

# STOCHASTIC FORCING OF CP AND EP ENSO EVENTS: OBSERVATIONS VS CESM-LE

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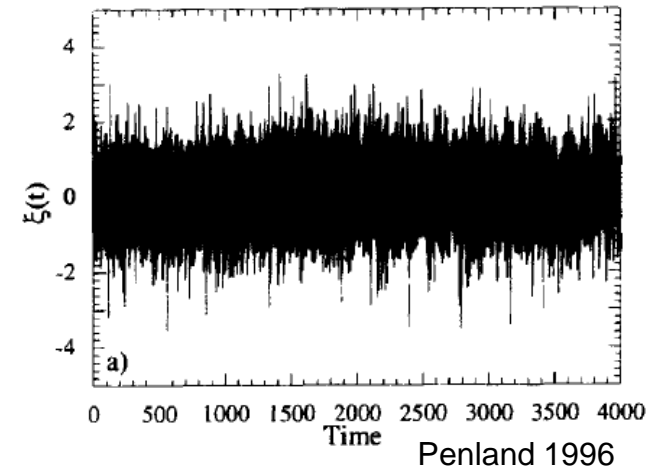


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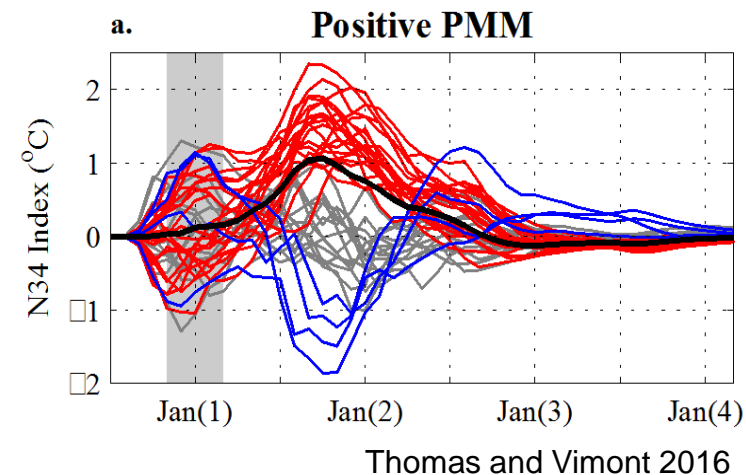
# What is Stochastic Forcing ?

- Forcing that is white *in time* (not space)
- Physical systems contain processes on many time scales
  - Approximate the ‘fast’ processes (chaotic & non-linear) as white noise



# Why is it important?

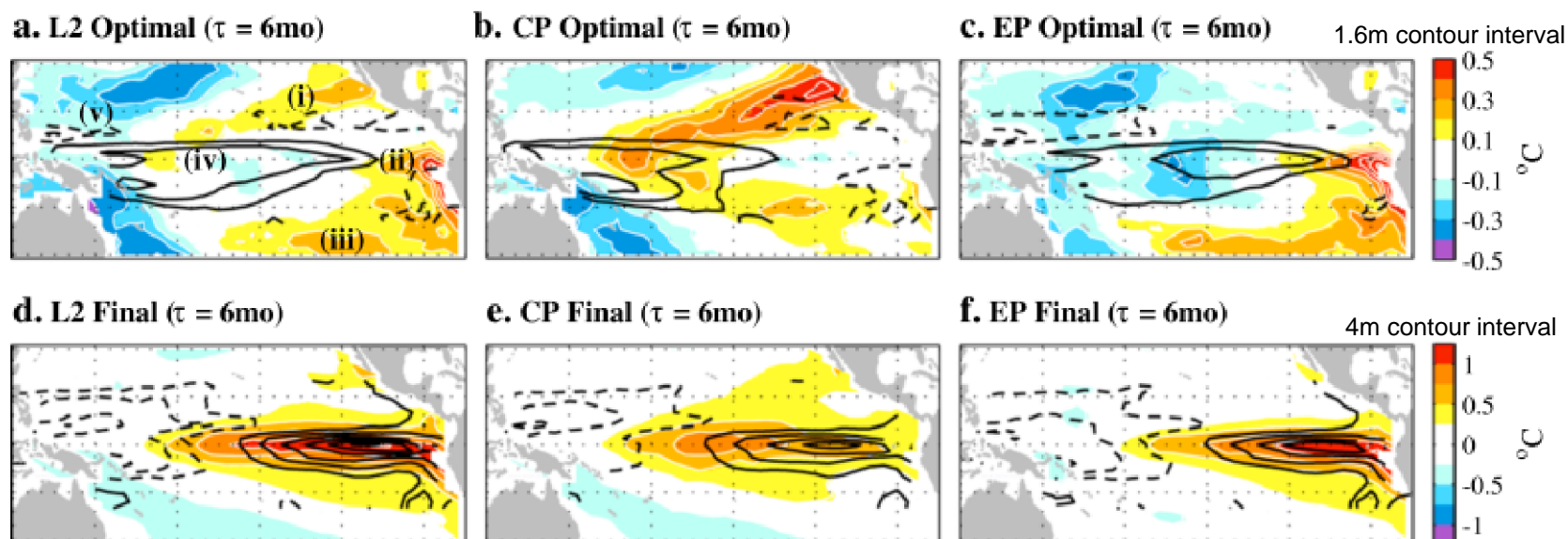
- Many physical model experiments show ENSO is sensitive to natural variability
  - Initial conditions
  - **Noise forcing**



# Role of Noise Forcing in Generating ENSO Diversity

- Observational evidence for *optimal initial conditions* that maximize EP and CP growth

