

Estimating the Role of Natural Variability in Climate Change Using Observations

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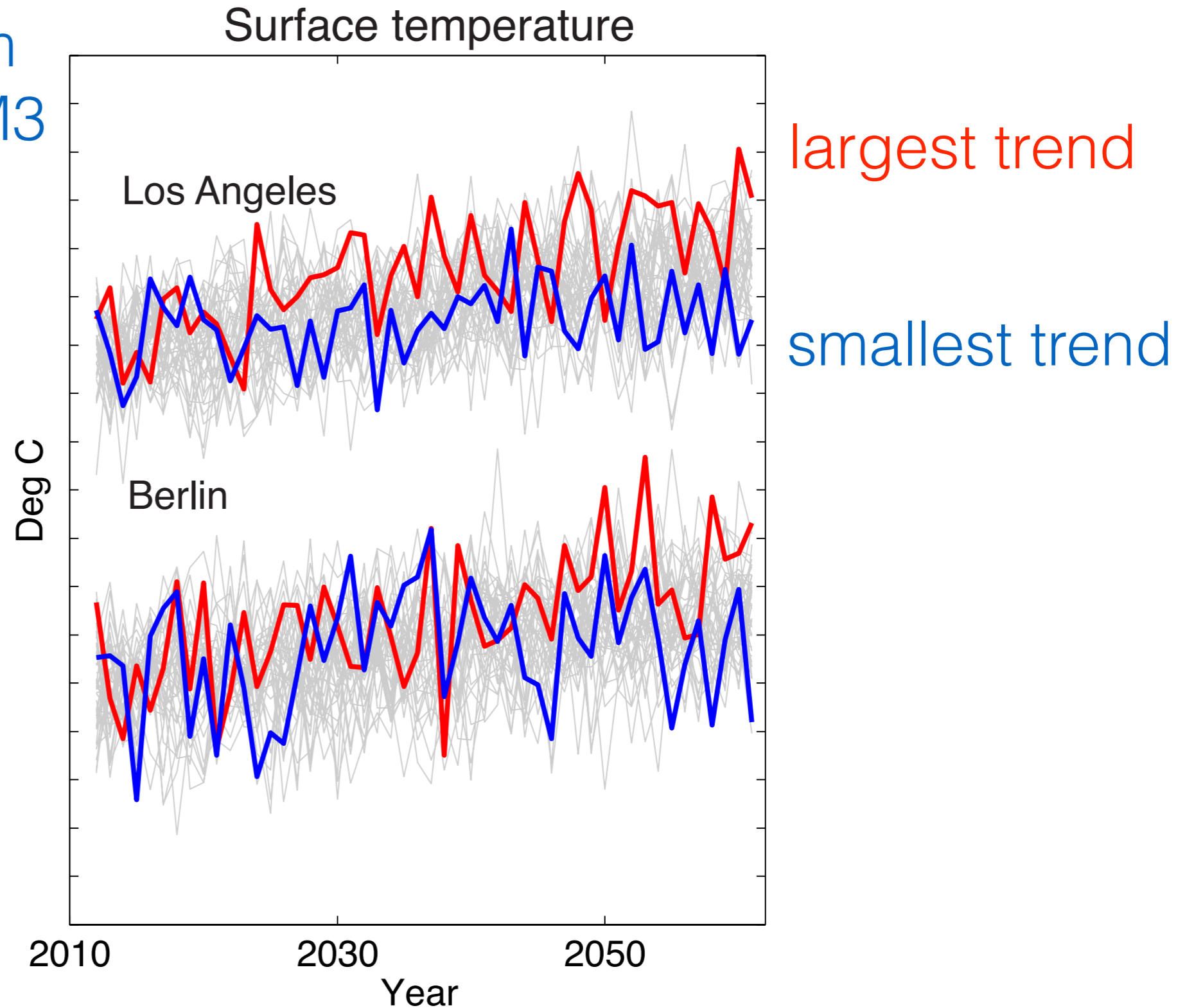
William E. Foust (CSU)

Adam S. Phillips (NCAR)

results drawing from:

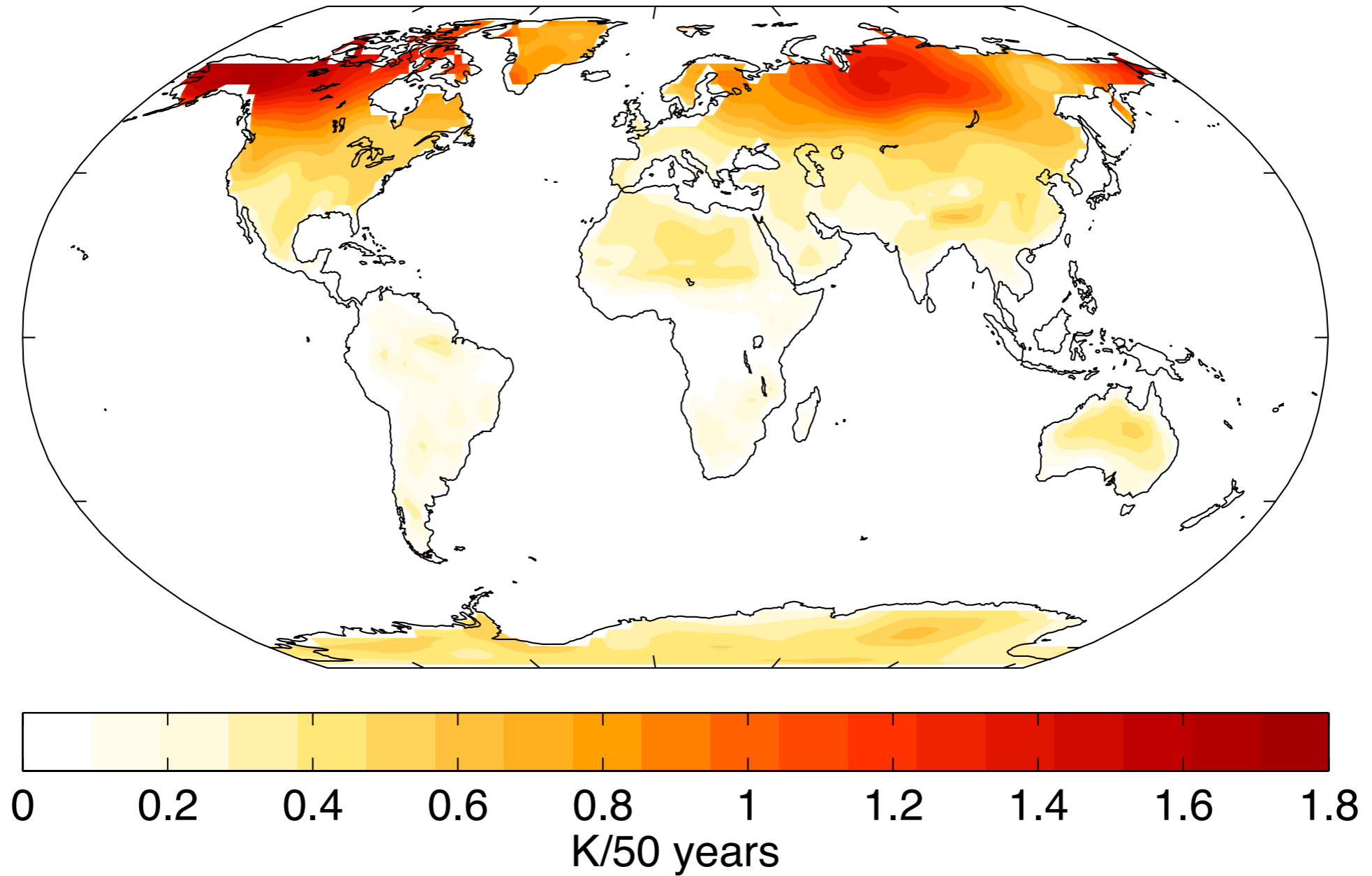
- Thompson et al. (submitted to Journal of Climate)
see www.atmos.colostate.edu/~davet

Time series of near surface temperature from the NCAR CCSM3 40-member ensemble.



Ticks at 1 deg.

Standard deviations of 50-year trends Surface temperature



Range of trends from all 40 ensemble members during
October-March.

- What determines the range of trends indicated by the large ensemble?
- Can the range in climate trends be accurately estimated from a *control simulation*?
- Can the range in the trends be accurately estimated from *observations*?

An analytic expression for the margins of error in a Gaussian process.

Consider a time series $\mathbf{x}(t)$ with mean zero and linear least-squares trend \mathbf{b} .

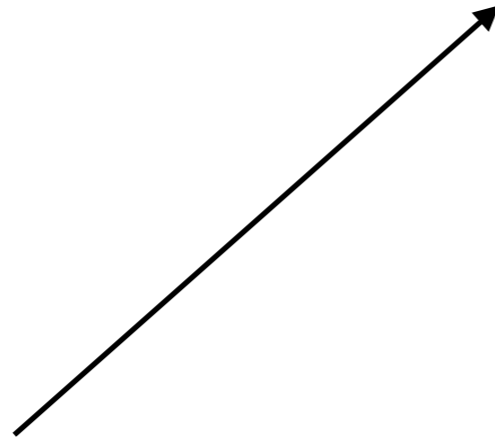
The confidence interval on the trend in $x(t)$ can be expressed as:

$$CI = b \pm e$$

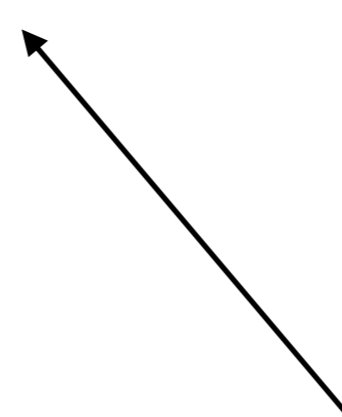
Where \mathbf{e} is the margin of error on the trend.

If the distribution of the deviations in $x(t)$ about its linear trend is Gaussian, then the margin of error on the trend in $x(t)$ is:

$$e = t_c s_b$$



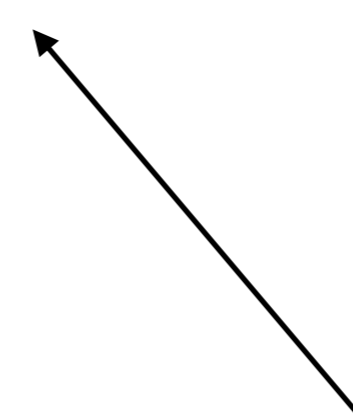
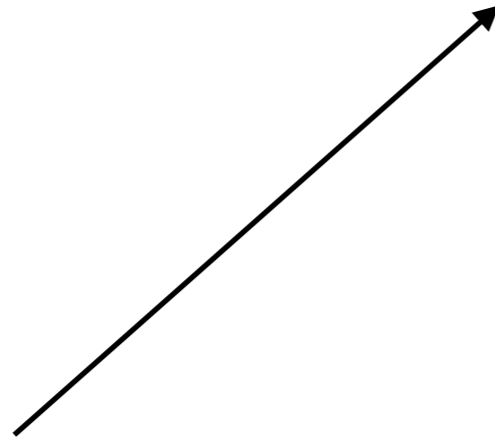
desired confidence level



standard error of the trend.

