

# Matrix tool to facilitate land carbon modeling: case studies from CLM4.5

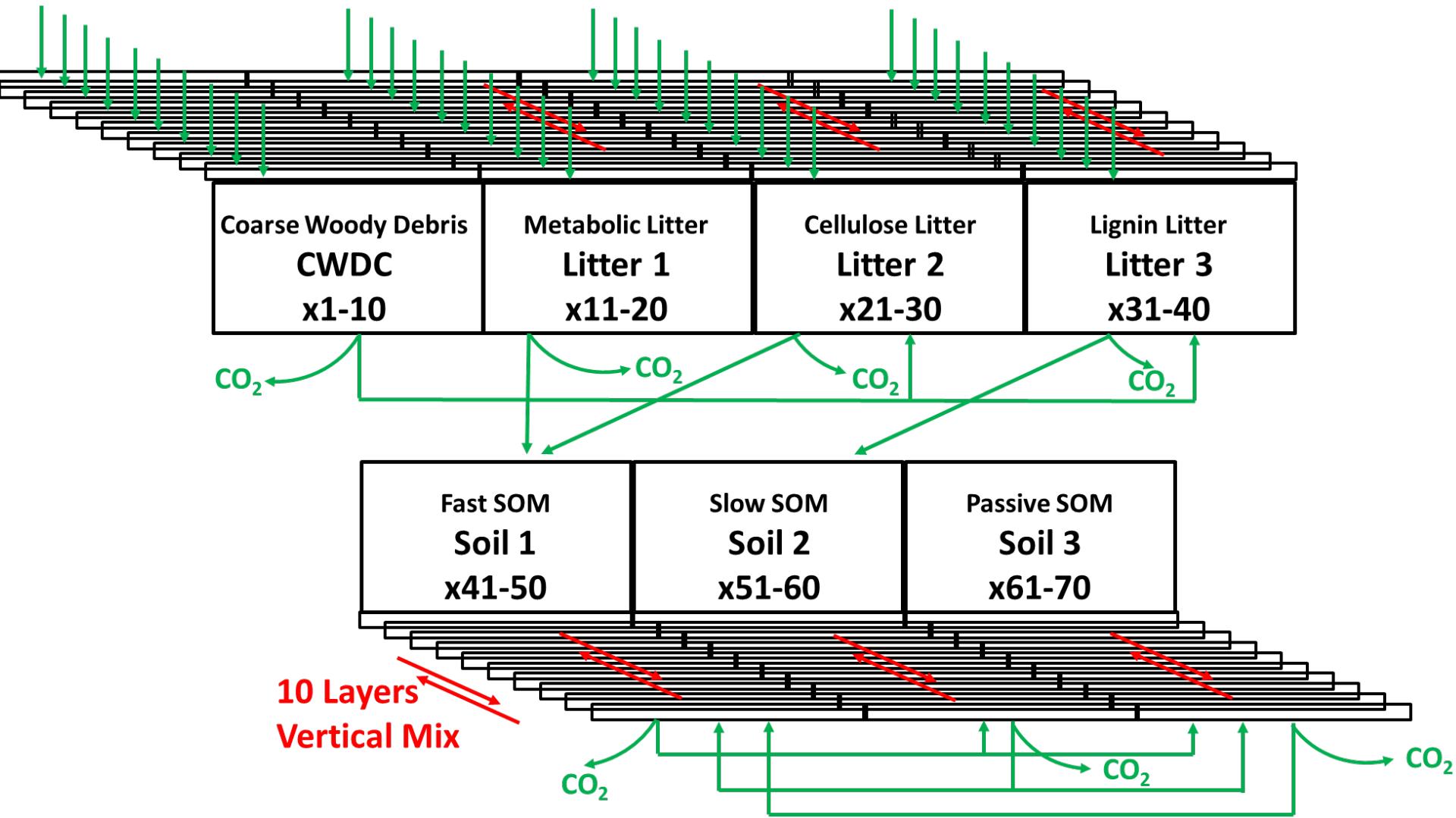
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2017 CESM Working Group Meeting



# CLM4.5 dead C pool structure



# Matrix representation

$$\frac{dX}{dt} = BI - A\varepsilon kX - VX$$

Annotations:

- $X, C \text{ pools}$  points to  $dX$
- $A, \text{ transfer matrix}$  points to  $A$
- $\varepsilon, \text{ scalar}$  points to  $\varepsilon$
- $V, \text{ vertical mixing}$  points to  $V$
- $I, \text{ external input}$  points to  $BI$
- $B, \text{ allocation}$  points to  $BI$
- $k, \text{ decomposition rate}$  points to  $kX$