## Optimal Initial Conditions, and Final Conditions



Vimont, Alexander and Newman 2014

- **What noise forcing can *lead to the generation* of these optimals?**

# Methods

1. Estimate Dynamics - Linear Inverse Model (LIM)
2. Identify Optimal Initial Conditions
3. Calculate Noise Forcing

## Observations

1982-2015

SST: monthly + daily IOSST

Thermocline depth (20° Isotherm depth): monthly + daily GODAS

Daily NCEP Reanalysis

## CESM Large Ensemble

1982-2015

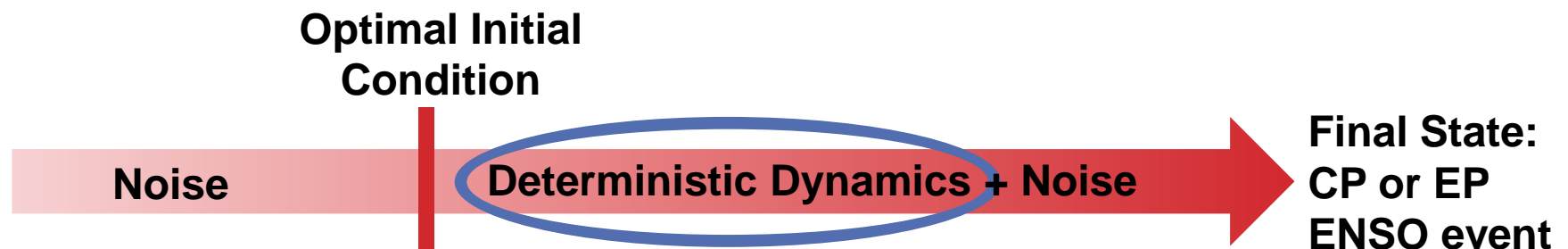
35 Ensemble Members

SST: monthly + daily

SSH: monthly + daily

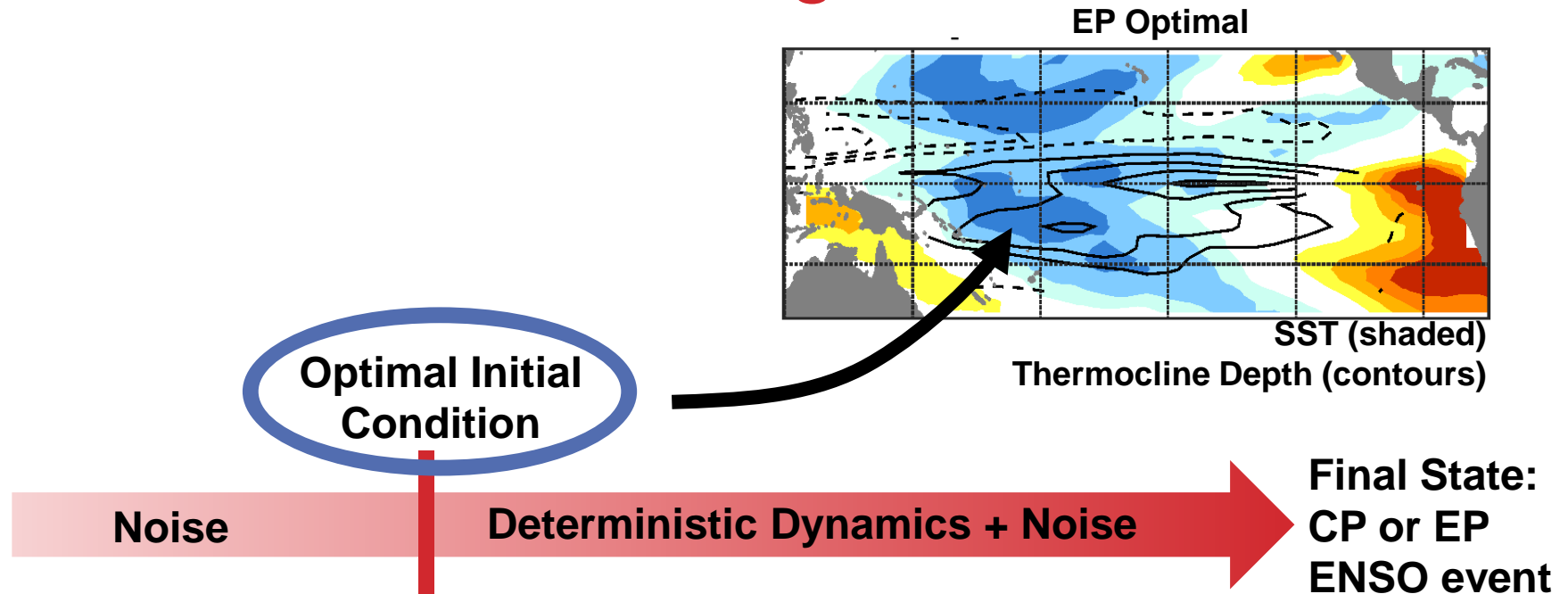
Daily Atmospheric Variables

# Using Linear Inverse Modeling (LIM) to Estimate Noise Forcing



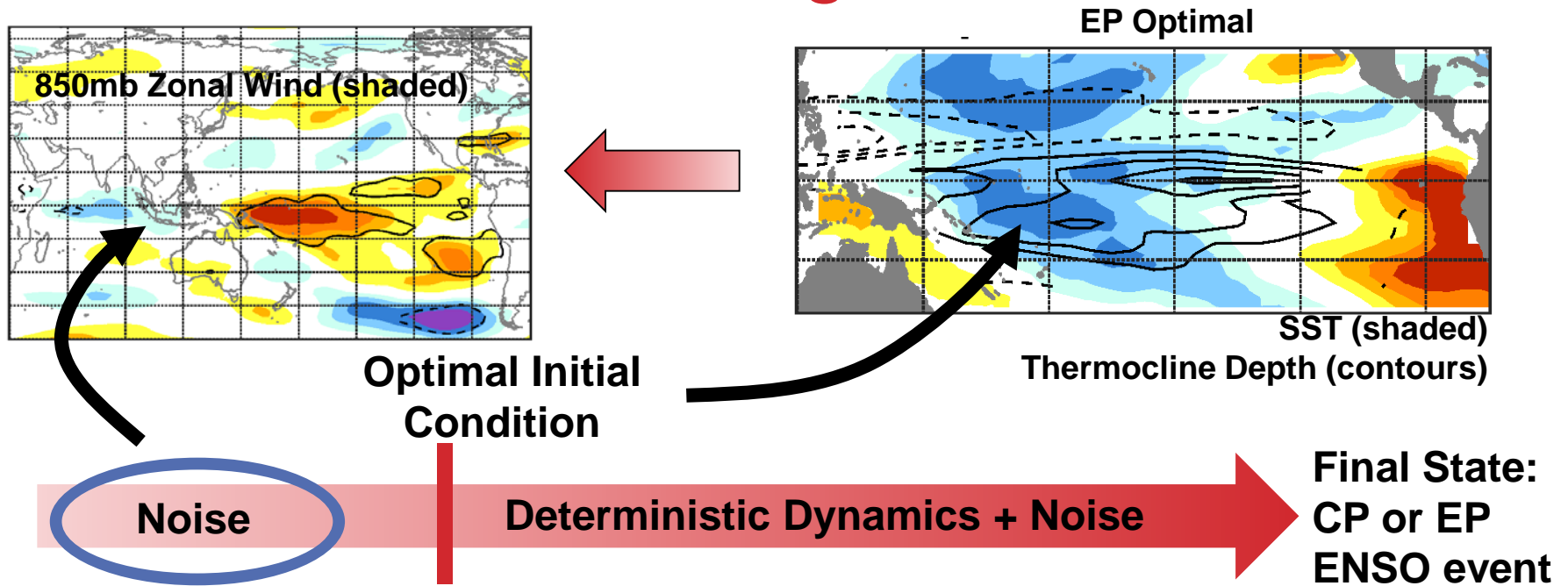
- 1) Calculate Dynamics,
- 2) Identify the Optimal Initial Conditions,
- 3) Estimate Noise Forcing

