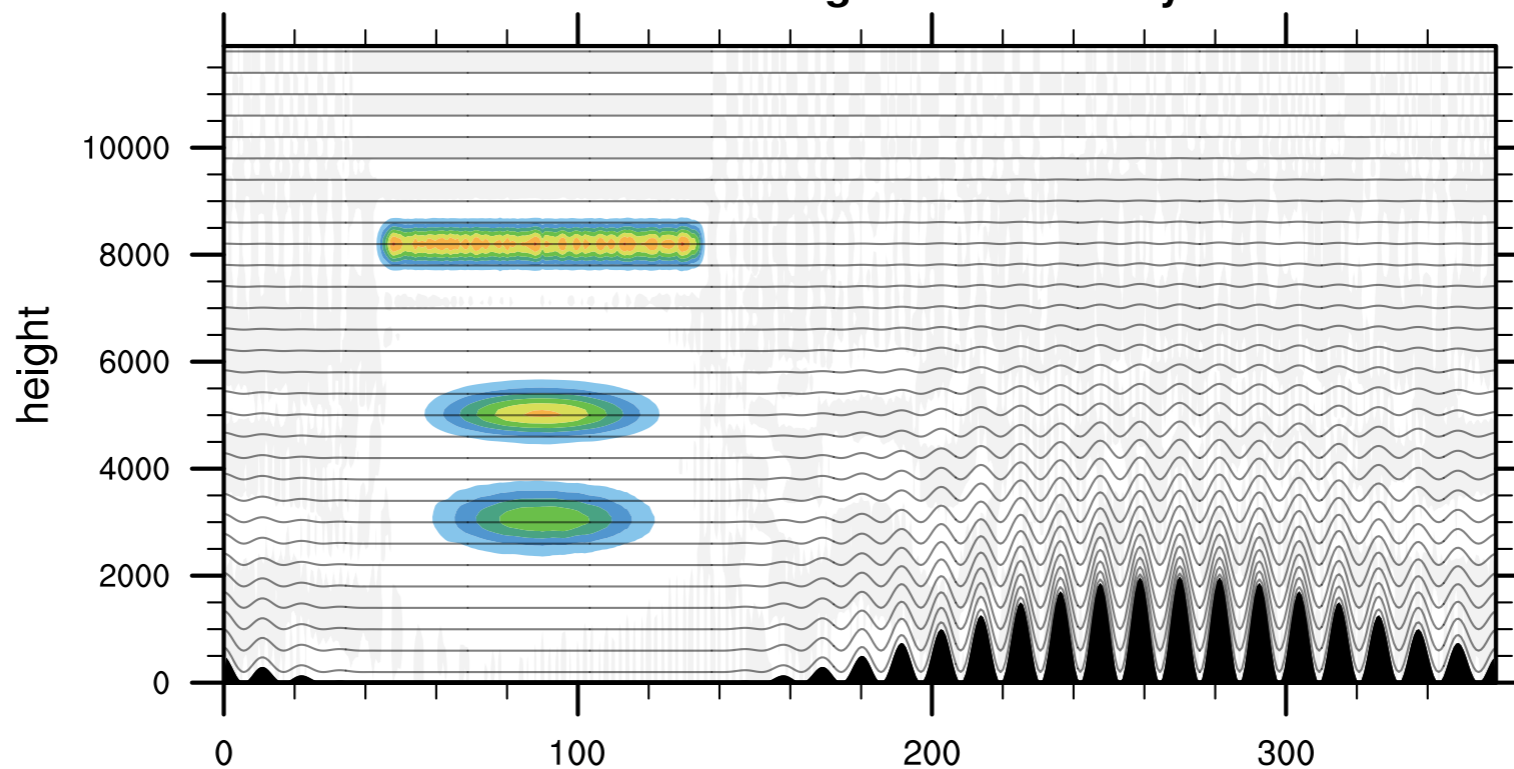
spectral  
vertical



# DCMIP 1-3: HORIZONTAL THIN CLOUD TRANSPORT

DCMIP 1-3 1 dg L30 12.00 days

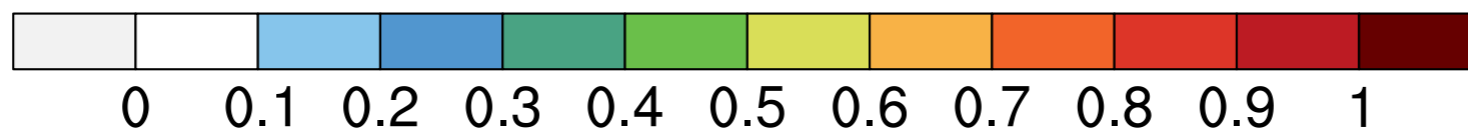
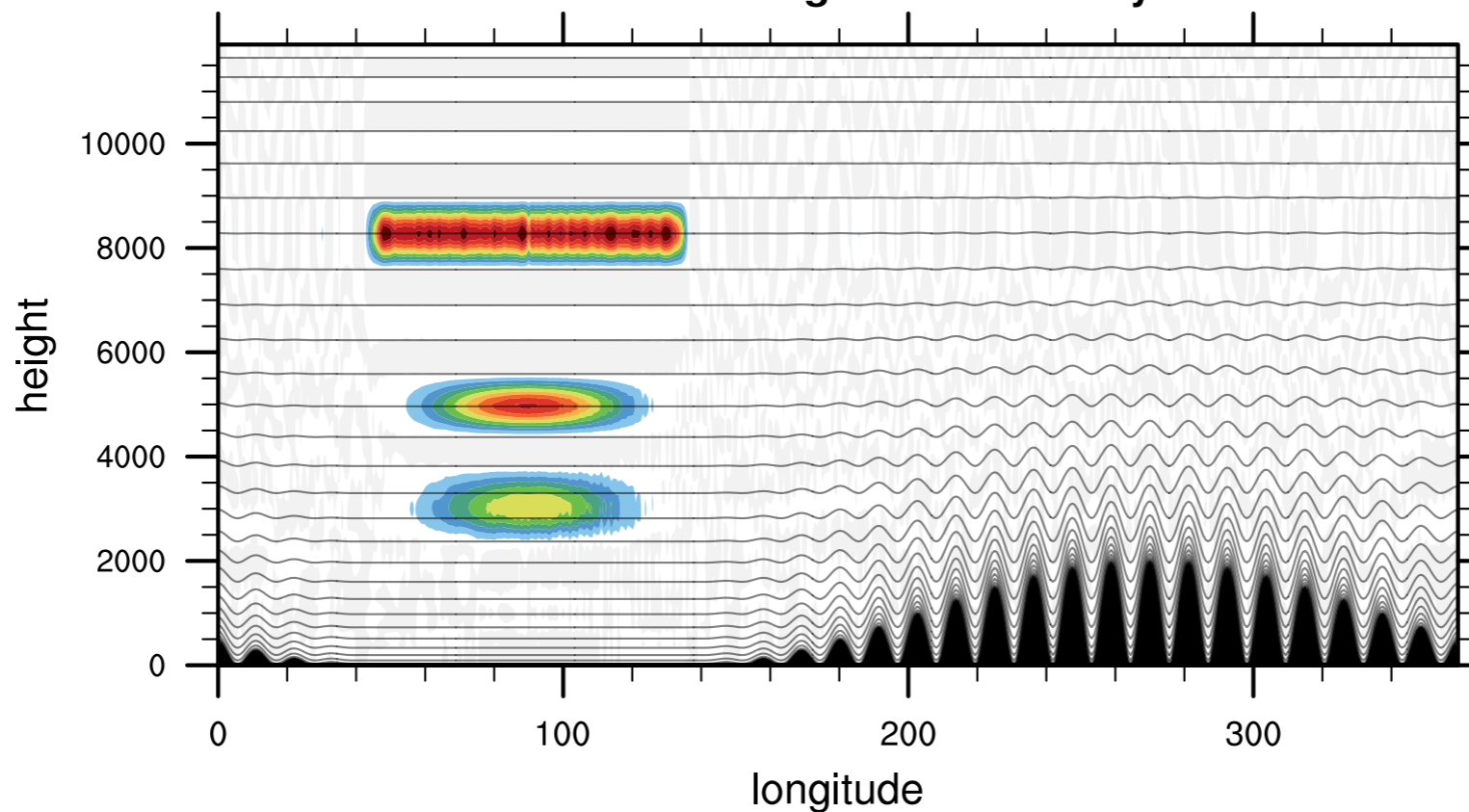
default  
method



FINAL STATE

DCMIP 1-3 1 dg L30 12.00 days

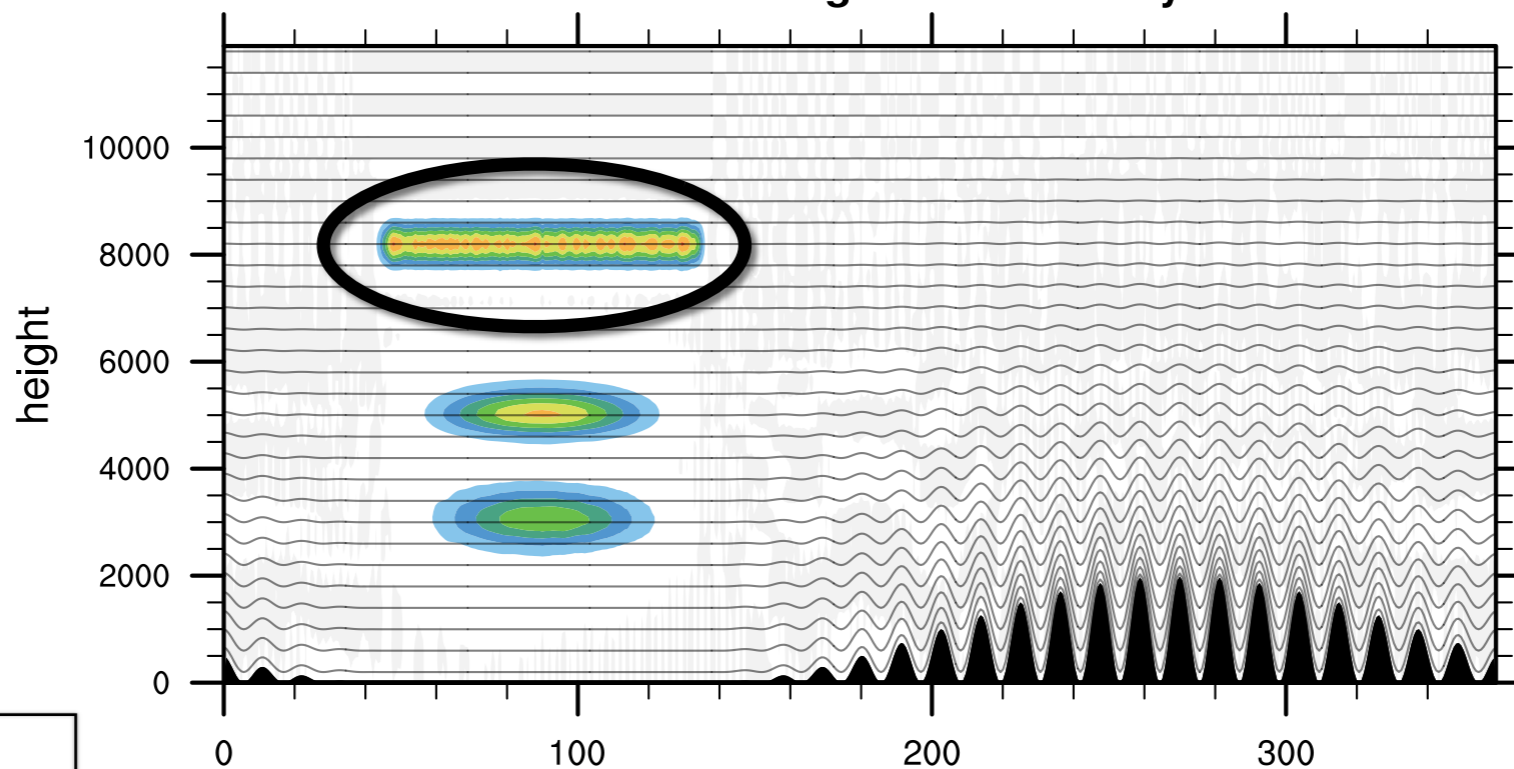
spectral  
vertical



# DCMIP 1-3: HORIZONTAL THIN CLOUD TRANSPORT

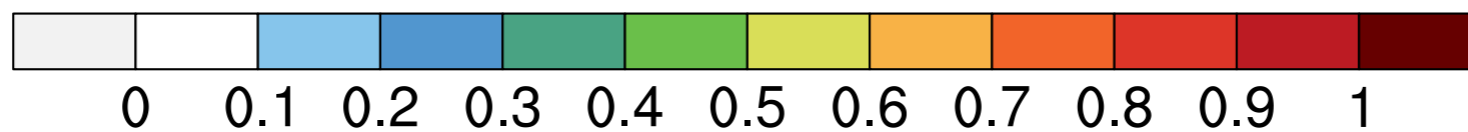
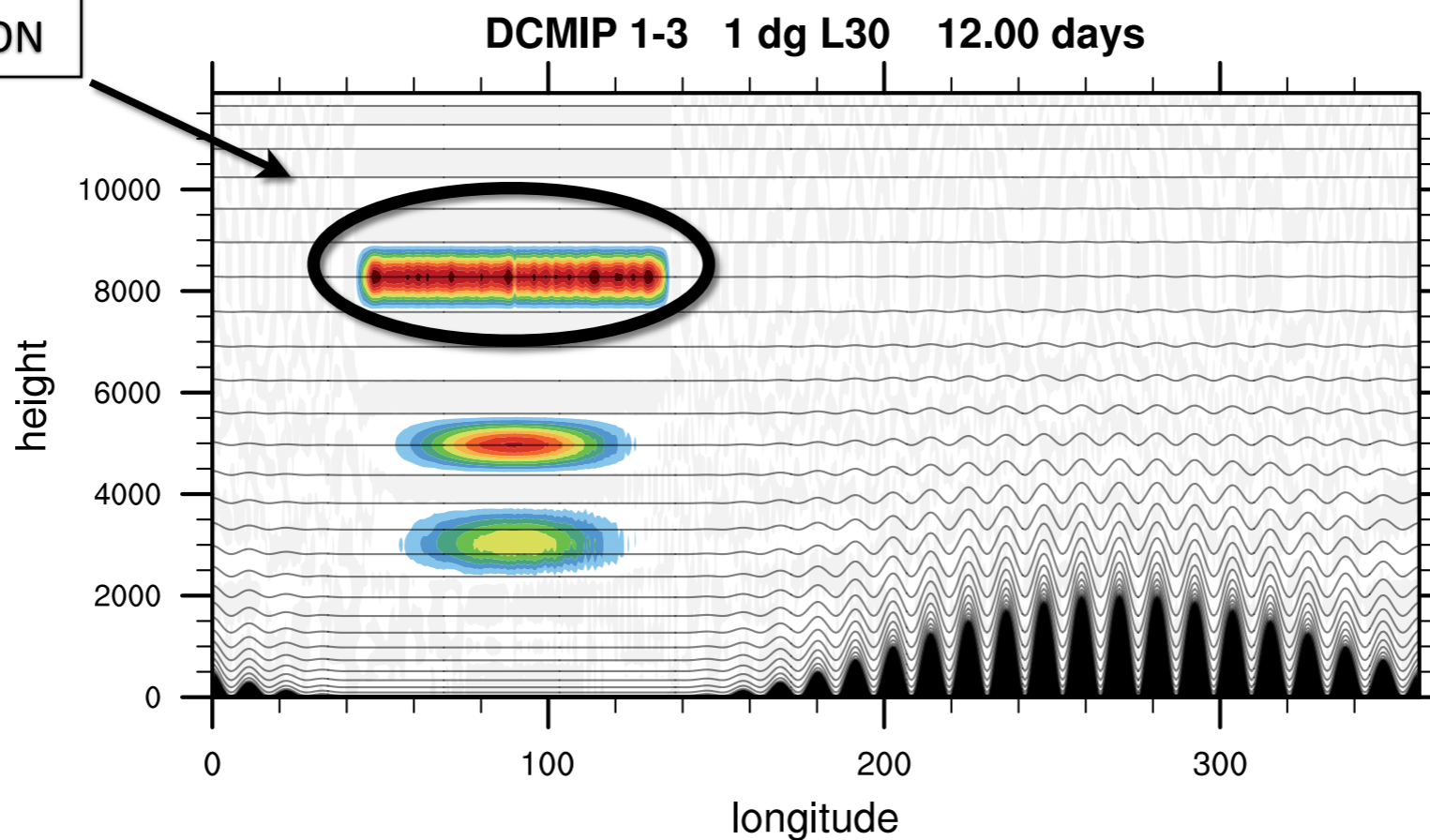
DCMIP 1-3 1 dg L30 12.00 days