$X$  : 70x1 7 C types by 10 layers

$I$  : 1x1 C inputs to cwd and litter

$B$  : 70x1 allocation of C inputs

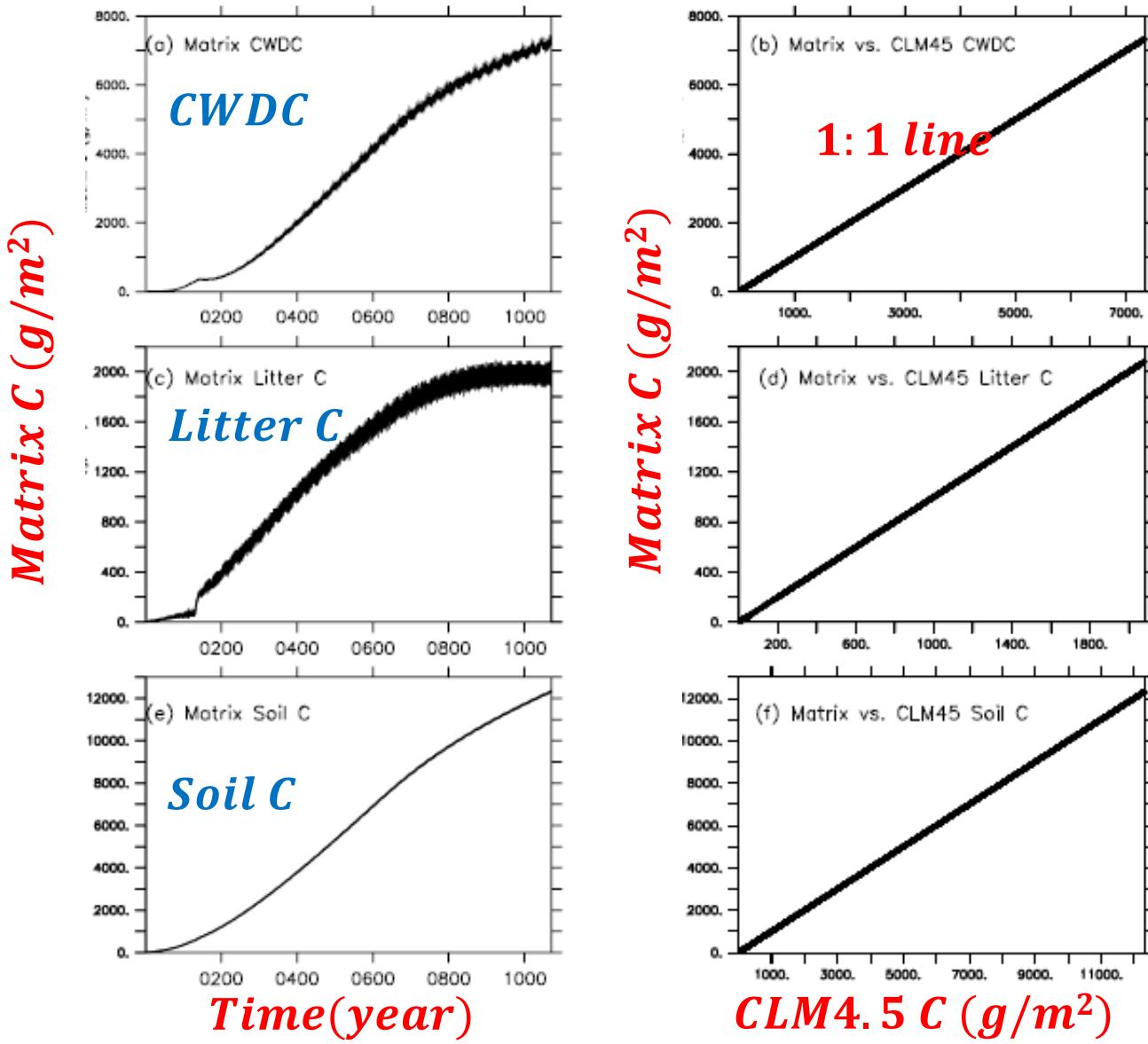
$A$  : 70x70 transfer of C among 7 C types