# Using Linear Inverse Modeling (LIM) to Estimate Noise Forcing



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# Using Linear Inverse Modeling (LIM) to Estimate Noise Forcing



- 1) Calculate Dynamics,
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# Dynamics: Linear Inverse Model

General linearized model describes the Tropical Pacific:

$$d\mathbf{X}/dt = \mathbf{L}\mathbf{X} + \boldsymbol{\xi}$$

↑  
Deterministic Dynamics

← White Noise Forcing  
(does not include atmospheric noise)

$\mathbf{X}$  = State Vector [SST; Thermocline Depth or SSH]

$\mathbf{L}$  = Linear Operator describing the slow, linear dynamics of the system

$\boldsymbol{\xi}$  = Noise Forcing

Solution:

$$\mathbf{X}(\tau) = \exp(\mathbf{L}\tau)\mathbf{X}(0)$$

Calculate Linear Dynamics  $\mathbf{L}$  from *statistics* of observations:

$$\mathbf{C}(\tau) = \exp(\mathbf{L}\tau)\mathbf{C}(0)$$

$$\mathbf{L} = \ln(\mathbf{C}_\tau/\mathbf{C}_0)/\tau$$



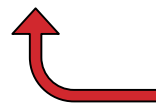
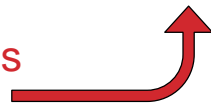
# Optimal Initial Conditions

$$\mathbf{X}(\tau) = \exp(\mathbf{L}\tau) \mathbf{X}(0) = \mathbf{G}_\tau \mathbf{X}(0)$$

Solve generalized eigenvalue problem for *optimal* initial conditions ( $\mathbf{p}$ ) that *maximize growth* ( $\mu$ ) in the direction specified by *Norm* ( $\mathbf{N}$ )

$$\mathbf{G}_\tau^T \mathbf{N} \mathbf{G}_\tau \mathbf{p} = \mu(\tau) \mathbf{p}$$

“CP” or “EP Norm” defines  
*direction of growth*



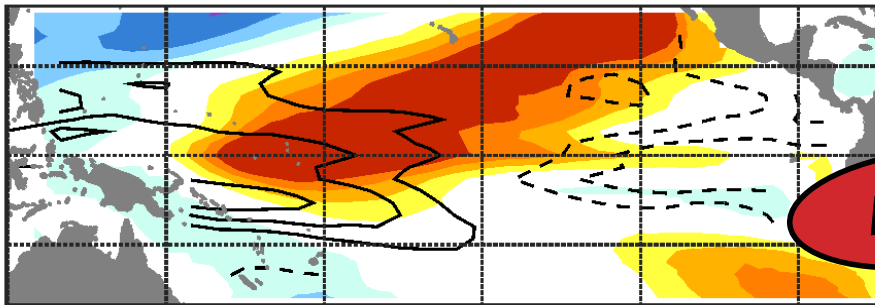
Maximized Growth

**Optimal Initial Condition**

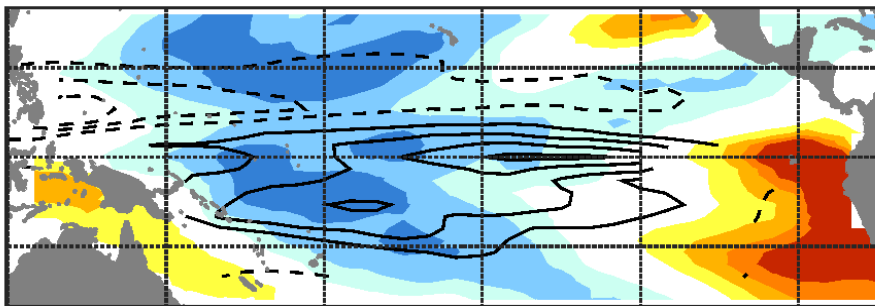
# Optimal Initial Conditions

## Observations

6mo CP Optimal



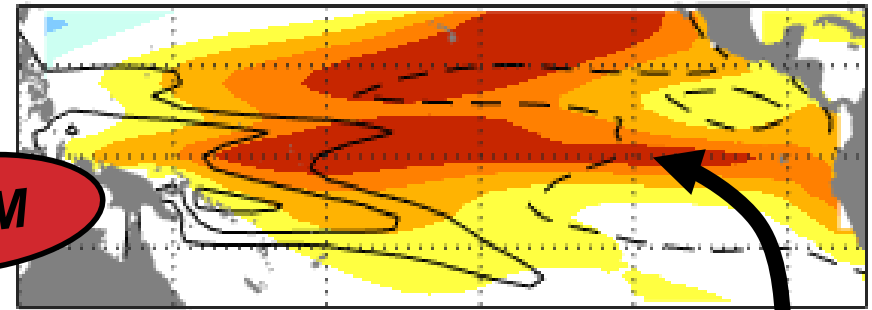
6mo EP Optimal



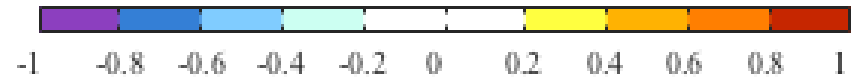
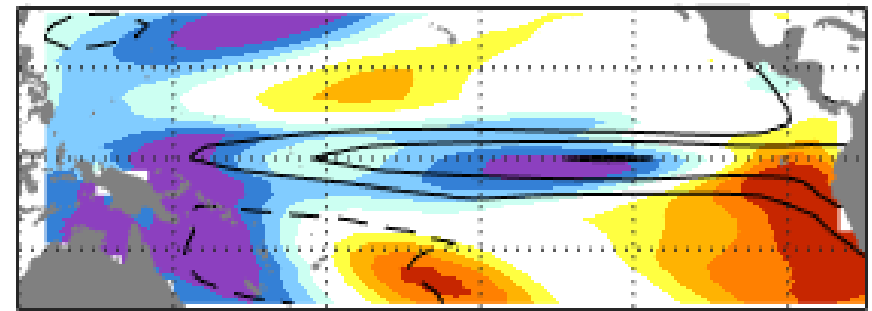
Thermocline contour interval: 4m