If the distribution of the deviations in $x(t)$ about its linear trend is Gaussian, then the margin of error on the trend in $x(t)$ is:

$$e = t_c s_b$$



desired confidence level

standard error of the trend.

$$s_b = \frac{n_t s_e}{\sqrt{\sum_{i=1}^{n_t} (i - \bar{i})^2}}$$

After some algebra...

length of the record

*standard deviation
of the residuals*

$$e = t_c \cdot n_t \cdot \sigma \cdot \gamma(n_t, r_1) \cdot g(n_t)$$

*scaling factor
to account for
autocorrelation*

*arises from variance
of the time axis*

$$\gamma(n_t, r_1) \equiv \left(\frac{[n_t - 2]}{\left[n_t \left(\frac{1 - r_1}{1 + r_1} \right) - 2 \right]} \right)^{1/2}$$

$$g(n_t) \equiv \sqrt{\frac{12}{n_t^3 - n_t}}$$

The margin of error on a trend in a Gaussian process is a function of three statistics:

- 1) the standard deviation of the internal (unforced) variability.
- 2) the lag-one autocorrelation of the internal (unforced) variability.
- 3) the number of time steps in the time series.

If the residuals are serially uncorrelated and the trend is 50 time steps, then:

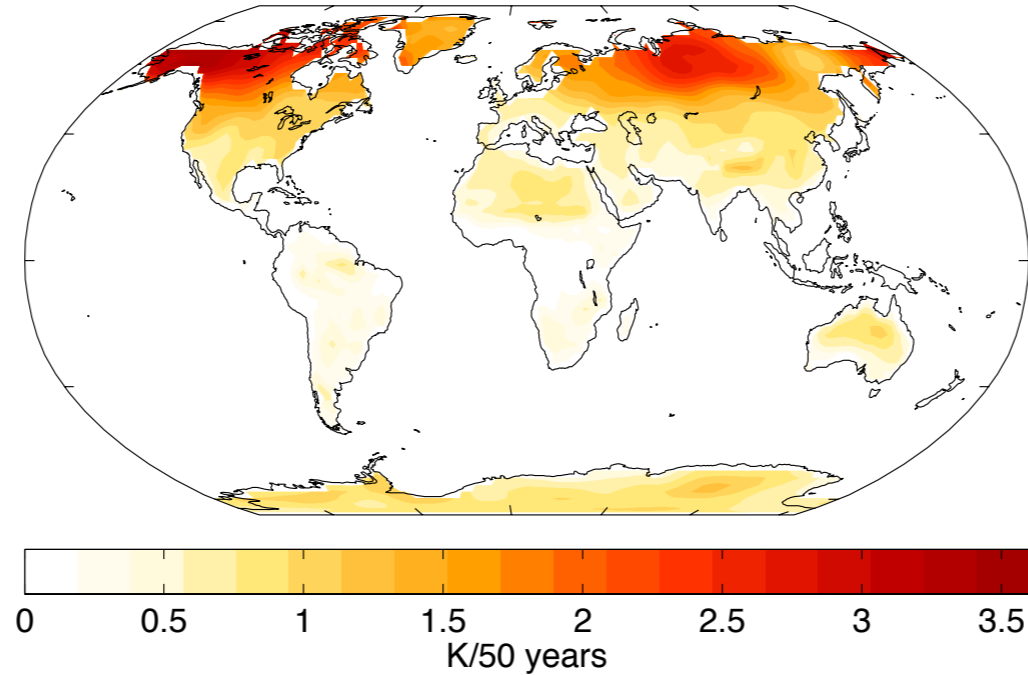
$$e_{95\%} \sim \sigma \text{ (for } n_t = 50 \text{ and } r_1 \sim 0 \text{)}$$

*95% margin of error
on 50 year trend*

interannual standard deviation

... testing the analytic model in the NCAR CCSM3 large ensemble

“Actual” 95% margin of error on trends
(from 40 ensemble members)

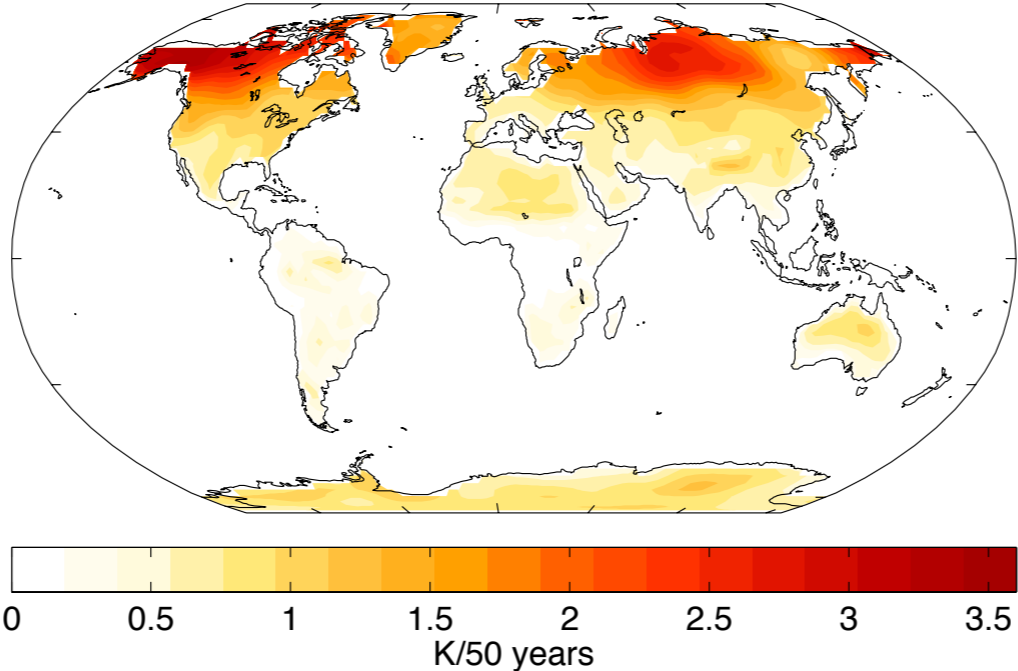


50 year trends in Oct-March surface temperature

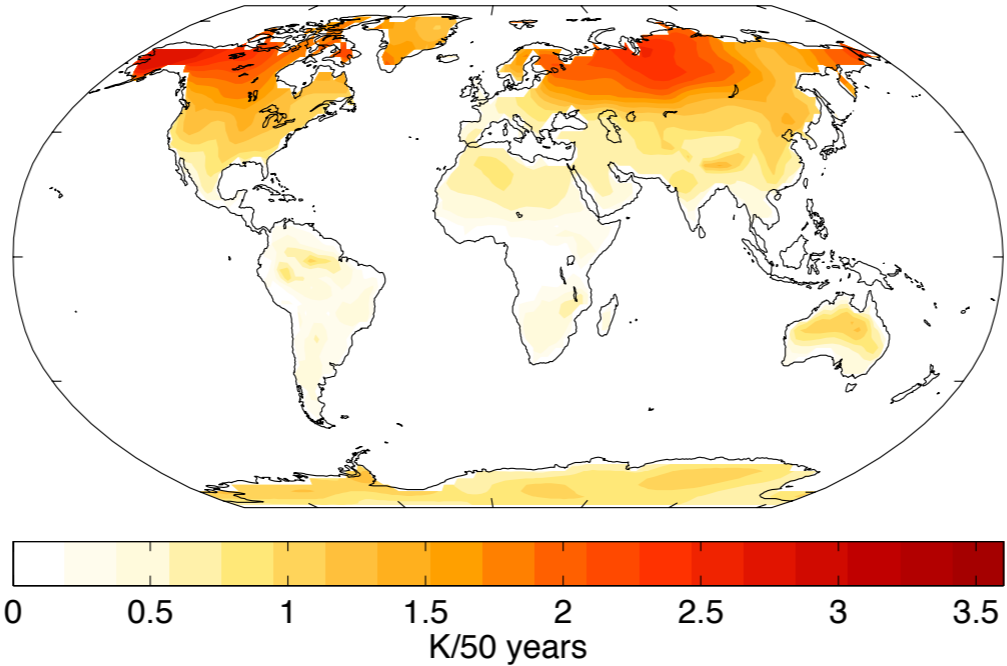
From Thompson et al. 2015

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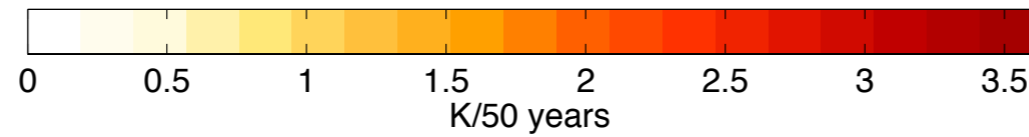
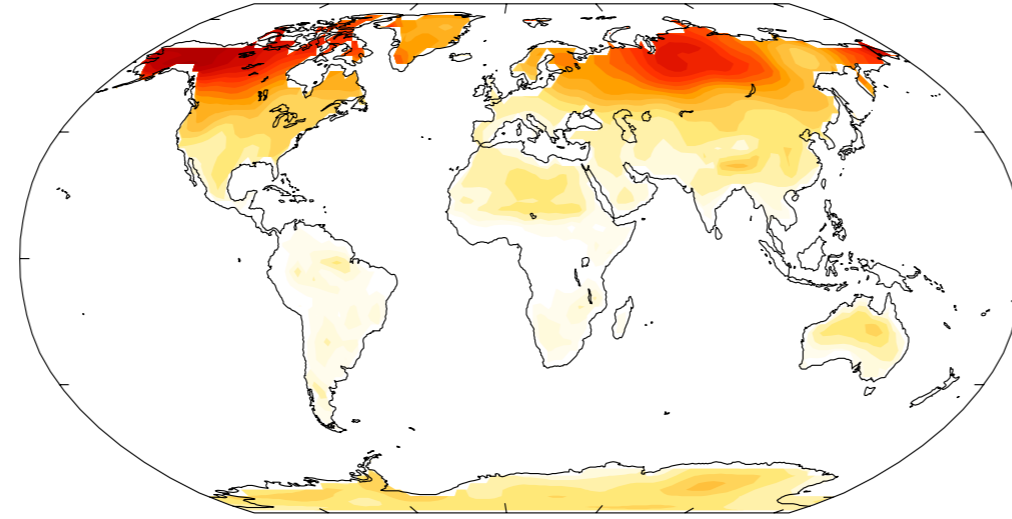
“Predicted” 95% margin of error
(from interannual standard deviation of control run)