default  
method



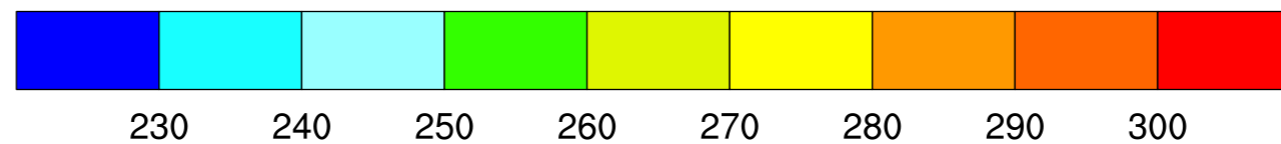
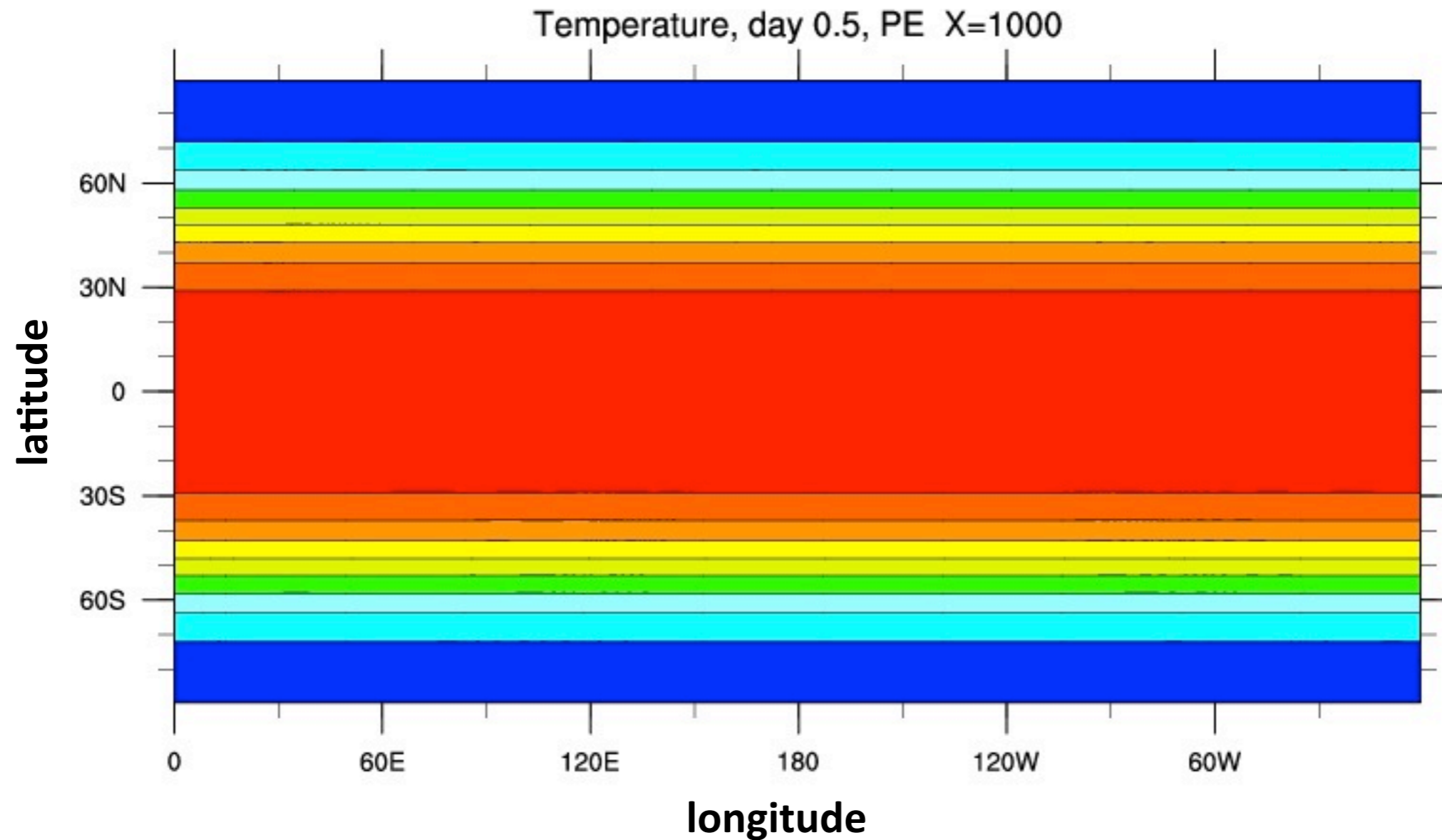
GREATLY REDUCED  
NUMERICAL DIFFUSION

spectral  
vertical



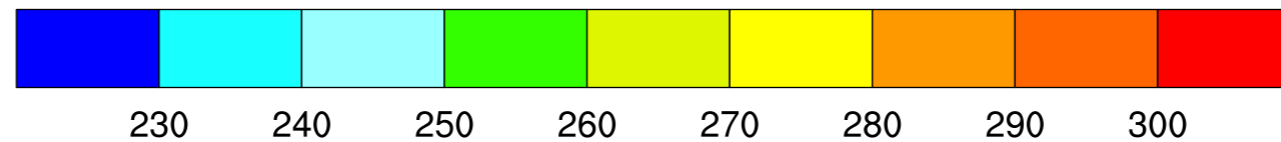
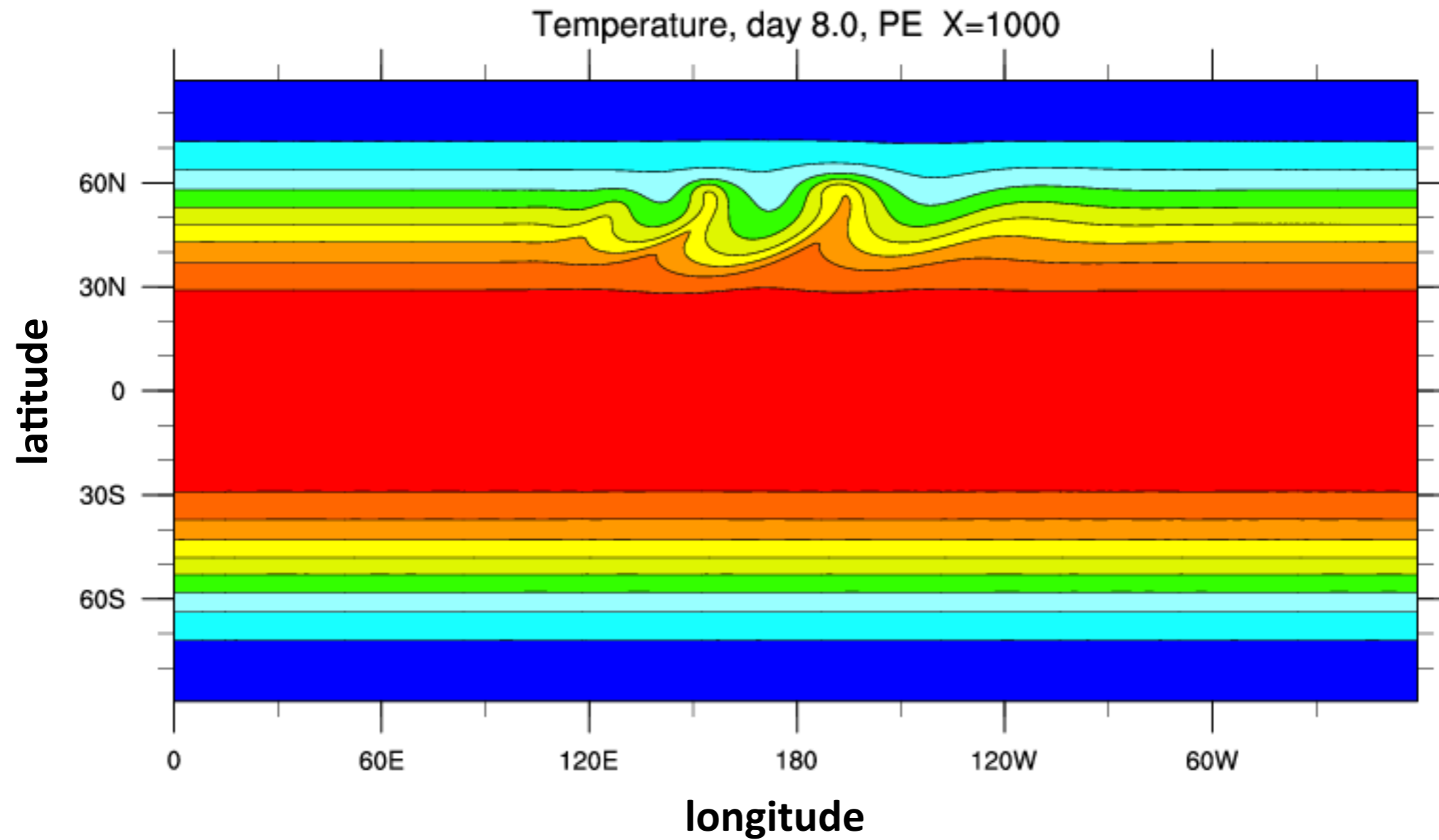
# DCMIP 4-1: DESCRIPTION

- Development of a baroclinic instability over 30 days
- Tests **primitive equation** dynamics (not just tracer transport)
- **Horizontal cross-sections** shown here



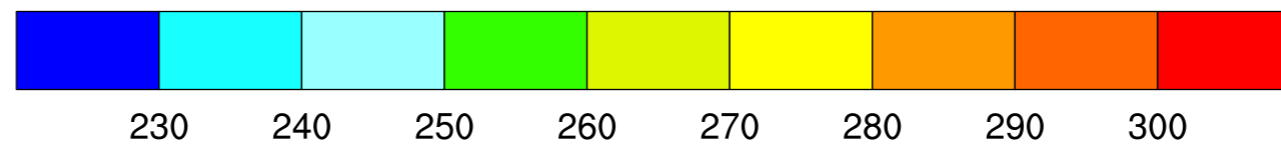
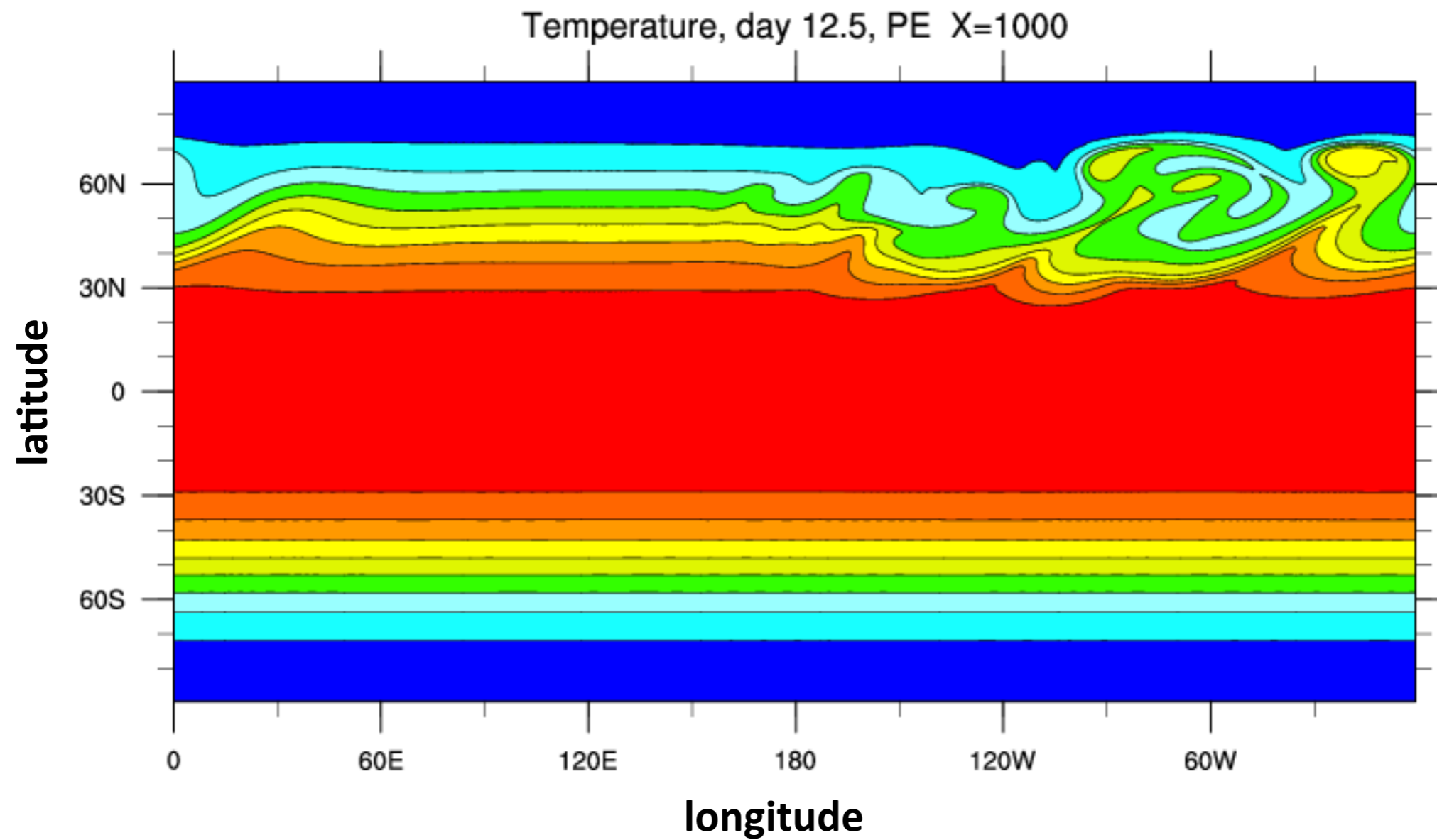
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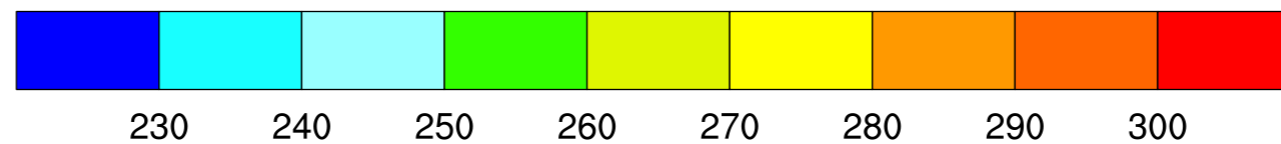
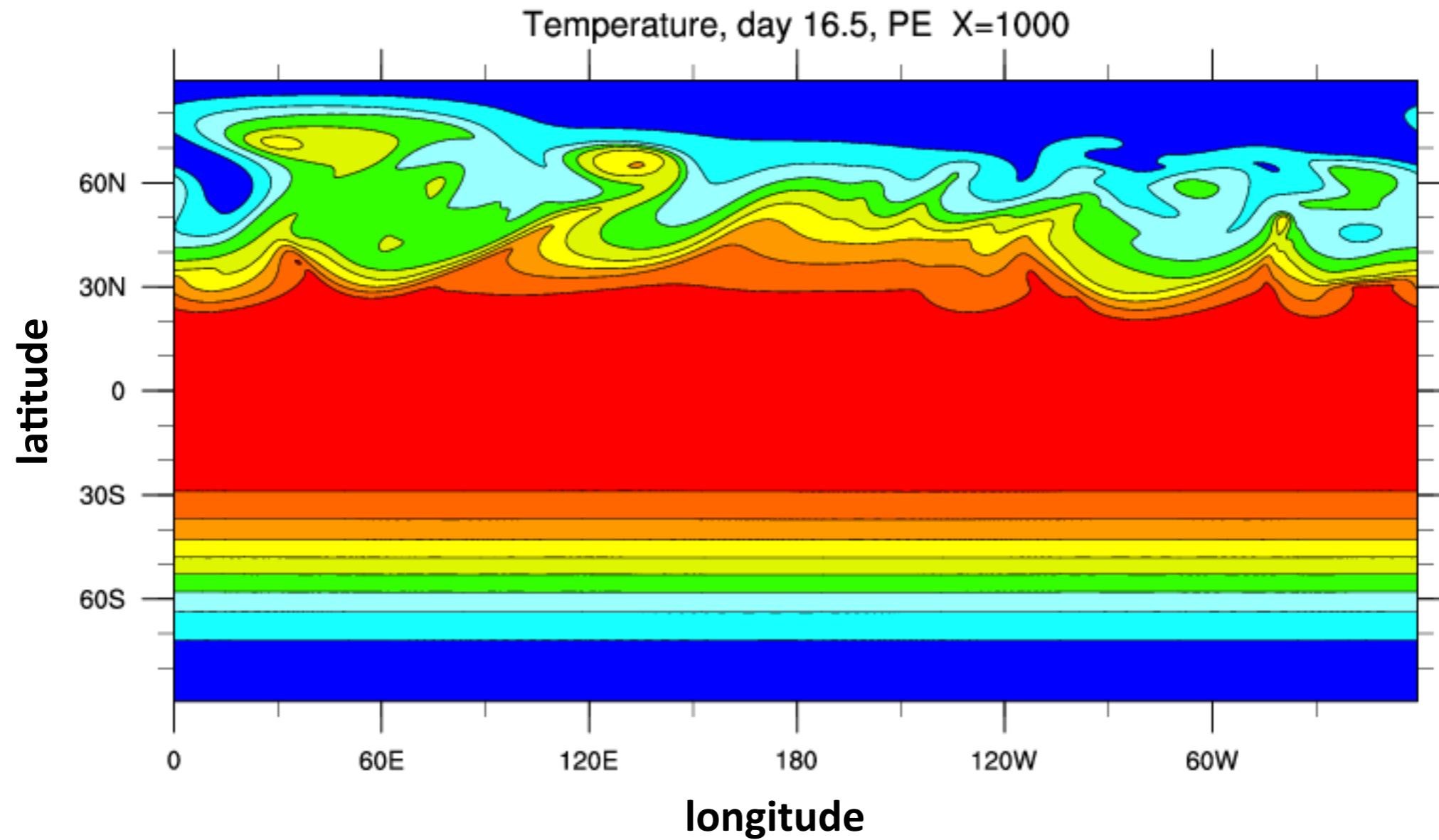
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- Tests primitive equation dynamics (not just tracer transport)
- Horizontal cross-sections shown here





