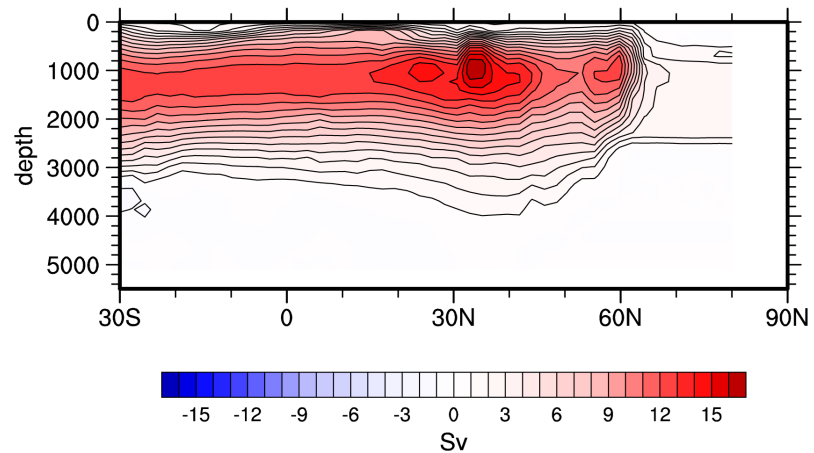


# Optimal **Atmospheric** Excitation of AMOC on Decadal Time Scales in CCSM4

Grant Branstator, NCAR  
Andrey Gritsun, RAS



**CCSM4 mean AMOC**  
*T31, 3deg 8000 year control*

# (Simplified, Quasi-gaussian) Fluctuation Dissipation Theorem (Leith, 1975; Deker&Haake, 1975; Risken, 1984)

Suppose have a discretized dynamical system with noise and a F-P eqn with unique solutions. Also assume gradients of the system PDF are well approximated by a Gaussian fit. Then the PDF-averaged response to weak forcing  $f$  is

$$r(t) = \int_{t_0}^t C(t - \tau) C^{-1}(0) f(\tau) d\tau$$

for  $C(\tau) = \text{lag-}\tau$  cov matrix

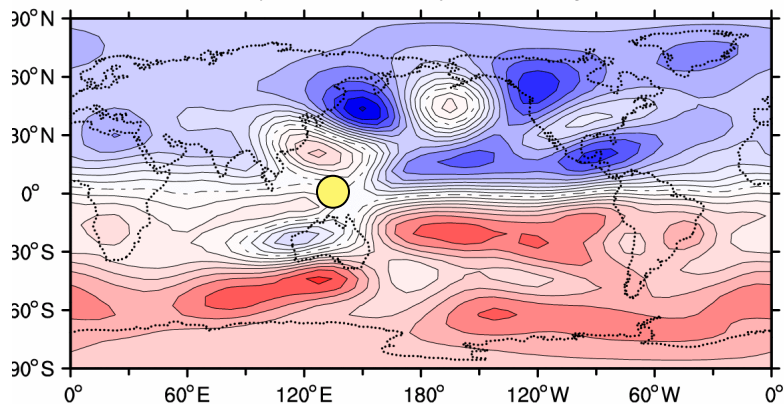
Sufficient data to find  $C$

Atmospheric applications:

- \* Gritsun, Branstator (2007)
- \* Gritsun, Branstator, Majda (2008)
- \* Liu et al. (2012)

# CCM0

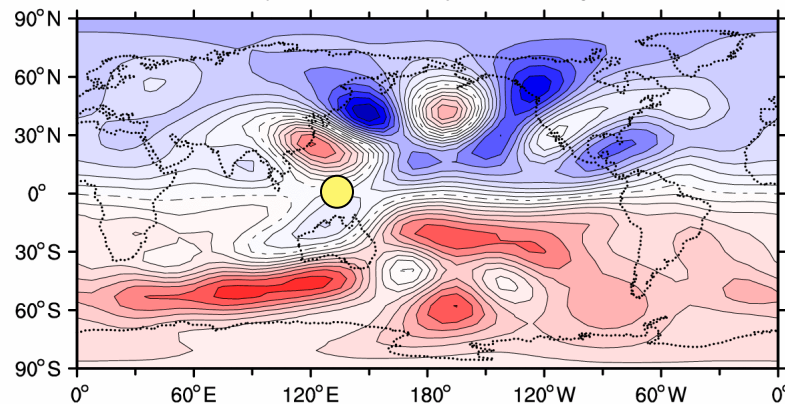
CCM0 strong forcing  
psi336  
(135.00, 0.00) 2.5C/day



CONTOUR FROM -500 TO 400 BY 50 ( $\times 10^4$ )  
FD vs CCM0 multifield cor= 0.81

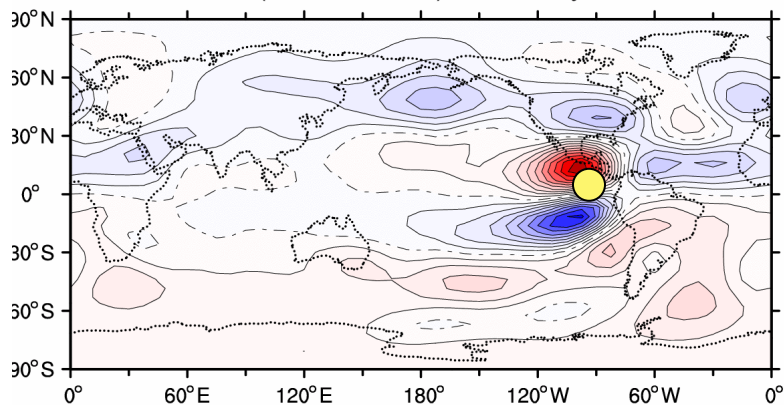
# FDT

FD  
psi336  
(135.00, 0.00) 2.5C/day



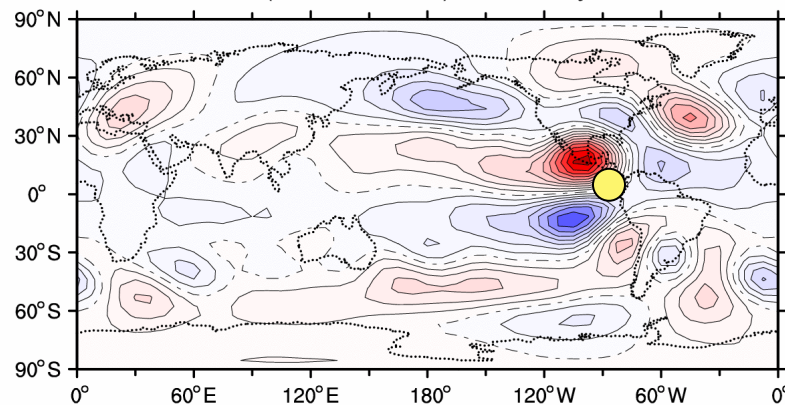
CONTOUR FROM -500 TO 400 BY 50 ( $\times 10^4$ )  
FD vs CCM0 multifield cor= 0.81

CCM0 strong forcing  
psi336  
(-90.00, 0.00) 2.5C/day



CONTOUR FROM -450 TO 500 BY 50 ( $\times 10^4$ )  
FD vs CCM0 multifield cor= 0.77

FD  
psi336  
(-90.00, 0.00) 2.5C/day



CONTOUR FROM -350 TO 500 BY 50 ( $\times 10^4$ )  
FD vs CCM0 multifield cor= 0.77

*Gritsun & Branstator (2007)*

## CCSM4

*T31, 3deg, 26L 8000 year control*

$$\begin{bmatrix} T(t) \\ S(t) \\ u(t) \\ v(t) \end{bmatrix} = r(t) = \mathbf{M}_t \bar{f} = \mathbf{M}_t \begin{bmatrix} \dot{T} \\ \dot{S} \\ \dot{u} \\ \dot{v} \end{bmatrix}$$

