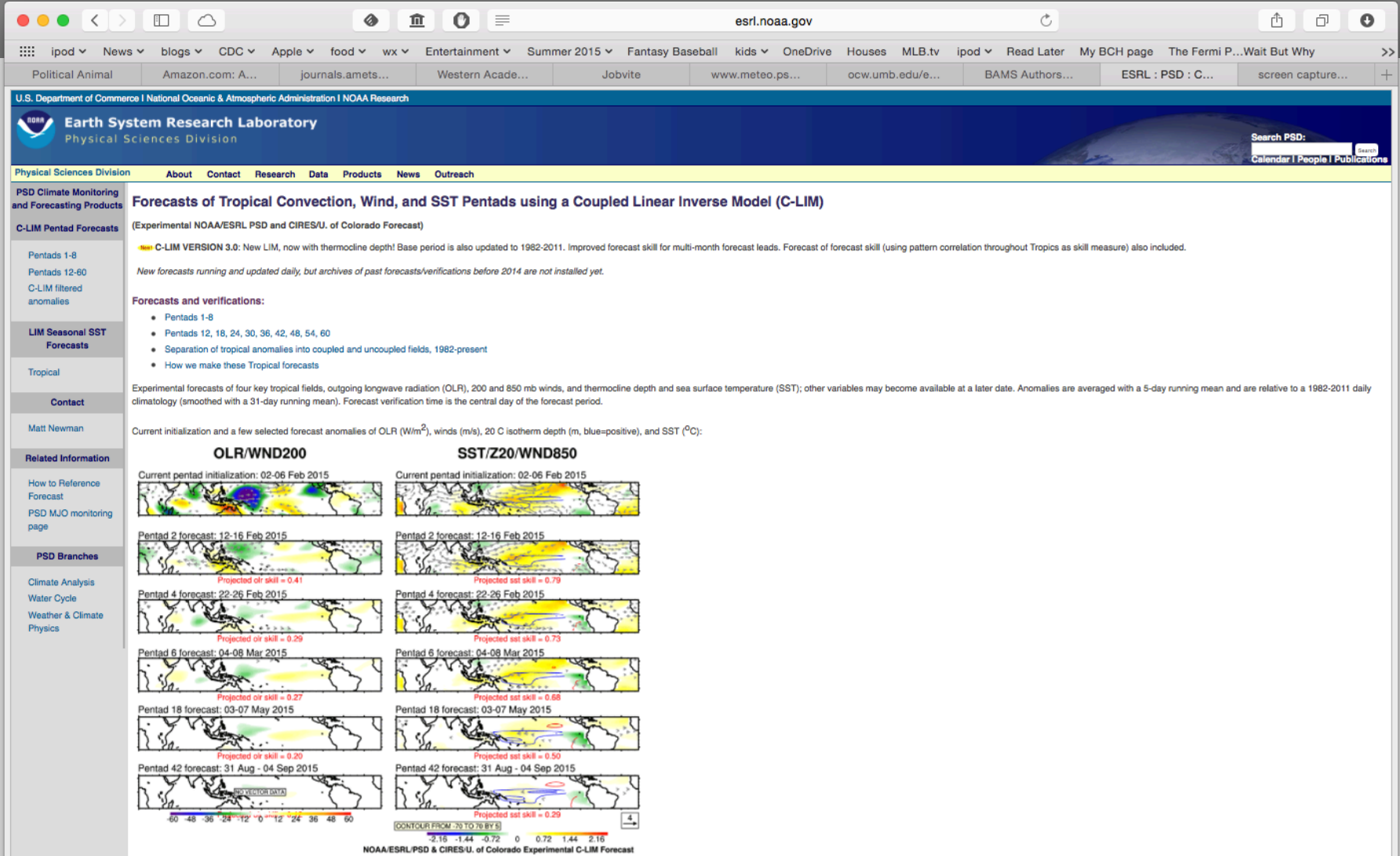


# Diagnosing ENSO predictability from observations and models

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# “Multivariate Red Noise\*” null hypothesis

$$dx/dt = \mathbf{L}x + \mathbf{F}_s$$

$\mathbf{x}(t)$  is a series of maps,  $\mathbf{L}$  is stable, and  $\mathbf{F}_s$  is white noise (maps)

- Determine  $\mathbf{L}$  and  $\mathbf{F}_s$  using “Linear Inverse Model” (LIM)
  - $\mathbf{x}$  is ocean (**SST/Z20**) and atmosphere (**OLR/200&850 mb wind**) 5-day running mean anomalies in Tropics, 1982-2011 (similar to Newman, Sardeshmukh, Penland 2009 and Newman, Alexander, Scott 2011)
  - prefiltered in reduced EOF space
  - LIM determined from specified lag  $\tau_0=5$  days (e.g., the data averaging interval) as in AR1 model, using  $\tau_0$ - and zero-lag covariance of  $\mathbf{x}$
  - Test the LIM over much longer time intervals: observed spatio-temporal lag-covariance statistics very well reproduced
  - Hindcasts determined from cross-validation (10% data withheld to recompute  $\mathbf{L}$ )

\*Multivariate Ornstein-Uhlenbeck process

# Using LIM to estimate predictability

$$d\mathbf{x}/dt = \mathbf{L}\mathbf{x} + \mathbf{F}_s$$

$\mathbf{L}$  = constant,  $\mathbf{F}_s$  = additive (state-independent) noise.

$$\mathbf{x}(t + \tau) = \exp(\mathbf{L}\tau) \mathbf{x}(t) + \boldsymbol{\varepsilon} = \mathbf{G}(\tau) \mathbf{x}(t) + \boldsymbol{\varepsilon}$$

“signal”

“noise”

Expected forecast error covariance

(assuming no initial error) :

$$\mathbf{E}(\tau) = \langle \boldsymbol{\varepsilon} \boldsymbol{\varepsilon}^T \rangle = \mathbf{C}(0) - \mathbf{G} \mathbf{C}(0) \mathbf{G}^T$$