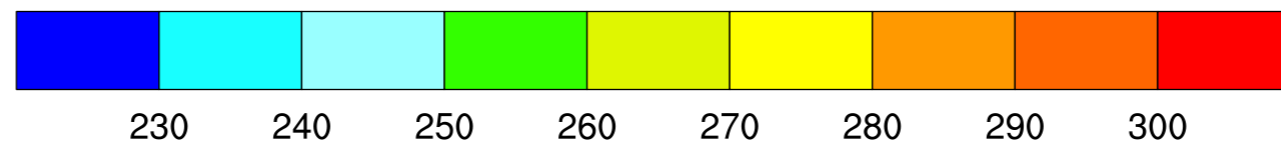
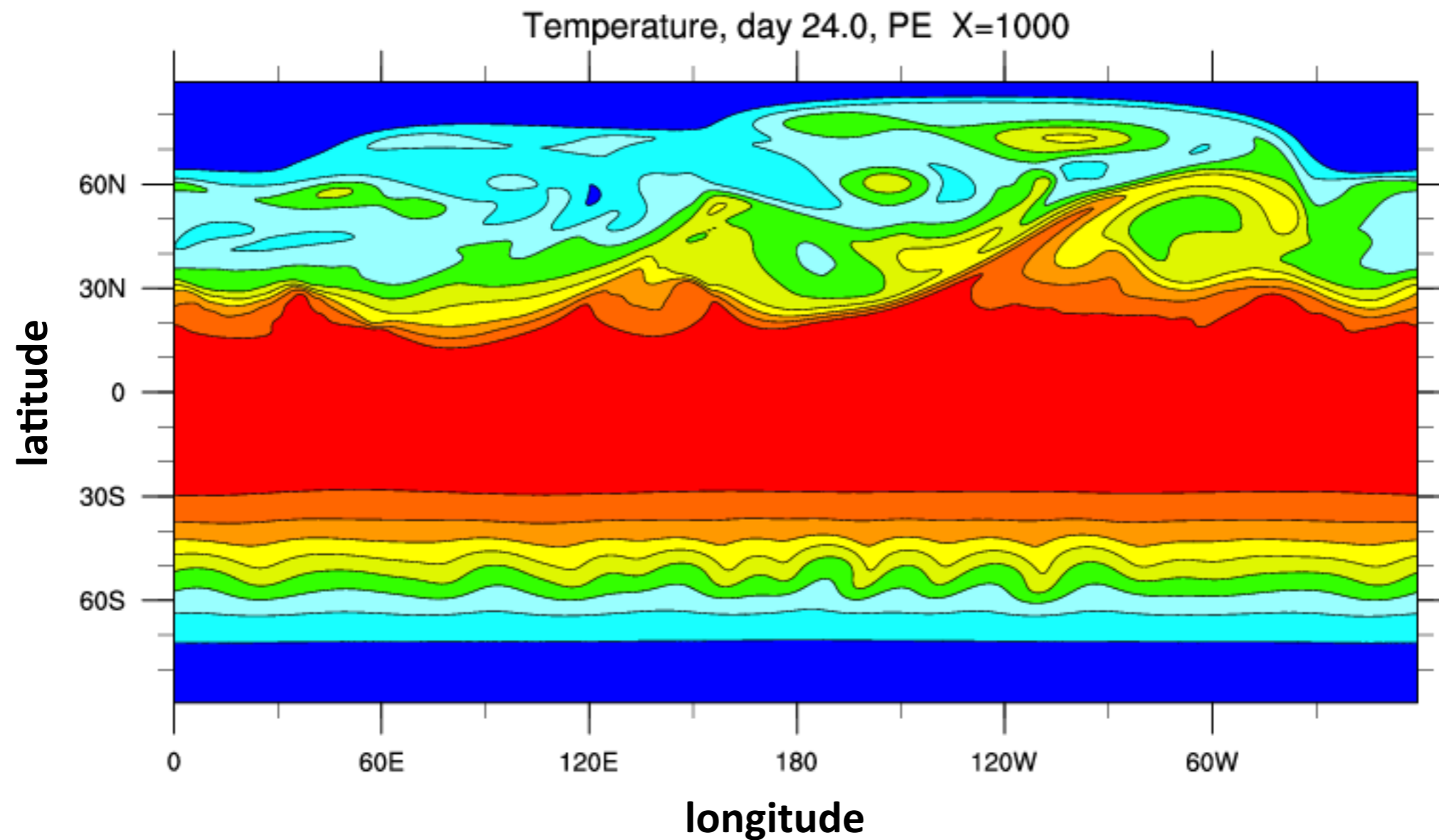
# DCMIP 4-1: DESCRIPTION

- Development of a baroclinic instability over 30 days
- Tests primitive equation dynamics (not just tracer transport)
- Horizontal cross-sections shown here



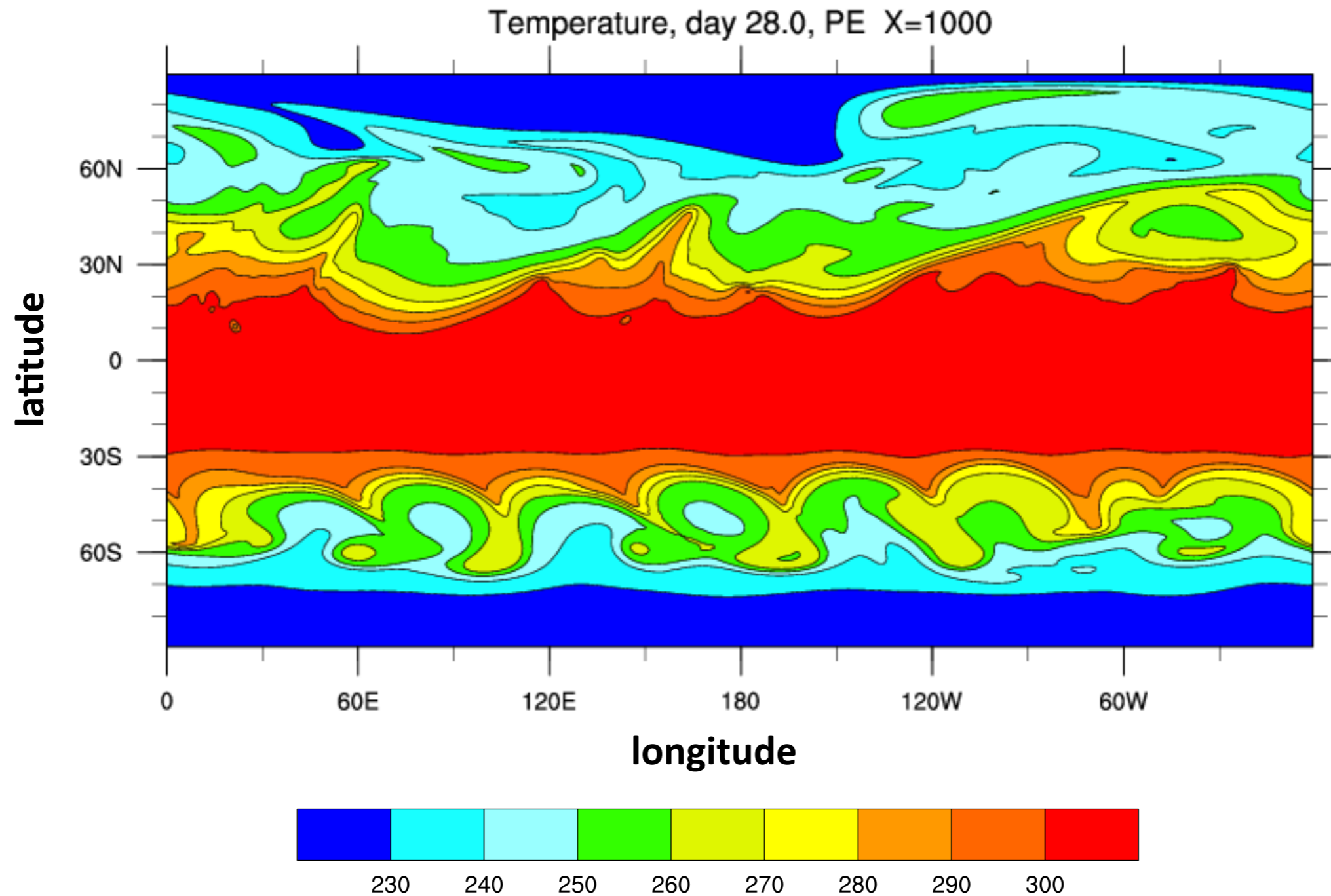
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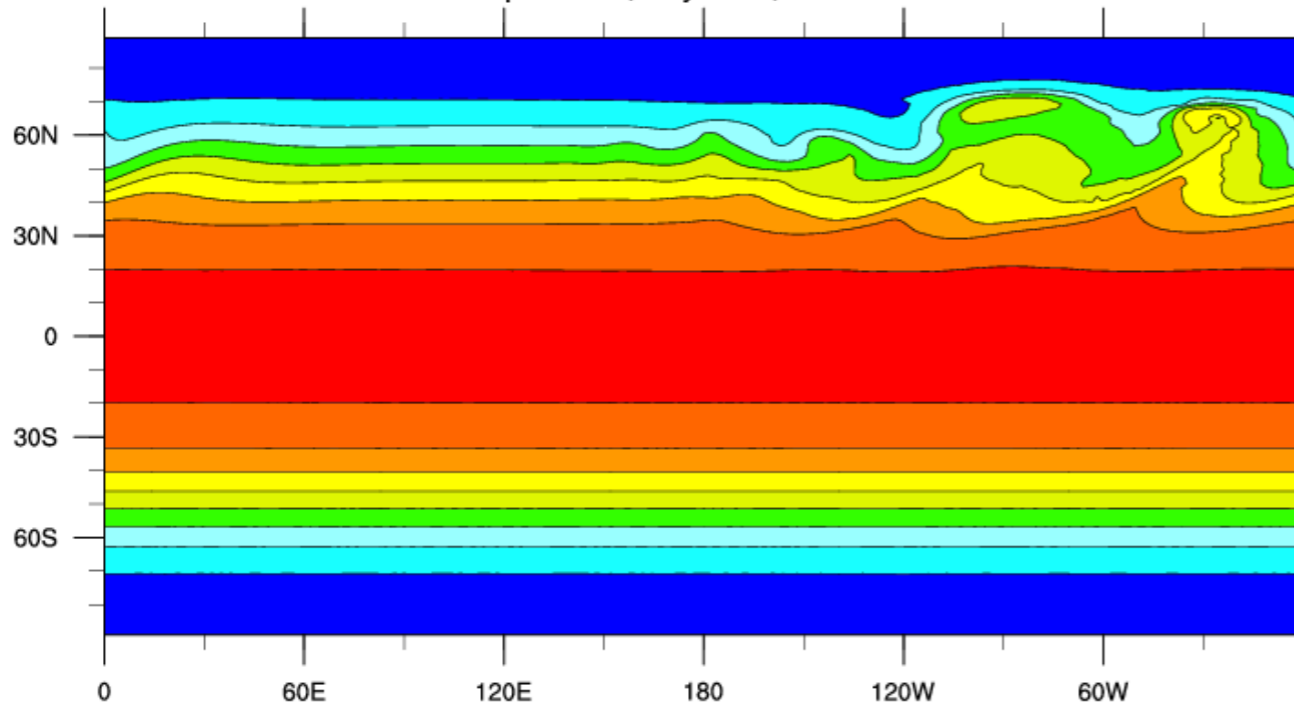
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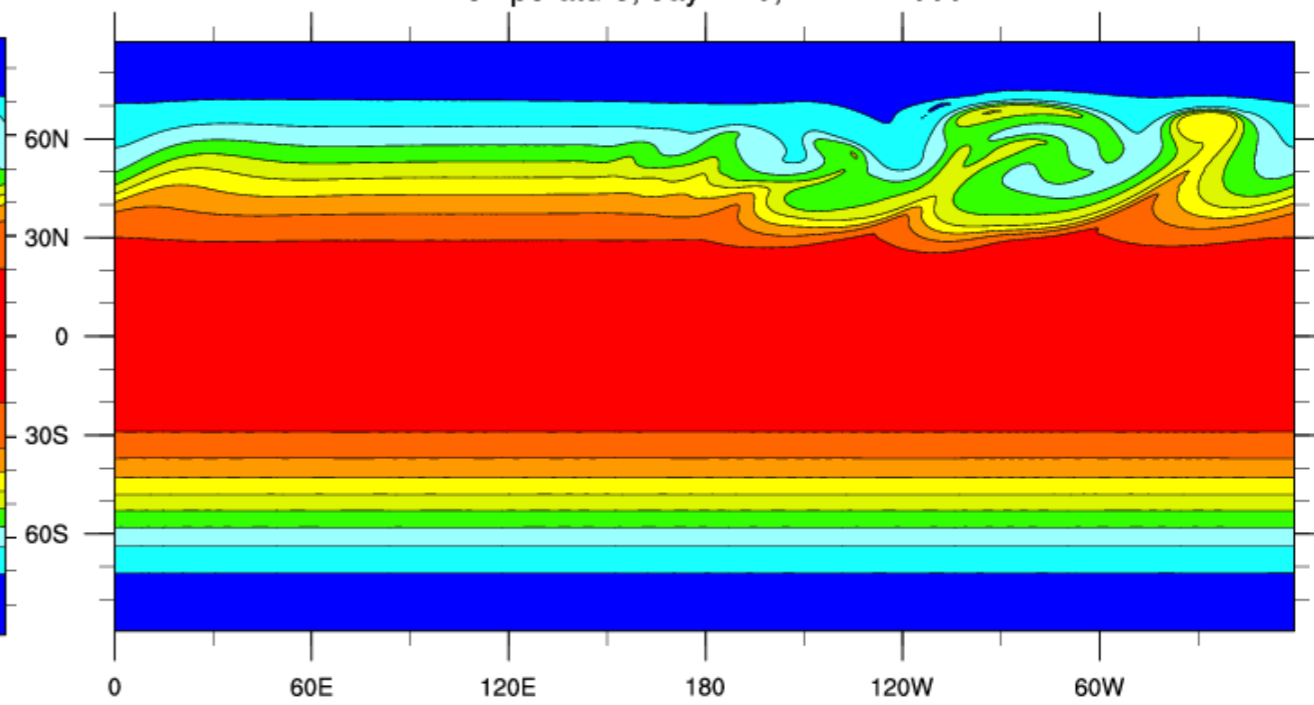
# DCMIP 4-1

- Vertical resolution impacts horizontal solution quality
- default method**                      **spectral vertical**