## CESM-LE

6mo CP Optimal



6mo EP Optimal

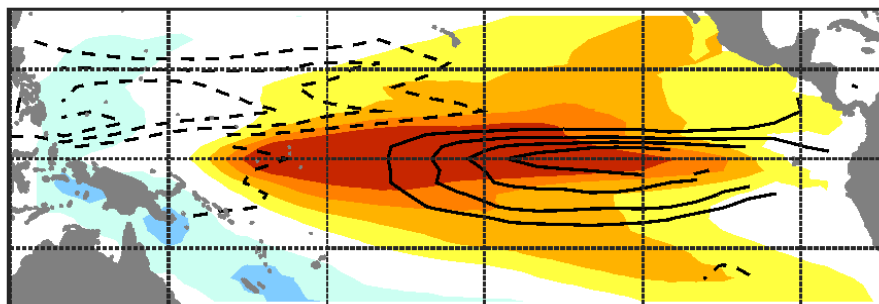


SSH contour interval: 2cm

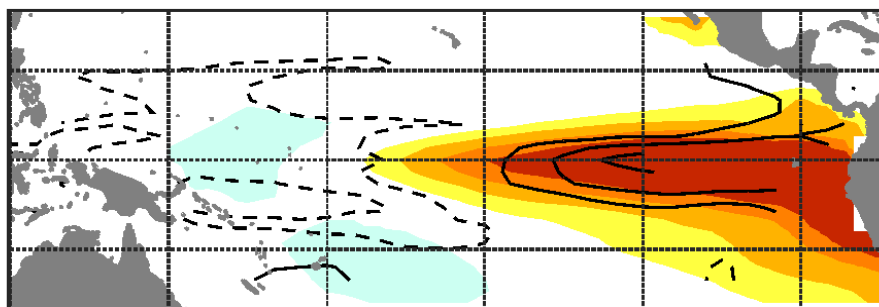
# Final Conditions

## Observations

### CP Final



### EP Final

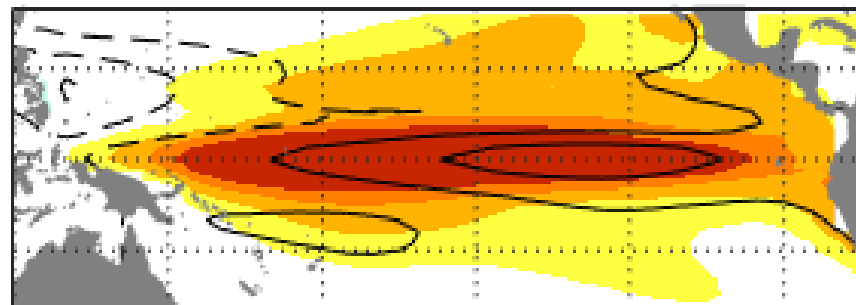


Thermocline contour interval: 8m

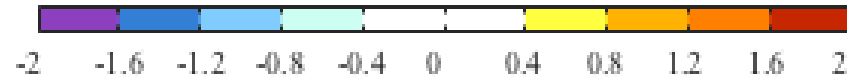
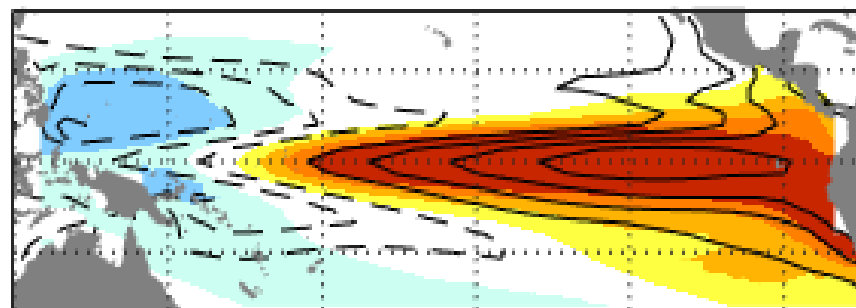
°C

## CESM-LE

### CP Final



### EP Final



SSH contour interval: 4cm

°C

# Noise Forcing

$$d\mathbf{X}/dt = \mathbf{L}\mathbf{X} + \xi$$

$$\xi(t) = \frac{[x(t+\Delta t) - x(t-\Delta t)]}{2} - Lx(t)$$

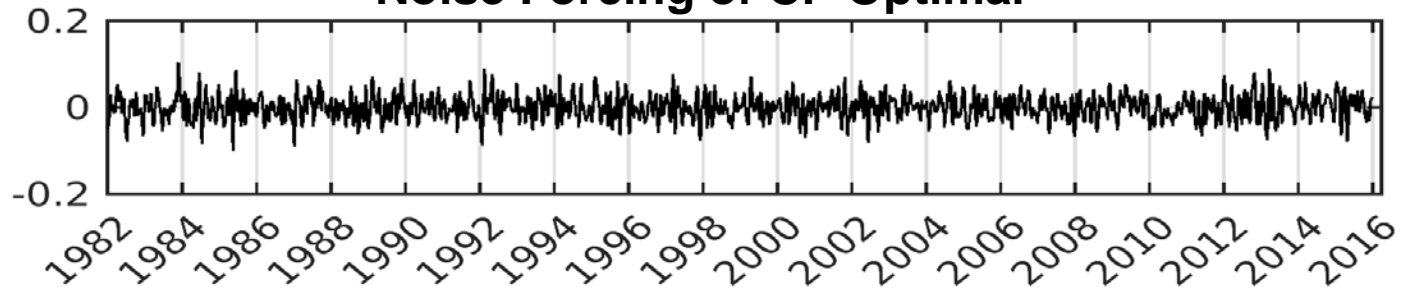
$\mathbf{x}$  = High Frequency (pentad) State Vector

$\mathbf{L}$  = Linear Dynamics of the system

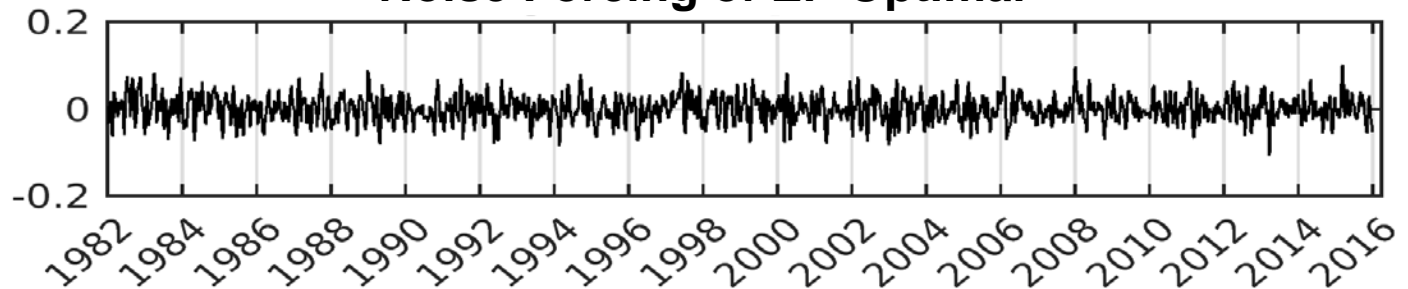
$\xi(t)$  = Noise Forcing (*time and space dependent*)