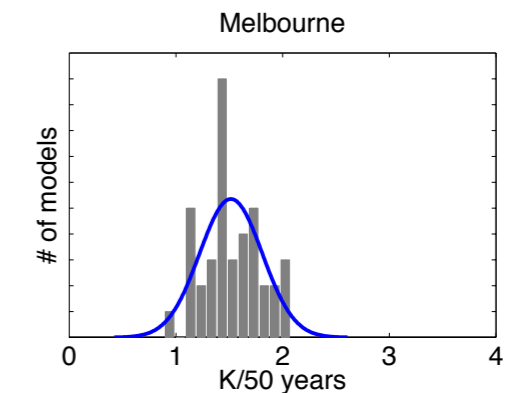
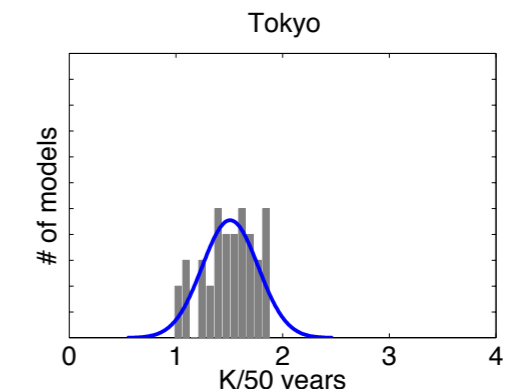
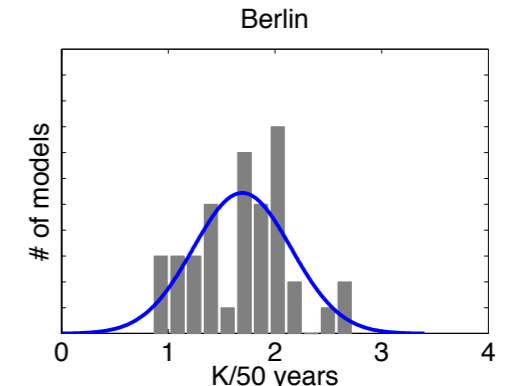
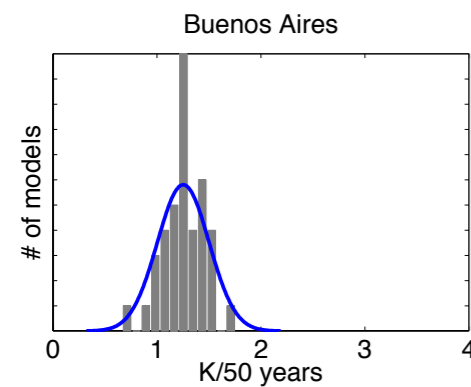
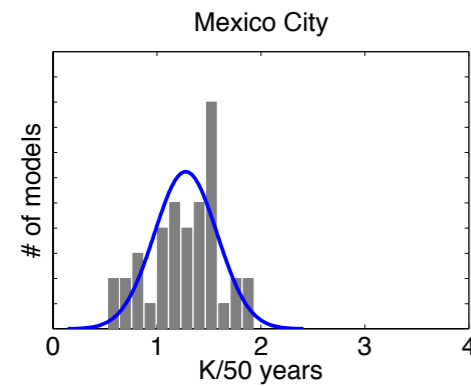
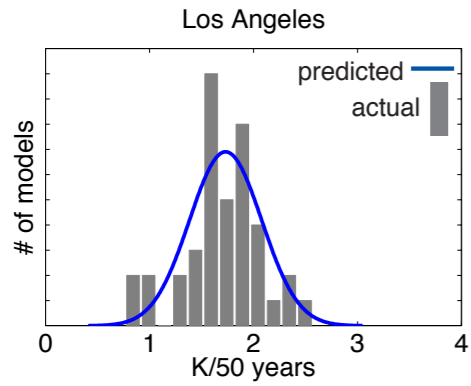
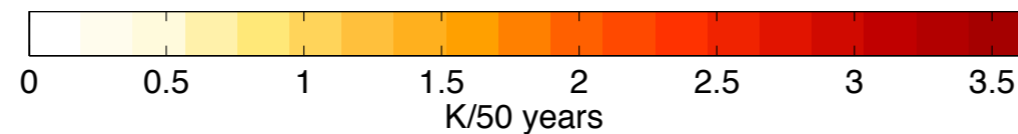
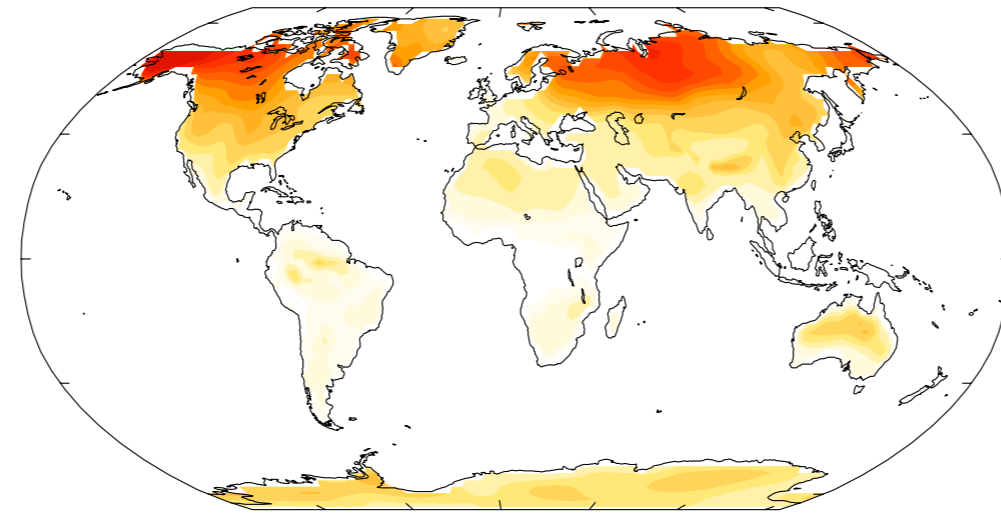
50 year trends in Oct-March surface temperature

... testing the analytic model in the NCAR CCSM3 large ensemble

“Actual” 95% margin of error on trends
(from 40 ensemble members)



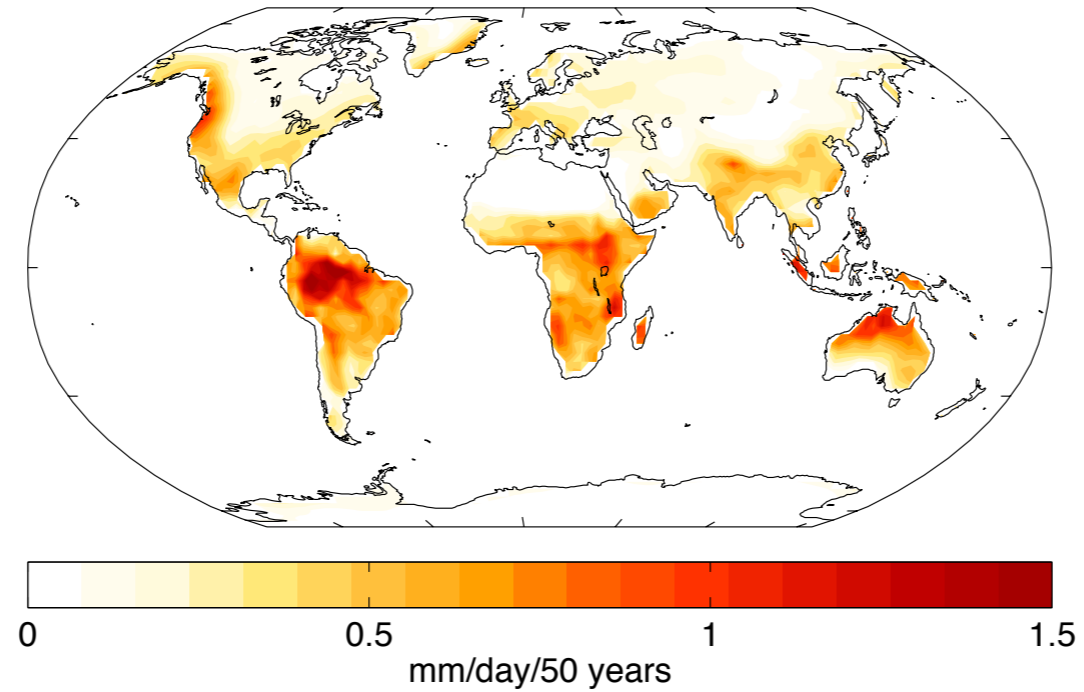
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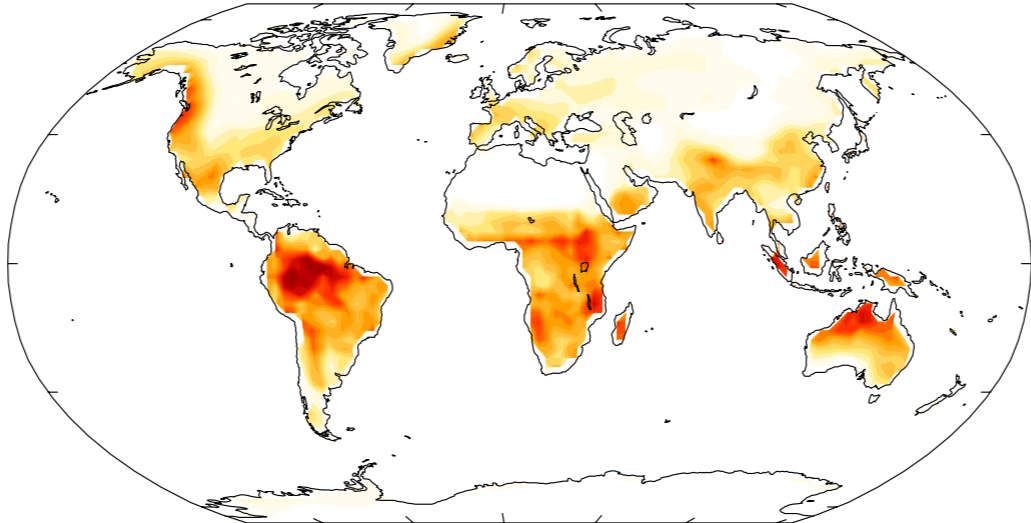
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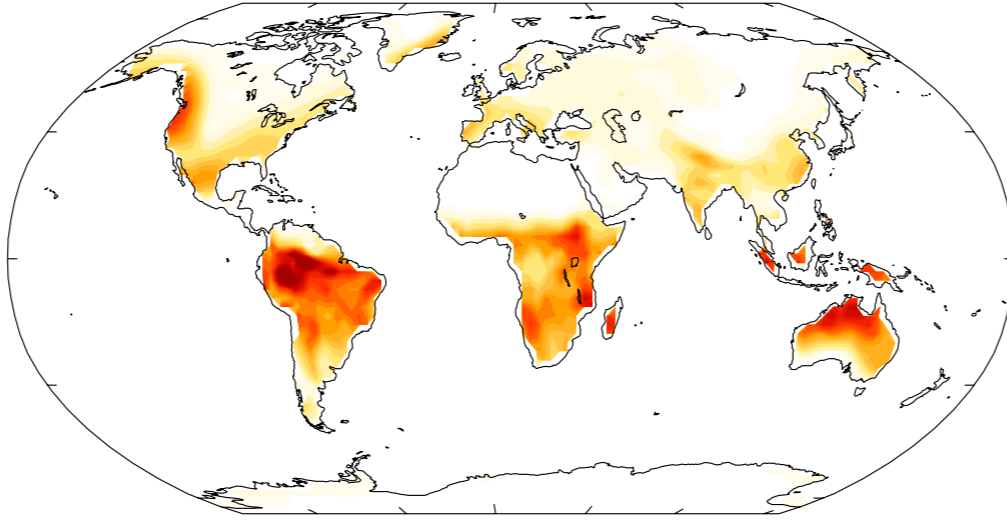
50 year trends in Oct-March precipitation *From Thompson et al. 2015*