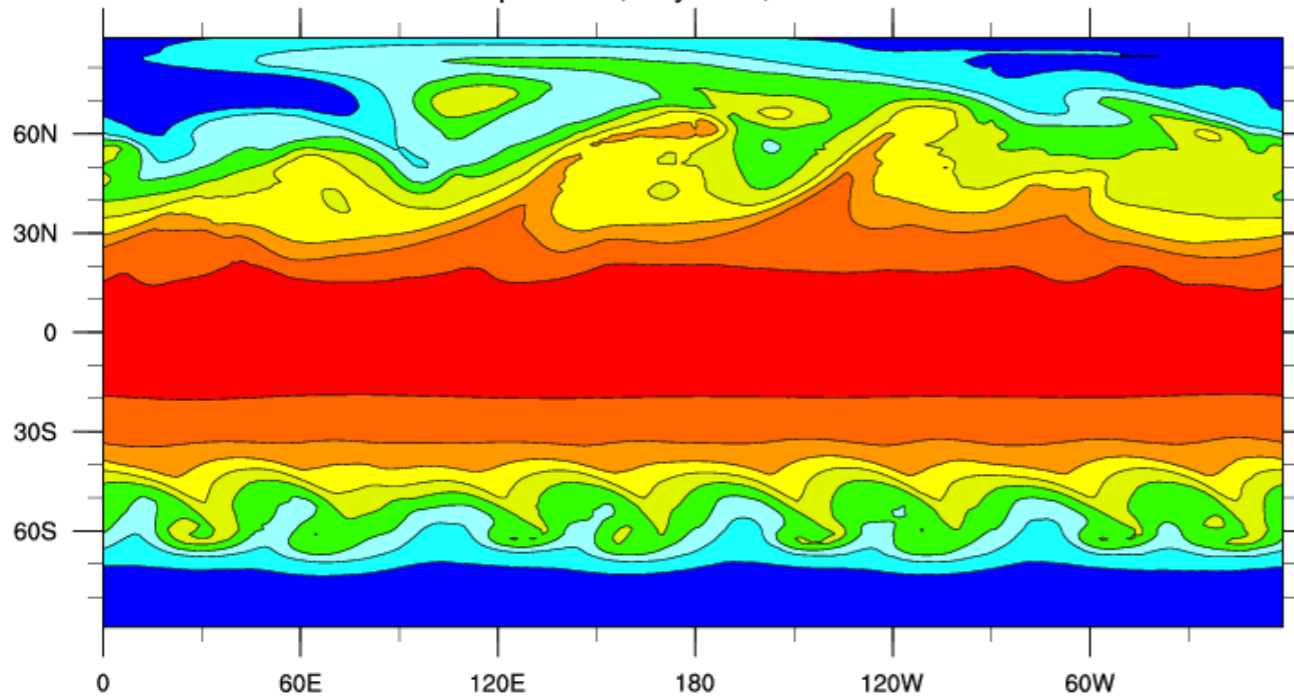
Temperature, day 12.0, PE X=1000



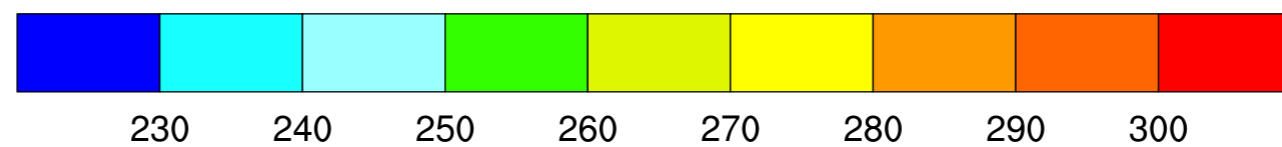
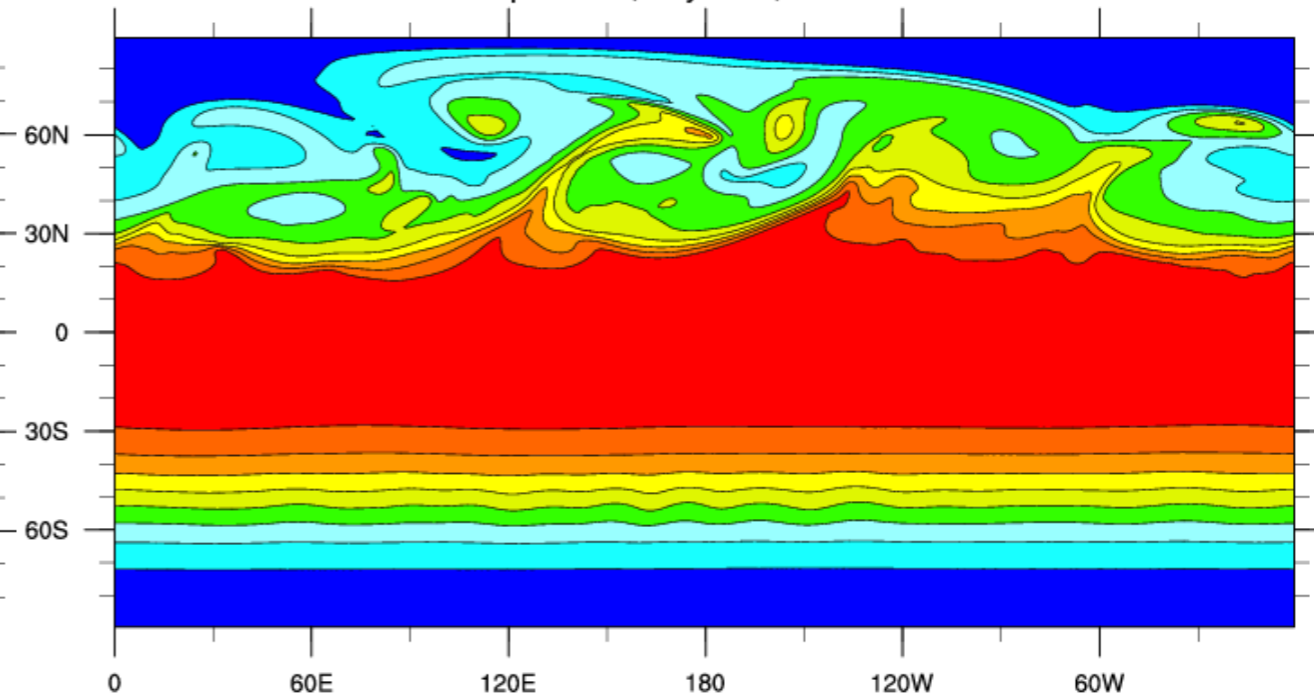
Temperature, day 12.0, PE X=1000



Temperature, day 22.0, PE X=1000



Temperature, day 22.0, PE X=1000



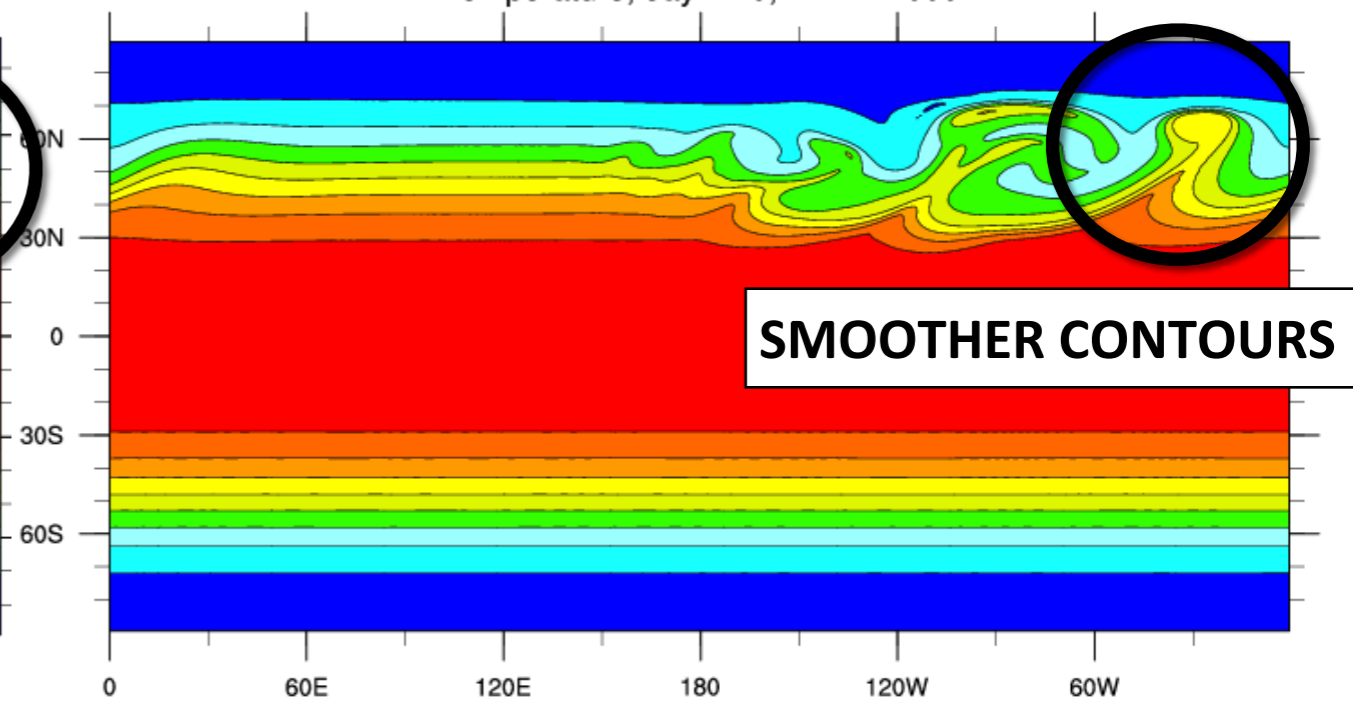
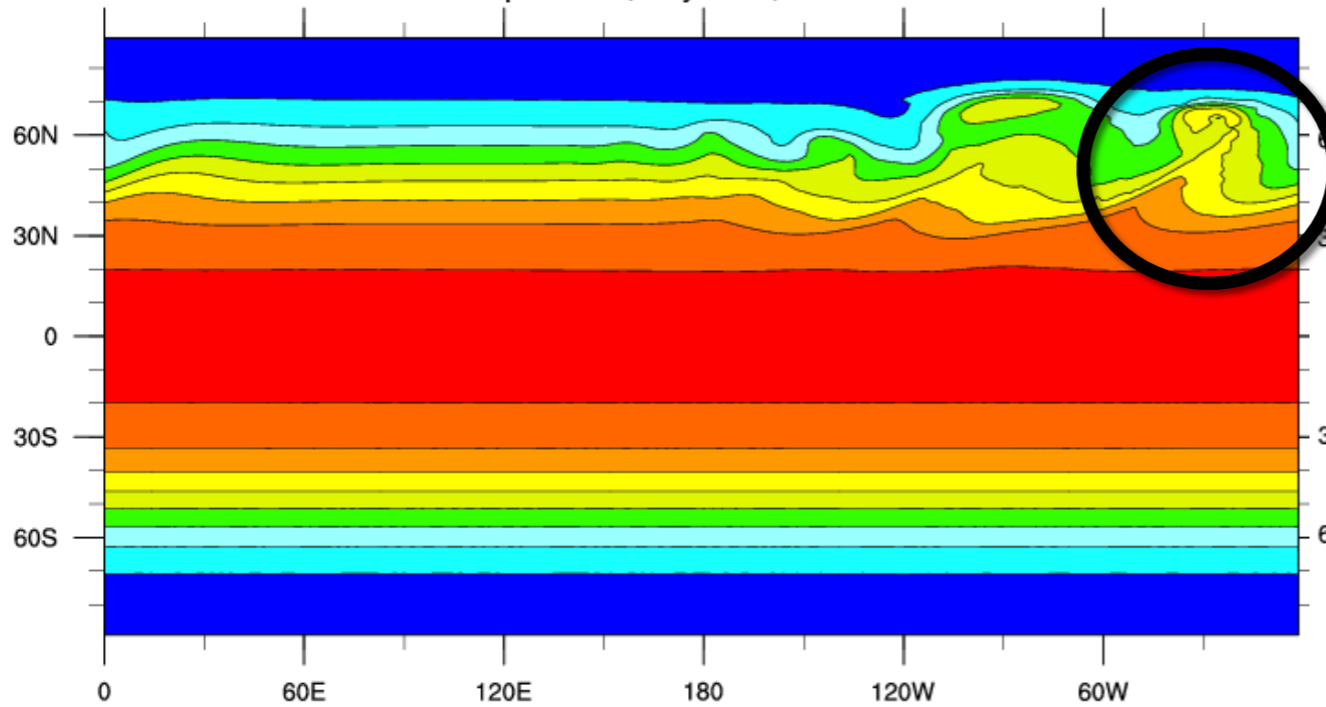
# DCMIP 4-1

## default method

## spectral vertical

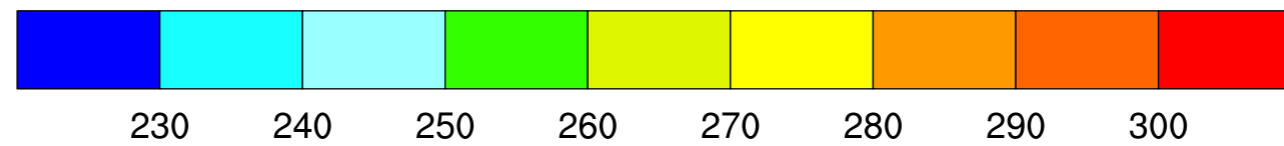
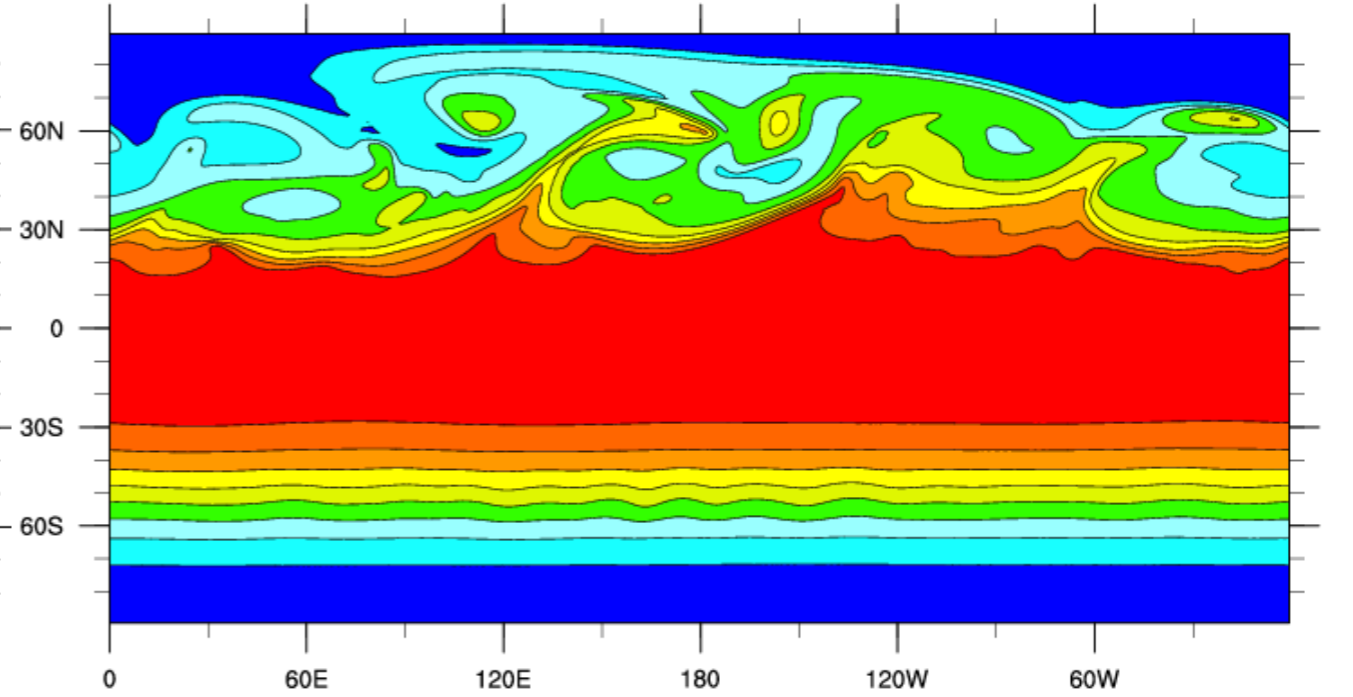
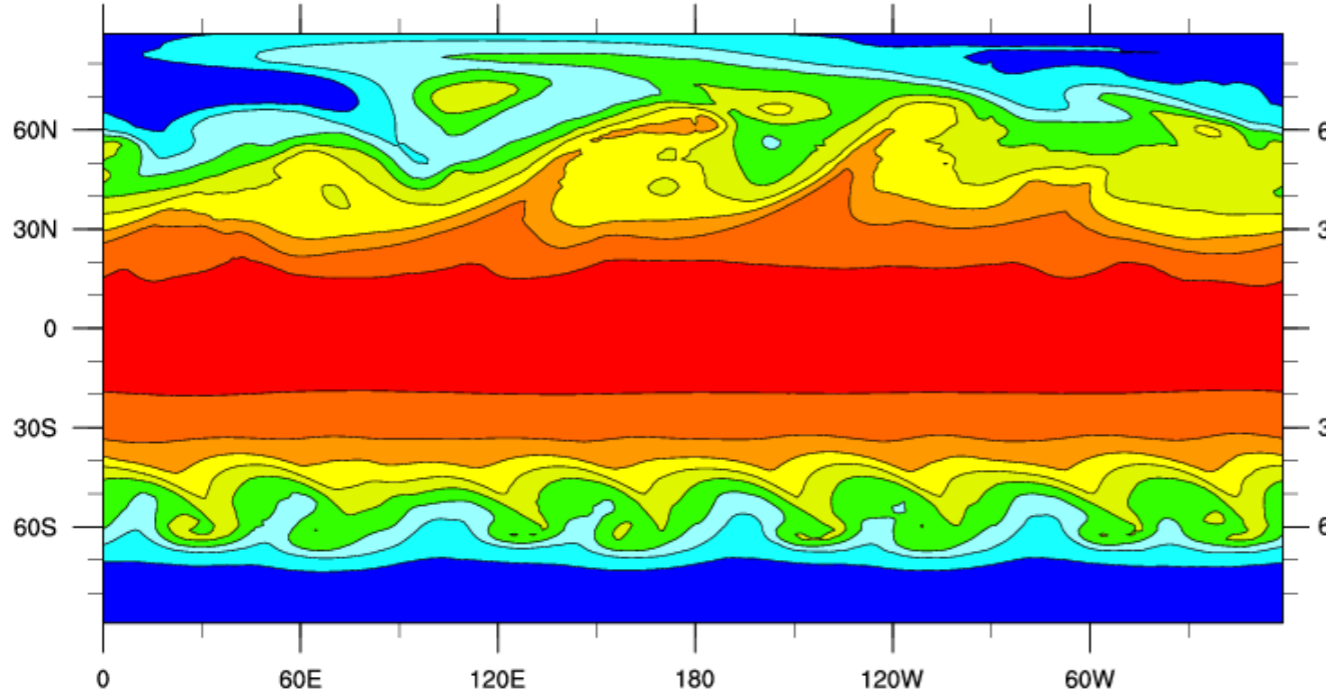
Temperature, day 12.0, PE X=1000