## Observations

### Noise Forcing of CP Optimal



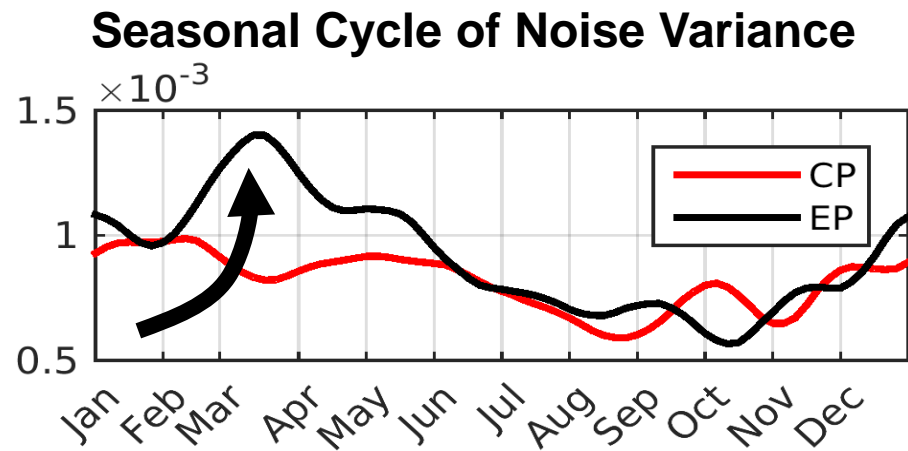
### Noise Forcing of EP Optimal



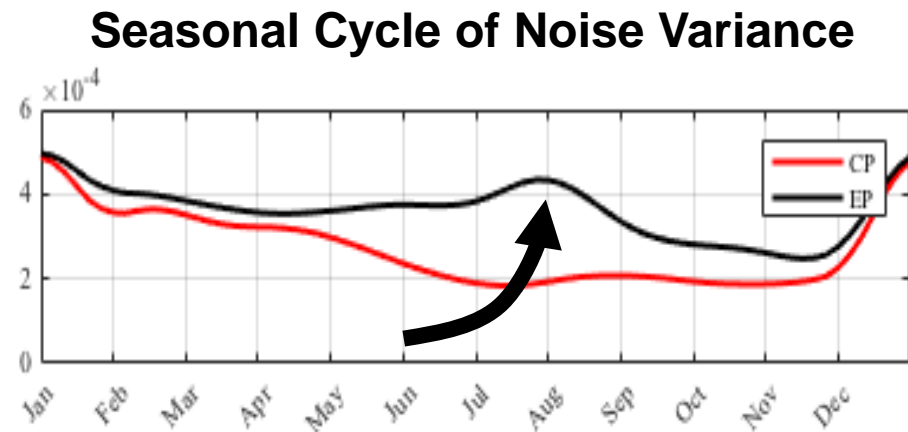
Regress  $\xi(t)$   
onto the spatial  
patterns of  
optimal initial  
conditions

# Noise Forcing

## Observations



## CESM-LE

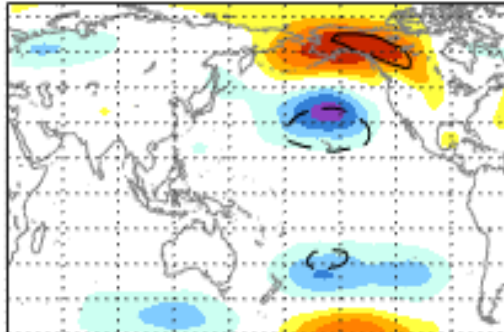


# CP Noise: Sea Level Pressure

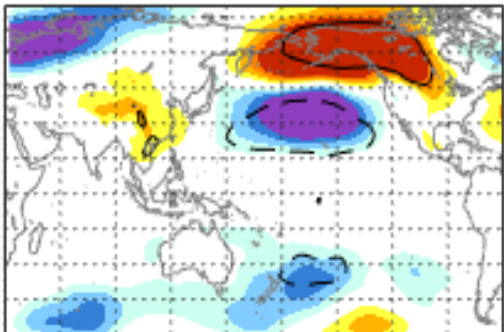
Observations

CESM-LE

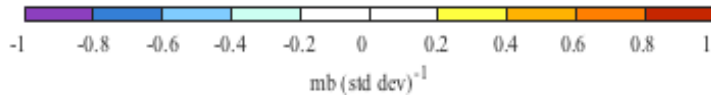
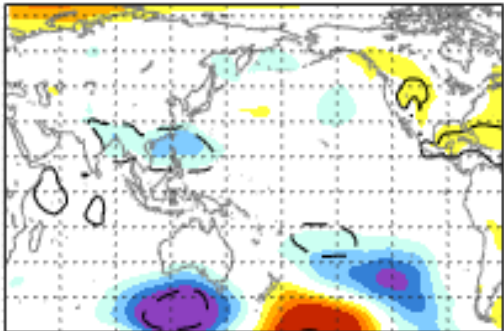
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DJF