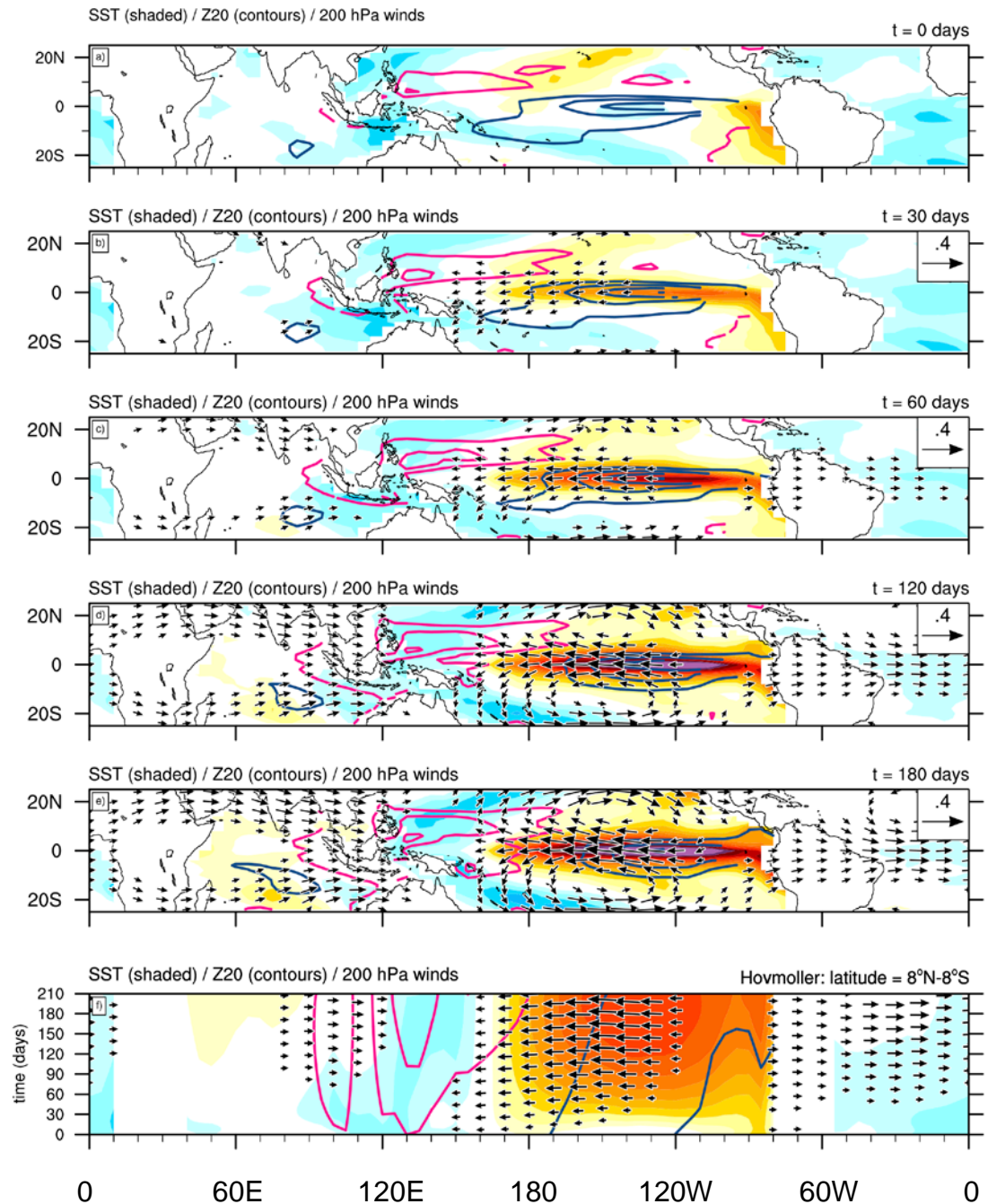
Expected forecast anomaly correlation

$$\rho_\infty = \frac{s}{\sqrt{1+s^2}}, \text{ where } s^2 = \frac{[\mathbf{G} \mathbf{C}(0) \mathbf{G}^T]_{ii}}{[\mathbf{E}(\tau)]_{ii}}$$

**Larger signal related to leading singular vector of  $\mathbf{G}(\tau)$**   
**Assumption (overly restrictive?):  $\mathbf{E}(\tau)$  depends *only* on  $\tau$**

“Optimal”  
structure leading  
to greatest  
tropical SST  
anomaly growth  
over 180 days

Shading: SST  
Contours:  $Z_{20}$   
Vectors: 200 mb winds



# Compare LIM to (some of the) National Multi-model Ensemble (NMME) Hindcasts, 1982-2010

LIM hindcasts averaged into 35-day “months”  
so “Month 6” skill is days 146-180

NMME hindcast ensemble monthly means from

- NCEP CFSv2
- NASA GEOS5
- NCAR CCSM3
- GFDL CM2.1/2.5
- CMC1-CanCM3/4
- ECHAM 4.5

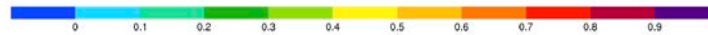
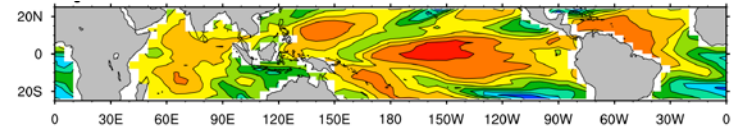
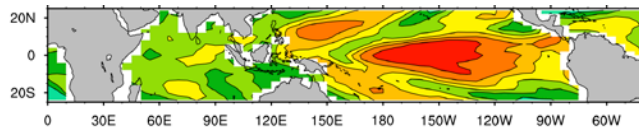
“Month 0.5” skill is first month, initialized in  
mid-month (see Kirtman et al. 2014)



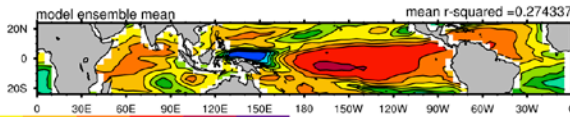
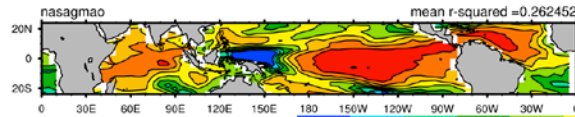
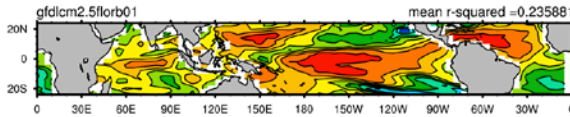
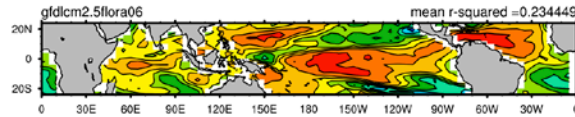
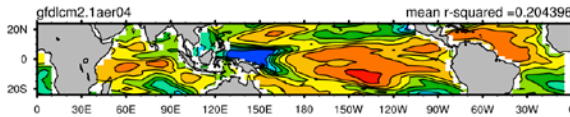
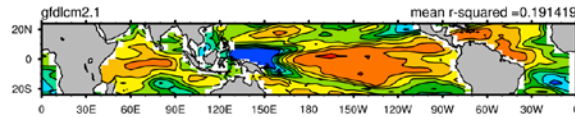
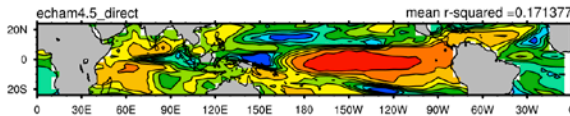
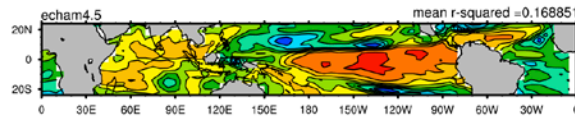
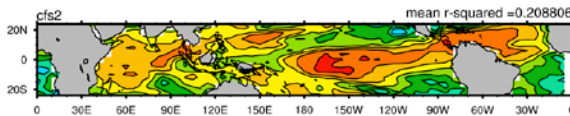
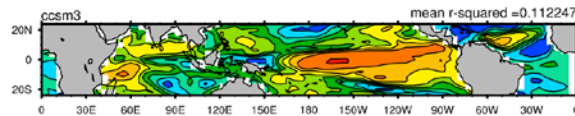
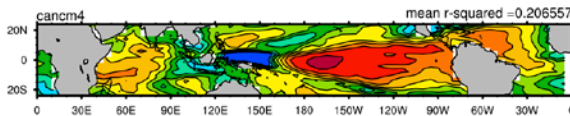
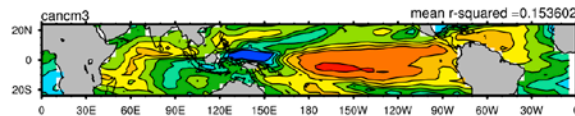
# Comparing predicted and actual forecast skill, or: some places are more predictable than others