Temperature, day 12.0, PE X=1000



Temperature, day 22.0, PE X=1000

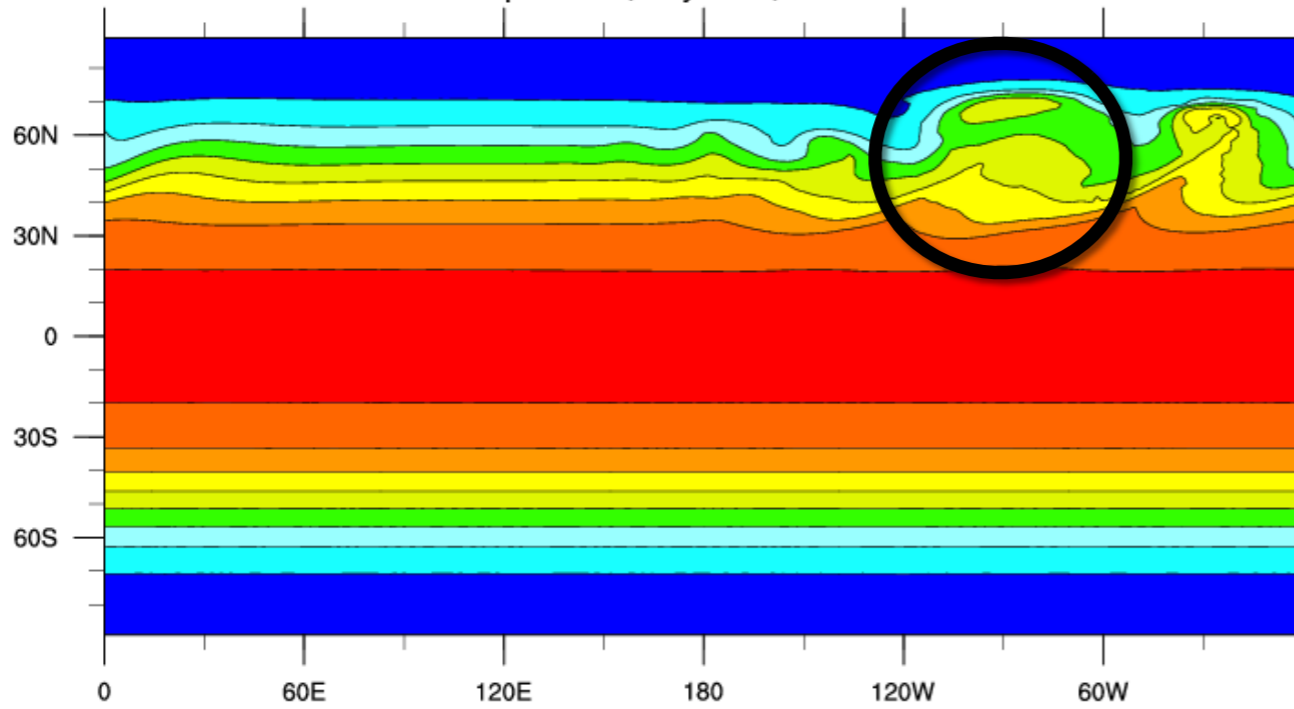
Temperature, day 22.0, PE X=1000



# DCMIP 4-1

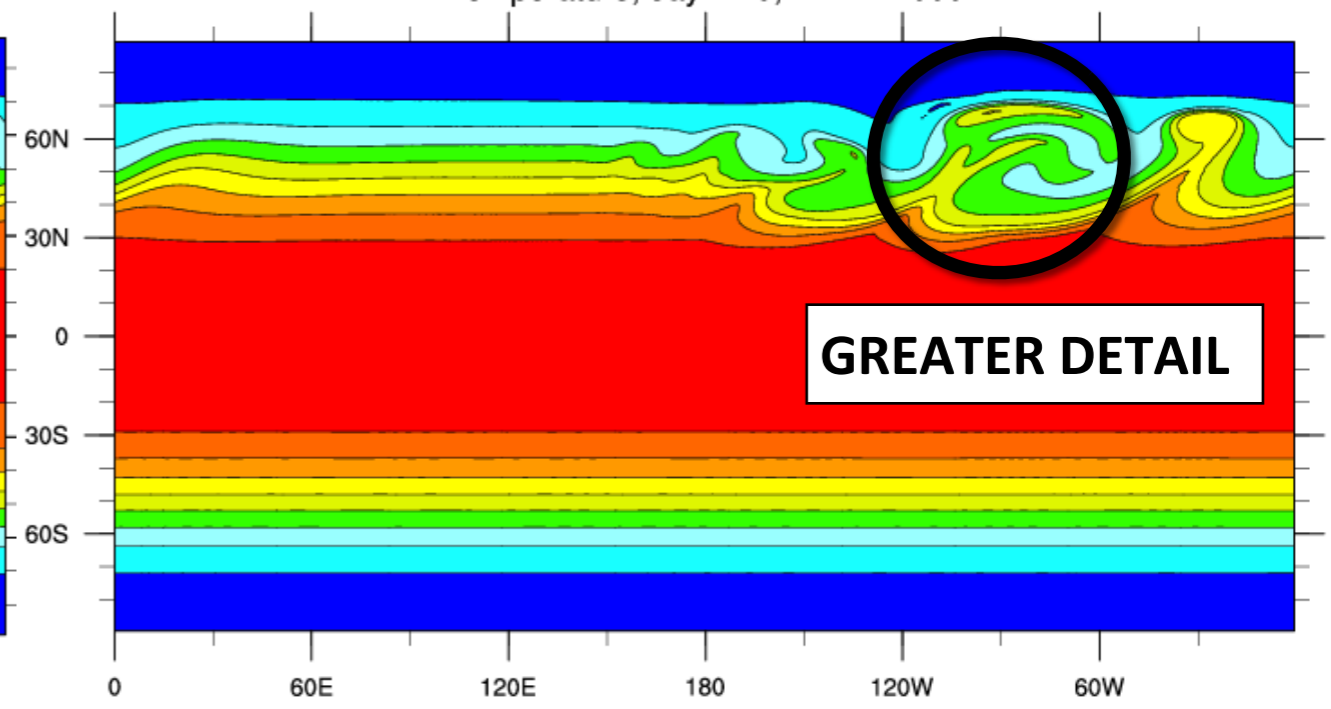
## default method

Temperature, day 12.0, PE X=1000

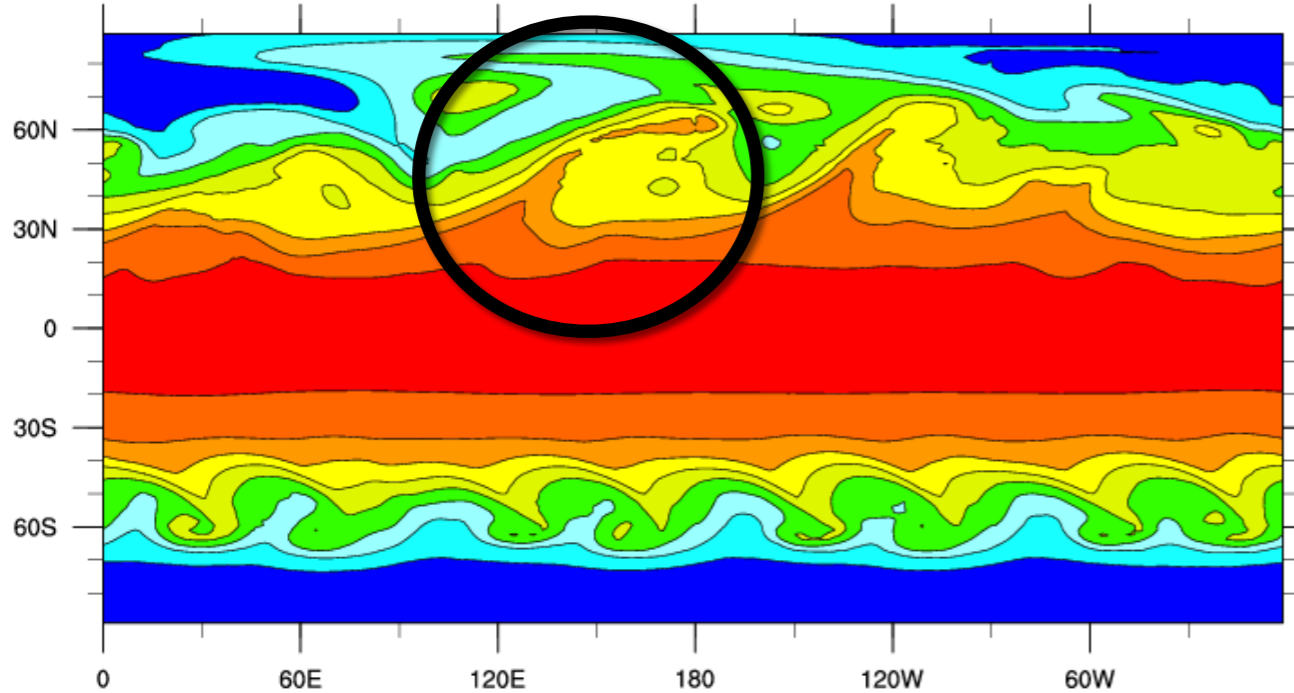


## spectral vertical

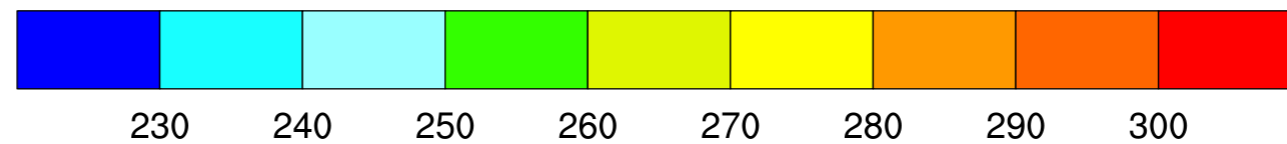
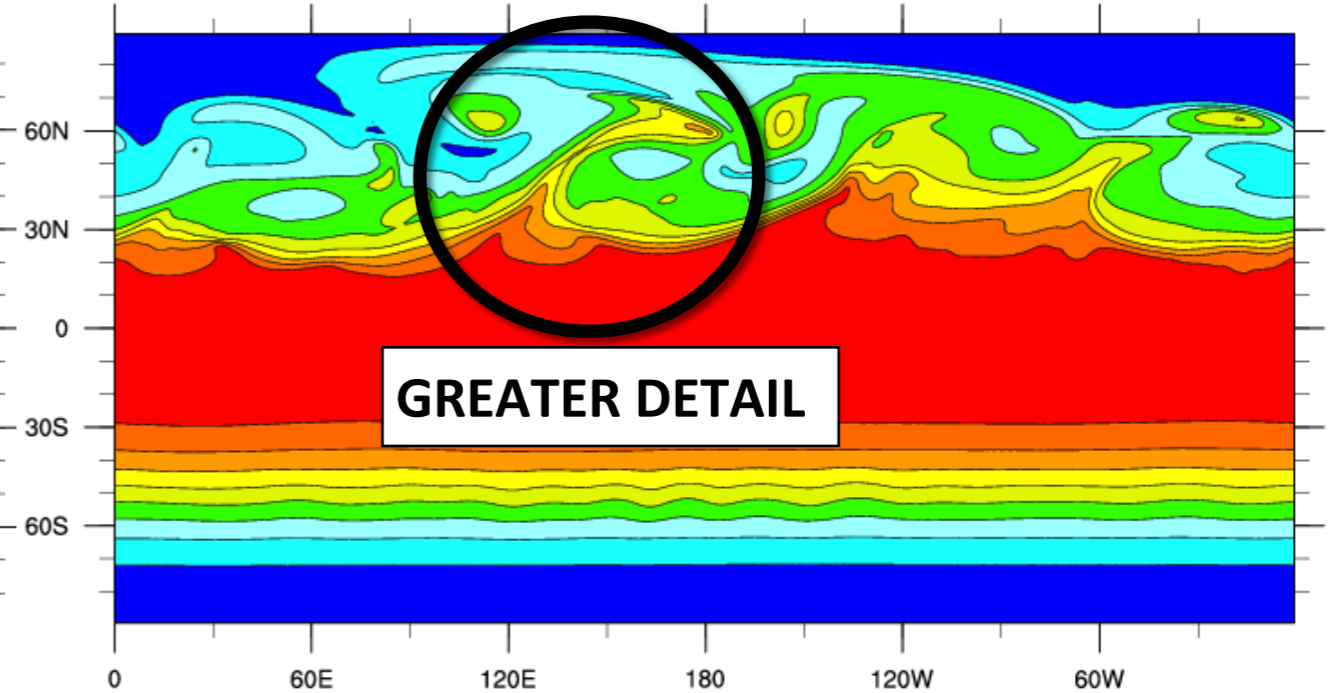
Temperature, day 12.0, PE X=1000



Temperature, day 22.0, PE X=1000



Temperature, day 22.0, PE X=1000



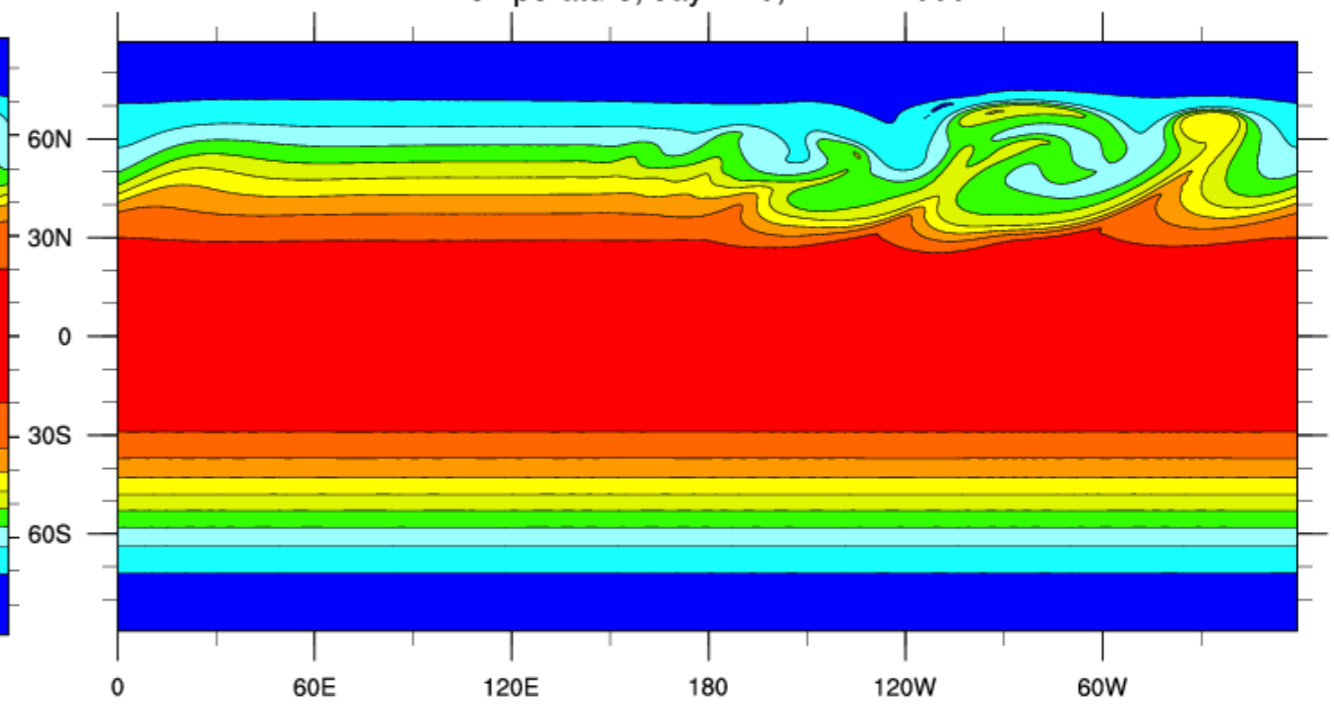
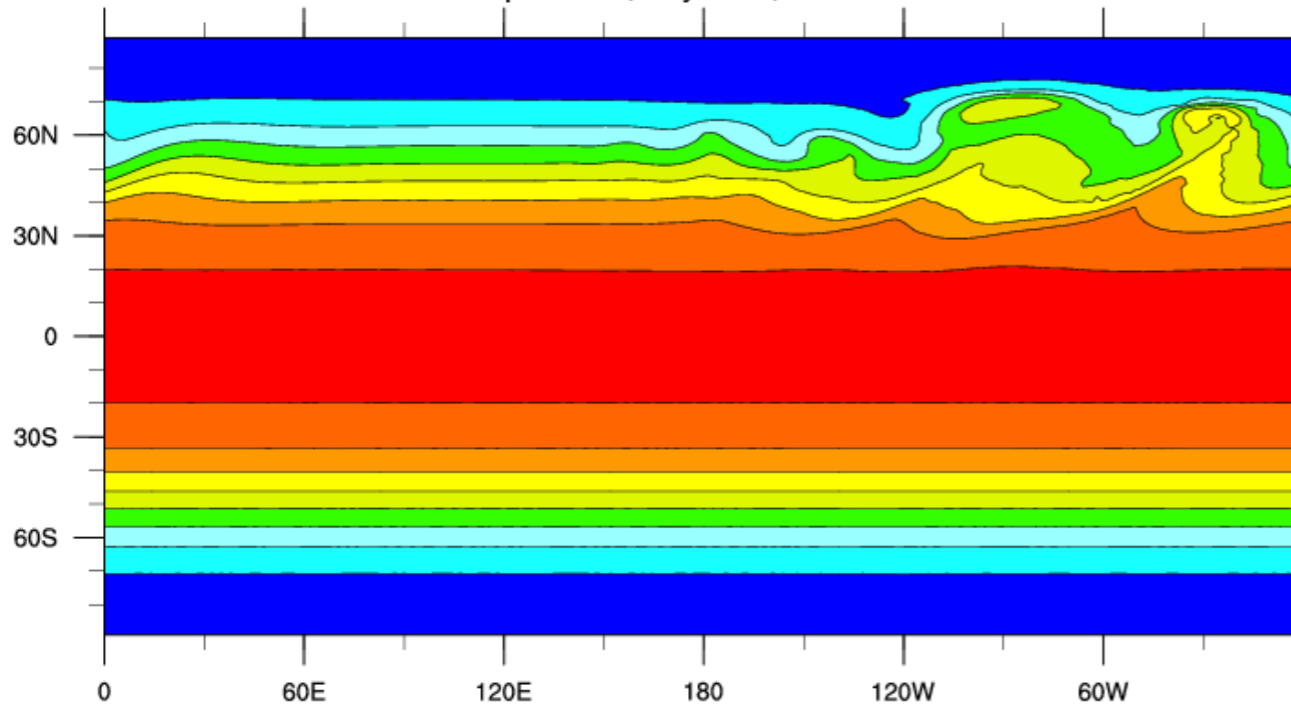
# DCMIP 4-1