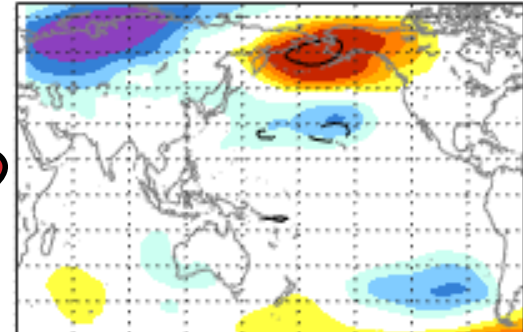
JJA



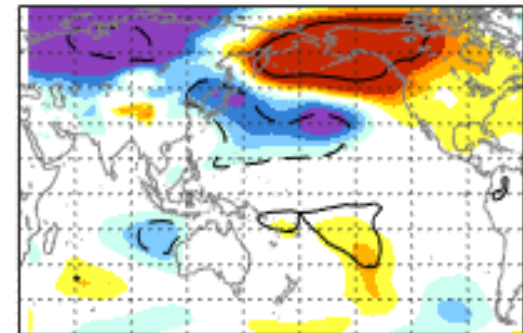
symmetric

NPO

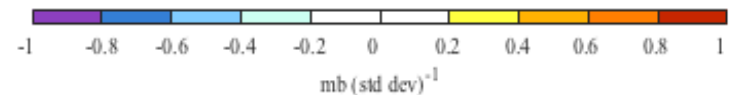
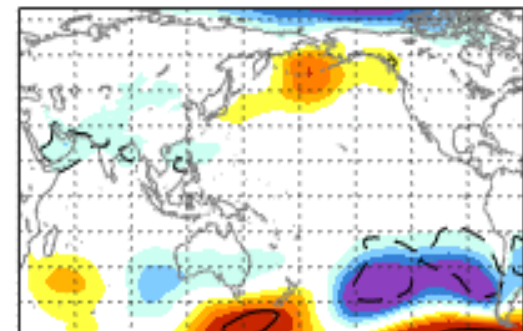
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DJF



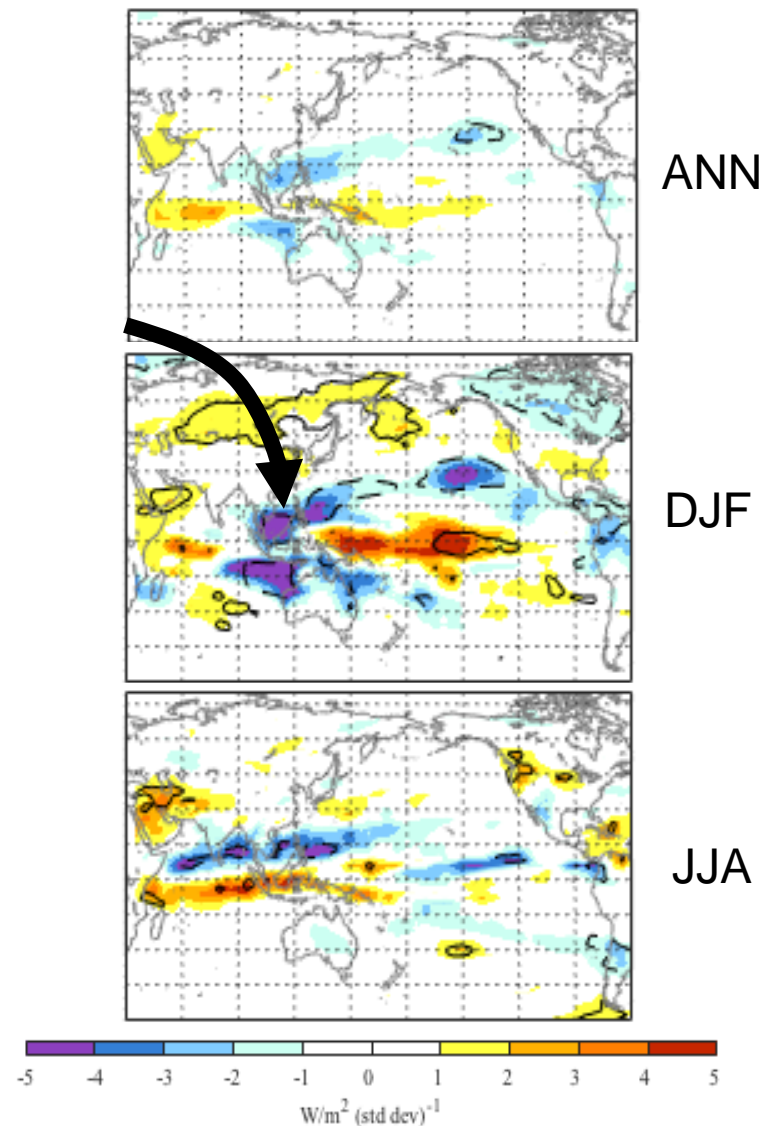
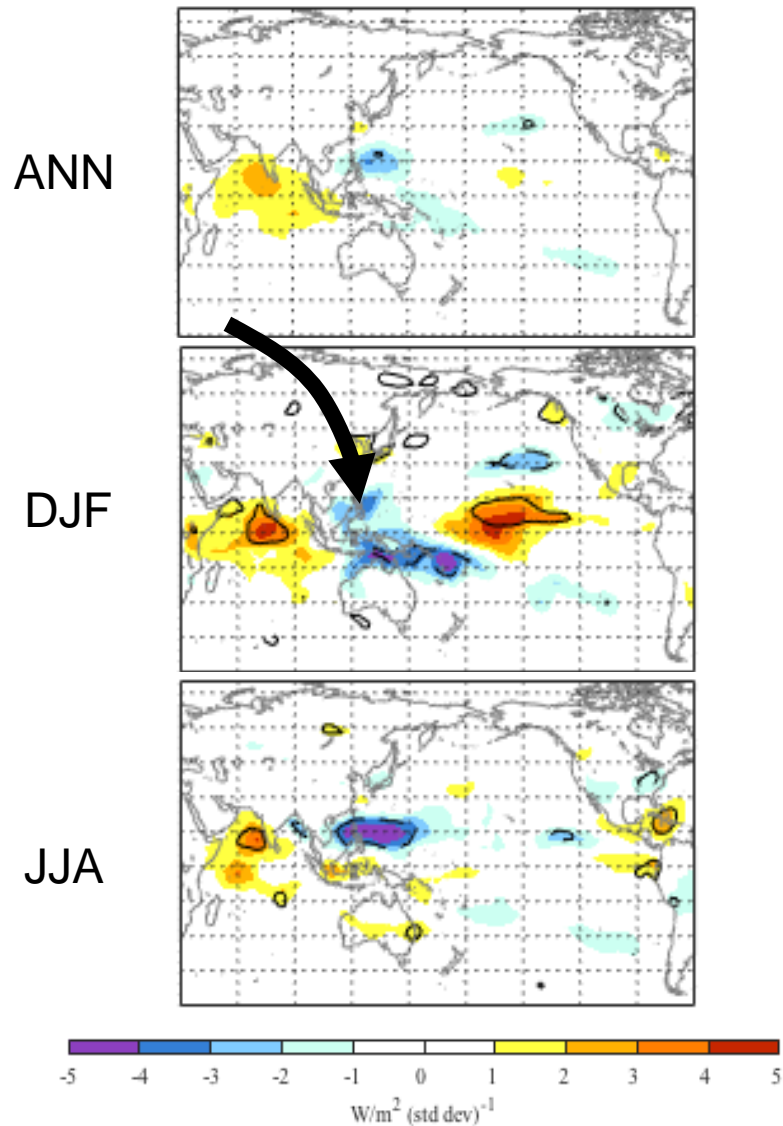
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# CP Noise: OLR