## Predicted Month 6 LIM skill

## Actual Month 6 LIM skill



NMME



NMME  
ensemble  
mean

# Comparing predicted and actual forecast skill, or: some **years** are more predictable than others

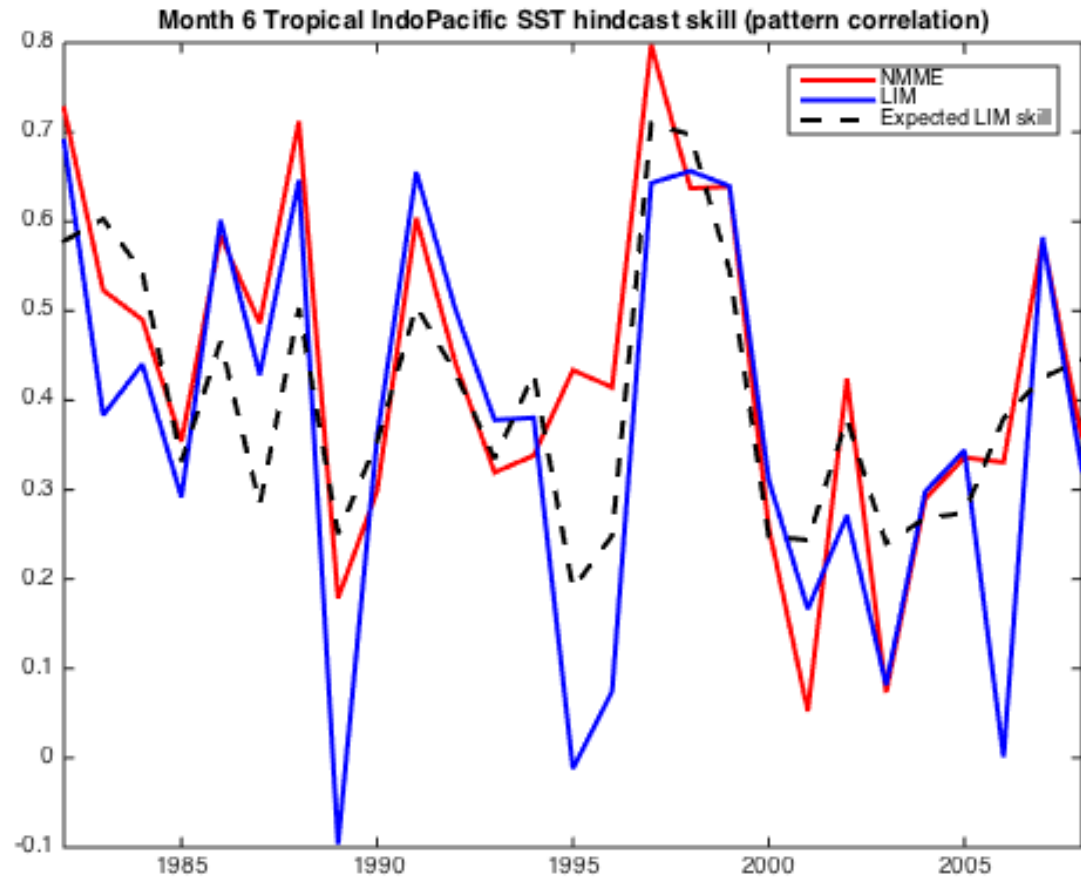
Skill averaged by  
year (based on  
initialization date)

**Actual skill:**  
Pattern  
correlation of  
tropical SST  
anomaly with  
SST forecast  
anomaly

Blue: LIM (0.40)

Red: NMME  
(0.45)

Predicted:  $\rho_{\infty}$  (0.43)



NMME and LIM skill correlated with  $\rho_{\infty}$  at 0.8

## A few other points

- LIM useful for diagnosis of predictability, **because** its forecast skill is comparable with coupled GCMs and it reproduces observed spatio-temporal statistics
- Subseasonal-interannual forecast skill may itself be **predicted based on LIM signal-to-noise**
  - In LIM, there is no “spread/skill” relationship, but note this need not be a constraint for all linearly predictable systems
- **Year-to-year variations in forecast skill** in the last few decades may be **due to random variations in initial conditions** and not necessarily to long-term “base state” changes



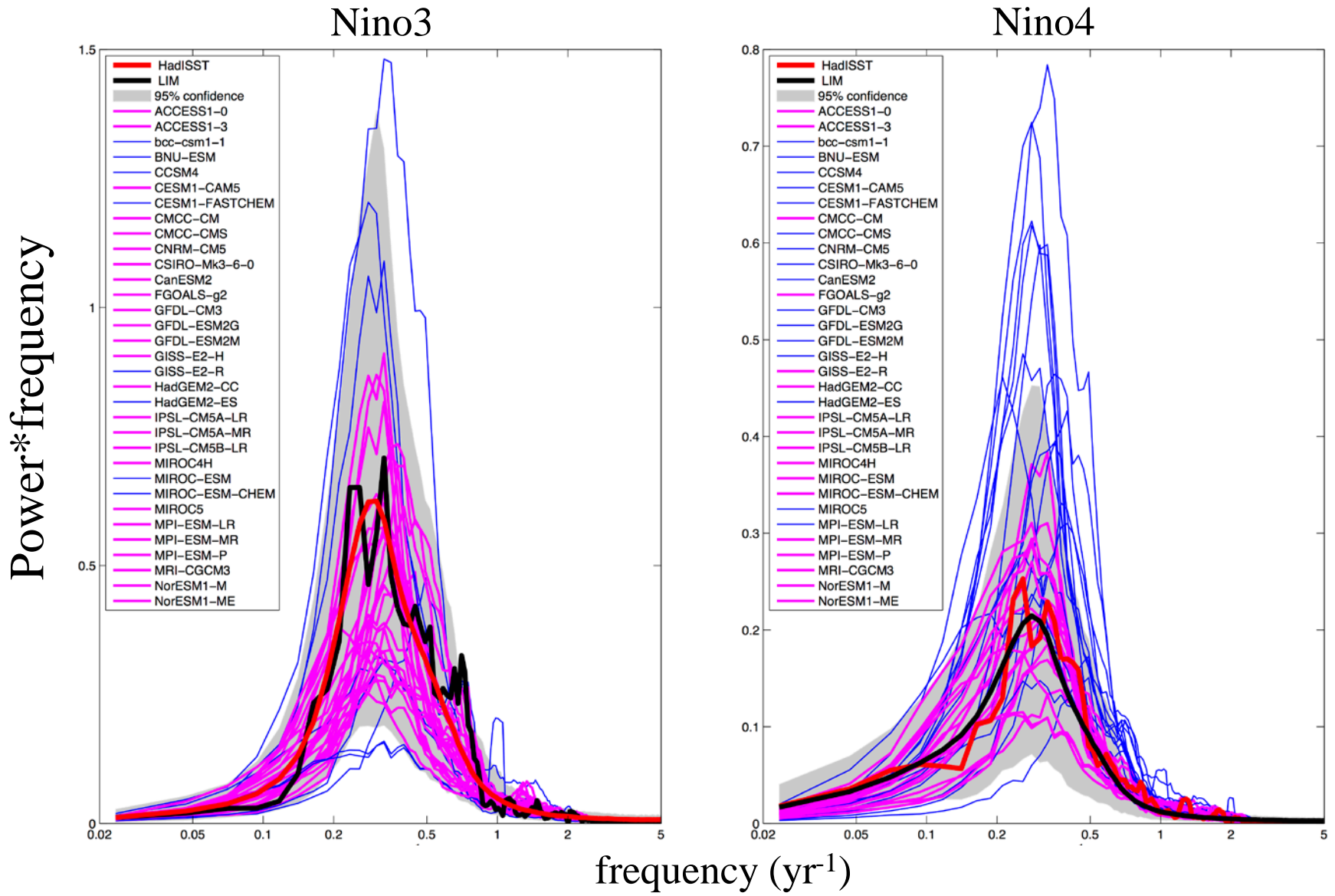
But...

what if there is a base state change?