$\varepsilon$  : 70x70 moisture, temperature, oxygen, N and depth scalars

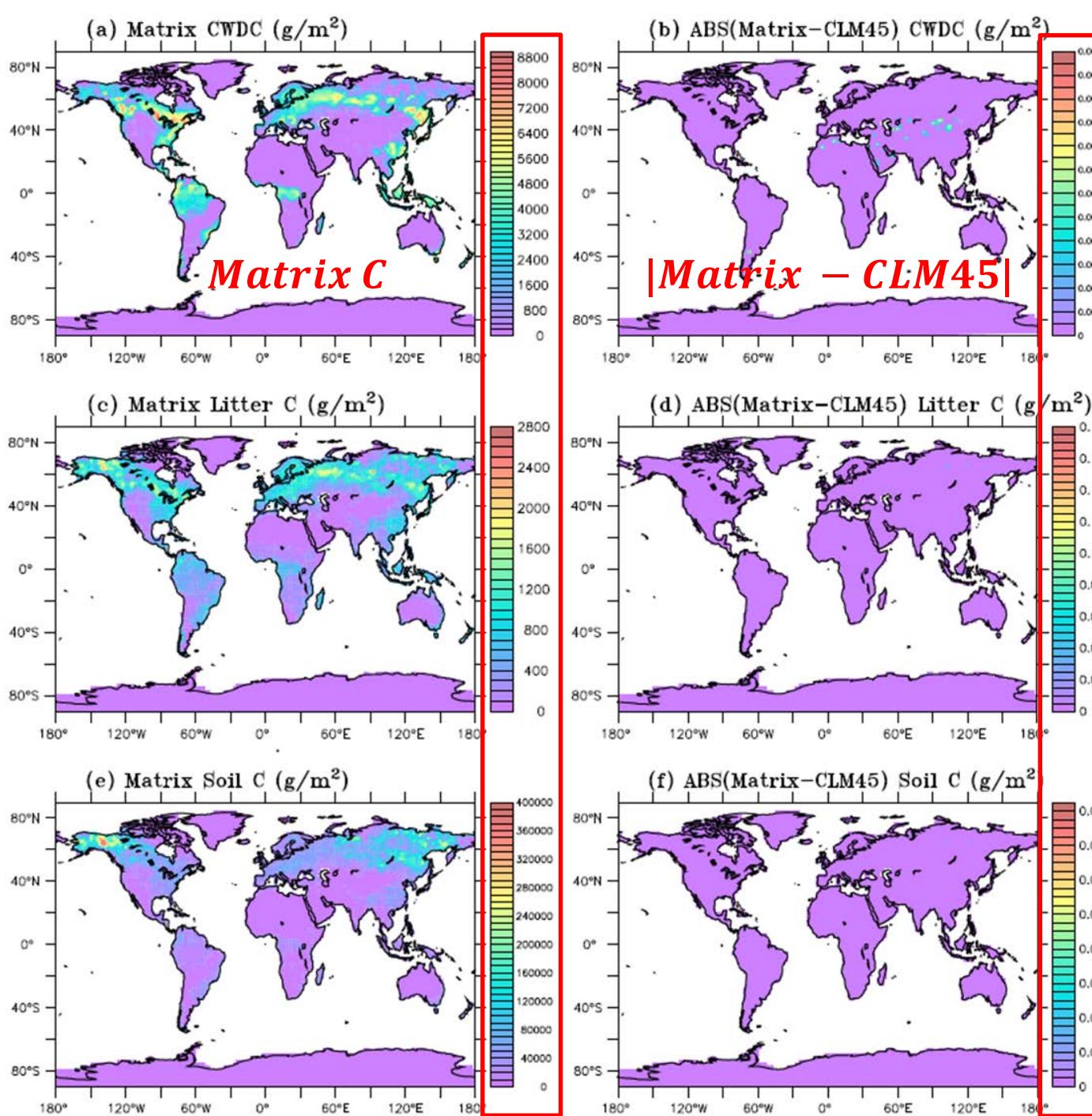
$k$  : 70x70 decomposition rate

$V$  : 70x70 vertical mixing of C

# Matrix vs. original CLM4.5bgc



**Matrix  
representation  
100%  
reproduces  
CLM45bgc  
dead C dynamics**

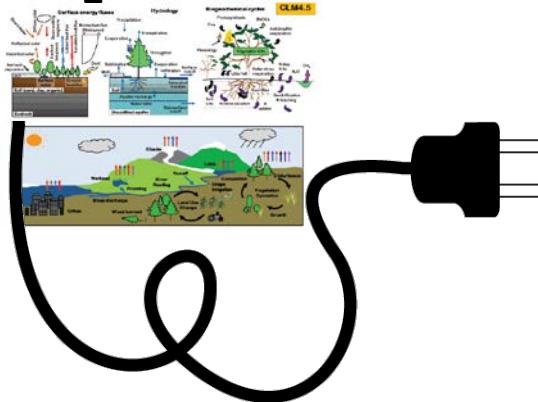


# Matrix Application 1

Attribute dead C response to global changes

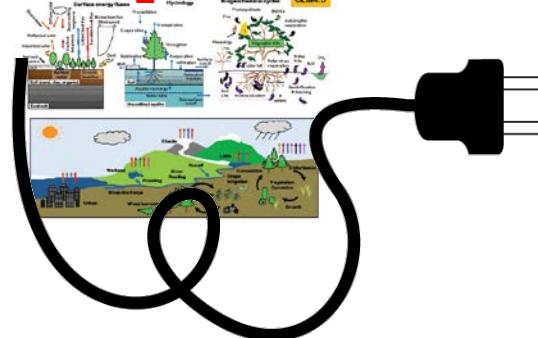
CLM Run 1

CO<sub>2</sub>(280ppm)



CLM Run 2

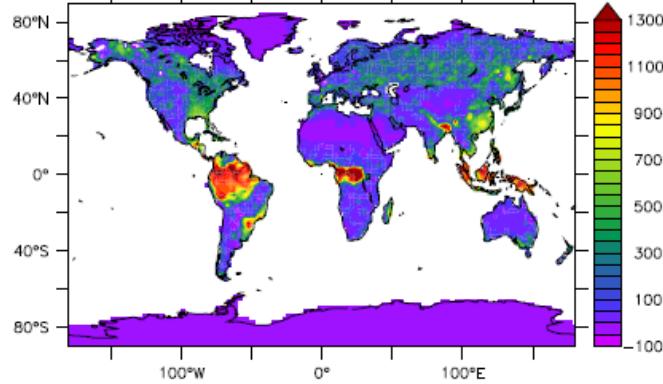
eCO<sub>2</sub>(560ppm)



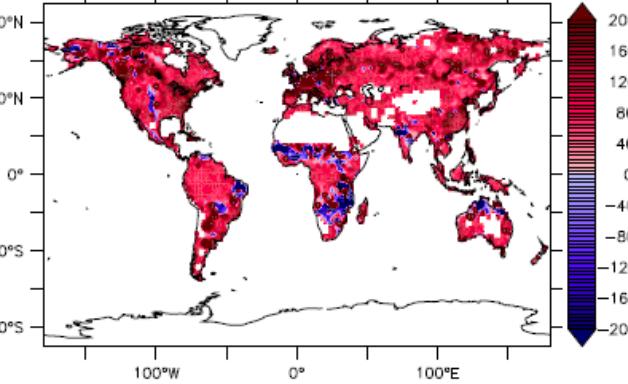
Matrix Simulations (matlab)

	S0	S1	S2	S3	S4	S5
I	I0	Ie	Ie	Ie	Ie	Ie
B	B0	B0	Be	Be	Be	Be
N	N0	N0	N0	Ne	Ne	Ne
$\varepsilon$	$\varepsilon 0$	$\varepsilon 0$	$\varepsilon 0$	$\varepsilon 0$	$\varepsilon e$	$\varepsilon e$
V	V0	V0	V0	V0	V0	Ve

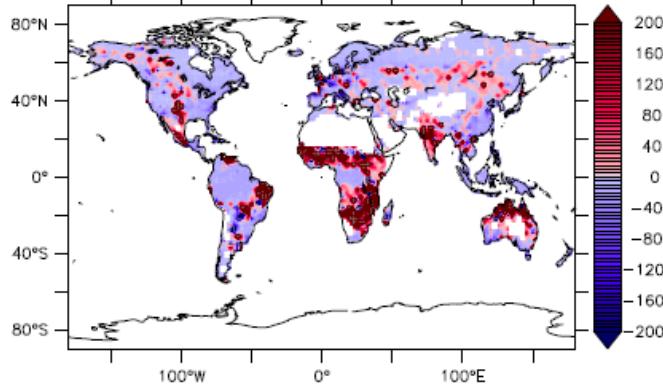
(a) Total eCO<sub>2</sub> effect (g/m<sup>2</sup>)