Observations

CESM-LE

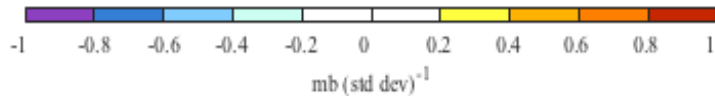
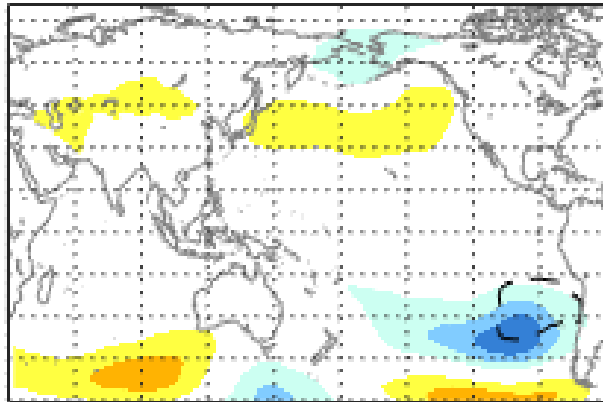


# EP Noise: Sea Level Pressure

Observations

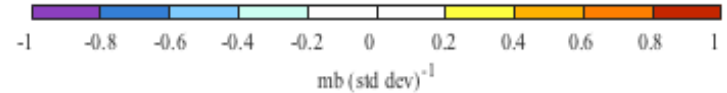
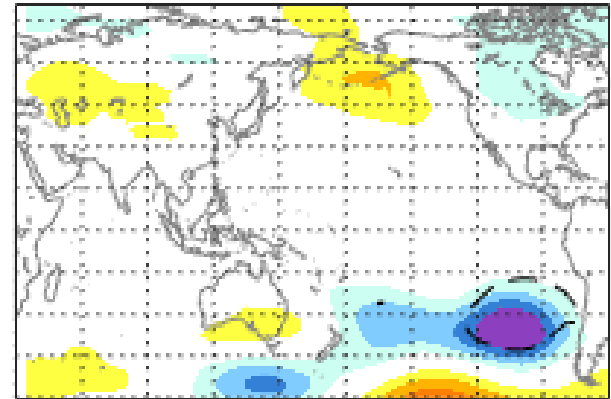
CESM-LE

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**weaker**

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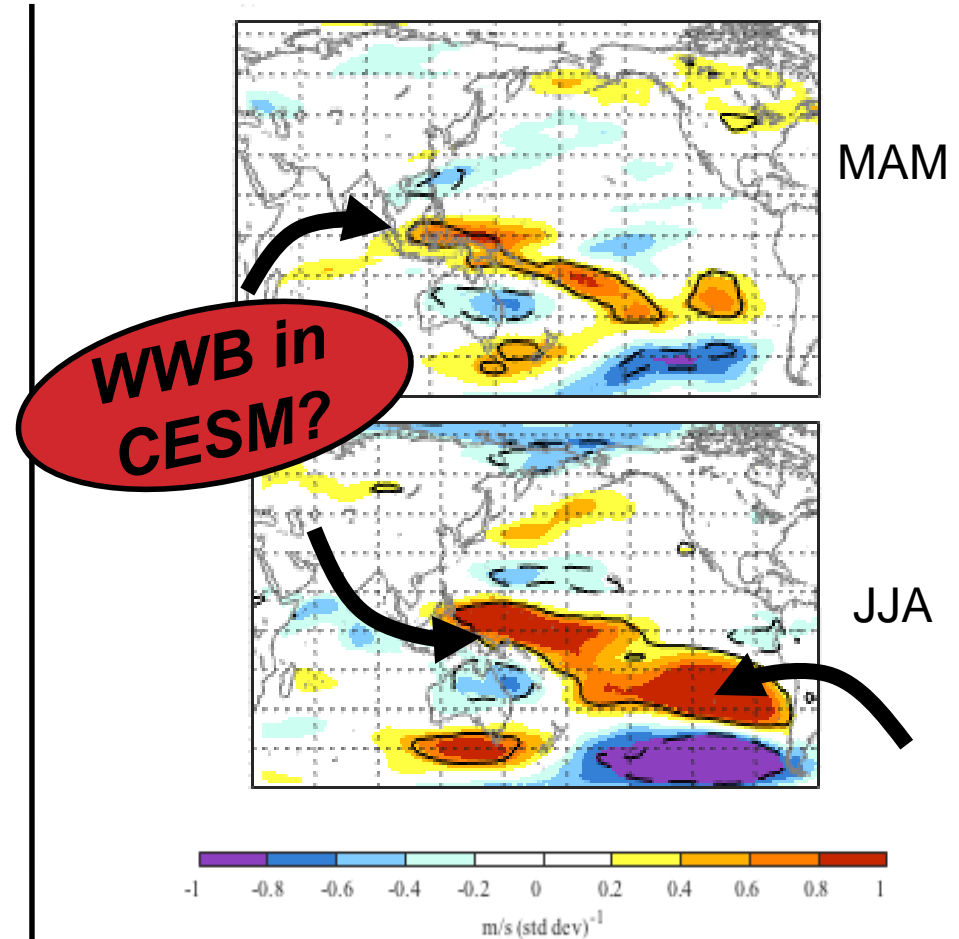
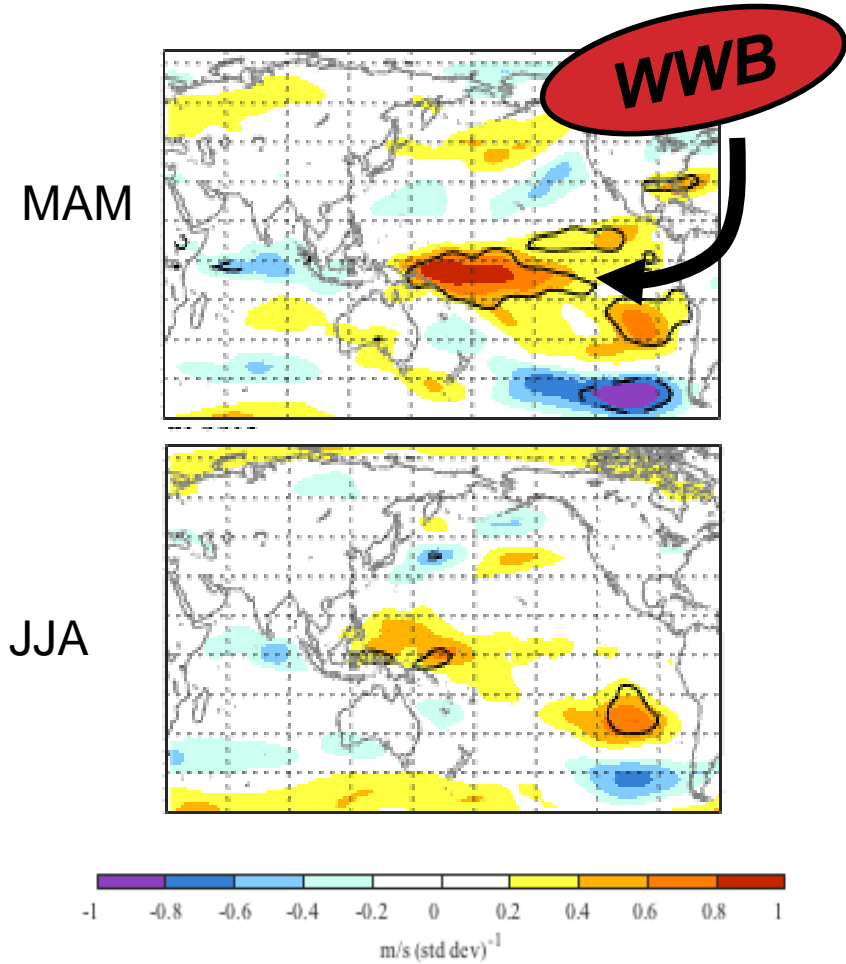