## default method

## spectral vertical

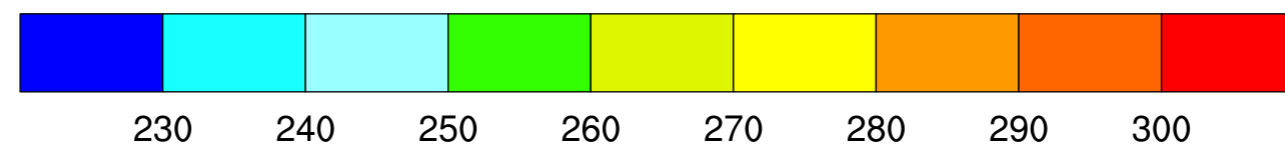
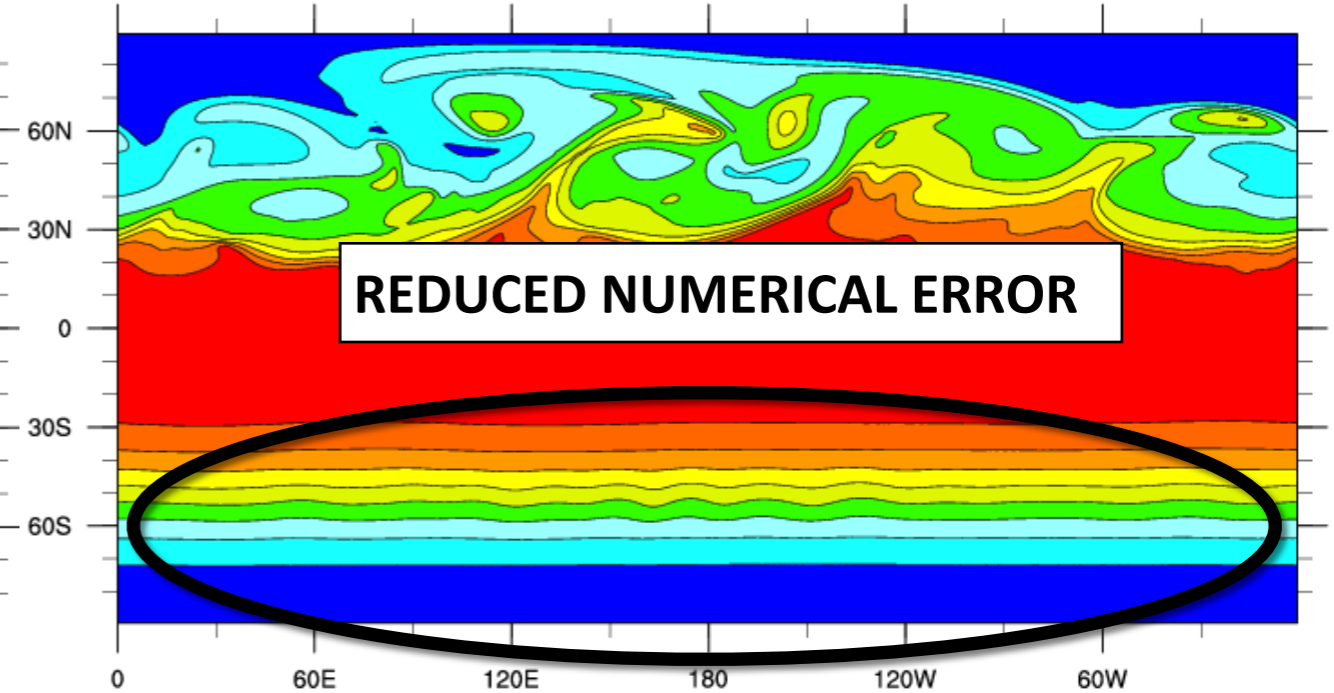
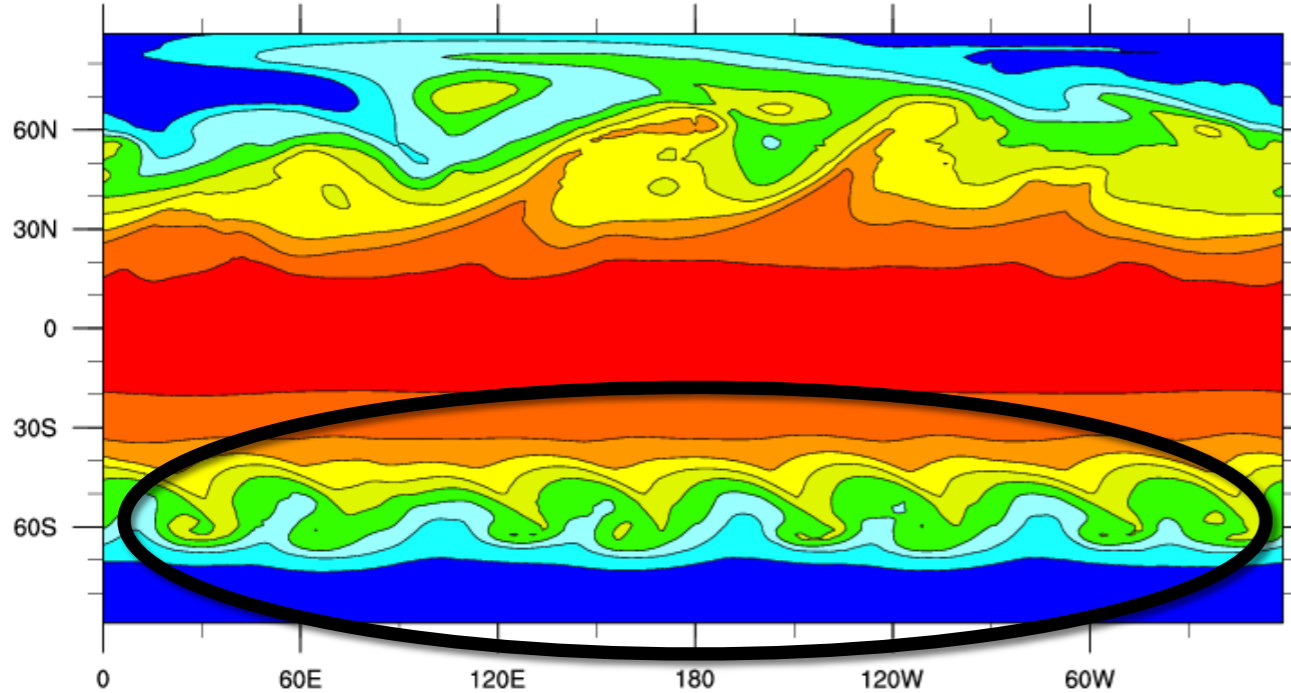
Temperature, day 12.0, PE X=1000

Temperature, day 12.0, PE X=1000

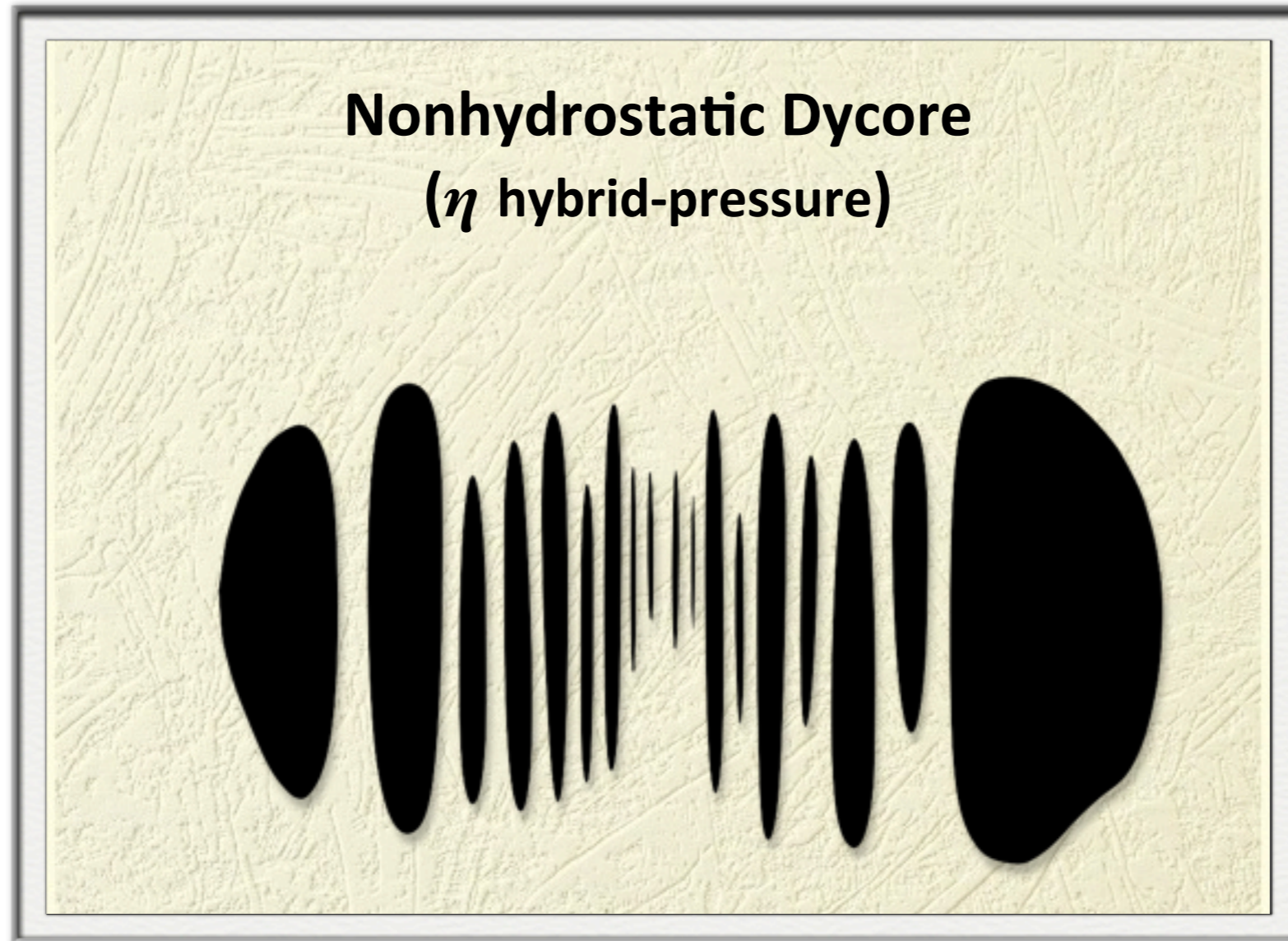


Temperature, day 22.0, PE X=1000

Temperature, day 22.0, PE X=1000



# NONHYDROSTATIC MODEL IN PRESSURE COORDS

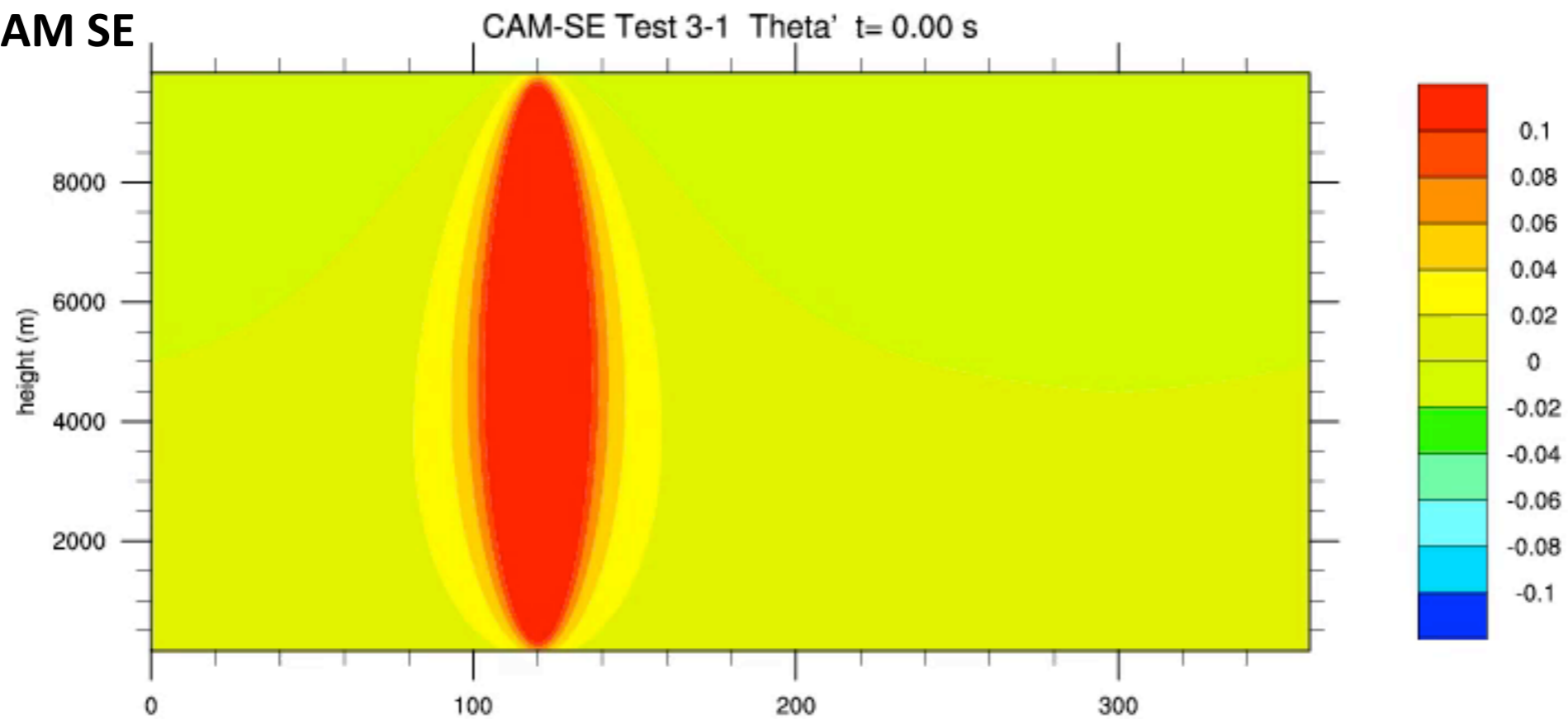


- Critical for horizontal resolutions finer than 10 km/cell
- Employs same spectral-vertical representation
- Works very well for orography-free simulations
- Orographic boundary conditions require further testing