To answer,

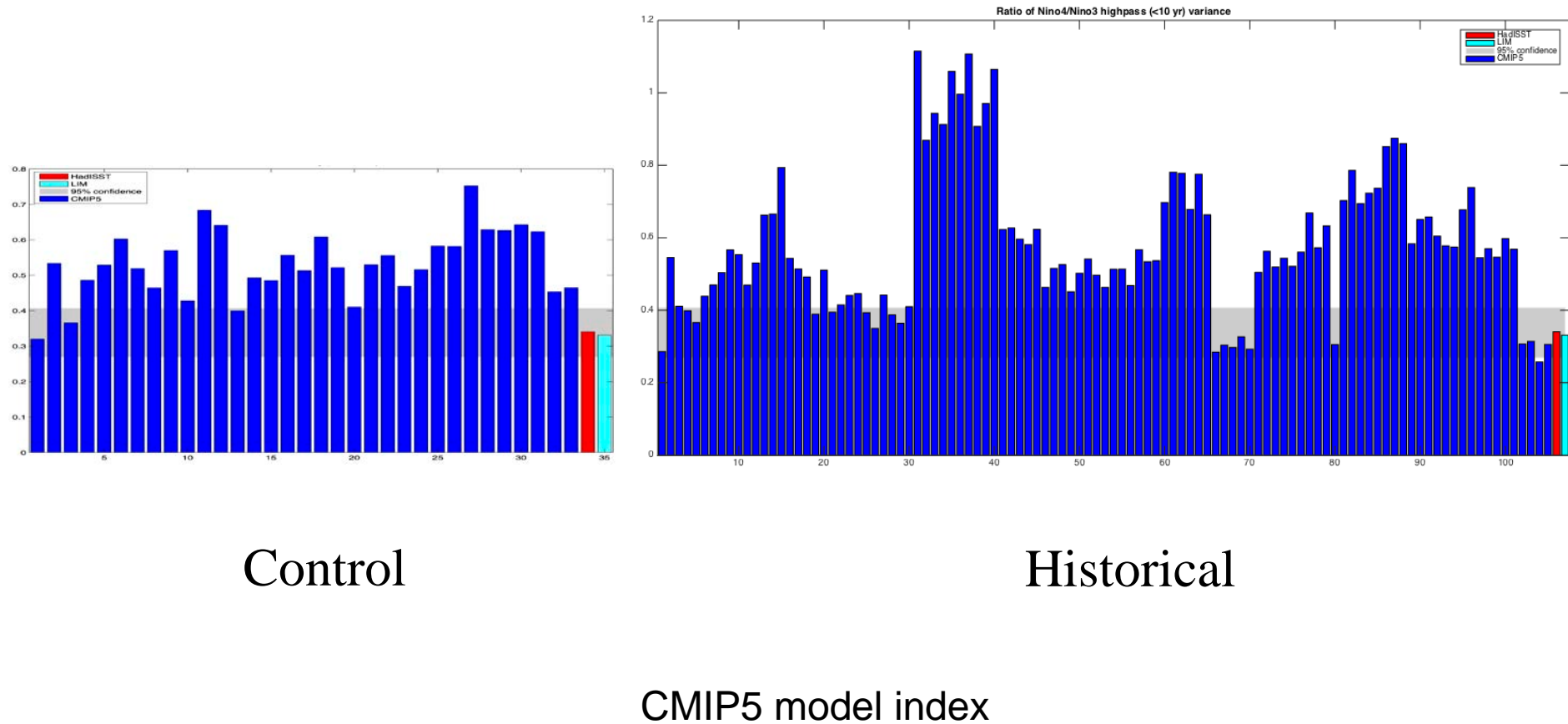
travel to other M-class planets

LIM based on one-season lag (now using SST, Z20, zonal wind stress) reproduces observed spectra; use for significance testing (blue: significantly different)



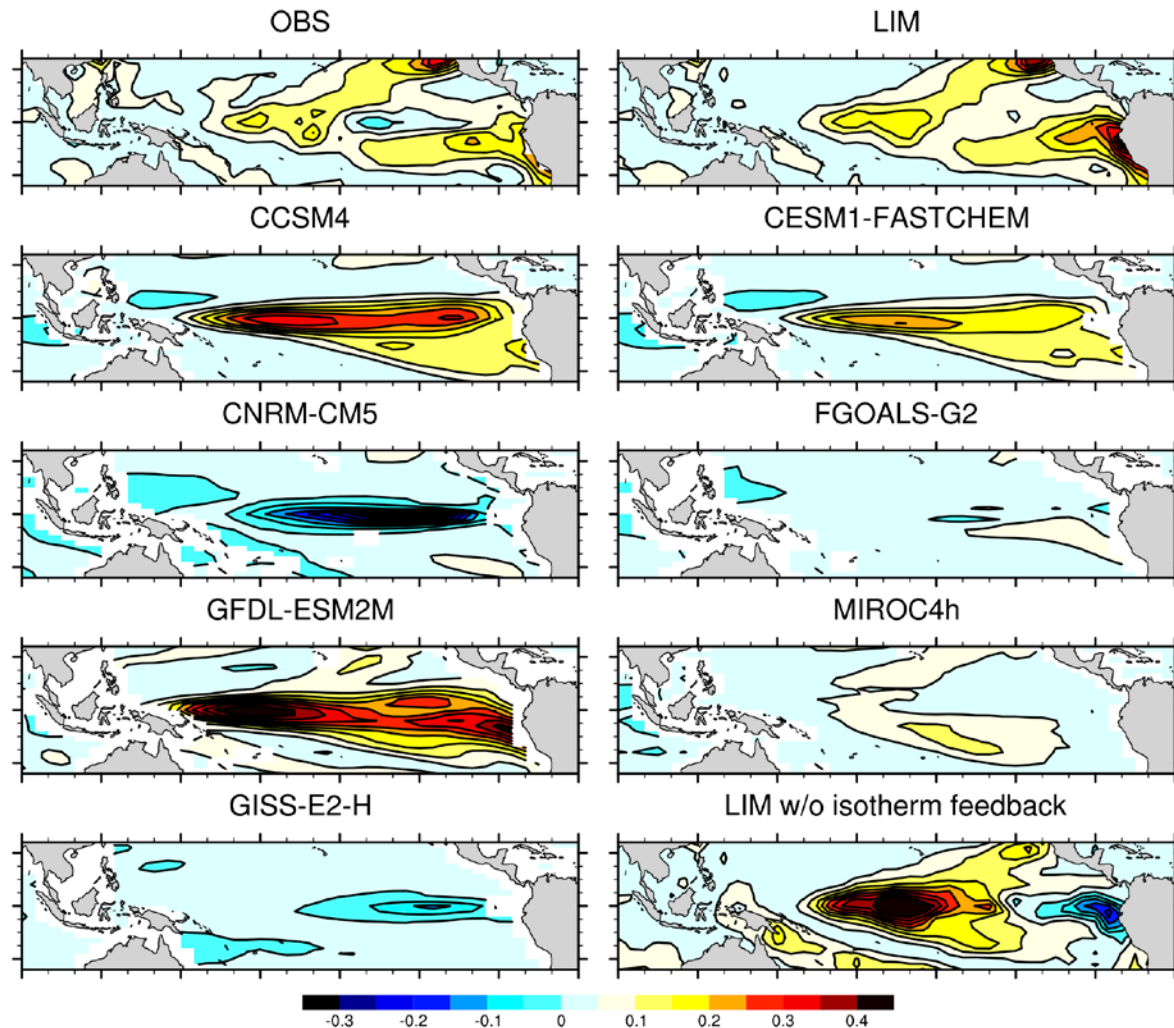
LIM based on one-season lag reproduces observed spectra  
and can be used for significance testing  
***CMIP5: Nino4 significantly too strong compared to Nino3***

Ratio of Nino4/Nino3 highpass (<10yr)