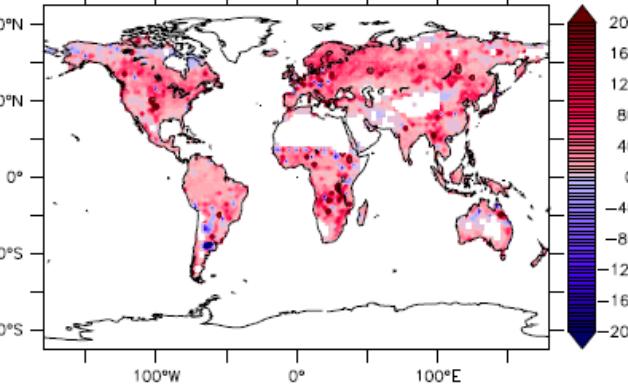
(b) Input (percent)



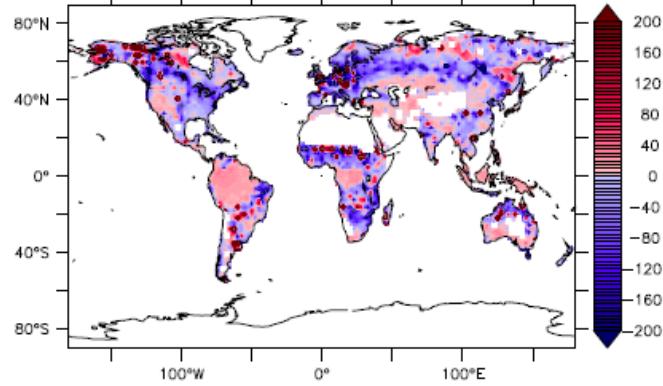
(c) Allocation (percent)



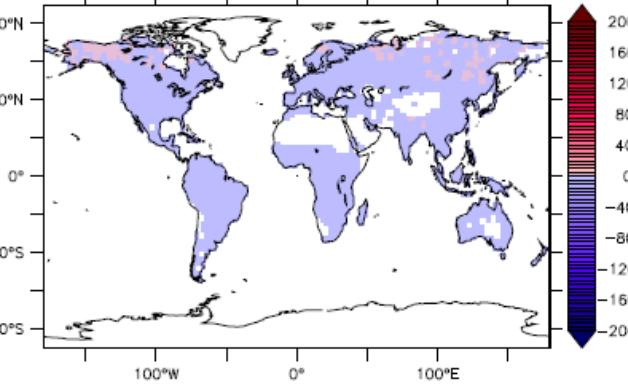
(d) Nitrogen (percent)



(e) Temperature+Moisture+Oxygen (percent)



(f) Vertical Mixing (percent)



# Matrix Application 2

## Diagnose CLM simulations

$$\bullet X(t) = \underbrace{(A\xi(t)K - V(t))^{-1}}_{\text{C storage } (X)} \underbrace{B(t)I(t)}_{\text{C storage Capacity } (X_c)} - \underbrace{(A\xi(t)K - V(t))^{-1} \frac{dX(t)}{dt}}_{\text{C storage Potential } (X_p)}$$

C storage  
( $X$ )

C storage Capacity  
( $X_c$ )

C storage Potential  
( $X_p$ )

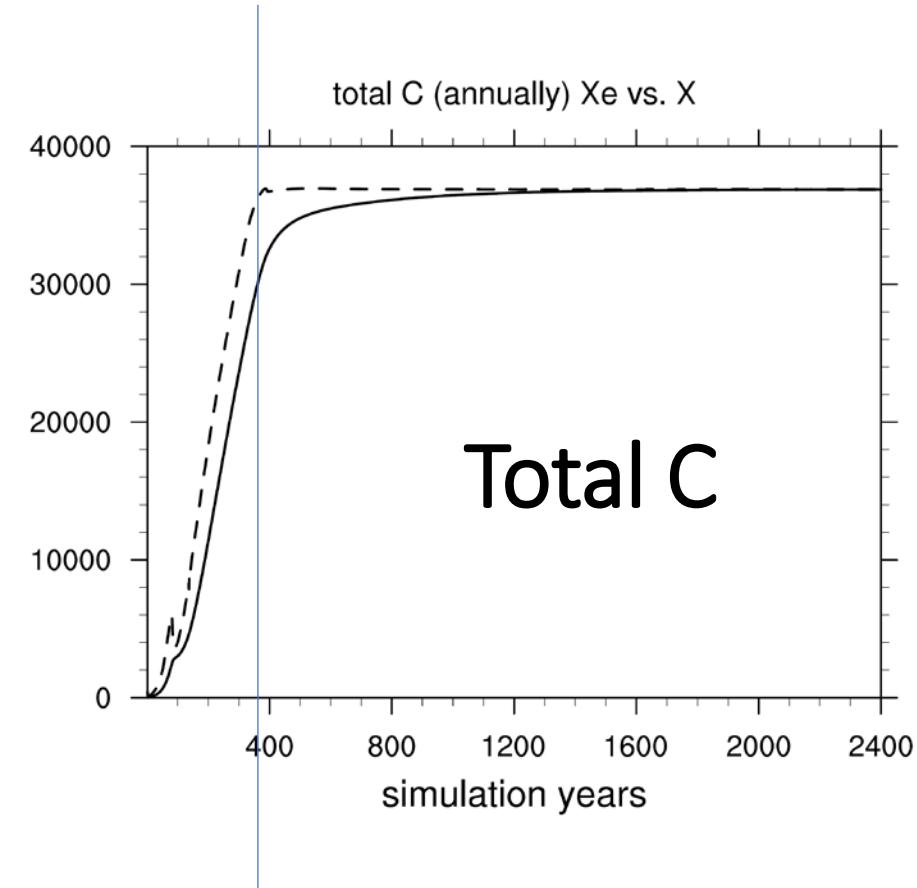
At steady state:

C storage potential approaches 0 ( $X_p = 0$ )