*state of multivariate 3D fields  
is represented by 675 EOFs*

## CCSM4

*T31, 3deg, 26L 8000 year control*

$$\begin{bmatrix} T(t) \\ S(t) \\ u(t) \\ v(t) \end{bmatrix} = r(t) = \mathbf{M}_t \bar{f} = \mathbf{M}_t \begin{bmatrix} \dot{T} \\ \dot{S} \\ \dot{u} \\ \dot{v} \end{bmatrix}$$

*t = 5 yrs*

*singular value decomposition*

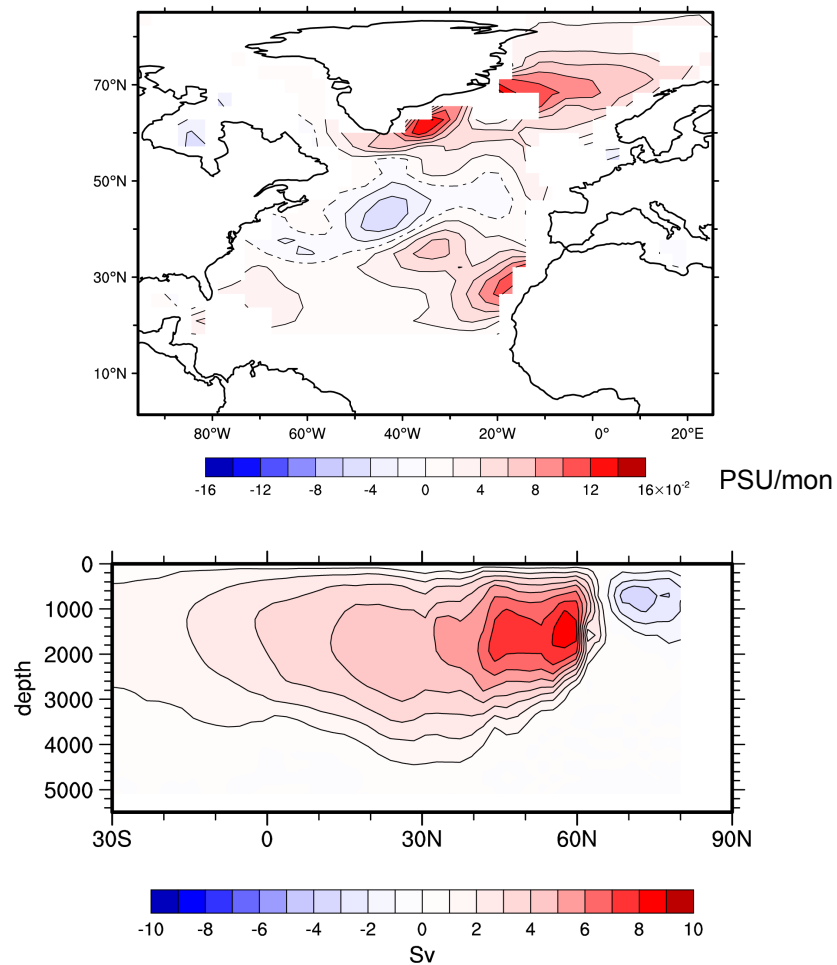
# Optimal N Atlantic Salinity Forcing of AMOC

5 year forcing; year 5 response

force 0-100m

*Singular Value Decomposition*

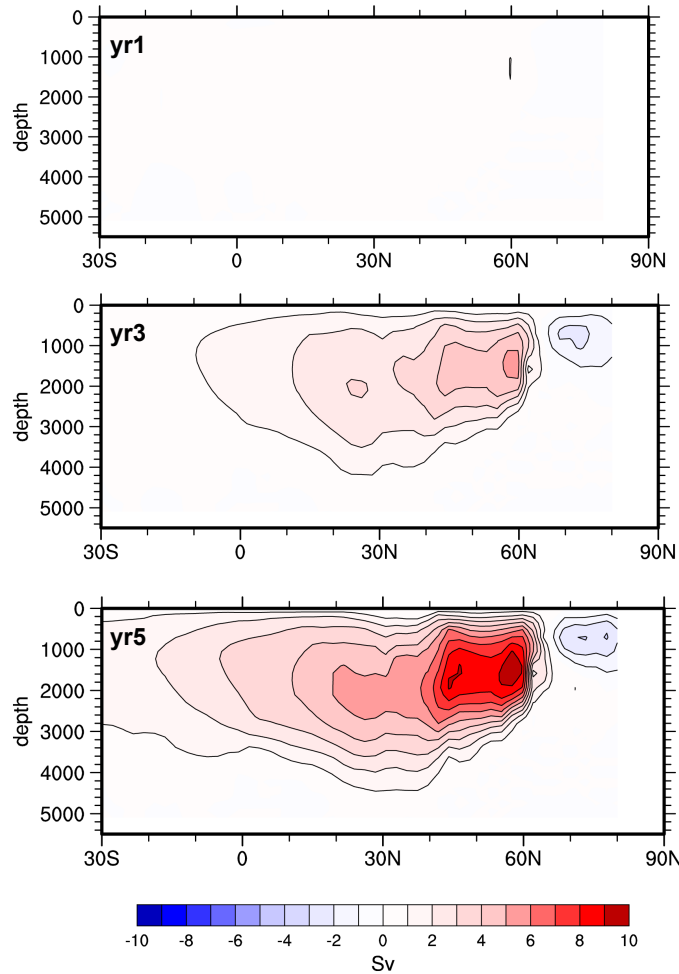
SV1 35x



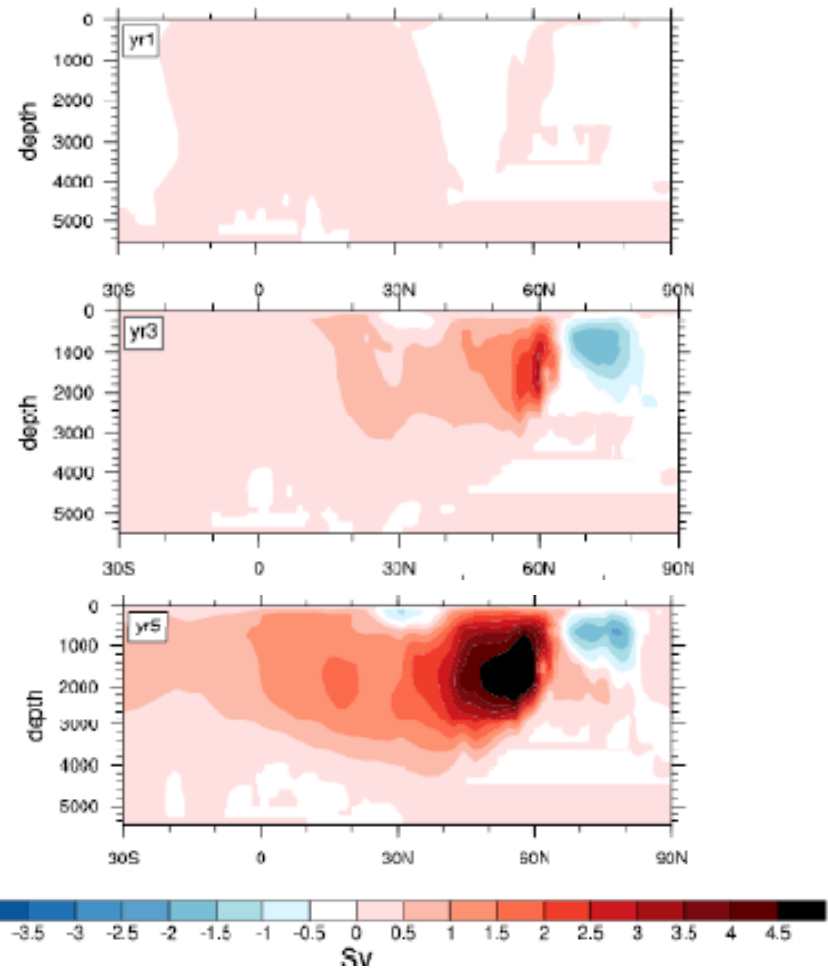
# Optimal & CCSM4 Response of AMOC to Salinity Forcing