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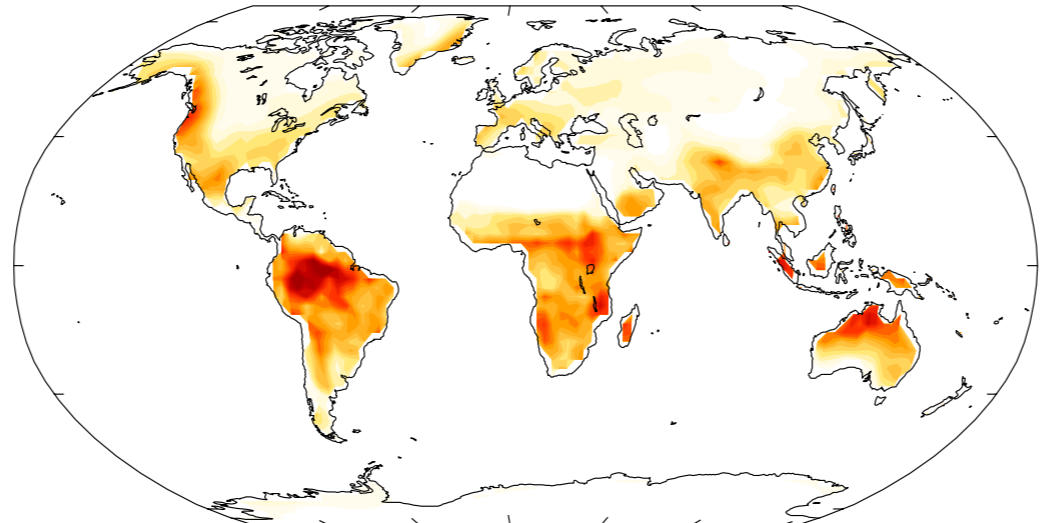
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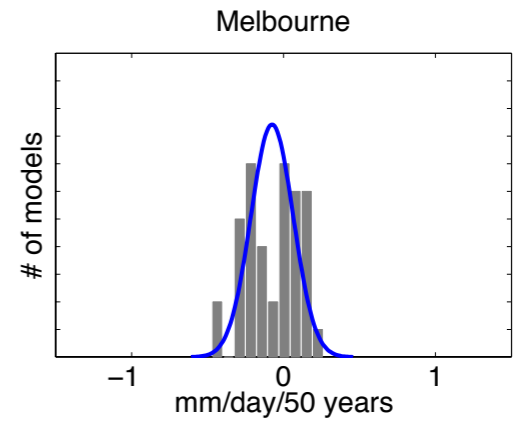
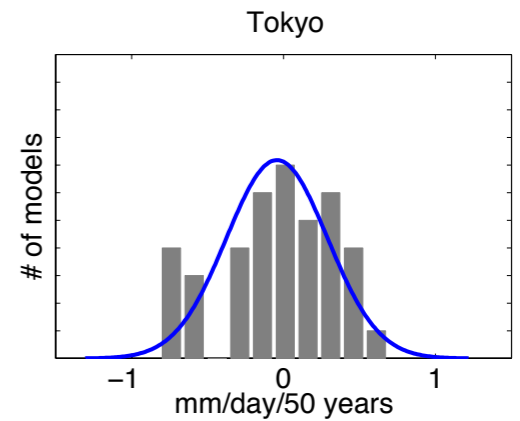
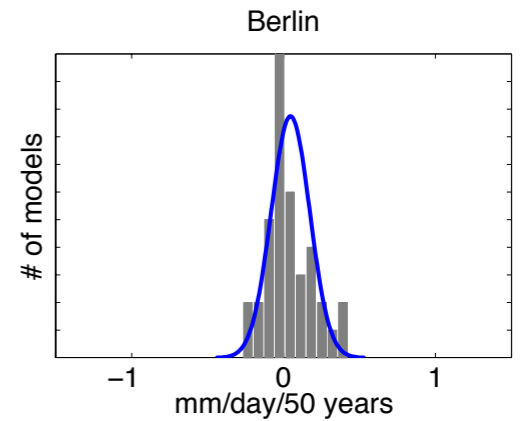
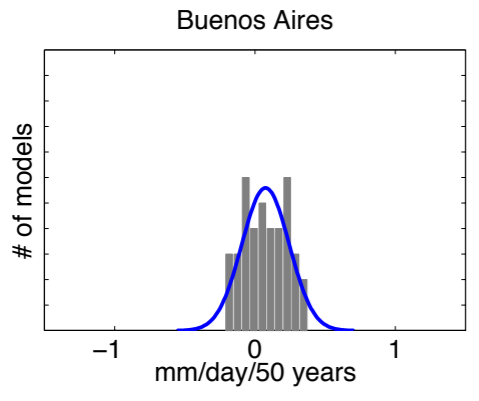
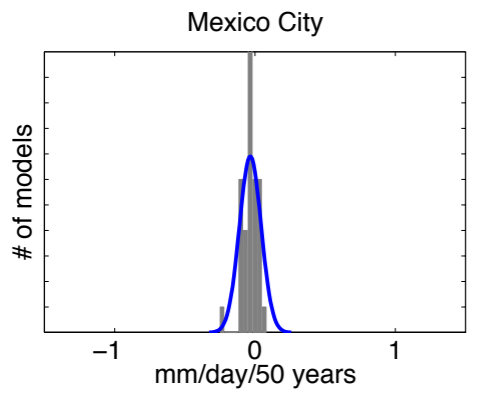
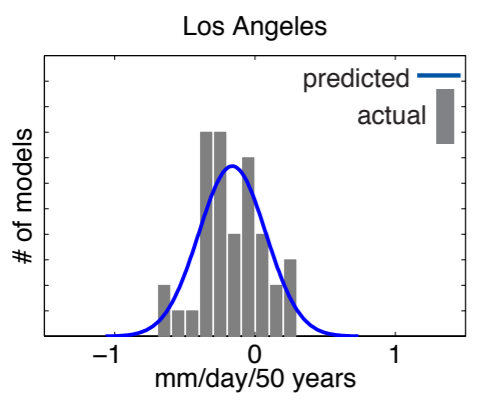
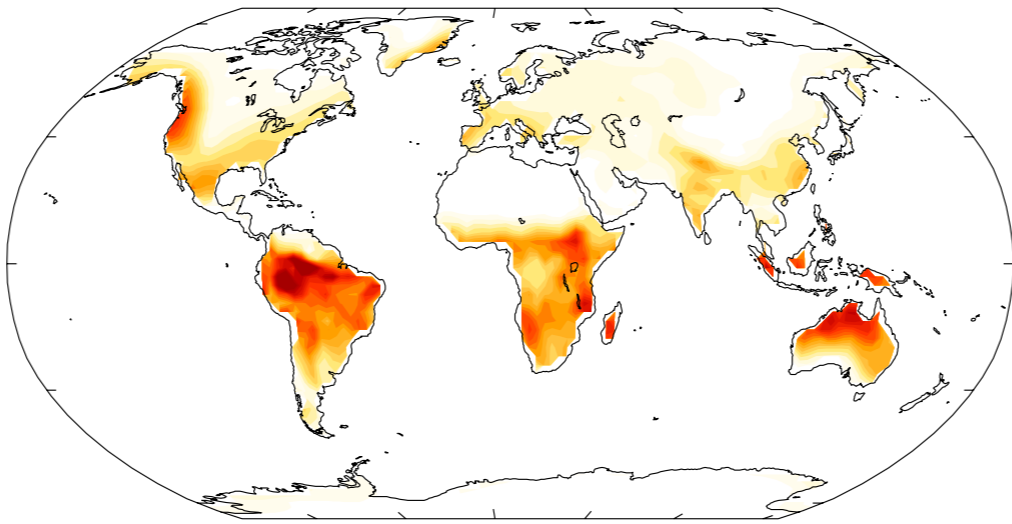
50 year trends in Oct-March precipitation

... testing the analytic model in the NCAR CCSM3 large ensemble

“Actual” 95% margin of error on trends
(from 40 ensemble members)



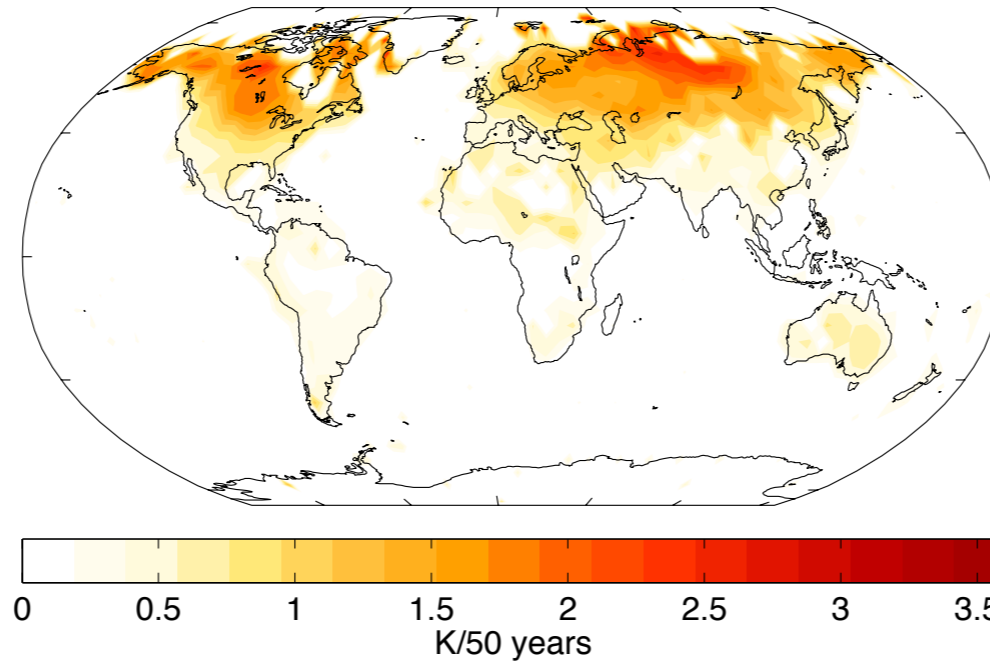
“Predicted” 95% margin of error
(from interannual standard deviation of control run)