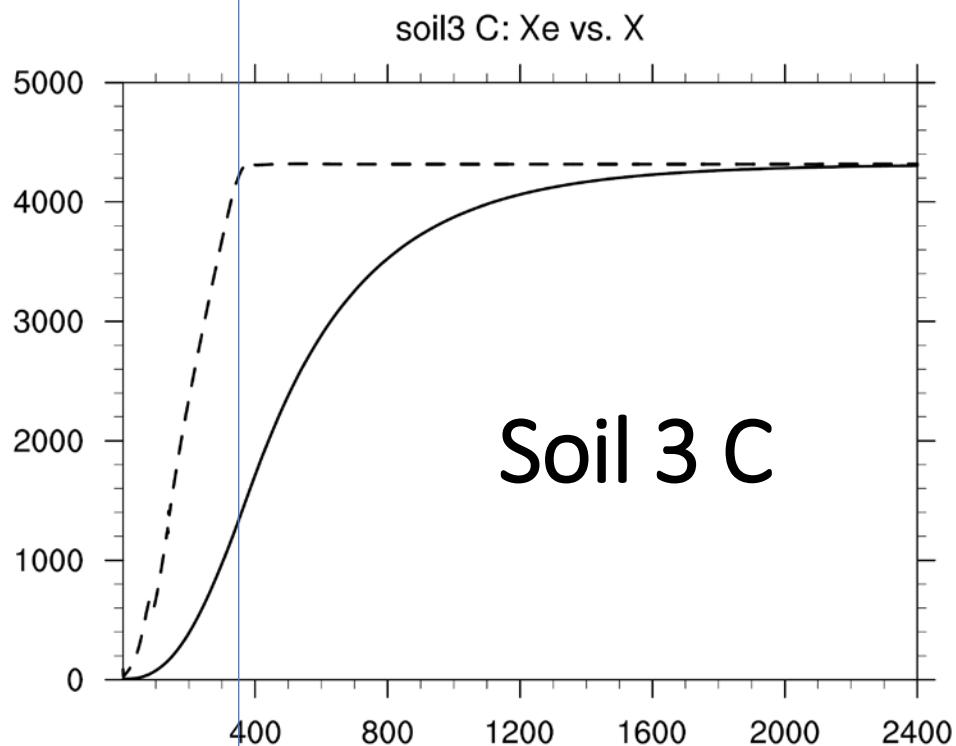
C storage equals C storage capacity ( $X = X_c$ )