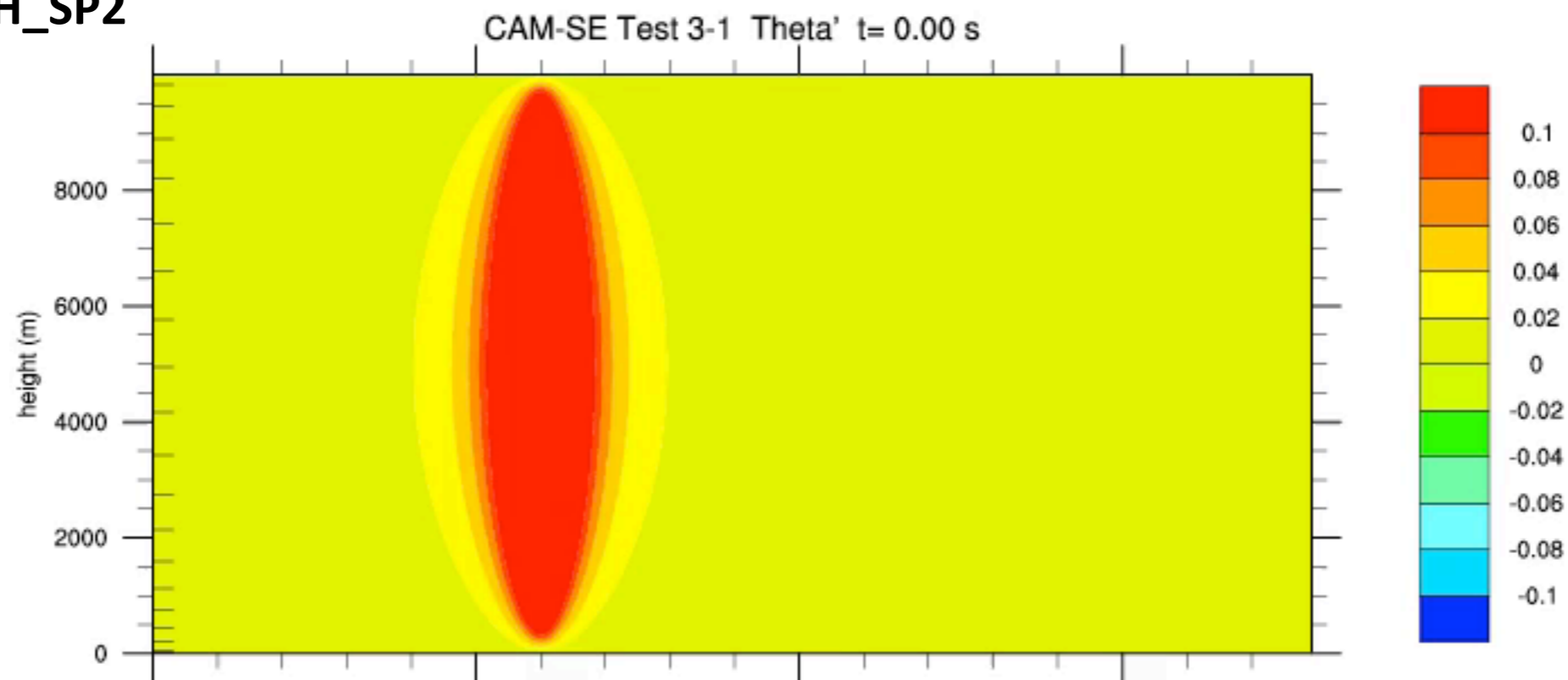


# DCMIP 3-1: PRIMITIVE VS NONHYDROSTATIC MODELS

**CAM SE**



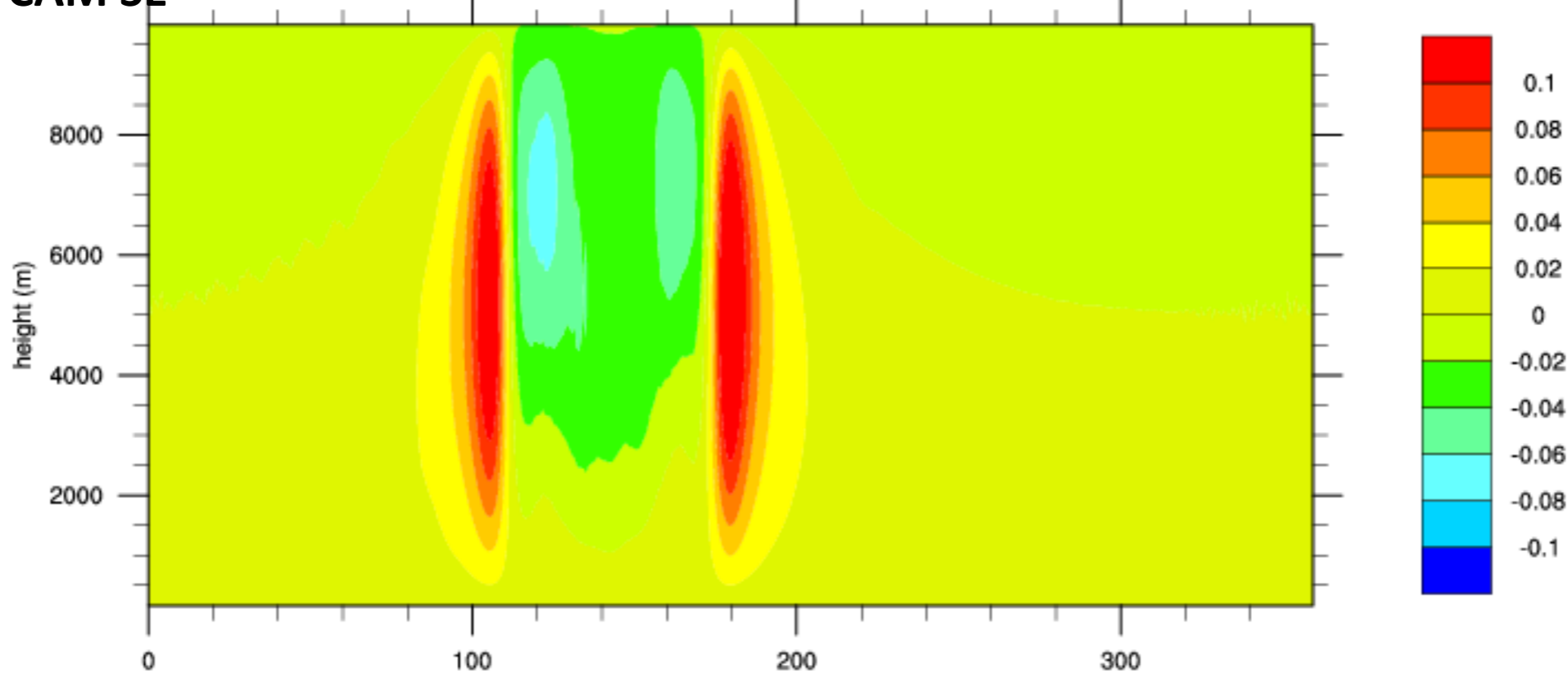
**NH\_SP2**



# DCMIP 3-1: PRIMITIVE VS NONHYDROSTATIC MODELS

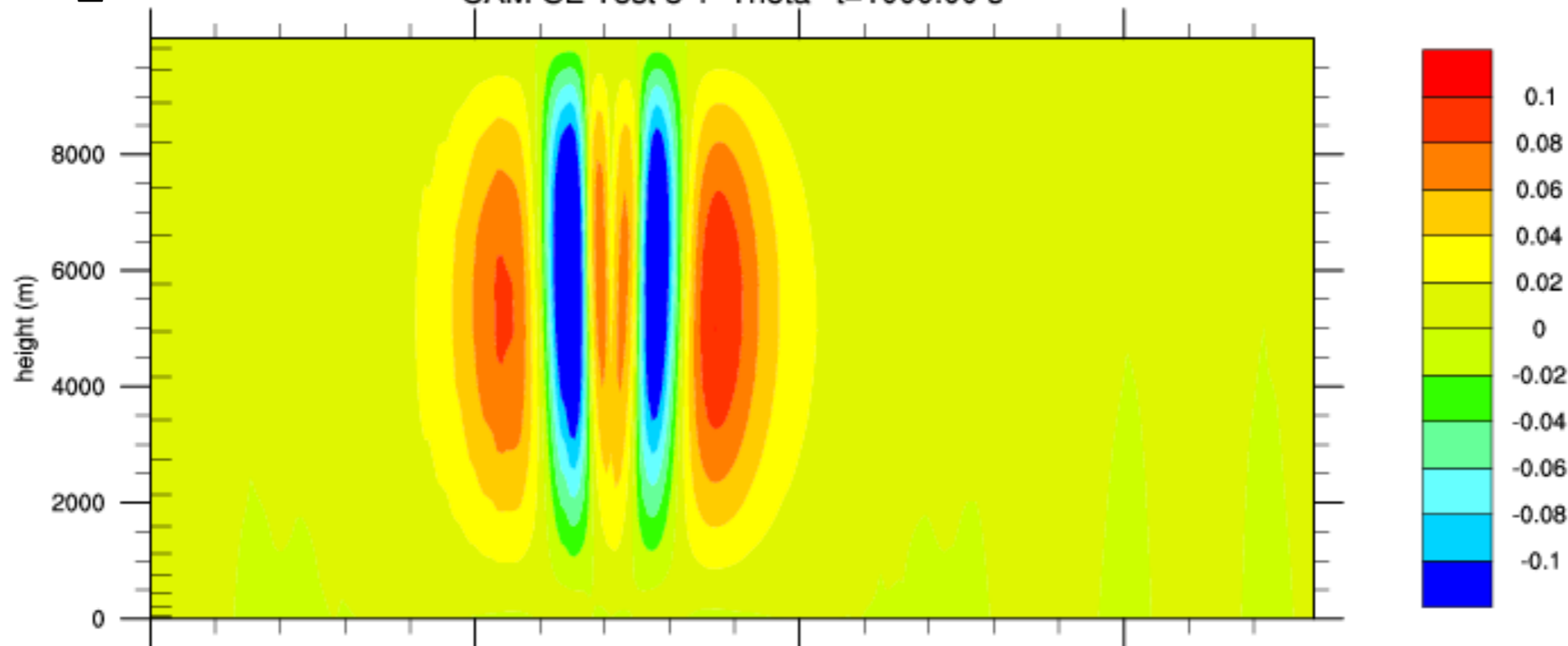
CAM SE

CAM-SE Test 3-1 Theta' t=1000.00 s



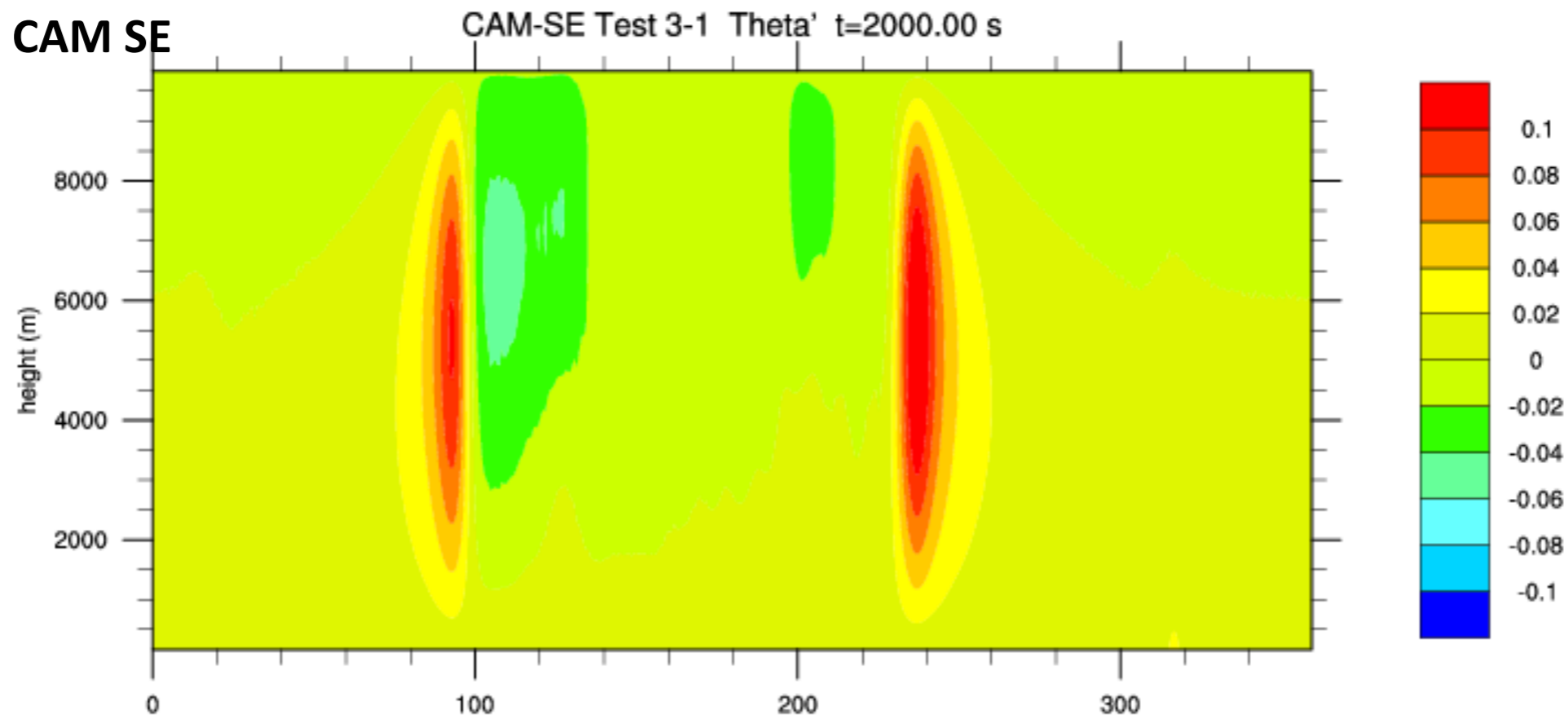
NH\_SP2

CAM-SE Test 3-1 Theta' t=1000.00 s

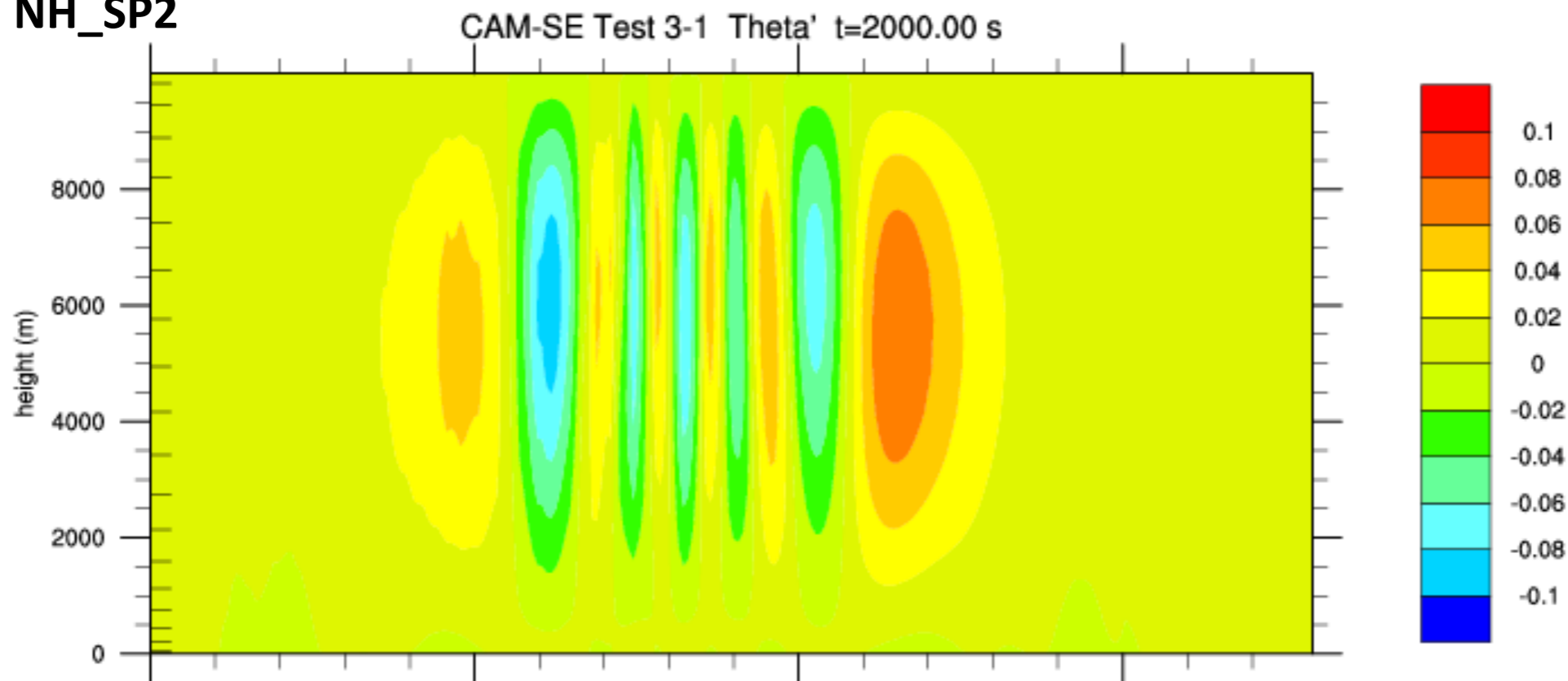


# DCMIP 3-1: PRIMITIVE VS NONHYDROSTATIC MODELS

**CAM SE**

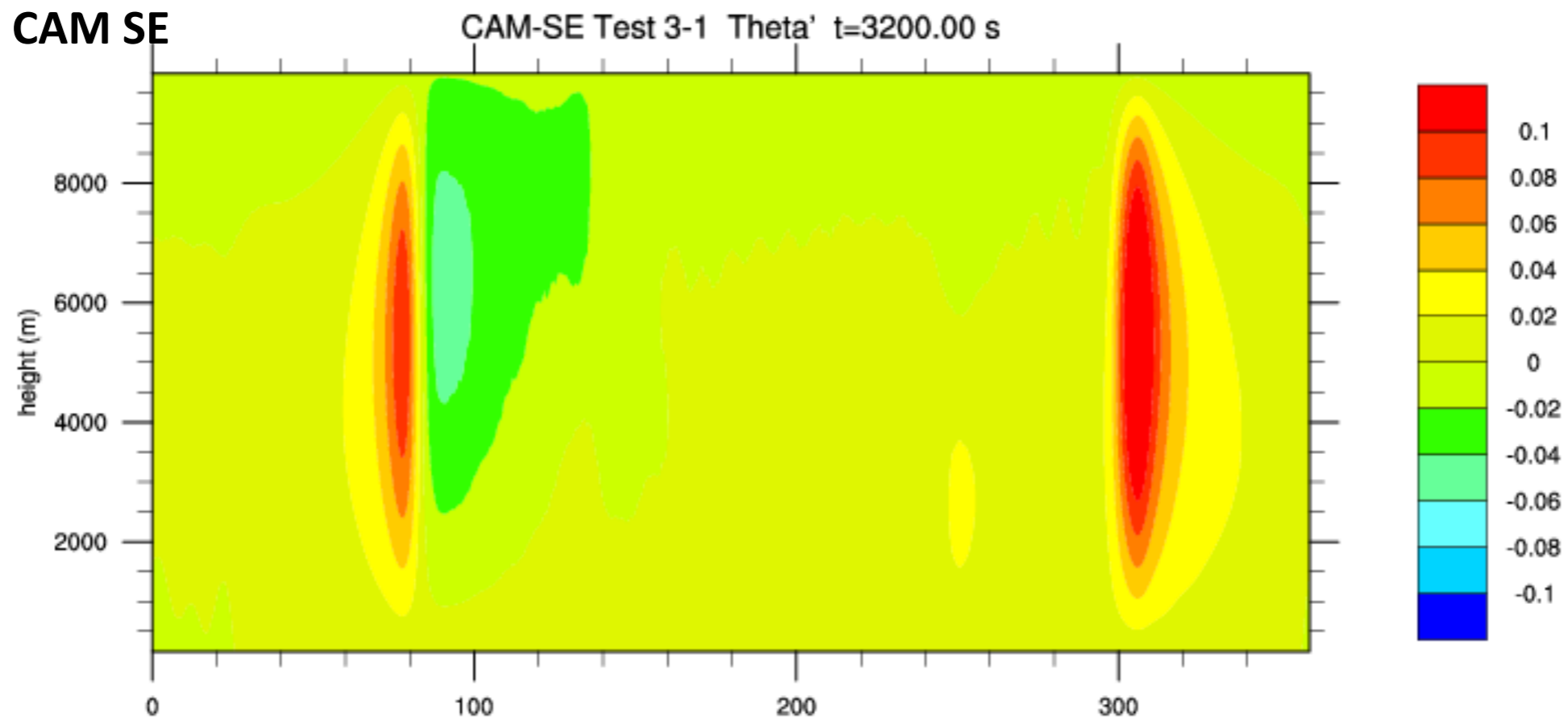


**NH\_SP2**

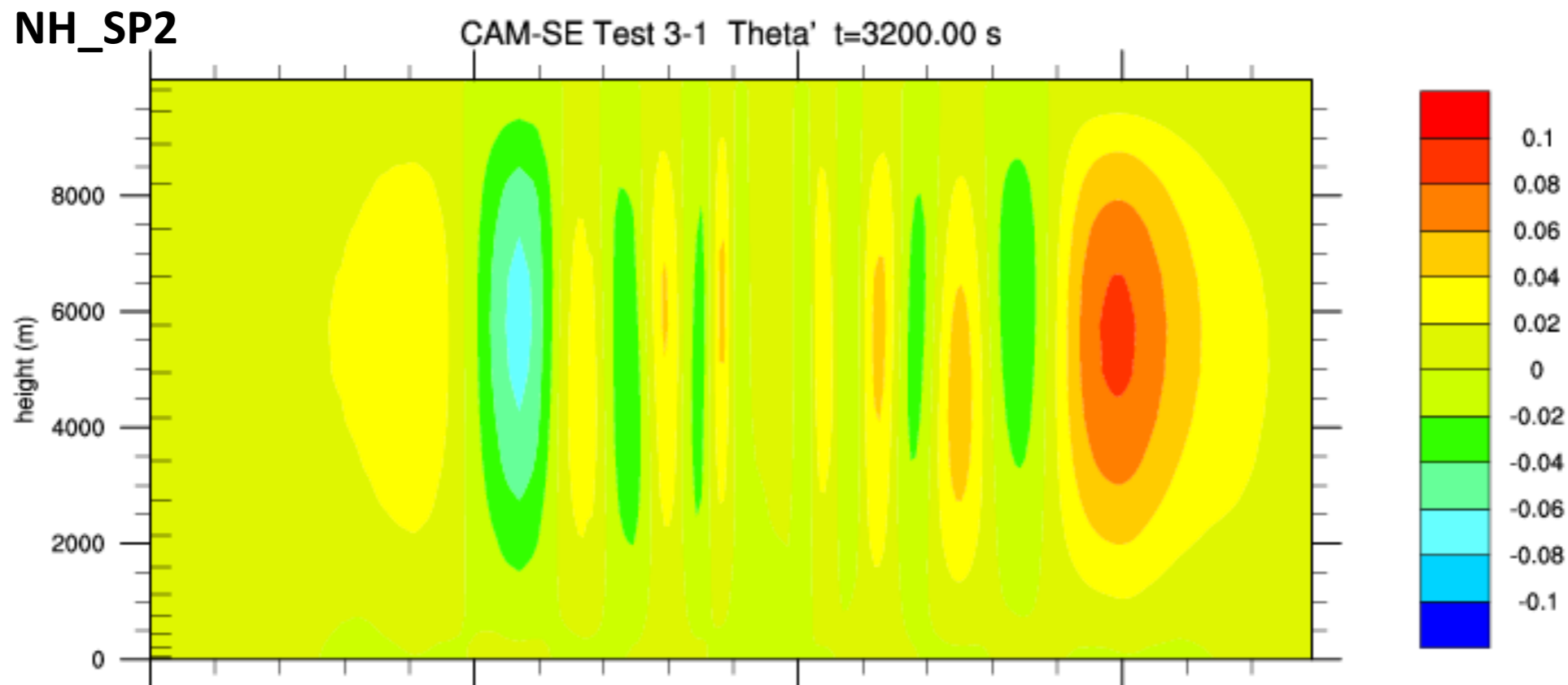


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CAM SE

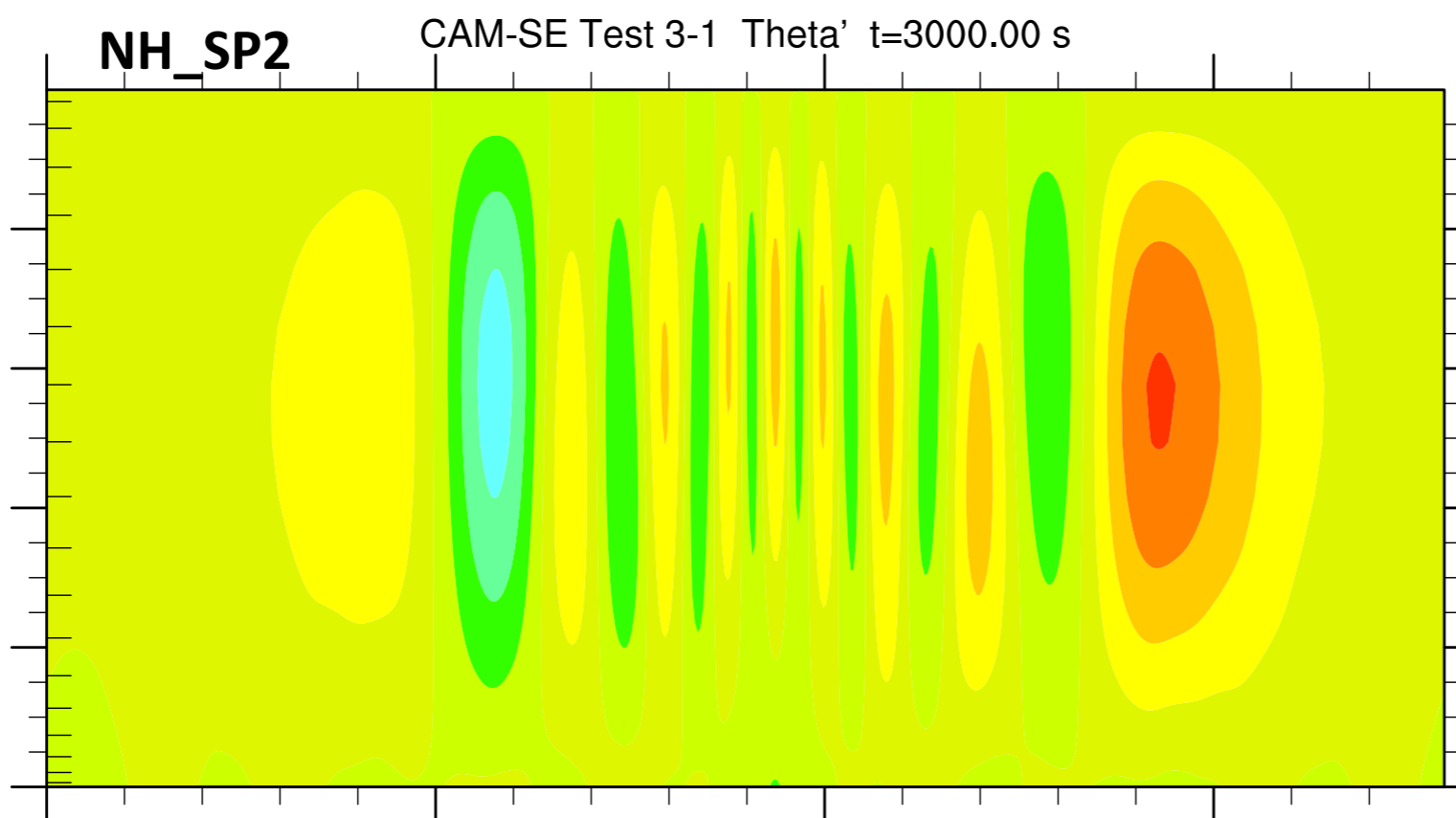
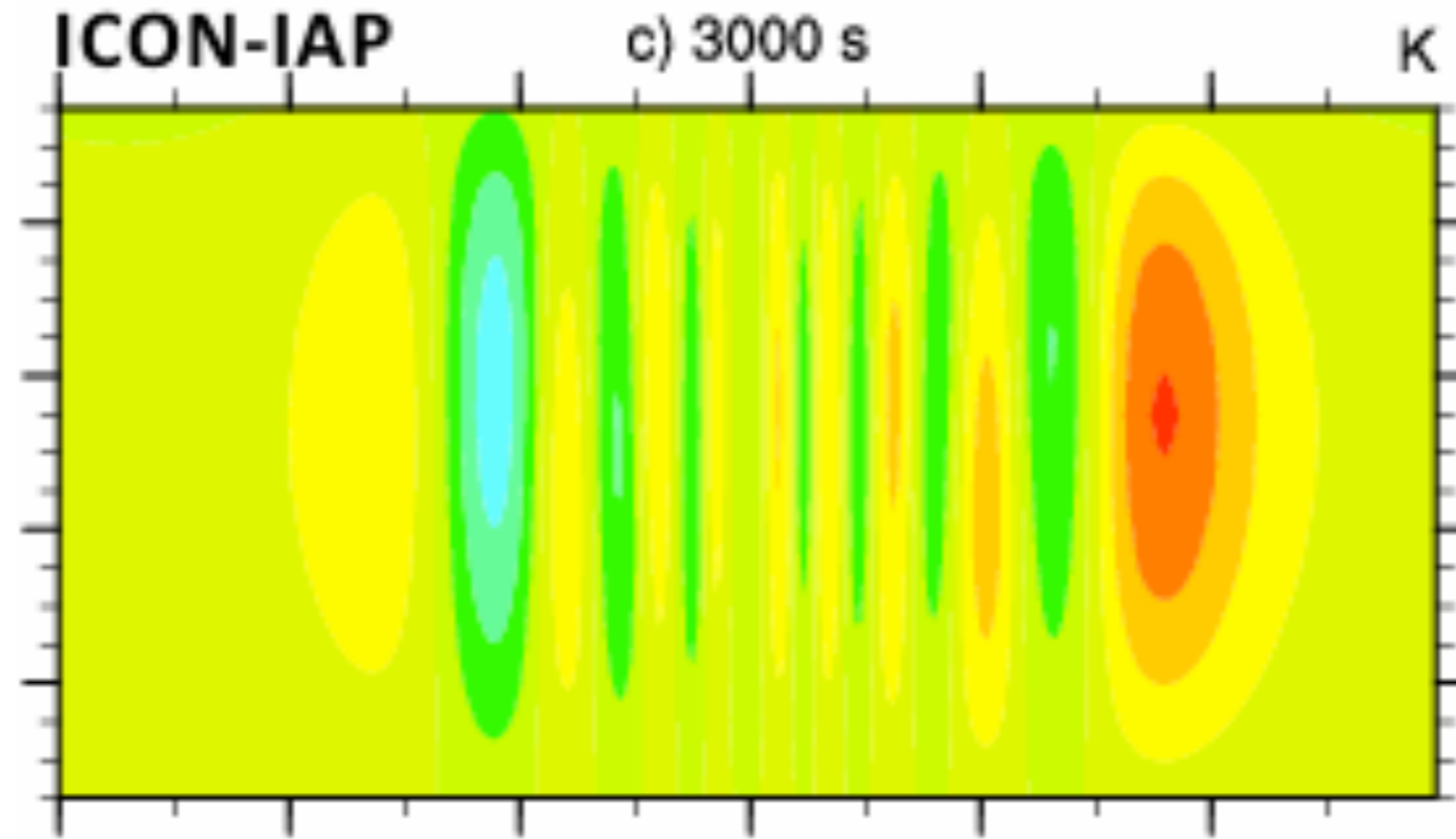


NH\_SP2



- Nonhydrostatic model results differ significantly from primitive equation results

# DCMIP 3-1: COMPARISON WITH ICON NH MODEL



- Matches other nonhydrostatic models (it's working correctly)

# IMPORTANT WORK REMAINS TO BE DONE:

- **Deliver** capabilities to **CAM trunk**
- Complete nonhydrostatic **orographic boundary condition** testing
- **Evaluate** both on Aqua-planet, AMIP



# PROBLEM: FUNDING

- Funding for this project has run out.
- Ideally, I am seeking additional funding to finish / deliver new capabilities
- Alternatively: Anyone need a skilled climate-model developer?

State of this project

multi-model framework

DCMIP Tests

vertical spectral representation

spectral tracer transport

nonhydrostatic, flat geopotential

L A T O U R E I F F E L

*L'avancement des travaux 1888 - 1889*

# SUMMARY

- **NEW SPECTRAL-VERTICAL REPRESENTATION**
- **SIGNIFICANTLY IMPROVES ACCURACY** IN CAM-SE **WITHOUT INCREASING THE COMPUTATIONAL COST**
- **OBSERVED IMPROVEMENTS:**
  - DCMIP 1-2: **REDUCED OVERSHOOTING, REDUCED GAPPING**
  - DCMIP 1-3: **REDUCED NUMERICAL DIFFUSION**
  - DCMIP 4-1: **GREATER DETAIL, SMOOTHER CONTOURS, REDUCED NUMERICAL ERROR**
- **A PLAUSIBLE ALTERNATIVE TO DOUBLING VERTICAL RESOLUTION**