force 0-100m

## FDT response SV1



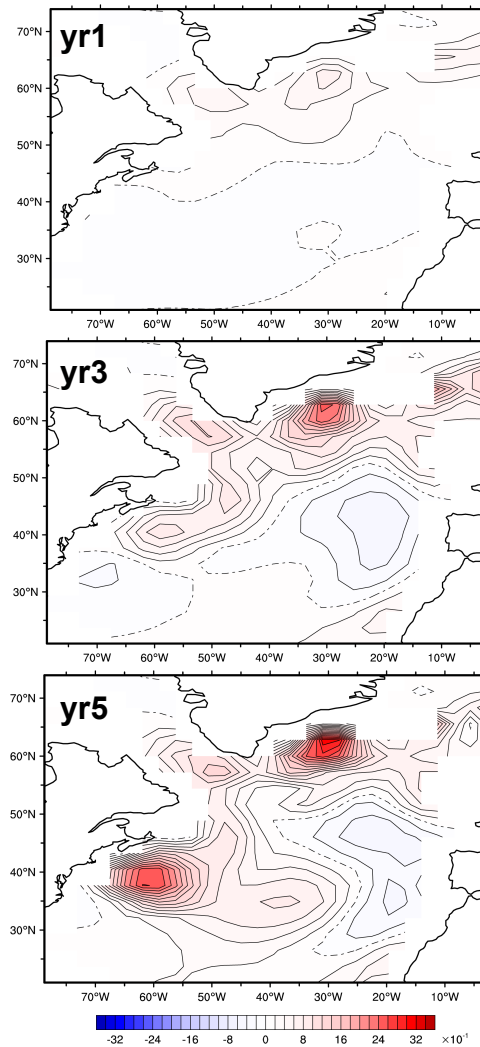
## difference of two 20 member CCSM4 ensembles



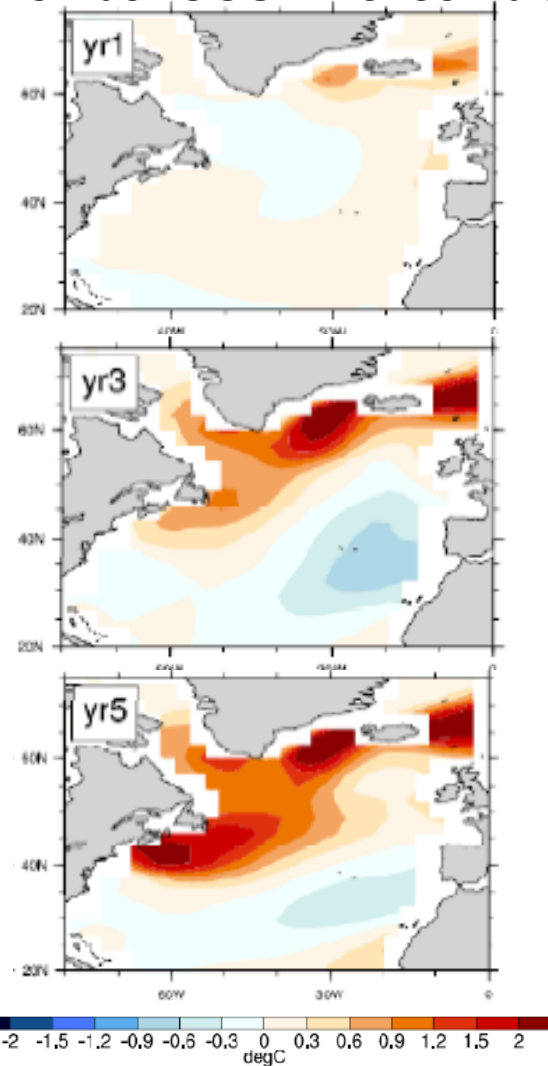
# FDT & CCSM4 SST Response to Optimal Salinity Forcing of AMOC

force 0-100m

FDT response



difference of two  
20 member CCSM4 ensembles





## Remember

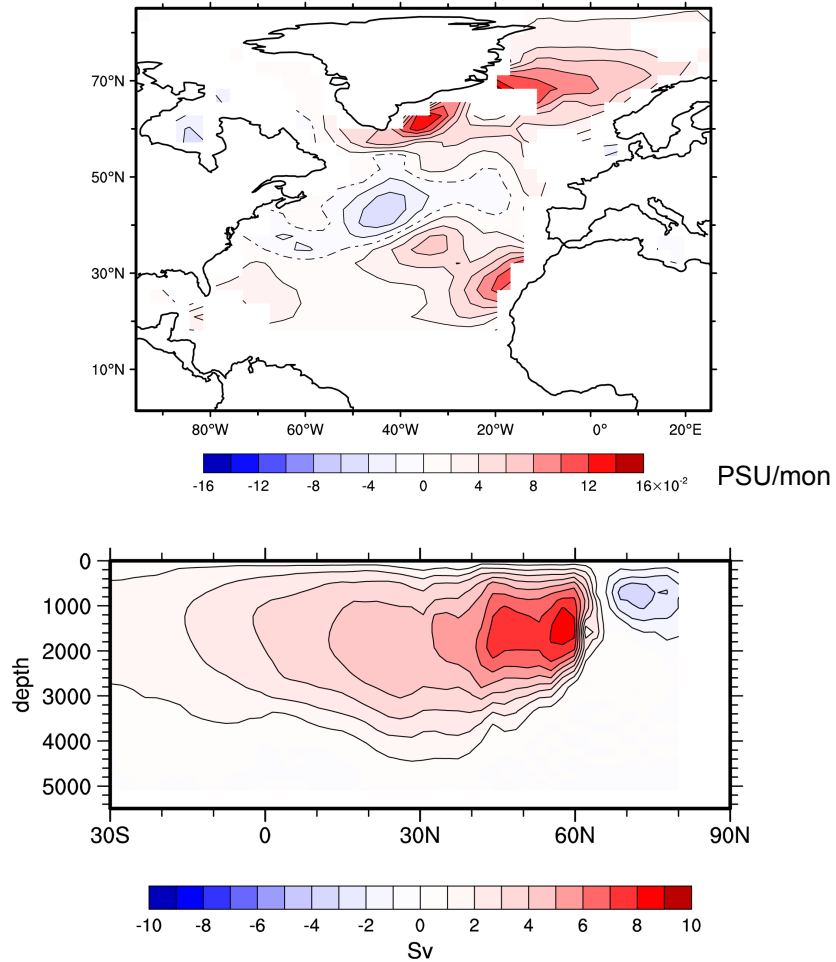
- FDT can be used to systematically study ocean response
- The leading patterns of AMOC variability do not depend on the existence of special atmospheric structures
- The effect of a given atmospheric pattern on AMOC depends strongly on details of its structure and of ocean dynamics
- The surface fields associated with AMOC anomalies depend on the atmospheric forcing