# Spin-up

— C Storage  
- - C Storage Capacity

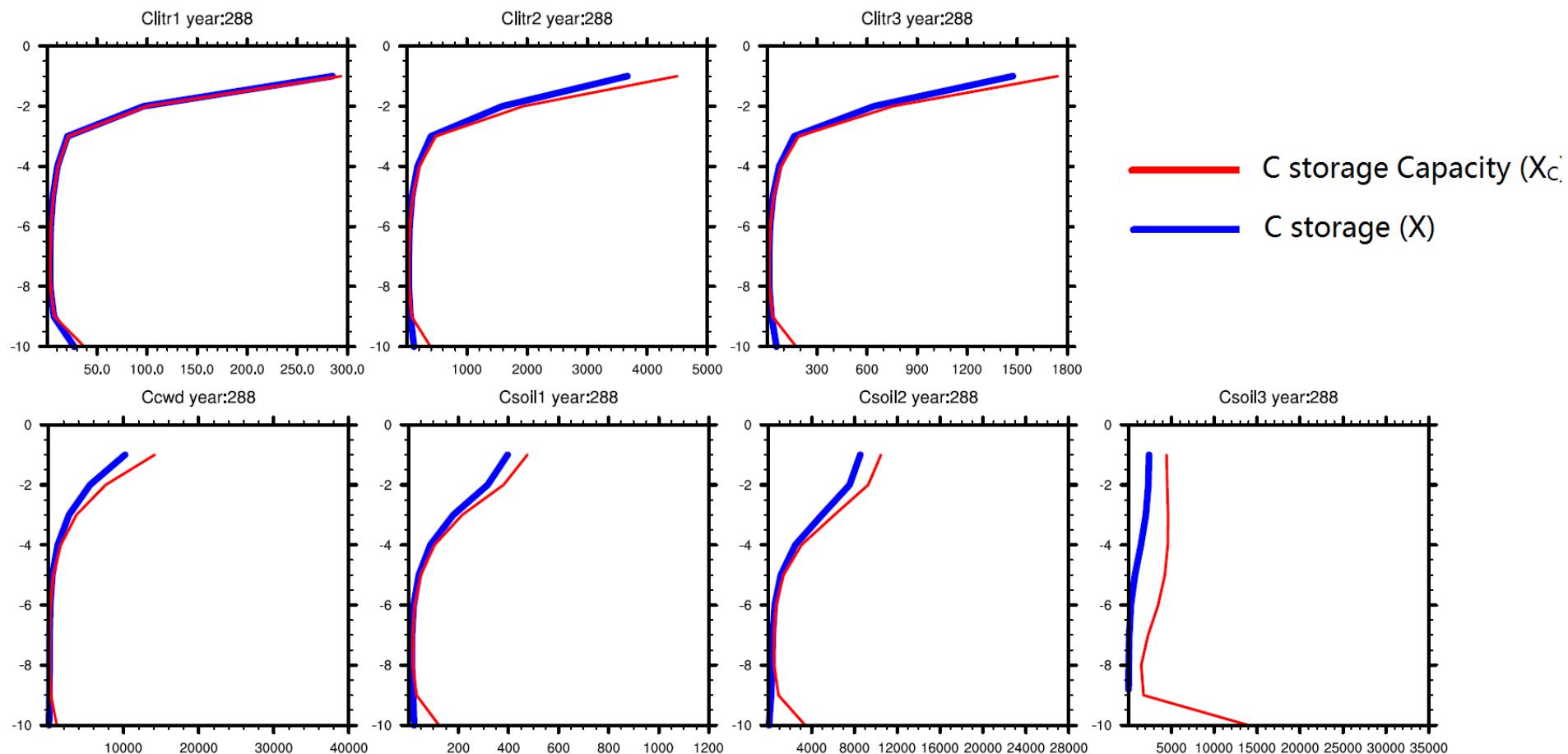


$Z_{\tau} = 10$



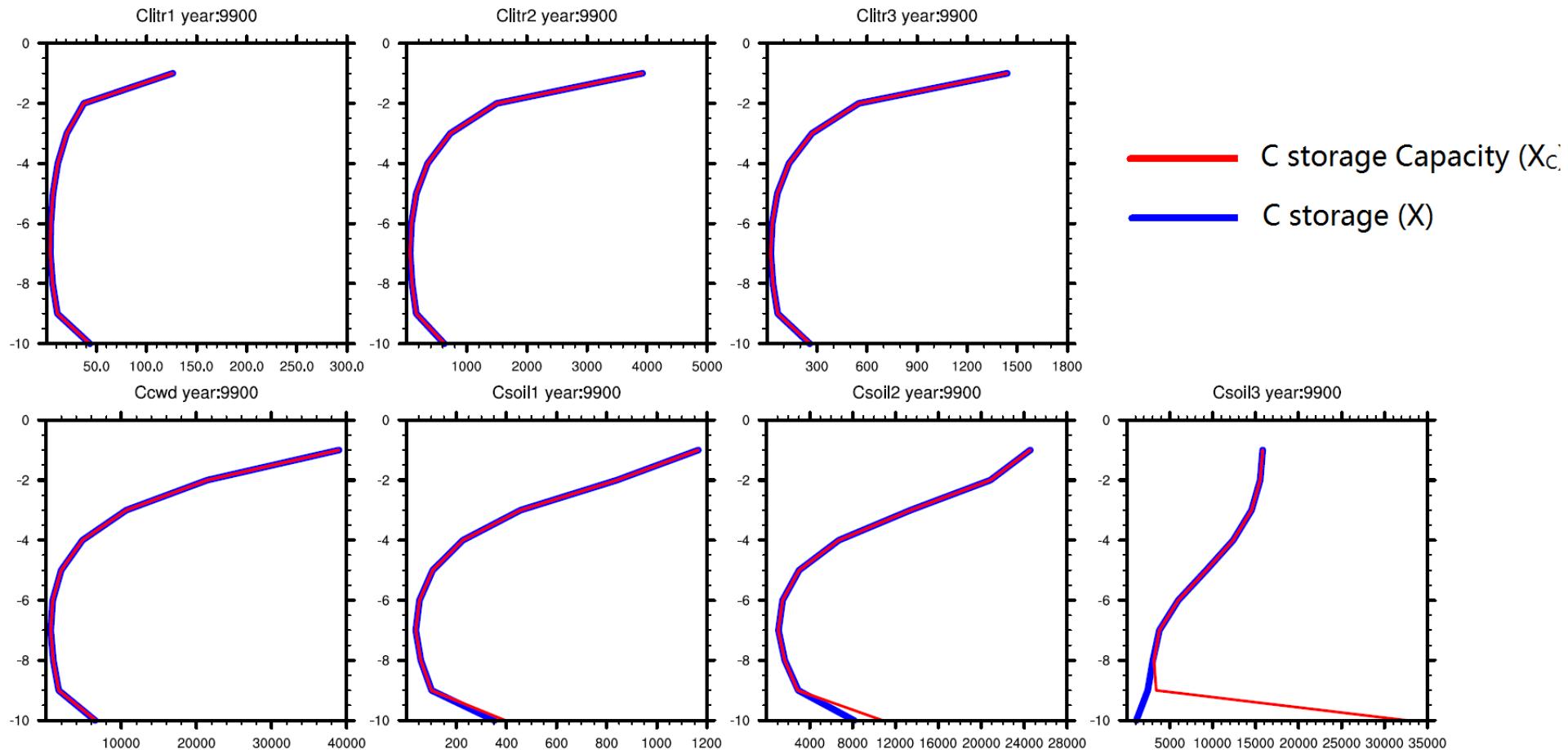
# Vertical profile of C storage capacity ( $X_C$ ) vs. C storage ( $X$ ) ( $z_{\tau}=0.5$ )