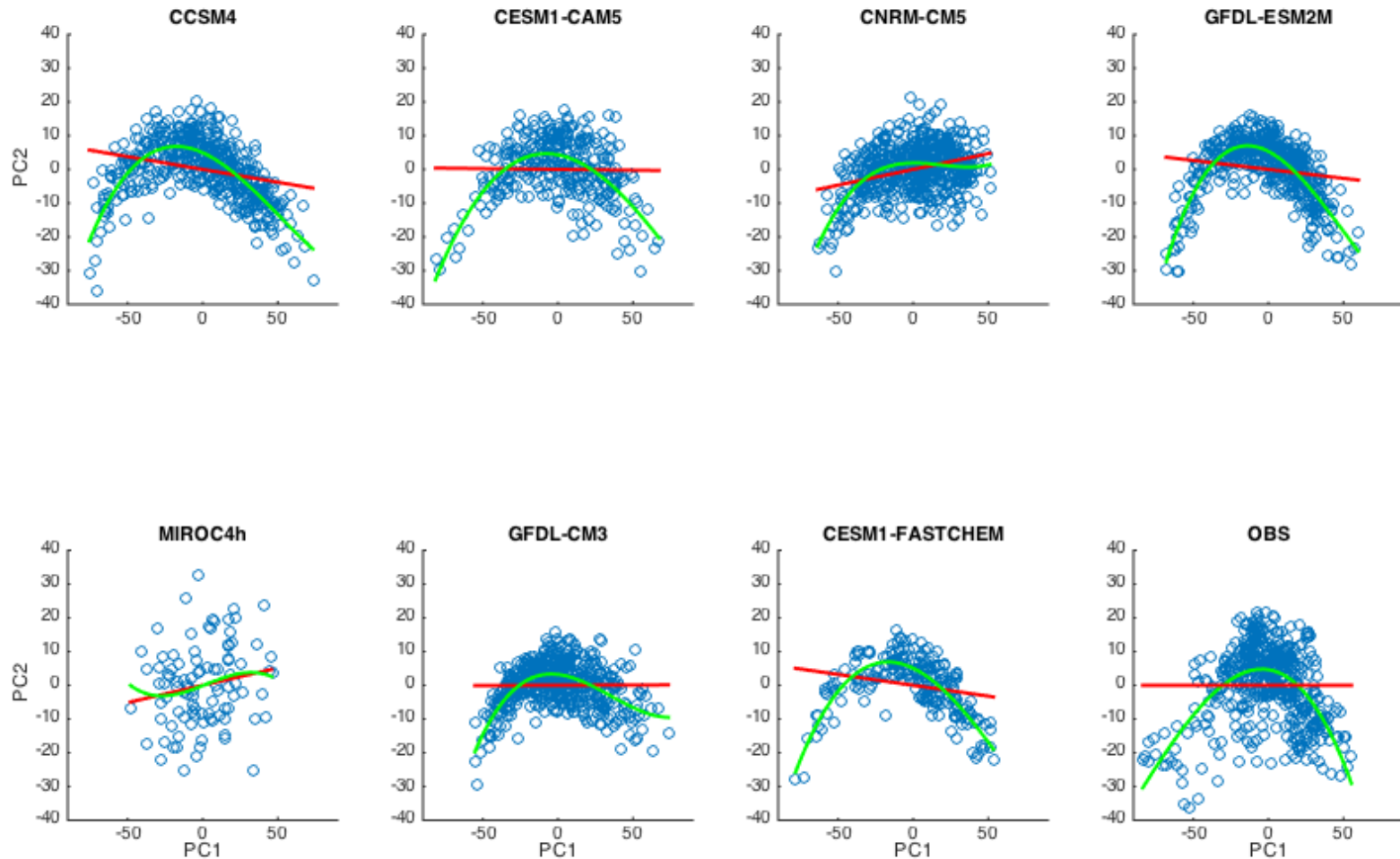


LIM based on 1-season lag reproduces evolution statistics at much longer leads.

### SST 9-month lag covariance



# How nonlinear is PC1/2 in the models compared to observations?



# How nonlinear is ENSO in models compared to obs? *CMIP5: nonlinearity in PC1/PC2 plane depends on ENSO strength*

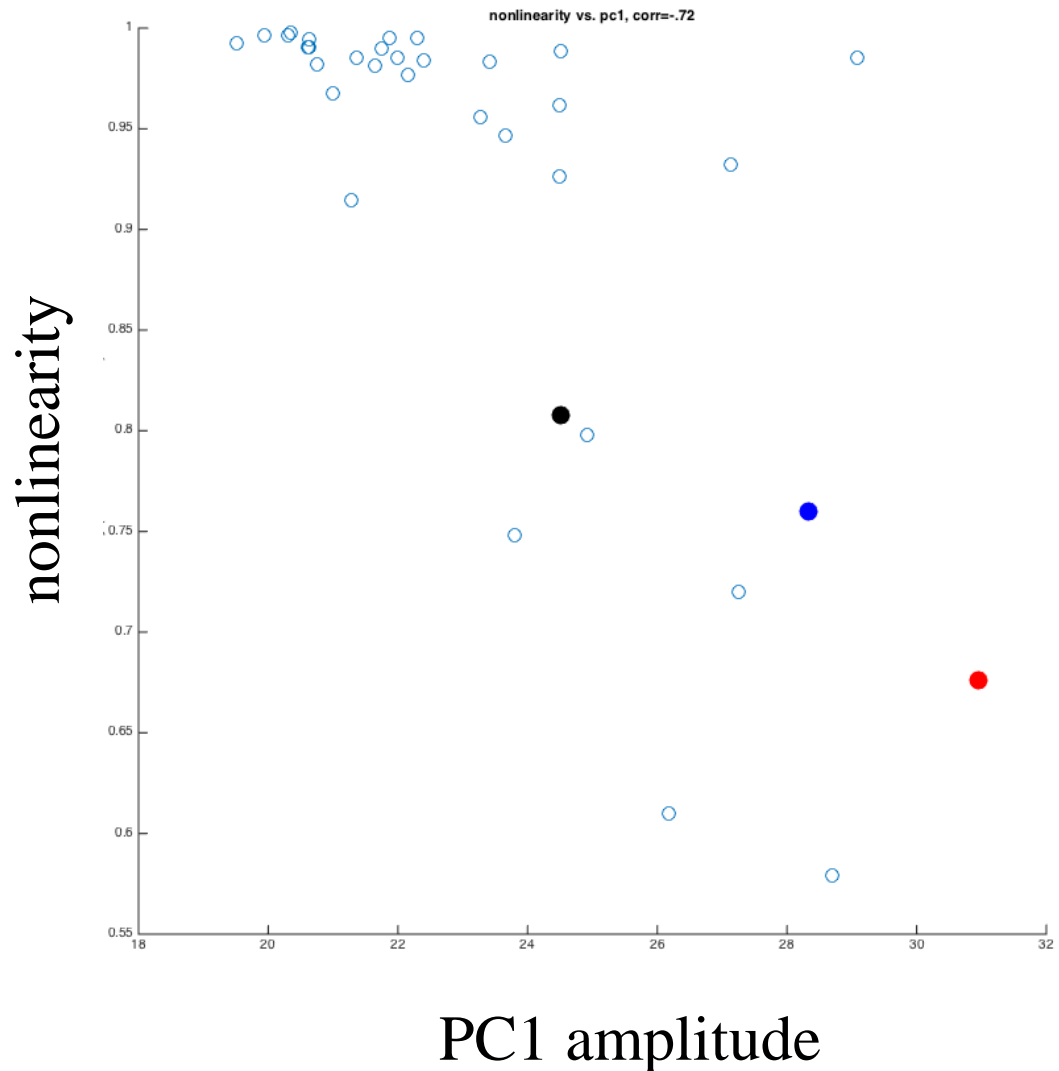
Measure of  
“nonlinearity”:

std error of cubic fit  
std error of linear fit

**OBS**

**CCSM4**

**CESM1-CAM5**





# Evolution of 6-month optimal structure

SST: shading

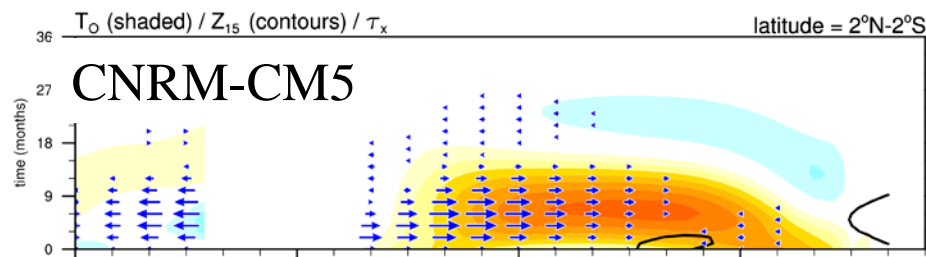
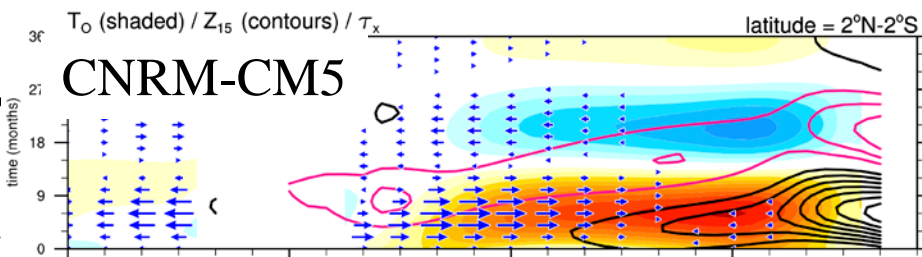
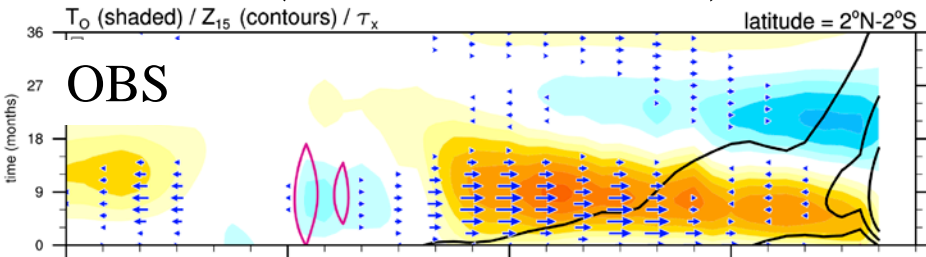
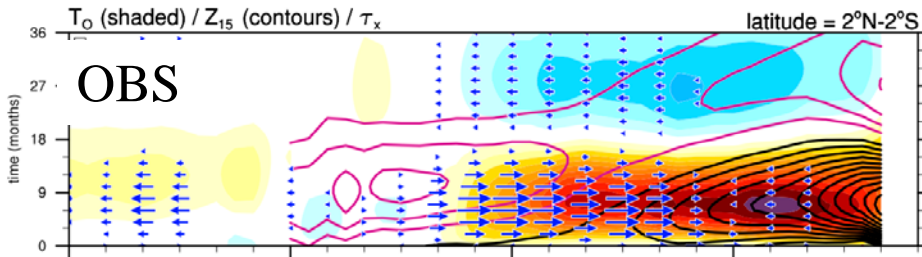
Thermocline depth: contours