50 year trends in Oct-March precipitation

... applying the analytic model to observations

“Predicted” 95% margin of error
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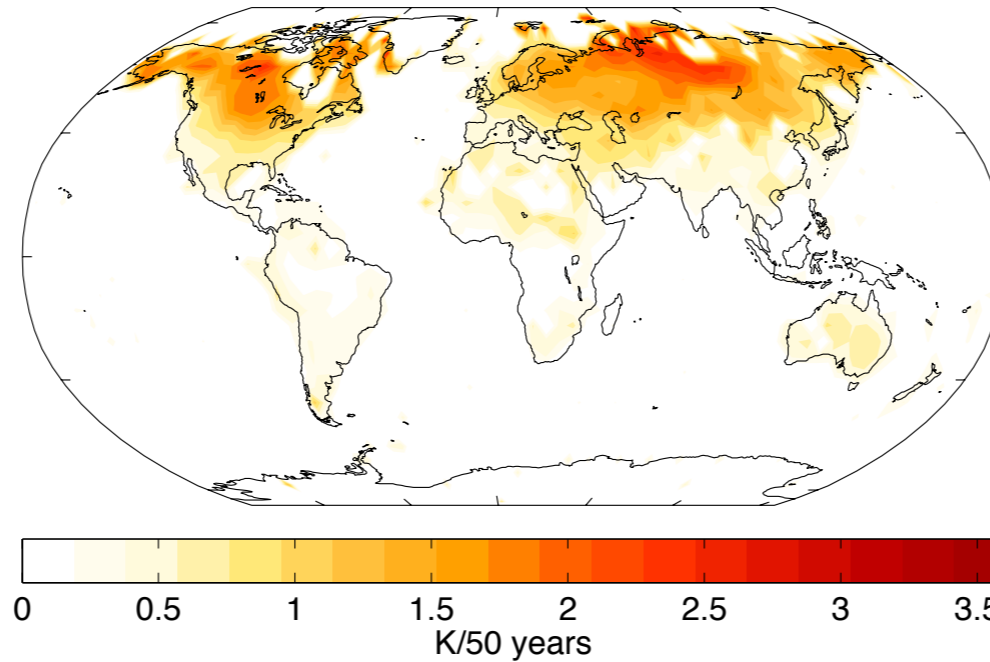
Observations from CRU

From Thompson et al. 2015

Predicted uncertainty in Oct-March surface temperature trends

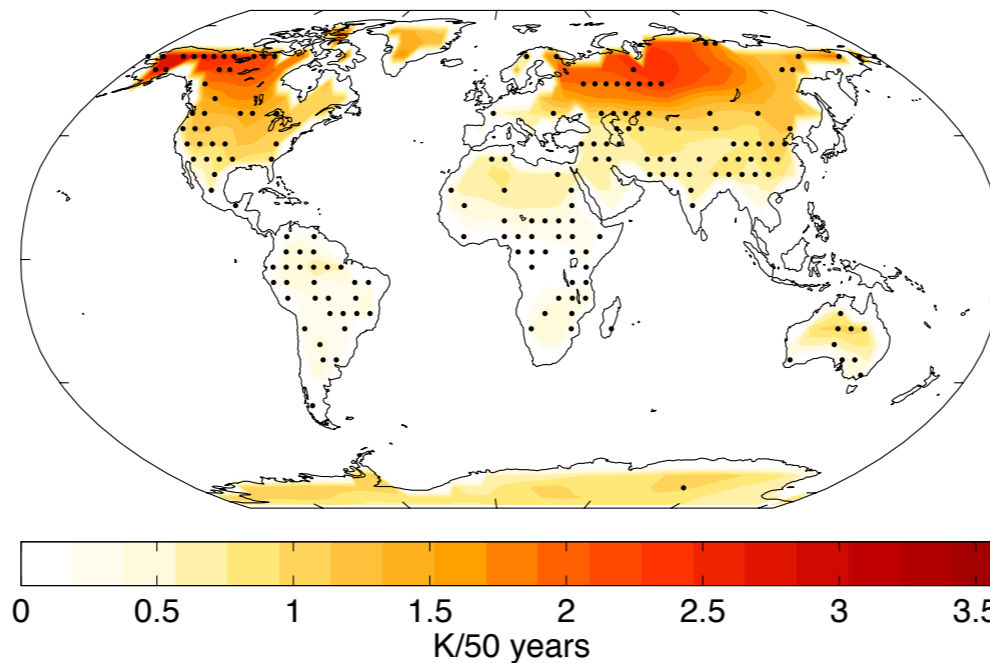
... applying the analytic model to observations

“Predicted” 95% margin of error
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Observations from CRU

“Predicted” 95% margin of error
(from interannual standard deviation of control run)

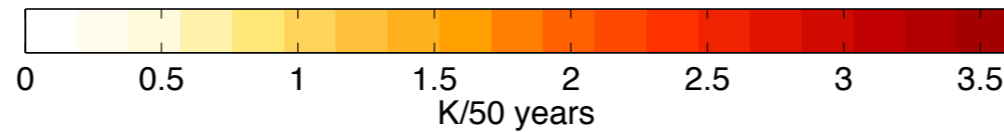
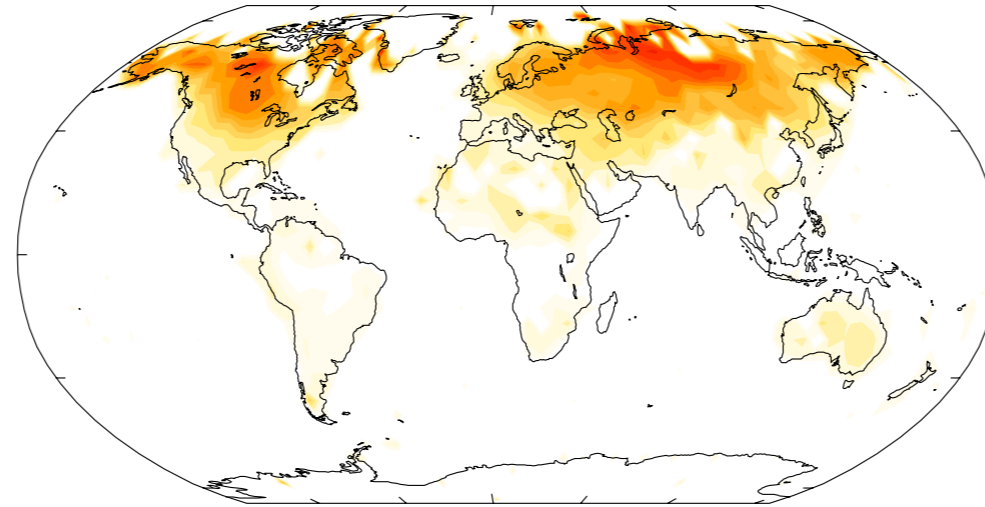


Control simulation

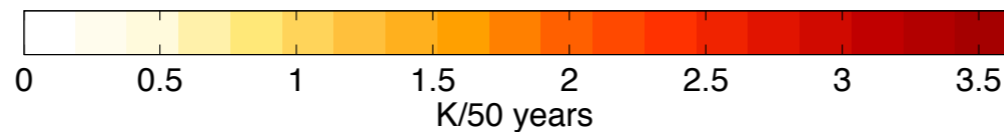
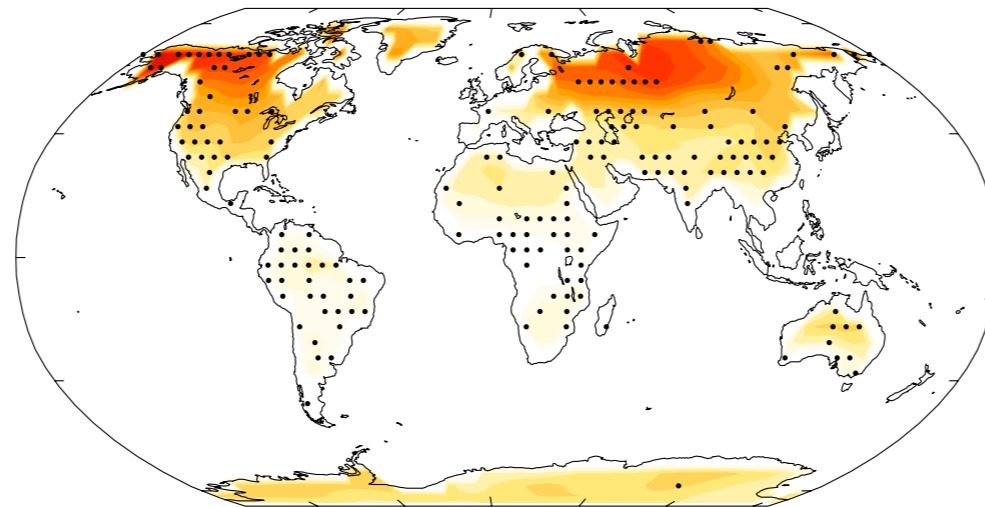
Predicted uncertainty in Oct-March surface temperature trends

... applying the analytic model to observations

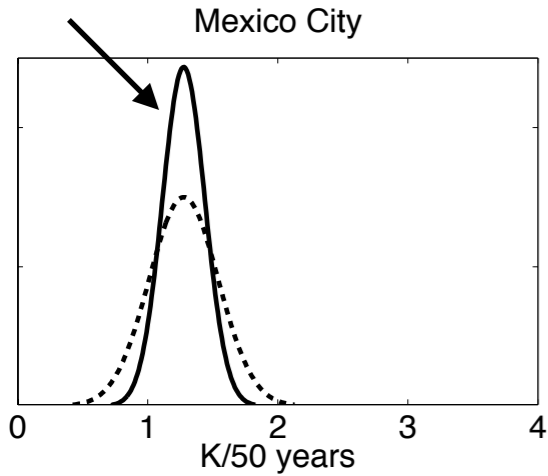
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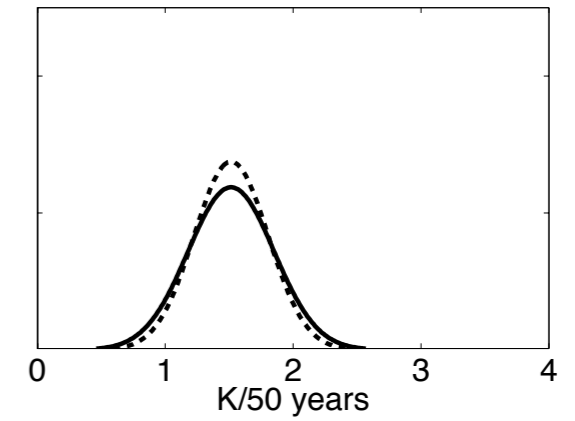
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Observations from CRU