# Optimal Salinity Forcing of AMOC

5 year forcing; year 5 response

force 0-100m

SV1 35x 55%

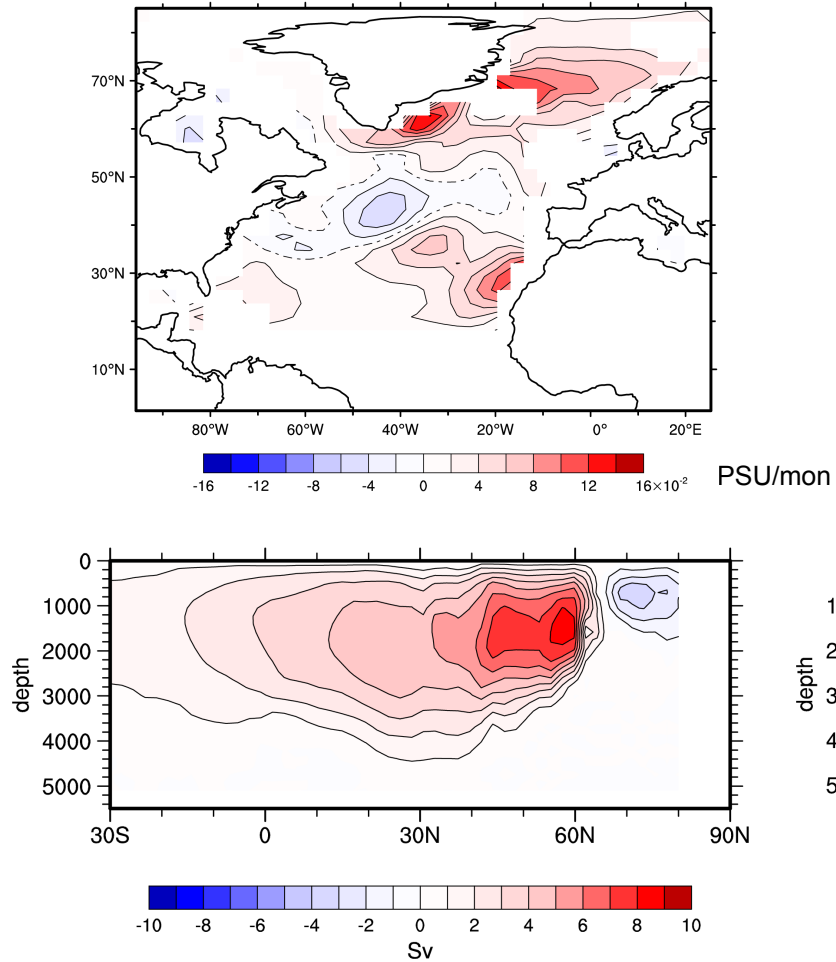


# Optimal Salinity Forcing of AMOC

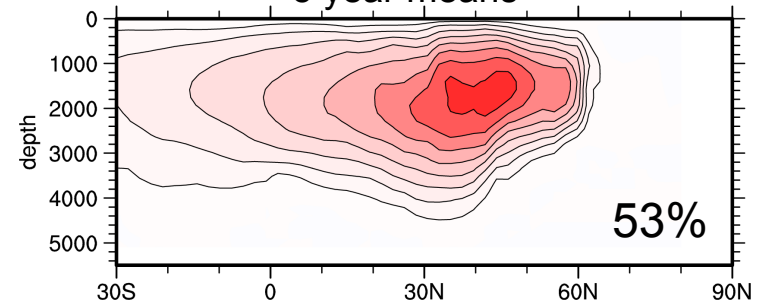
5 year forcing; year 5 response

force 0-100m

SV1 35x 55%



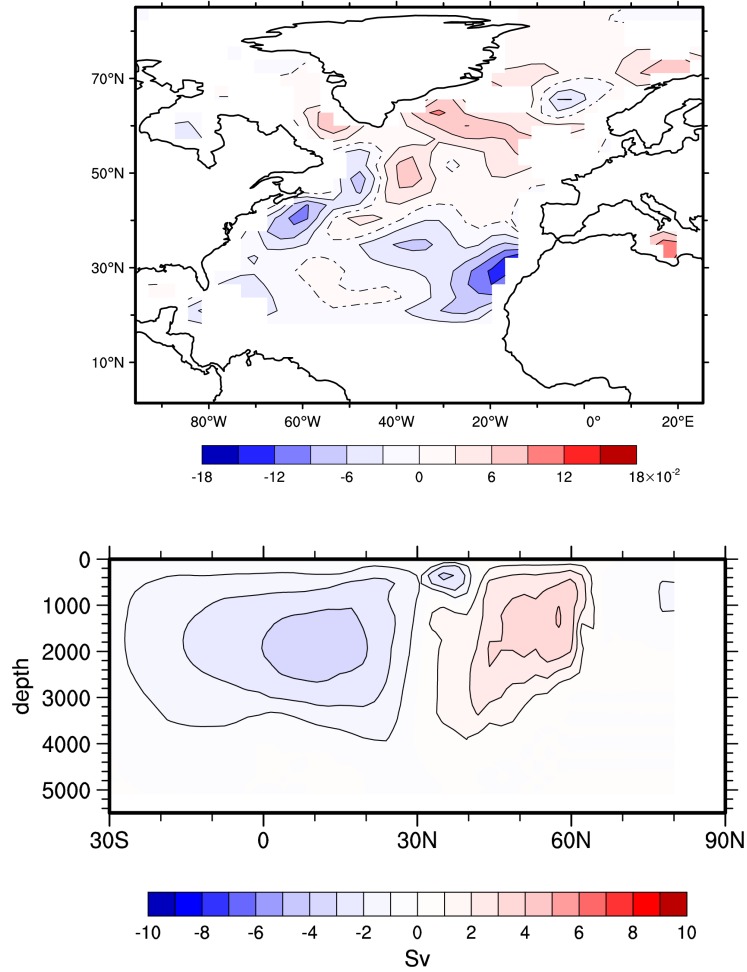
CCSM4 EOF1  
5 year means



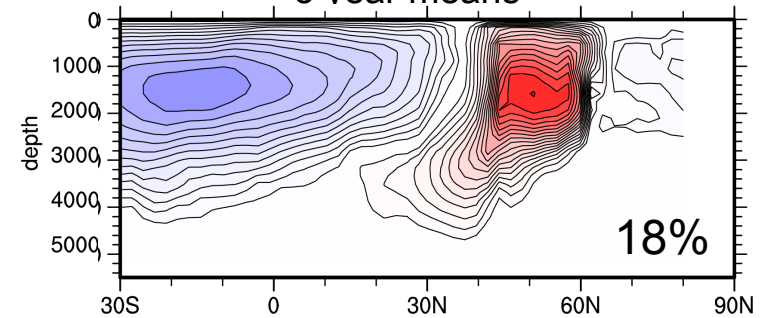
# Optimal Salinity Forcing of AMOC

5 year forcing; year 5 response  
force 0-100m

SV2 17x 14%



CCSM4 EOF2  
5 year means

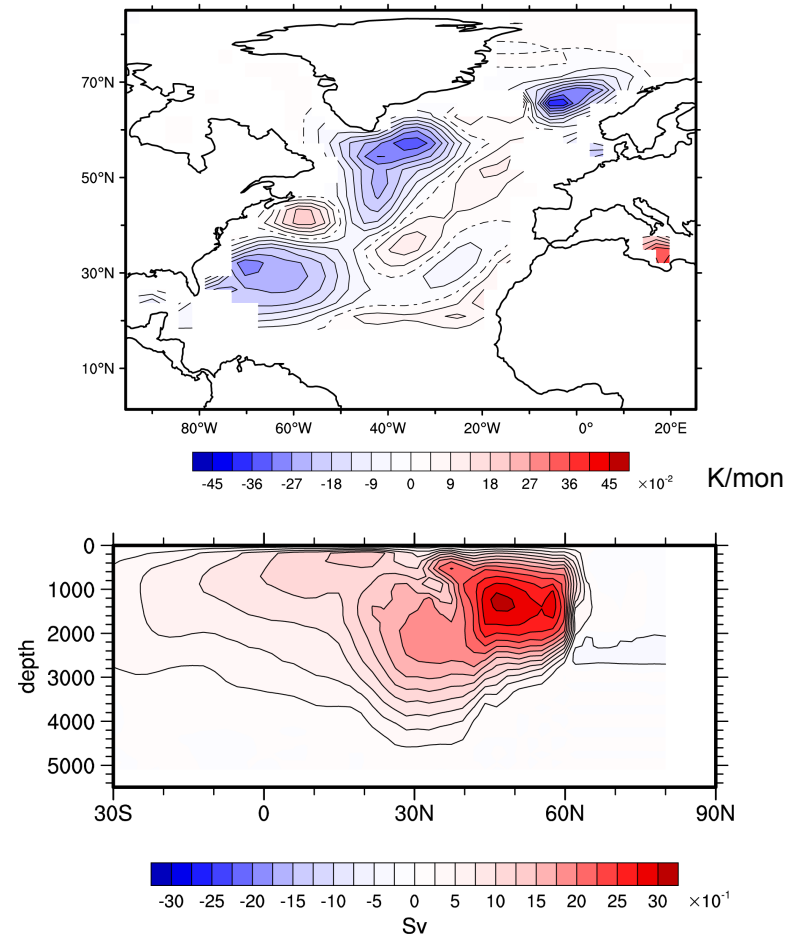


# Optimal North Atlantic Temperature Forcing of AMOC

5 year forcing; year 5 response

force 0-100m

SV1 34x

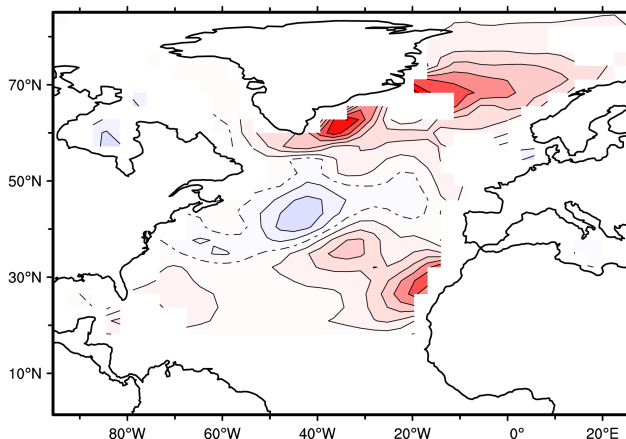


# Optimal Salinity & Temperature Forcing of AMOC

5 year forcing; year 5 response

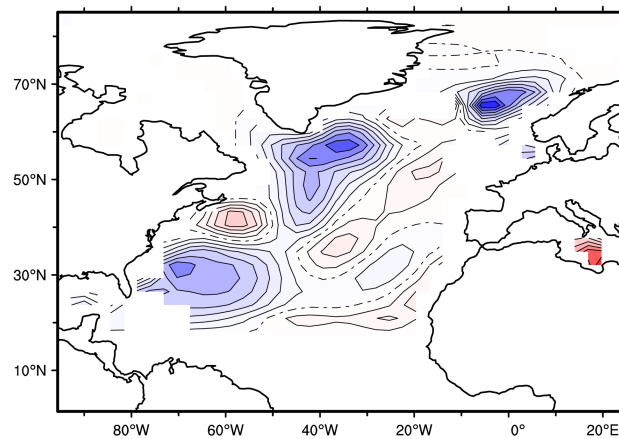
force 0-100m

SV1 35x



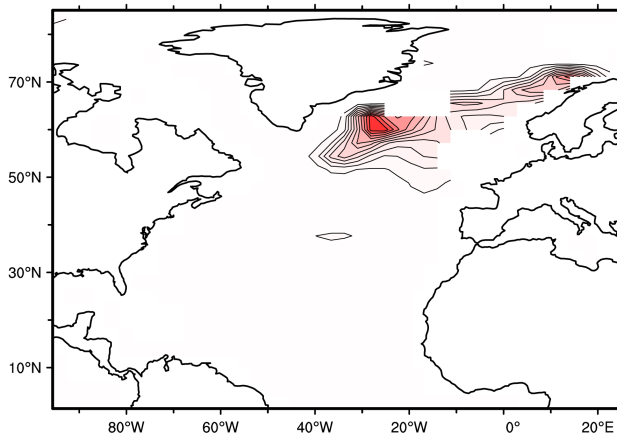