Zonal wind stress: vectors

Equatorial Hovmuller, time running from 0 to 36 months

FULL

No thermocline term  
("Slab-like" LIM)



Thermocline term *strengthens* ENSO in east  
but slightly *damps* in central Pacific

# Evolution of 6-month optimal structure

SST: shading

Thermocline depth: contours

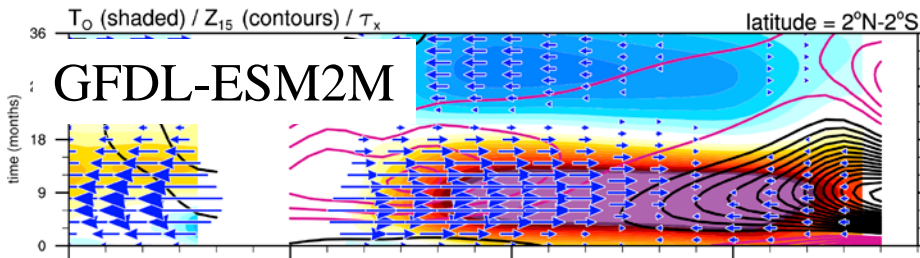
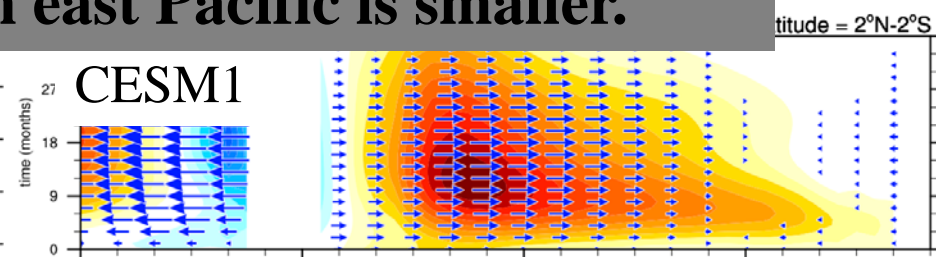
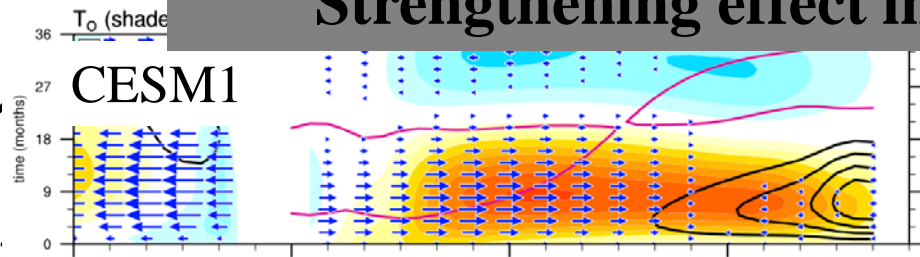
Zonal wind stress: vectors

Equatorial Hovmuller, time running from 0 to 36 months

FULL

No thermocline term  
("Slab-like" LIM)

In these models (and some others), thermocline term  
(all effects) *weakens* ENSO more in central Pacific.  
Strengthening effect in east Pacific is smaller.



# Conclusion 2

- **Coupled GCMs may not represent observed dynamics sufficiently well enough to study ENSO diversity if they have:**
  - Strong and unrealistic Nino4 variability within “east Pacific” ENSO events that swamps more purely “central Pacific” ENSO variability
  - Too strong “nonlinear” relationship in PC1/2 plane
  - Optimal structure for central Pacific ENSO in west Pacific
  - Thermocline term acting *damps too much* in central Pacific and drives *growth too little* in east Pacific

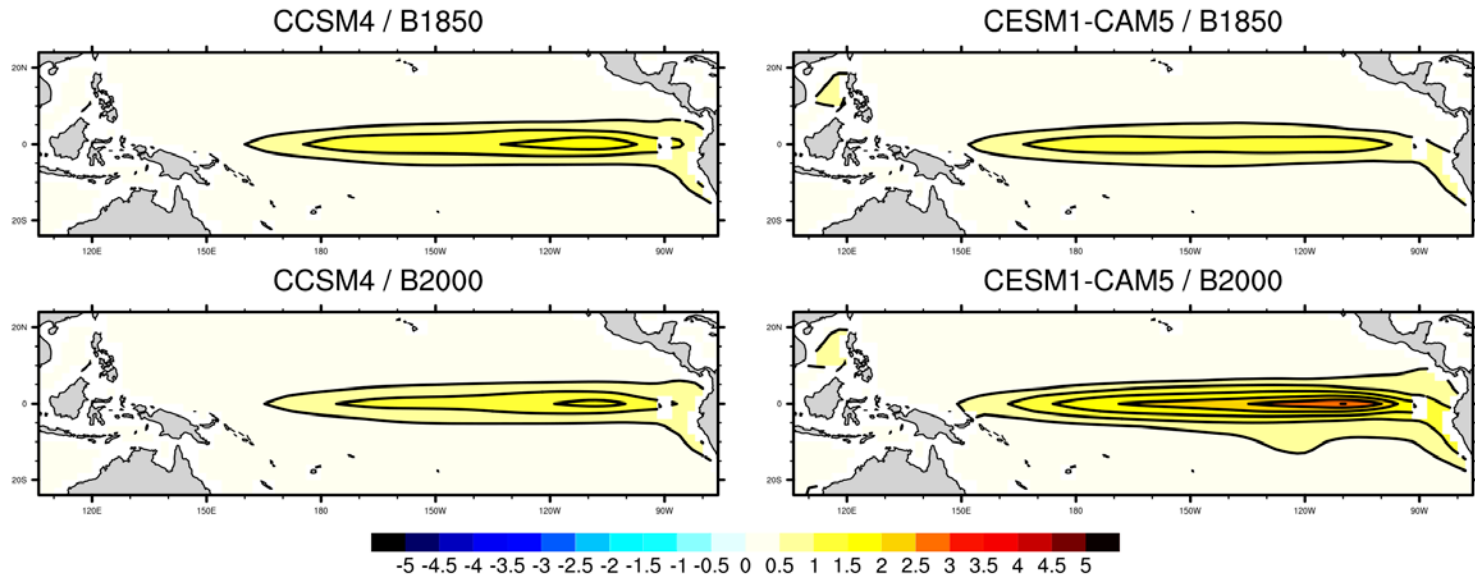
# Compare LIMs constructed from:

- CCSM4, 1100 yr run under radiative conditions from
  - 1850 (B1850)
  - 2000 (B2000)
- CESM1-CAM5, 700 yr run under radiative conditions from
  - 1850 (B1850)
  - 2000 (B2000)