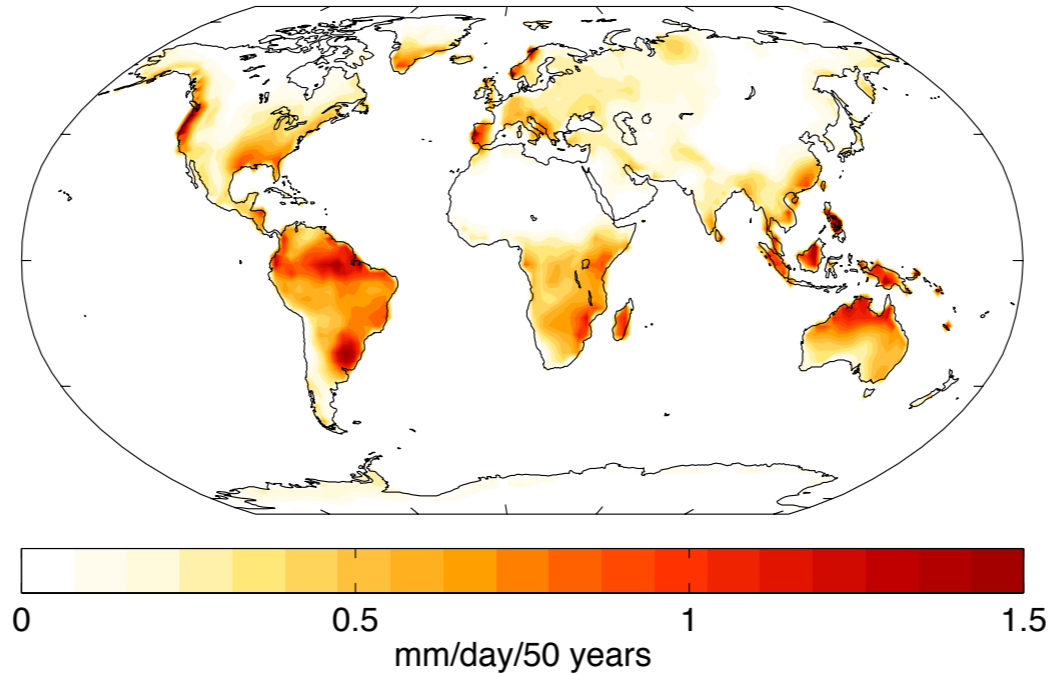
Melbourne



Predicted uncertainty in Oct-March surface temperature trends

... applying the analytic model to observations

“Predicted” 95% margin of error
(from interannual standard deviation of observations)



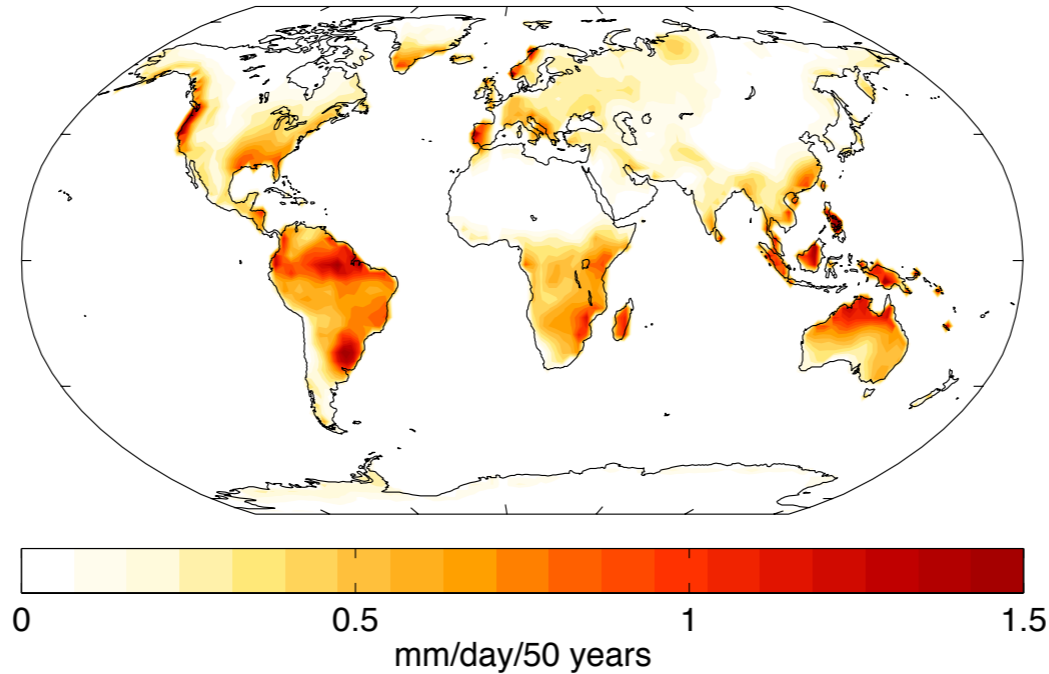
Observations from GPCP

From Thompson et al. 2015

Predicted uncertainty in Oct-March precipitation trends

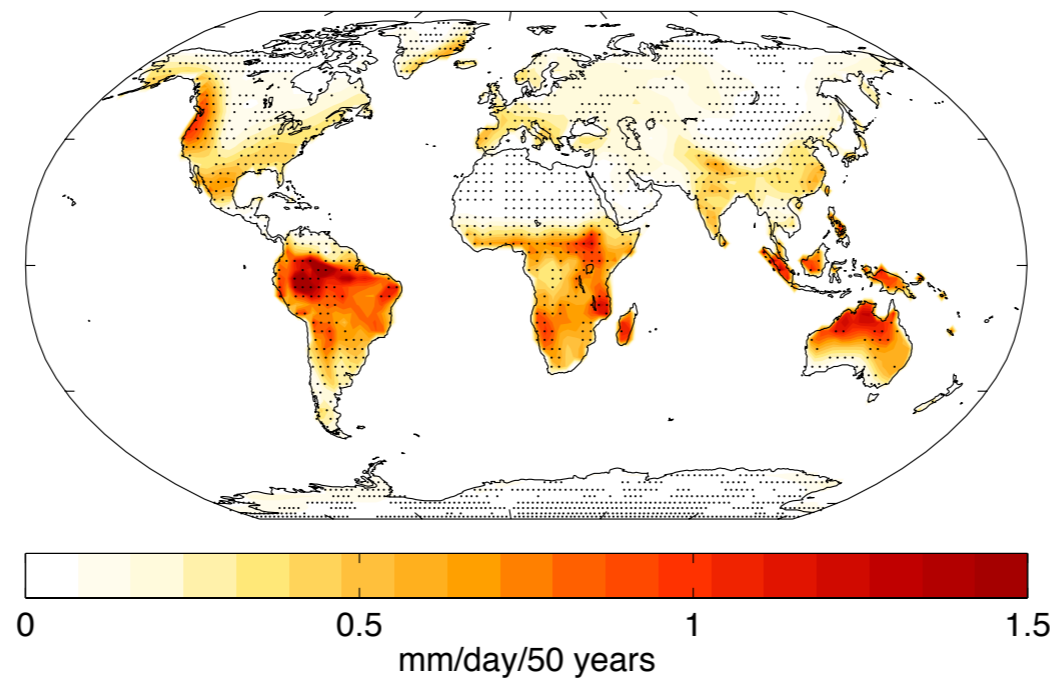
... applying the analytic model to observations

“Predicted” 95% margin of error
(from interannual standard deviation of observations)



Observations from GPCP

“Predicted” 95% margin of error
(from interannual standard deviation of control run)

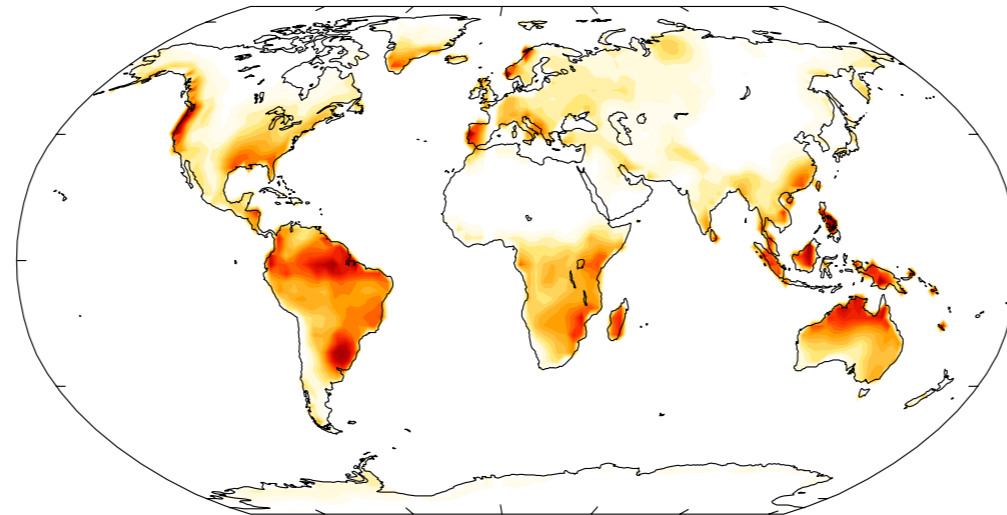


Control simulation

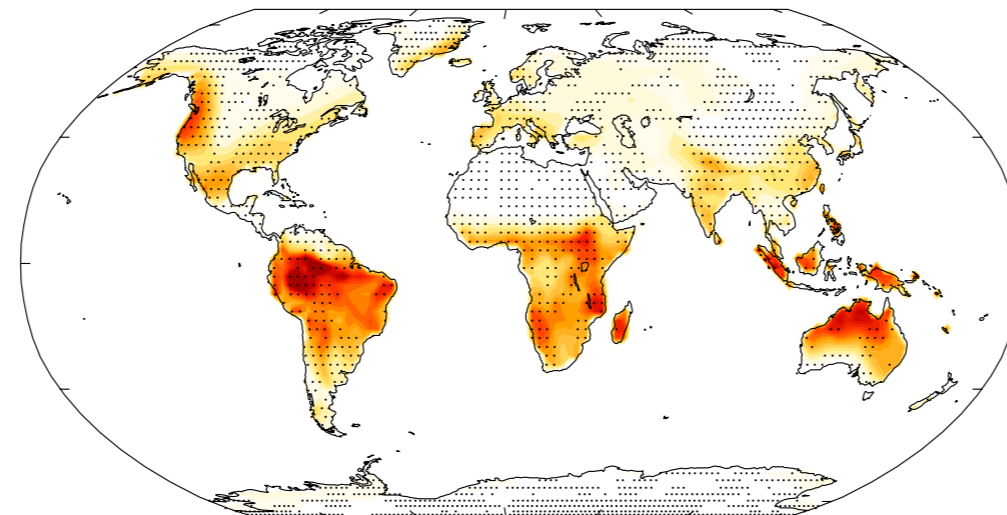
Predicted uncertainty in Oct-March precipitation trends