- Spin up for  $\sim 300$  years



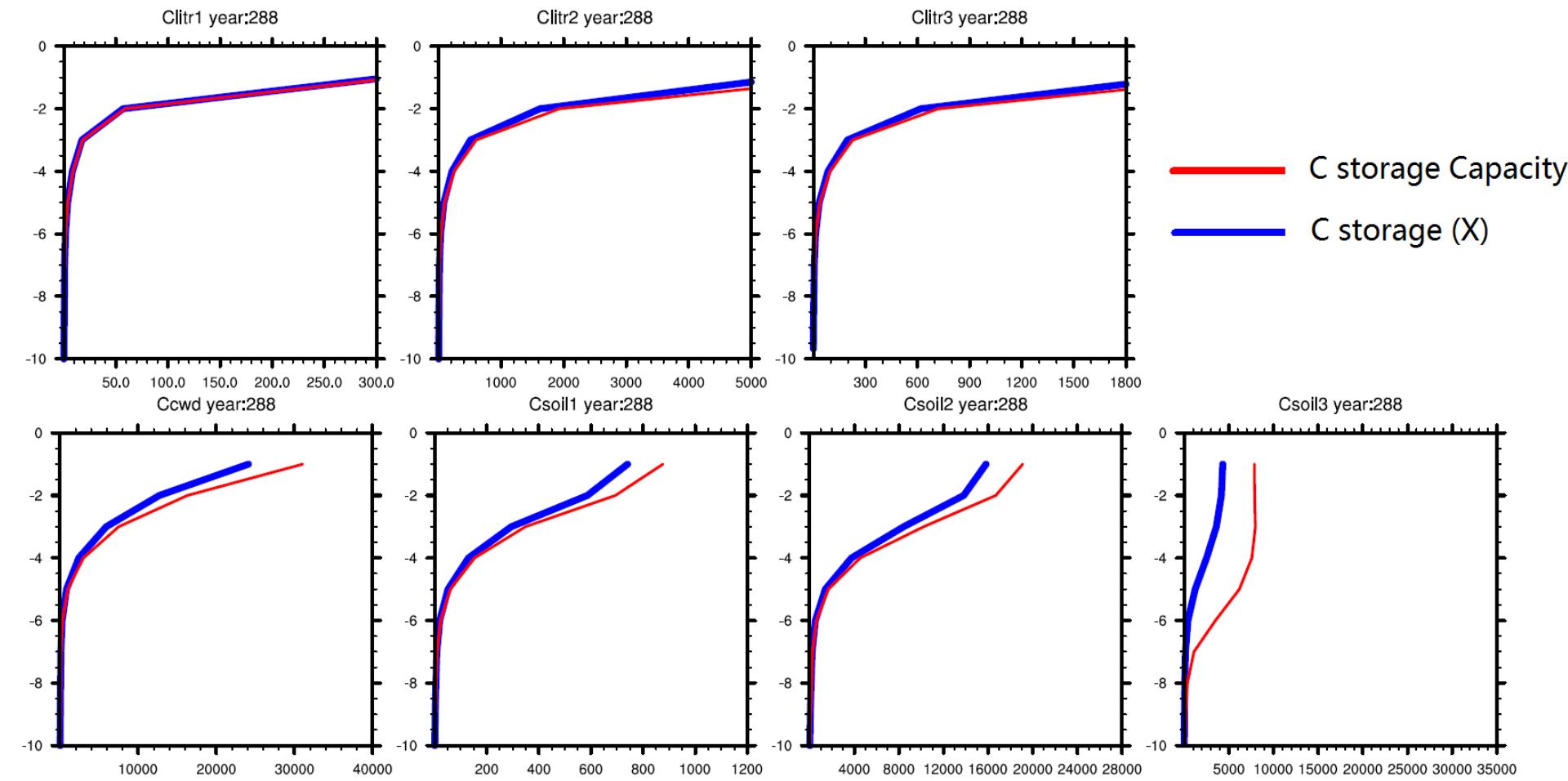
# Vertical profile of C storage capacity ( $X_C$ ) vs. C storage ( $X$ ) ( $z_{\tau}=0.5$ )

- Spin up for >5000 years



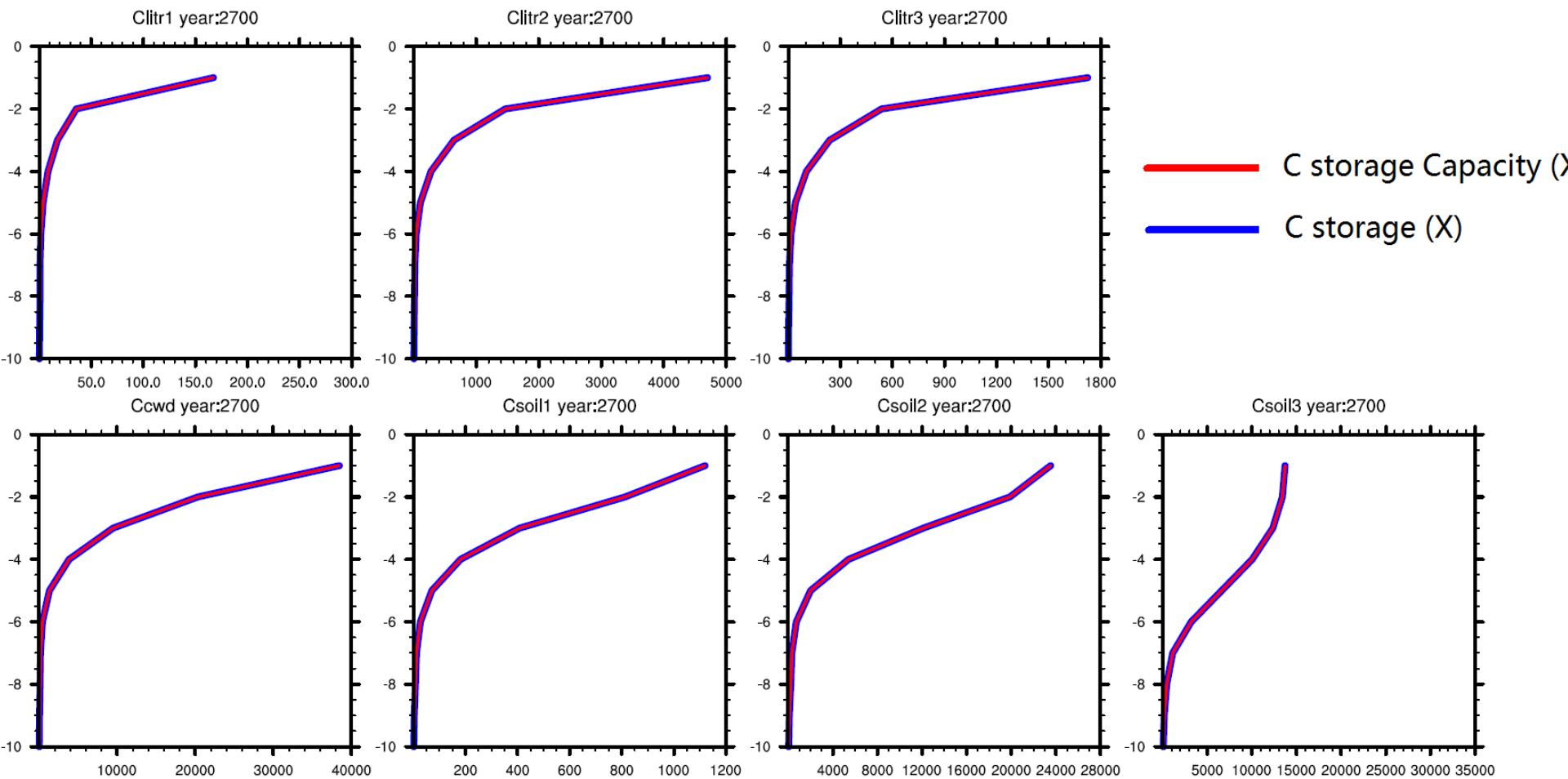
# Vertical profile of C storage capacity ( $X_C$ ) vs. C storage ( $X$ ) (z\_tau=10)