-16 -12 -8 -4 0 4 8 12 16  $\times 10^2$  PSU/month

SV1 34x



-45 -36 -27 -18 -9 0 9 18 27 36 45  $\times 10^2$  K/month

## Std Dev Boundary Layer Depth

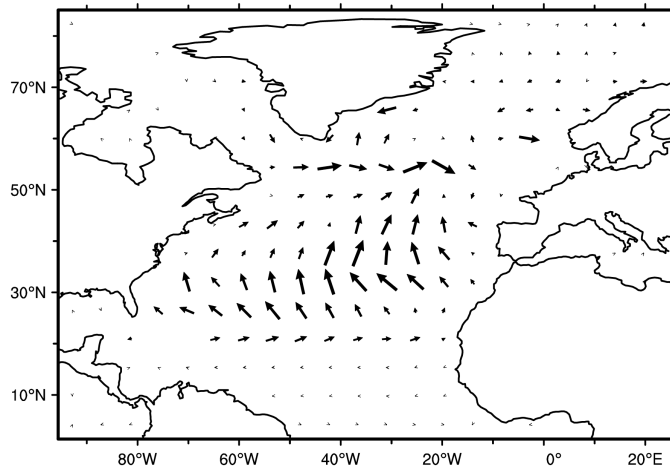


-75 -60 -45 -30 -15 0 15 30 45 60 75 m

# Optimal Excitation of AMOC by Currents in the North Atlantic

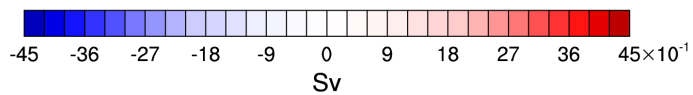
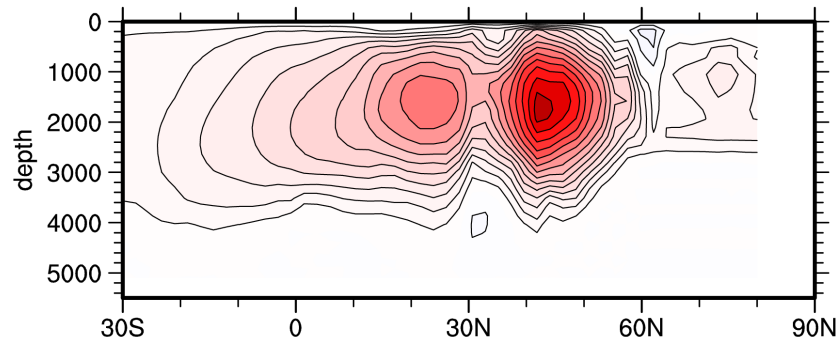
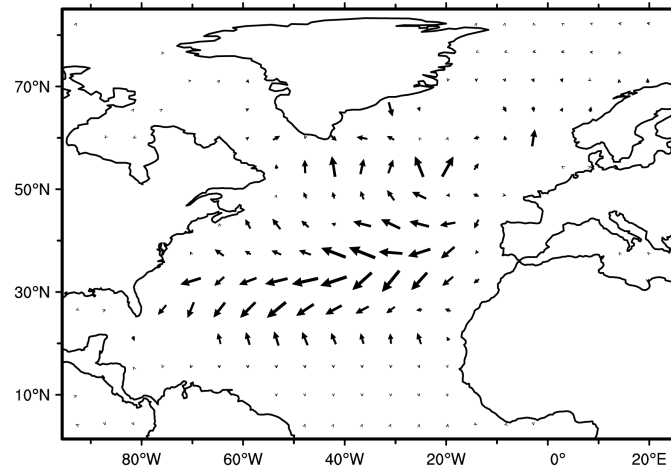
SV1 35x

forcing of 0-100m currents



$f = 7.2 \text{ cm s}^{-1}/\text{mon}$

wind stress



## Remember

- FDT can be used to systematically study ocean response
- The leading patterns of AMOC variability do not depend on the existence of special atmospheric structures
- The effect of a given atmospheric pattern on AMOC depends strongly on details of its structure and of ocean dynamics
- The surface fields associated with AMOC anomalies depend on the atmospheric forcing