... applying the analytic model to observations

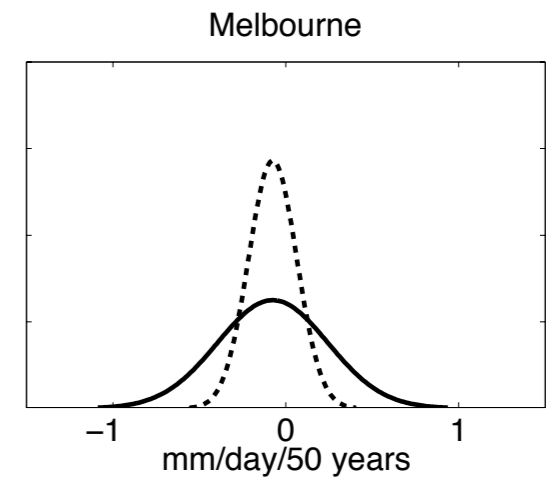
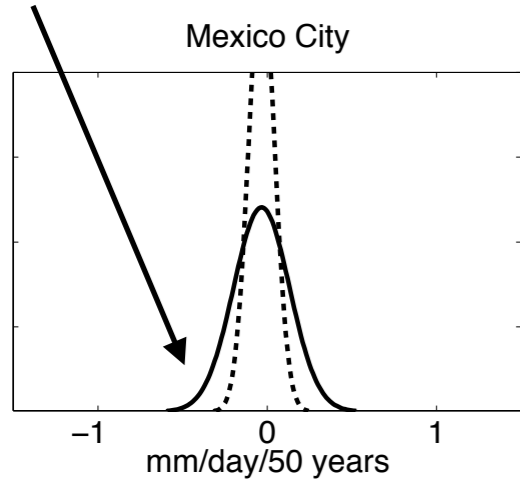
“Predicted” 95% margin of error
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“Predicted” 95% margin of error
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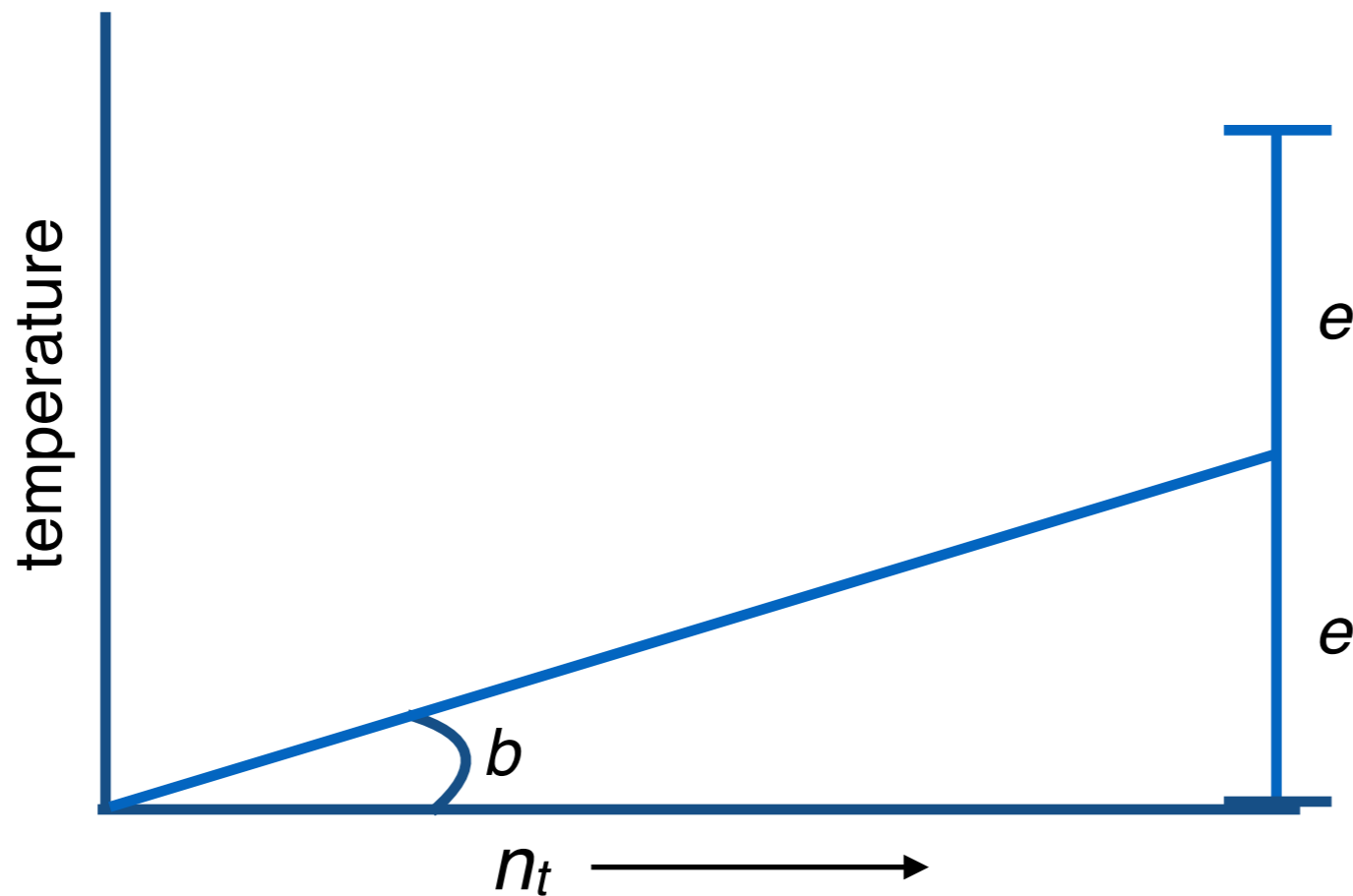


Observations from GPCP



Predicted uncertainty in Oct-March precipitation trends

Time of emergence / when is a trend significant?

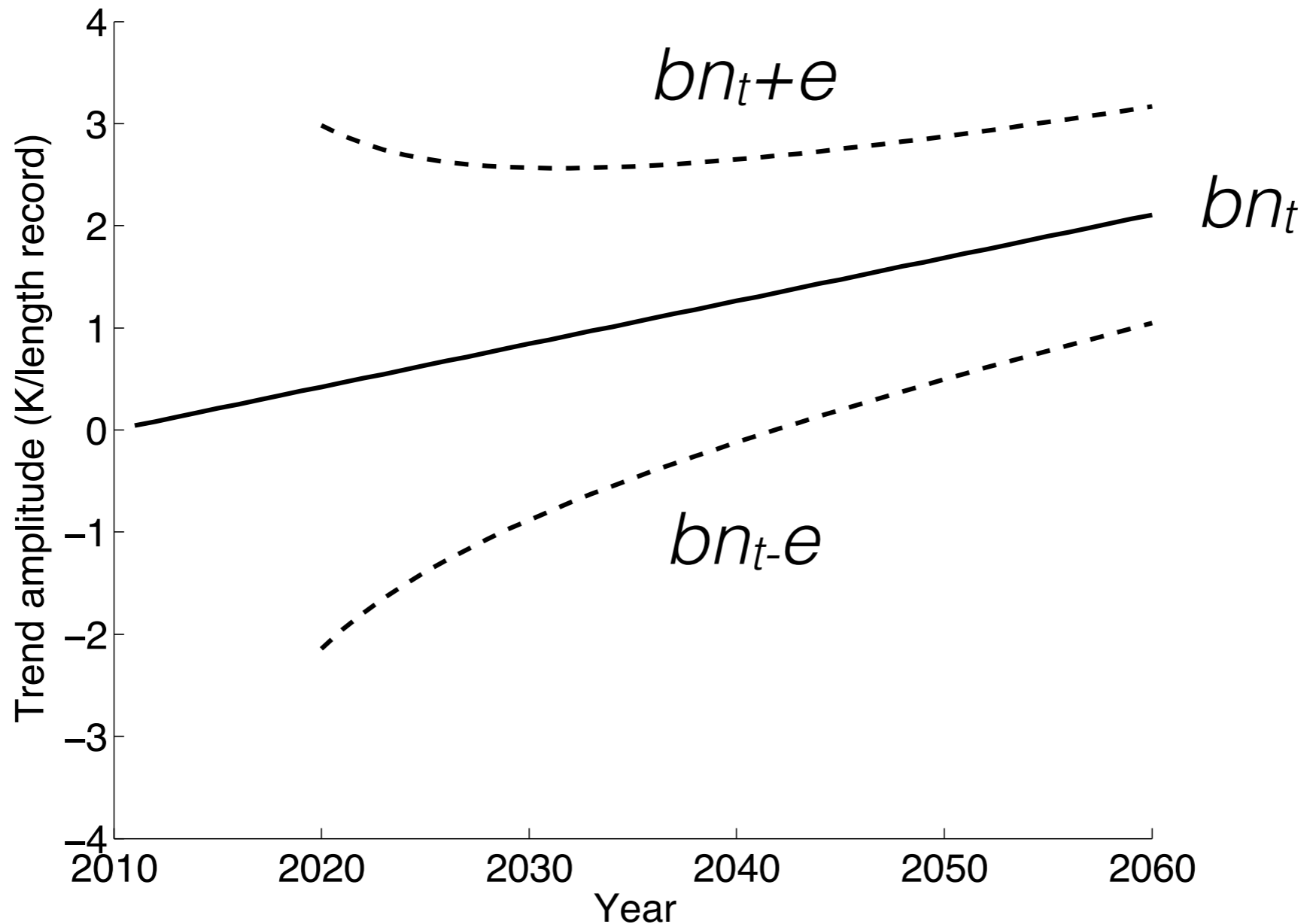


set $e = bn_t$ and solve for n_t

for seasonal-mean data
and $n_t \gtrsim 10$:

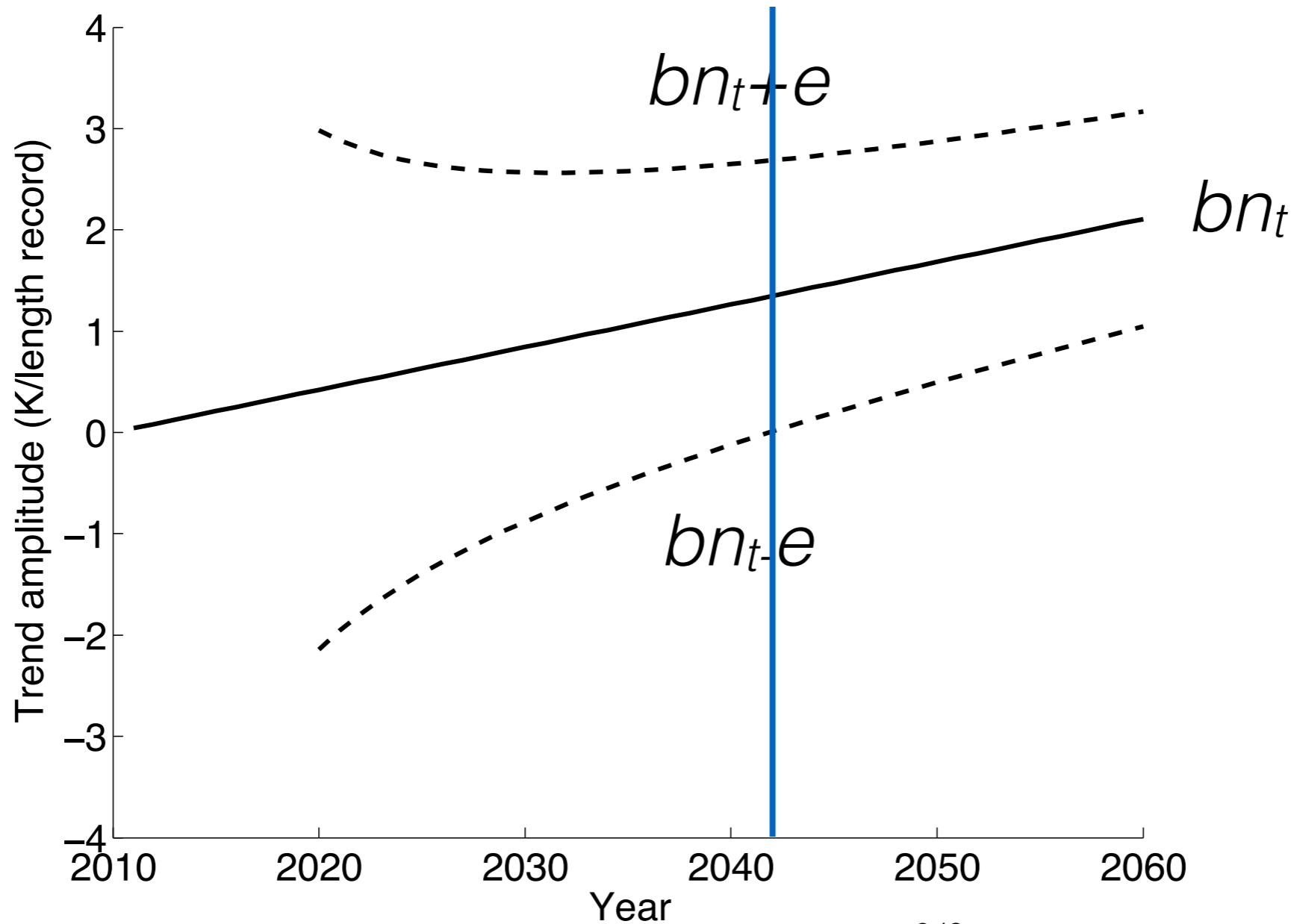
$$n_t = 12^{1/3} \left(\frac{t_c \sigma}{b} \right)^{2/3}$$