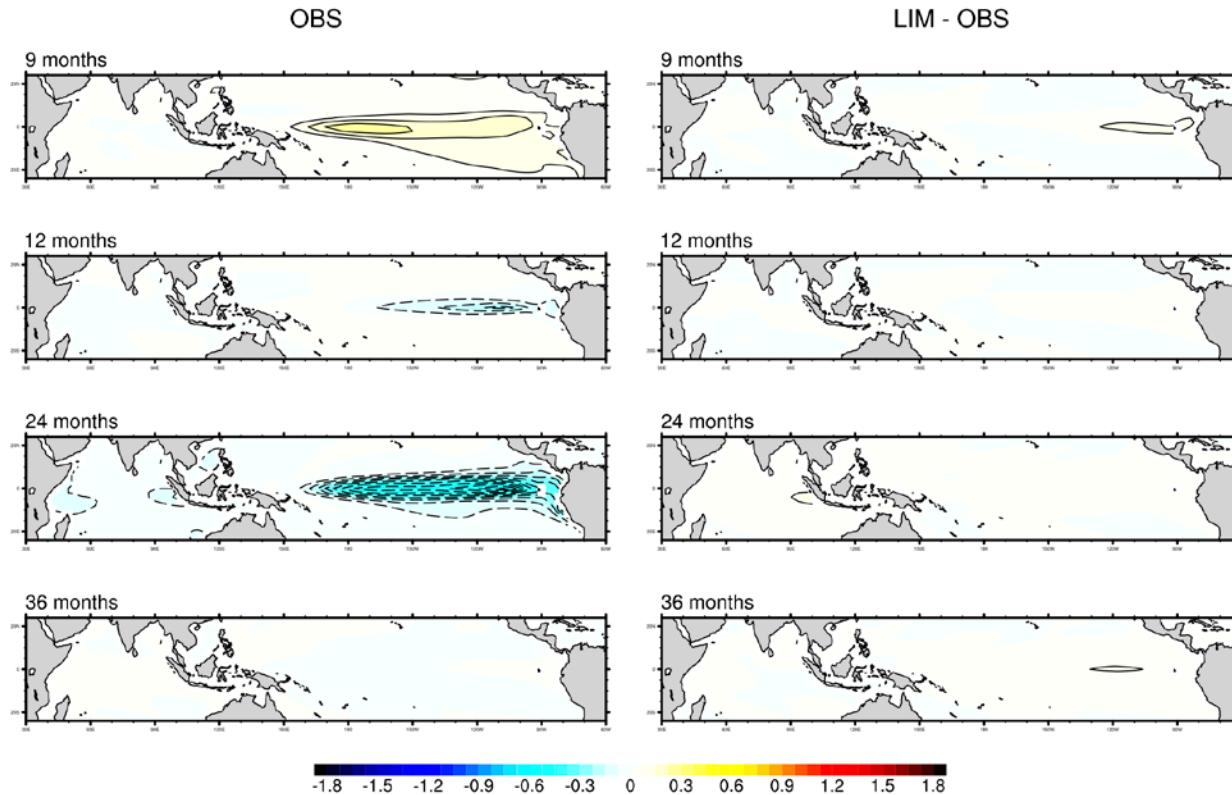
For all four cases, construct LIM from each half of record, use to make “forecasts” for the other half.

Variables are monthly anomalies of SST, Z20, and zonal wind stress.