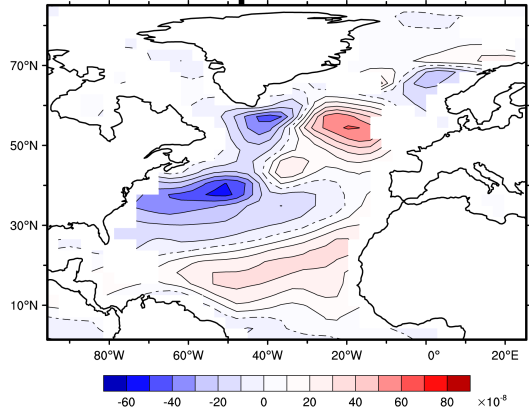


# Comparing NAO Fluxes & Optimal Forcing

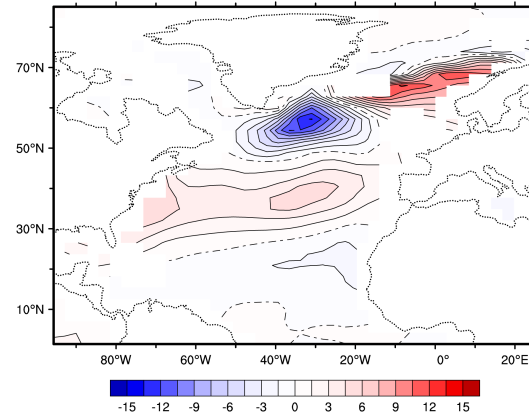
5 year forcing; year 5 response

## NAO

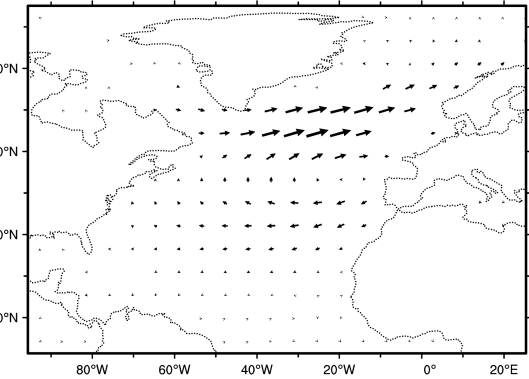
### Evaporation



### Surface heat flux

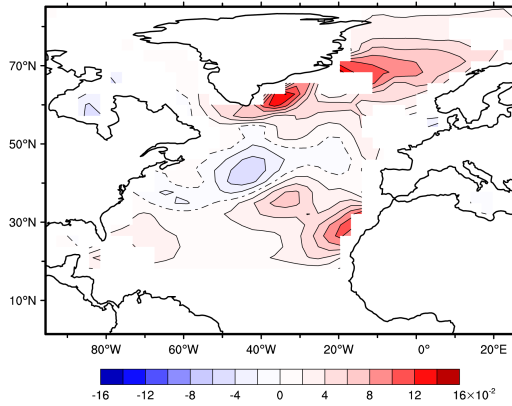


### Wind stress

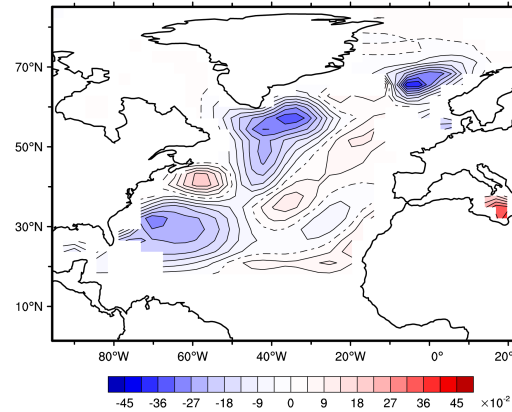


## Optimal forcing force 0-100m

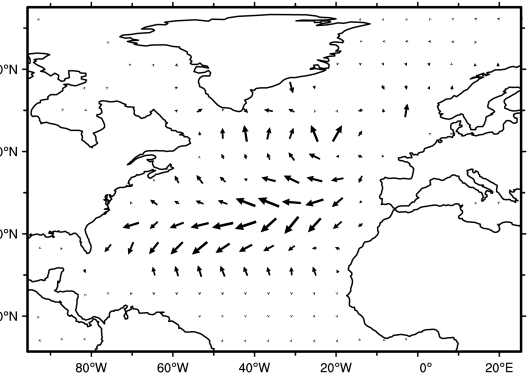
### Salinity



### Temperature



### Wind stress



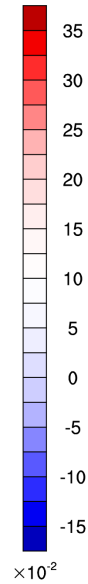
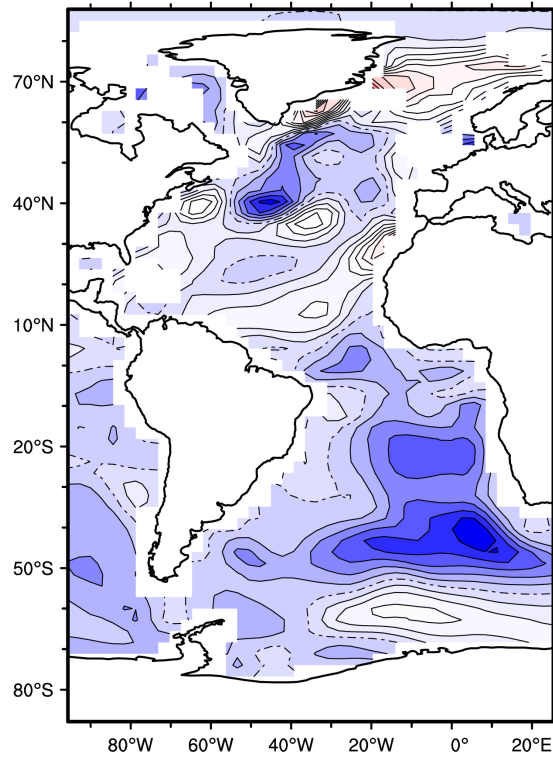
## Remember

- FDT can be used to systematically study ocean response
- The leading patterns of AMOC variability do not depend on the existence of special atmospheric structures
- **The effect of a given atmospheric pattern on AMOC depends strongly on details of its structure and of ocean dynamics**
- The surface fields associated with AMOC anomalies depend on the atmospheric forcing