Chicago wintertime



- bn_t is the ensemble mean trend (the forced response)
- e is the uncertainty predicted by control

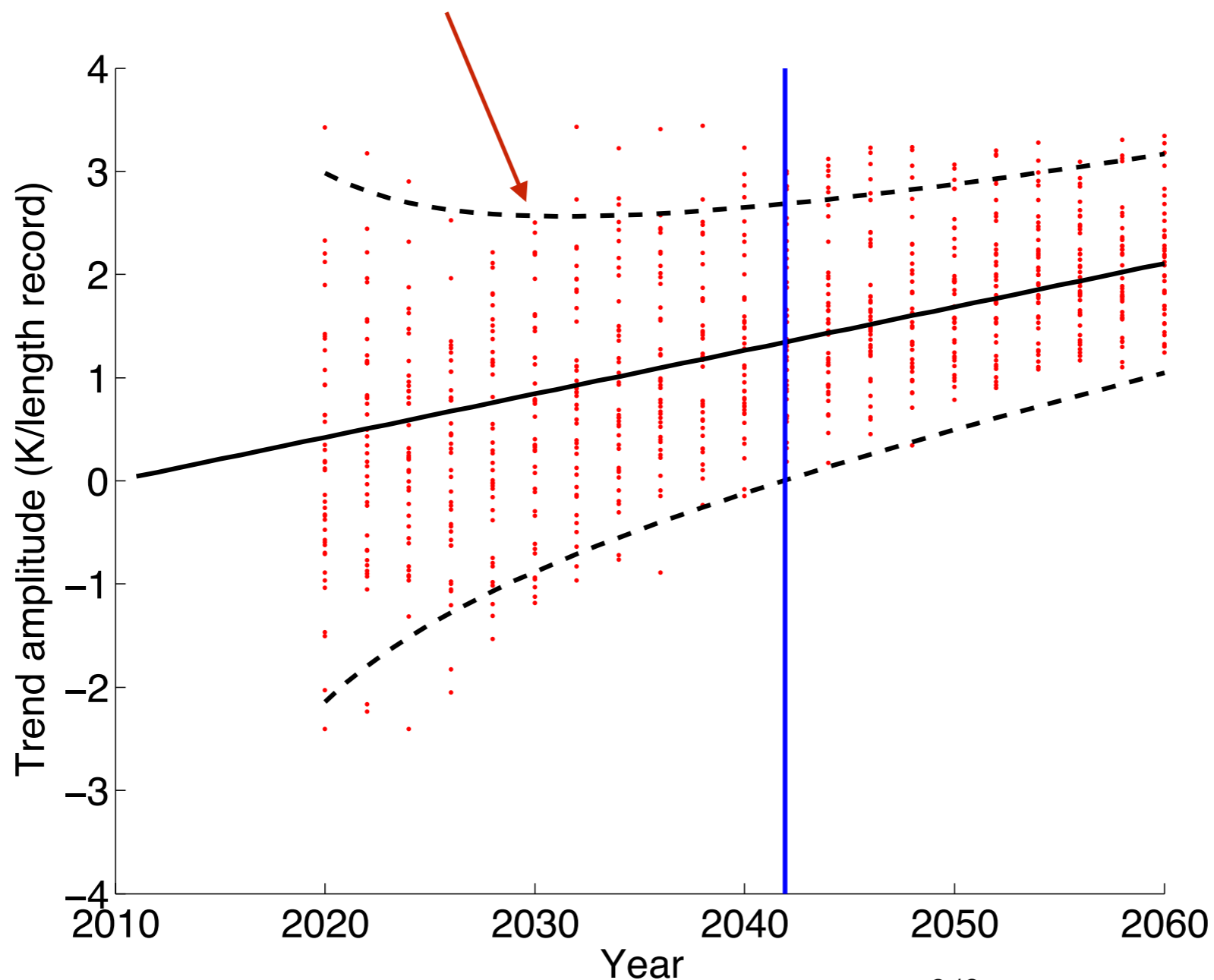
Chicago wintertime



$$n_t = 12^{1/3} \left(\frac{t_c \sigma}{b} \right)^{2/3}$$

n_t denotes the time step when 95% of the ensemble members (i.e., realizations of the real world) exceed a trend of 0.

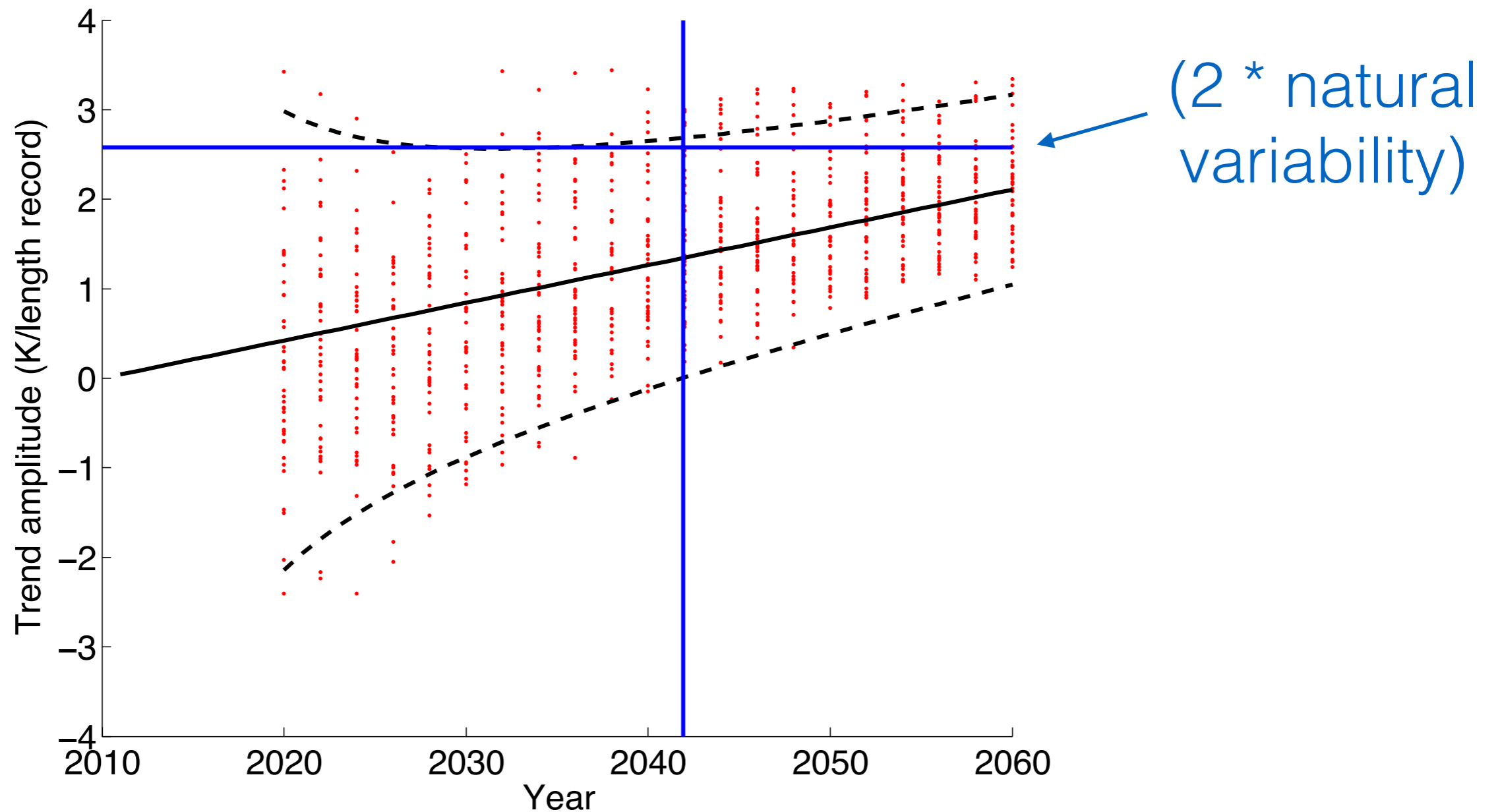
trends from individual ensemble members



$$n_t = 12^{1/3} \left(\frac{t_c \sigma}{b} \right)^{2/3}$$

n_t denotes the time step when 95% of the ensemble members (i.e., realizations of the real world) exceed a trend of 0.

Comparison with the time of emergence



the “time of emergence” given by an individual ensemble member does not:

- 1) correspond to the time step when the forced signal is significant
- 2) account for the uncertainty in the trend due to natural variability

The analytic model provides a zeroth order estimate of the uncertainty in future trends in any *Gaussian* process with *stationary* variance.

e.g., the atmospheric circulation at middle latitudes, precipitation averaged over a specific watershed, surface temperature averaged over a broad agricultural region, and global-mean temperature.

Large-ensembles provide seemingly little information on the role of internal variability in future climate that can not be inferred from a relatively short, unforced climate simulation.

(Multiple ensembles are required to estimate the forced response)

Arguably... the role of internal variability in future climate change is best estimated not from a climate model (which inevitably exhibits biases), but from the statistics of the observed climate.

(Decadal variability accounts for a relatively small fraction of the standard deviation on regional scales).

results drawing from:

- Thompson et al. (submitted to Journal of Climate)
see www.atmos.colostate.edu/~davet