- Spin up for  $\sim 300$  years



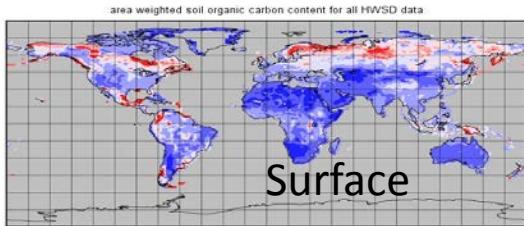
# Vertical profile of C storage capacity ( $X_C$ ) vs. C storage ( $X$ ) ( $z_{\tau}=10$ )

- Spin up for 2700 years

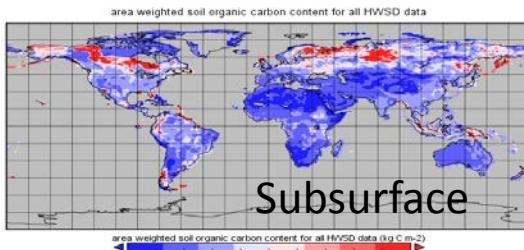


# Matrix Application 3

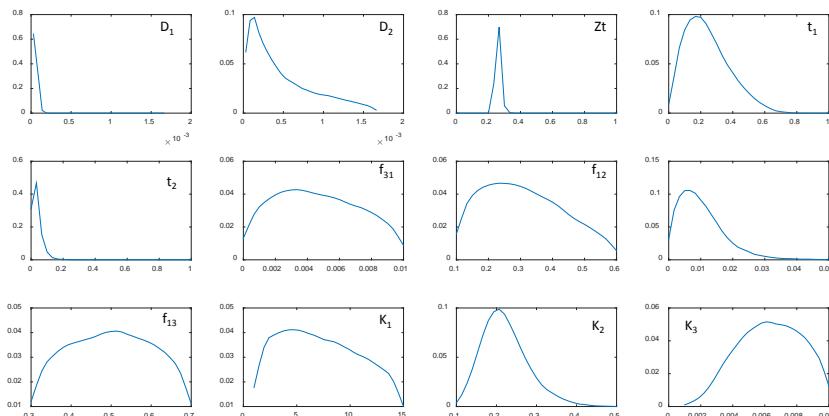
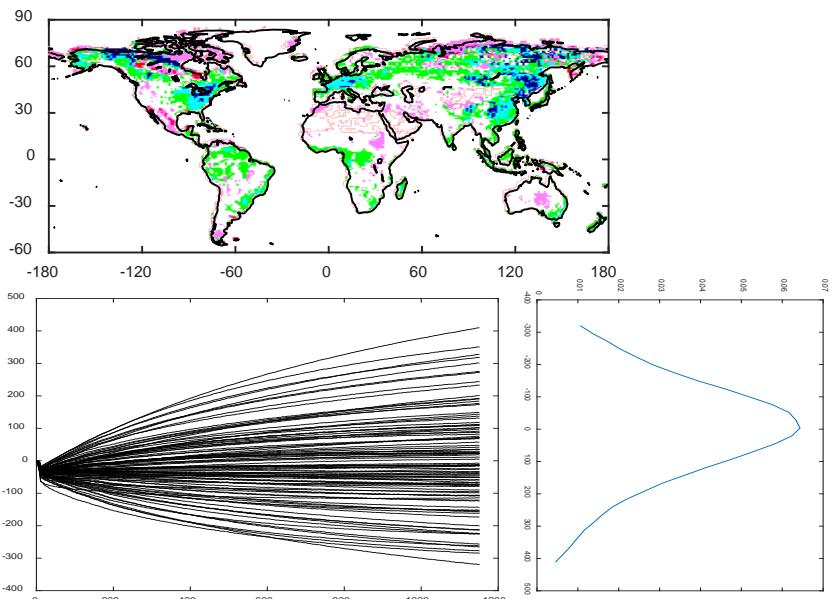
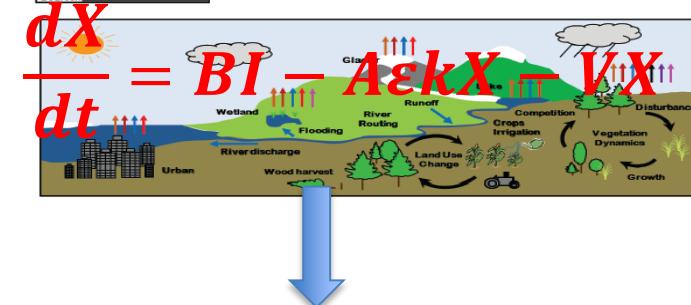
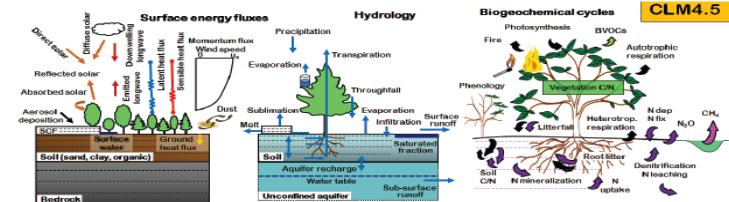
# Realize data assimilation to constrain global SOM



# MCMC



# Harmonized soil C content by Wieder et al., (2015)



# Summary

- One matrix equation to reproduce dead C dynamics
- Easy manipulation and exploration of different components
- Diagnose CLM simulations
- Promote data assimilation in SOM researches
- .....

**Thank you!**