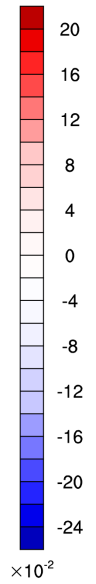
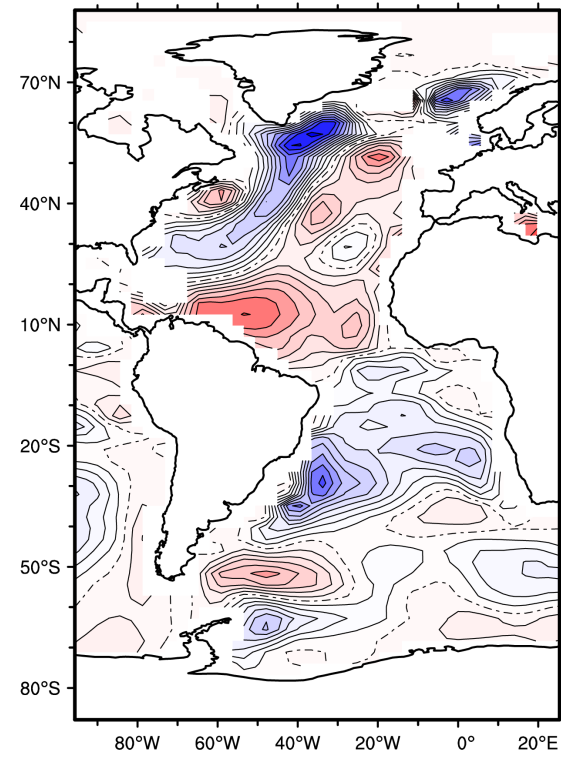
# Year 5 Response of AMOC PC1 to Point Sources

force 0-100m

*forcing = 0.1PSU/mon*



*forcing = 1K/mon*



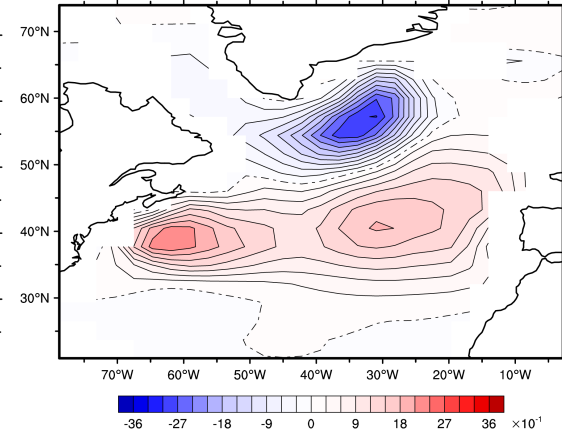
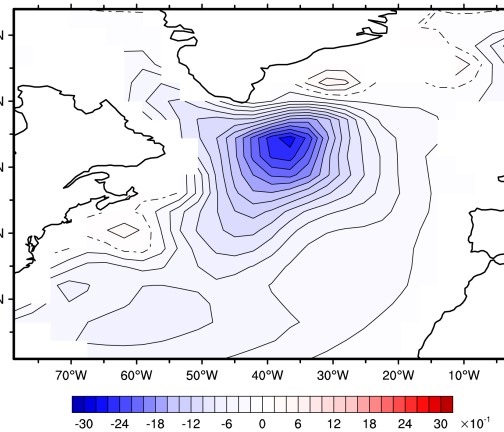
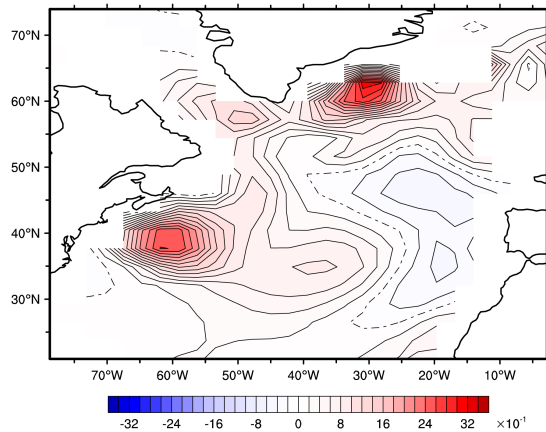
# Year 5 SST Response to Optimal AMOC Excitation by SHF, Salt & Wind stress force 0-100m

force the salinity

force by heat

force the currents

SST response

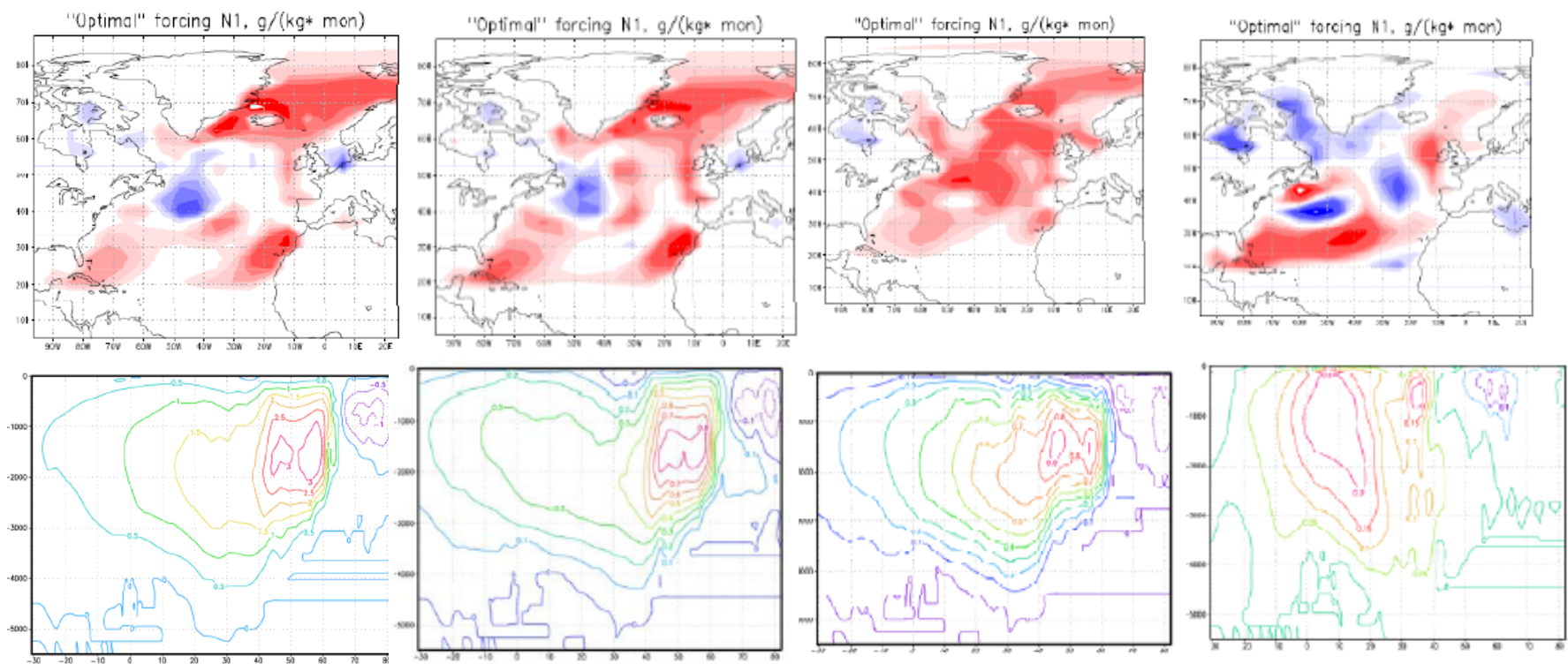


## Remember

- FDT can be used to systematically study ocean response
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- **The surface fields associated with AMOC anomalies depend on the atmospheric forcing**

## Remember

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- The leading patterns of AMOC variability do not depend on the existence of special atmospheric structures
- The effect of a given atmospheric pattern on AMOC depends strongly on details of its structure and of ocean dynamics
- The surface fields associated with AMOC anomalies depend on the atmospheric forcing



5y response to 5y forcing

5y response to 1y forcing

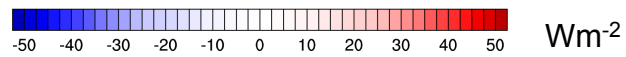
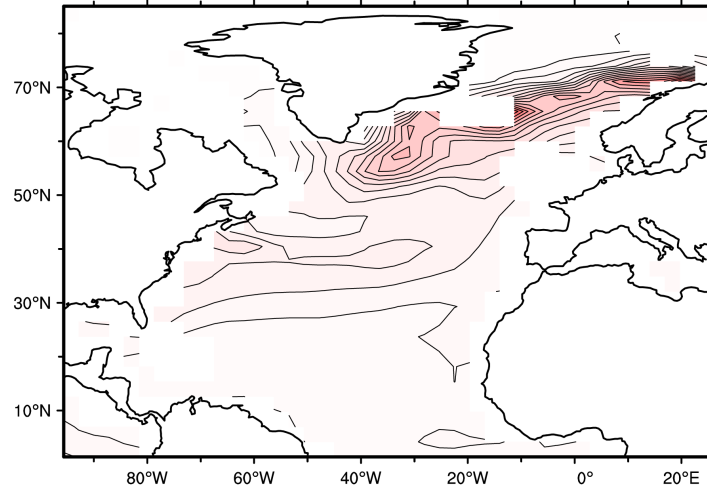
10y response to 1y forcing