# Noise: EP 850mb Zonal Wind

Observations

CESM-LE

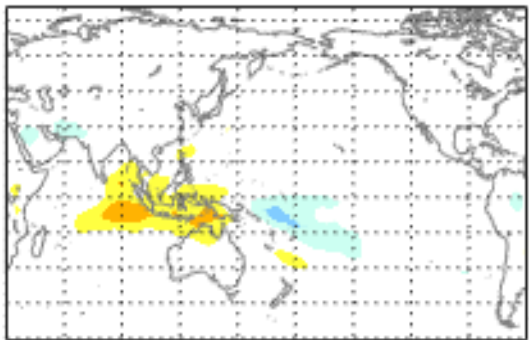


# Noise: EP OLR

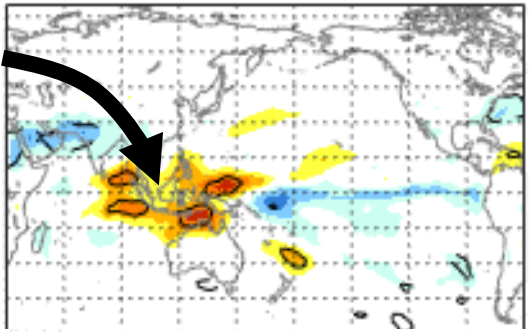
Observations

CESM-LE

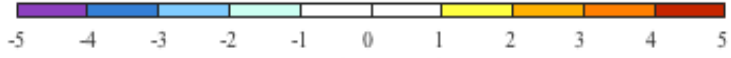
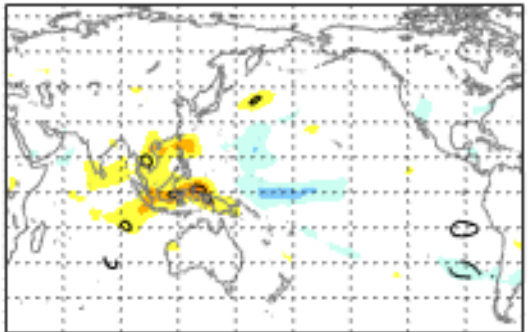
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MAM

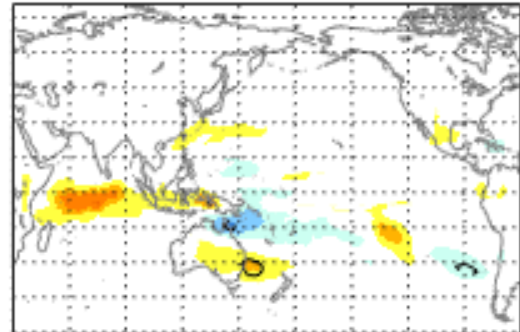


JJA

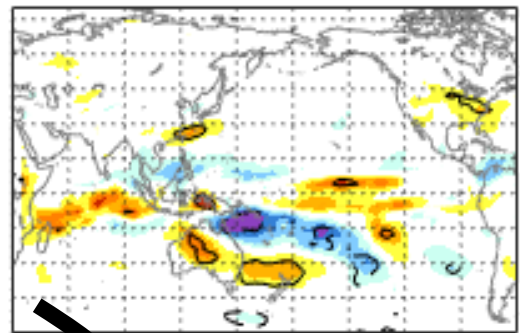


$W/m^2$  (std dev) $^{-1}$

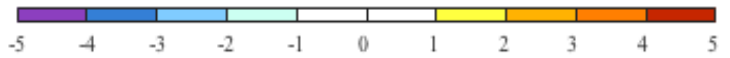
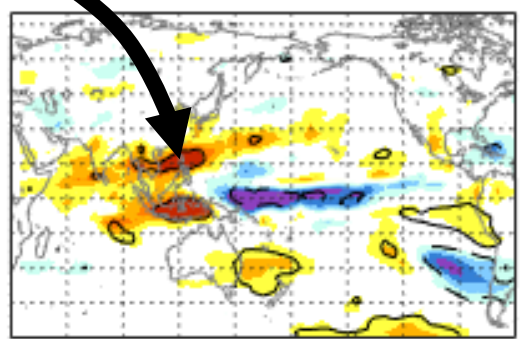
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MAM



JJA



$W/m^2$  (std dev) $^{-1}$

# Final Remarks:

## 1. Central Pacific:

- Optimal initial condition: **Pacific Meridional Mode**
- Noise forcing: **North Pacific Oscillation (DJF)**

## 2. Eastern Pacific:

- Optimal initial condition: SST anomalies in Eastern Pacific, depressed thermocline
  - Kelvin Wave / Thermocline
- Noise forcing: Zonal Wind anomalies (MAM)
  - WWB

## 3. Differences in CESM-LE analysis:

- CP Optimal + final
- EP Optimal + final
- EP Noise Variance: peaks in JJA
- EP Wind Structures: JJA

Thank you!