# Tropical SST variance



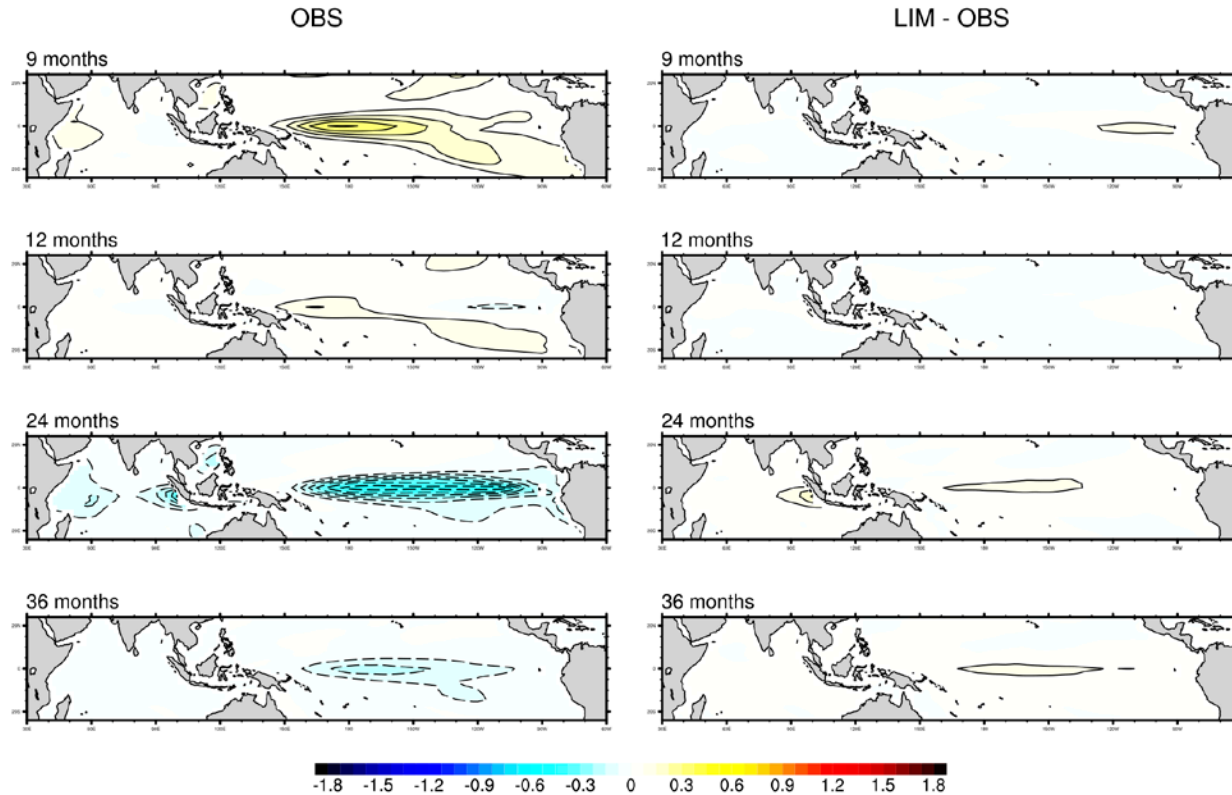
# Test LIM: Tropical SST lag covariance



CCSM4 B1850



# Test LIM: Tropical SST lag covariance

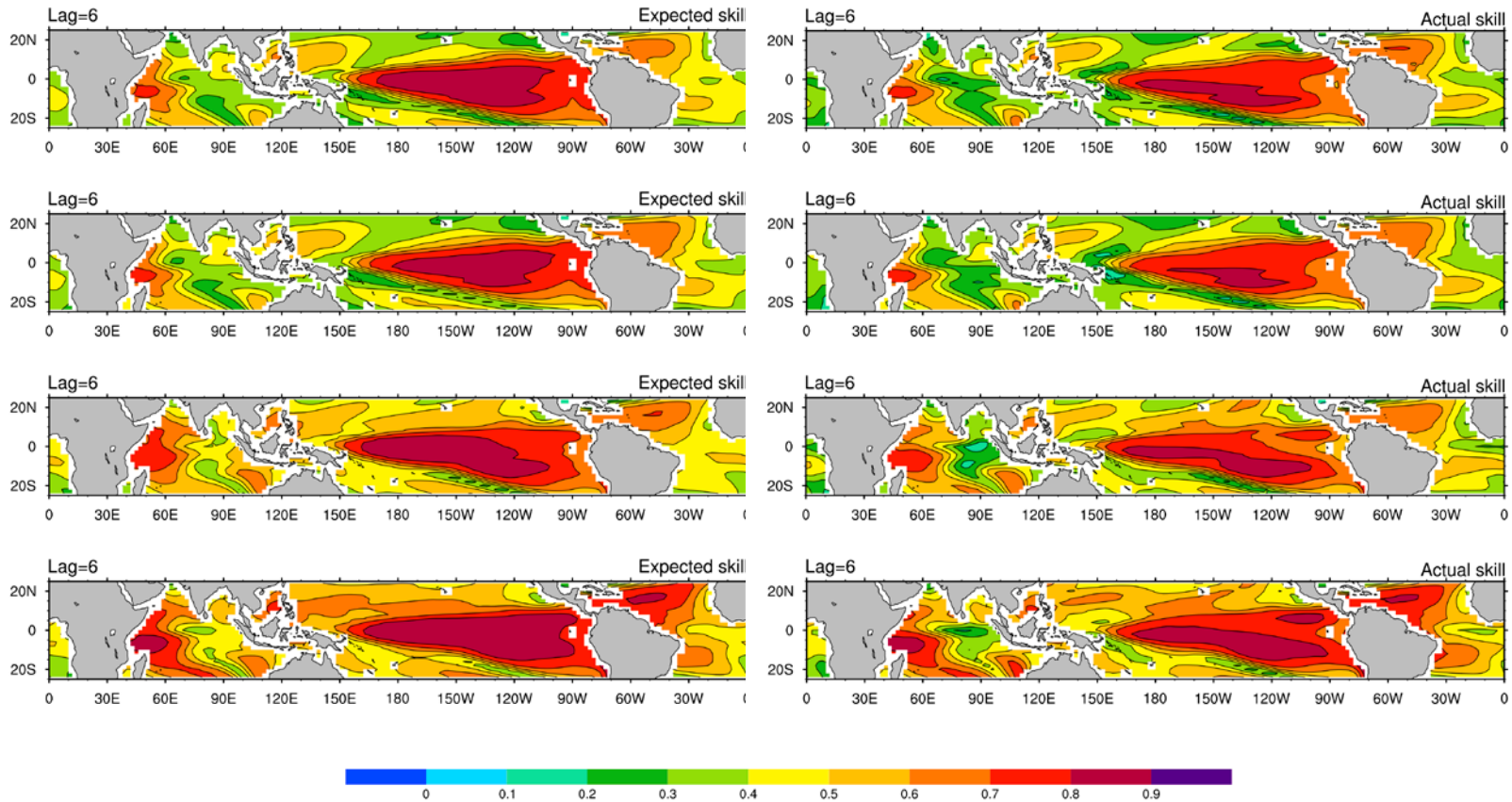


CESM1-CAM5 B1850

# Comparing predicted and actual forecast skill, or: some **places** are more predictable than others

## Predicted Month 6 LIM skill

## Actual Month 6 LIM skill



# Comparing predicted and actual CCSM4 forecast skill

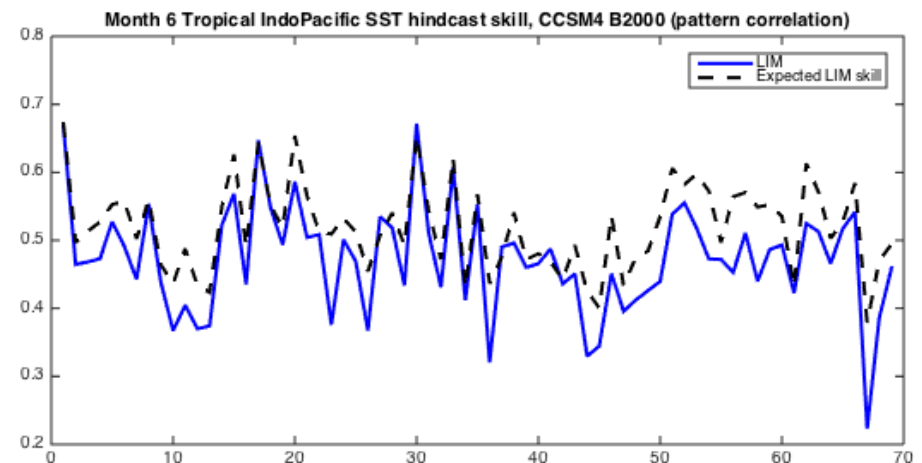
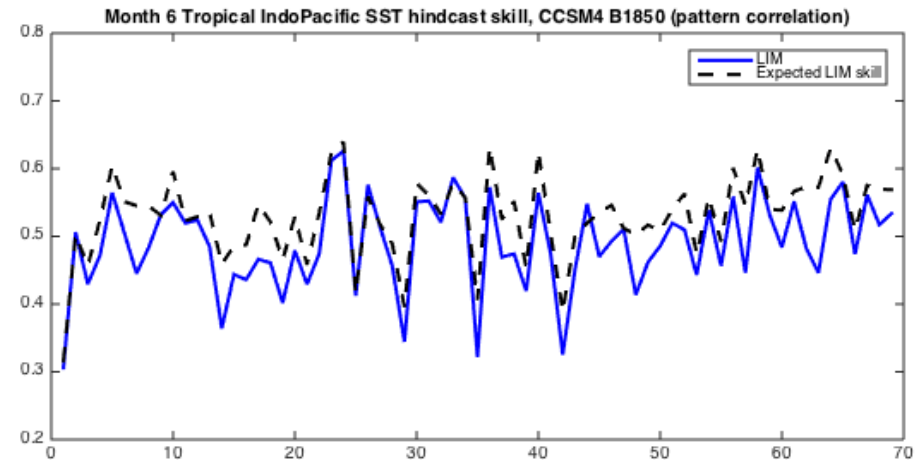
Skill averaged by **decade** (based on initialization date)

**Actual skill:** Pattern correlation of tropical SST anomaly with SST forecast anomaly

Blue: LIM (0.49/0.47)

Predicted:  $\rho_{\infty}$  (0.53/0.52)

LIM skill correlated with  $\rho_{\infty}$  at 0.9



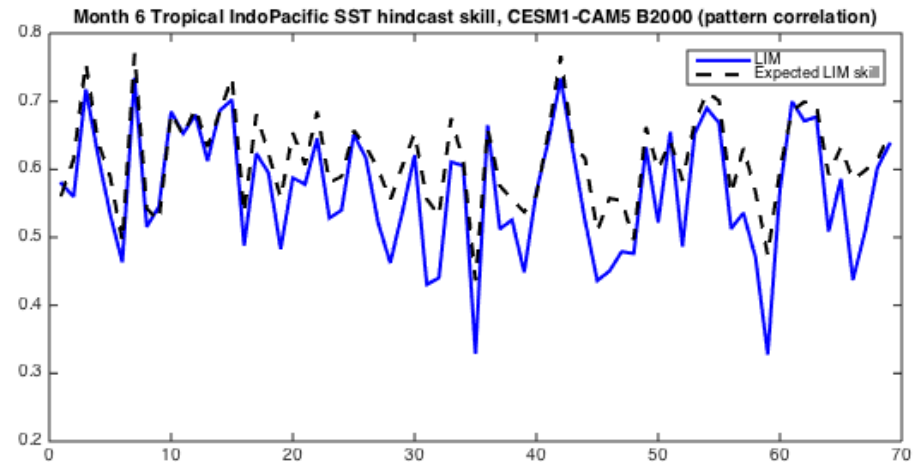
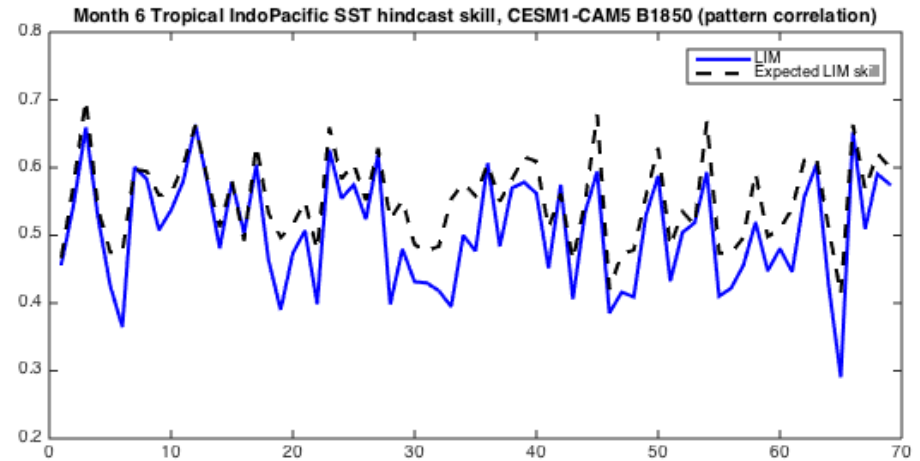
# Comparing predicted and actual forecast skill, or: some **years** are more predictable than others

Skill averaged by decade (based on initialization date)

**Actual skill:** Pattern correlation of tropical SST anomaly with SST forecast anomaly

Blue: LIM (0.51/0.57)  
Predicted:  $\rho_\infty$  (0.55/0.62)

LIM skill correlated with  $\rho_\infty$  at 0.9



# Conclusions

- LIM useful for diagnosis of predictability, **because** its forecast skill is comparable with coupled GCMs and it reproduces observed spatio-temporal statistics
- To use coupled CGMs to investigate changes in ENSO and its predictability we first need to gauge **how well do they reproduce observed ENSO dynamics**
- **Year-to-year variations in forecast skill** in the last few decades may be **due to random variations in initial conditions** and not necessarily to long-term “base state” changes
- Even if “base state” changes drive variations in forecast skill, these may be swamped by random variations in initial conditions