1y response to 1y forcing

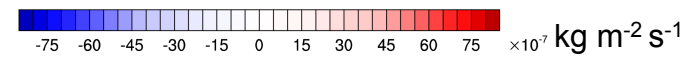
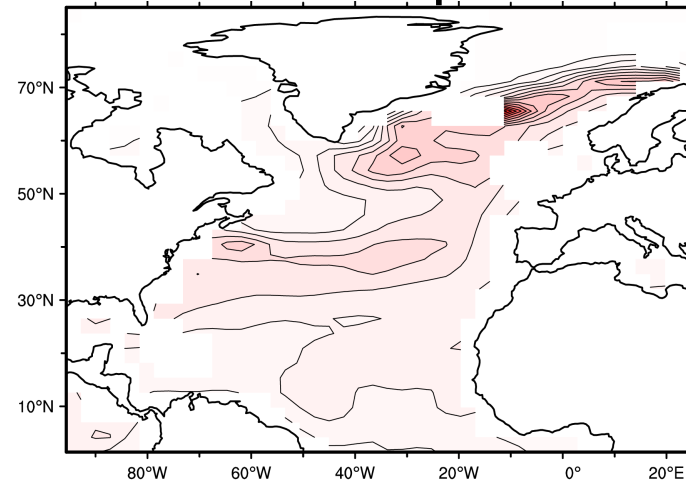
note SV2 for this case is like SV1 in other cases

# Std dev of Annual Mean Surface Forcing Fields

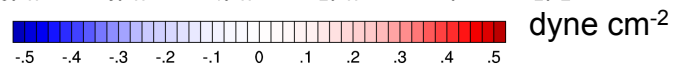
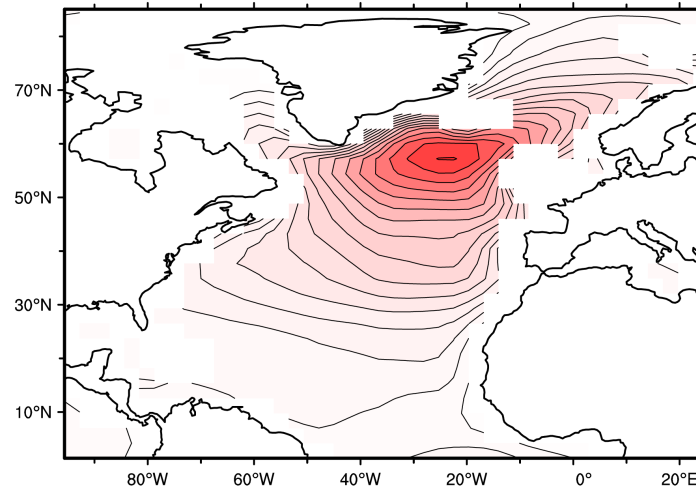
## Surface Heat Flux



## Surface Evaporation

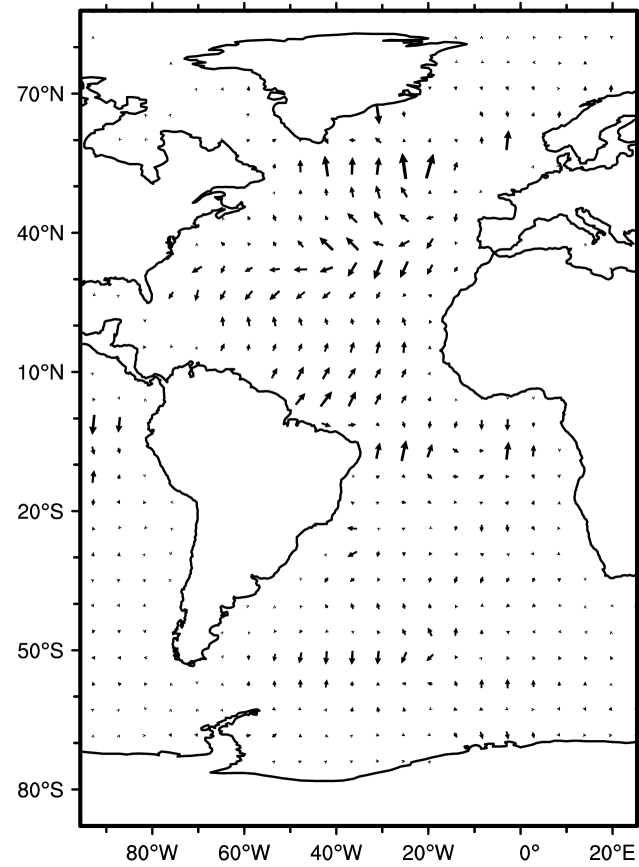


## Wind Stress

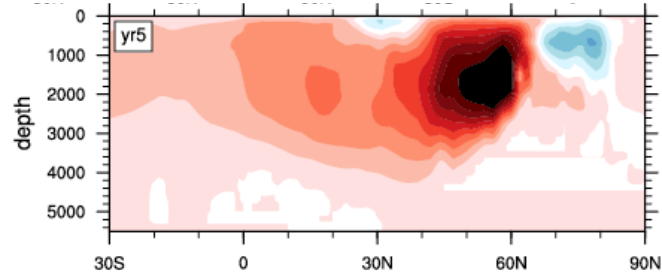




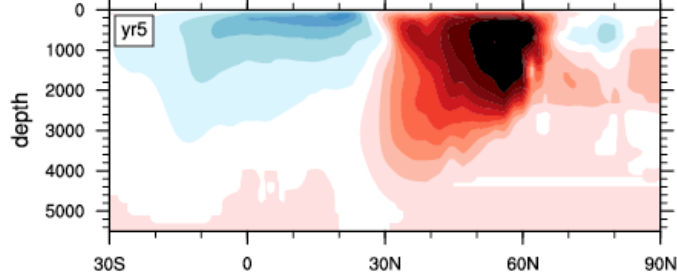
# Green's function of AMOC EOF1 for wind stress force 0-100m



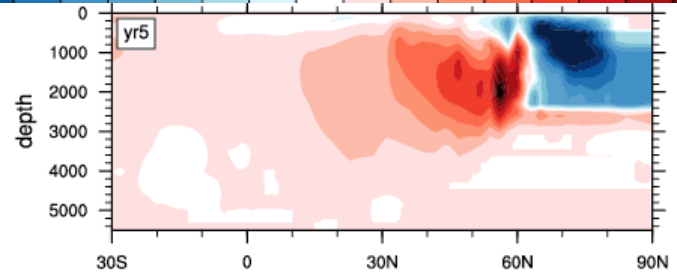
SV1



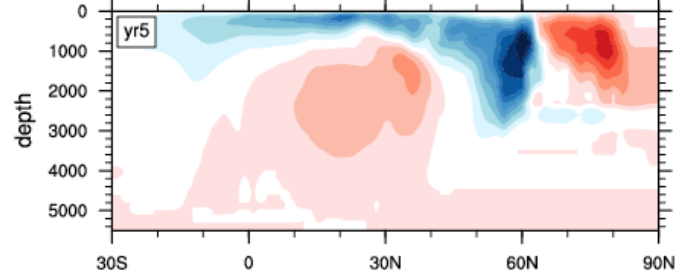
SV2



SV3



SV4



Sv

CCSM4 response to SV forcing

