



MOM6 Capabilities for Modeling Sea Level Rise

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NOAA/GFDL and Princeton AOS/CICS

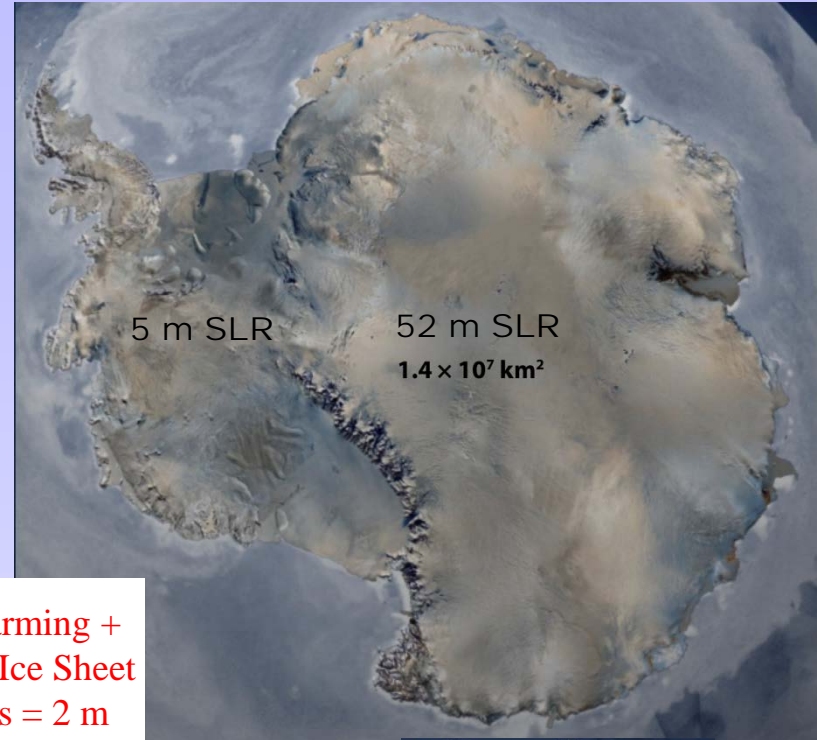
with contributions from

Alistair Adcroft, Steve Griffies, Matt Harrison,
Gustavo Marques, Olga Sergienko & Alon Stern

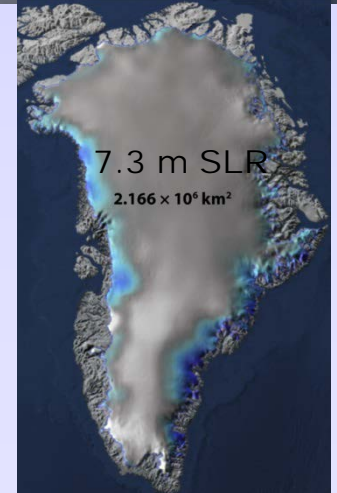
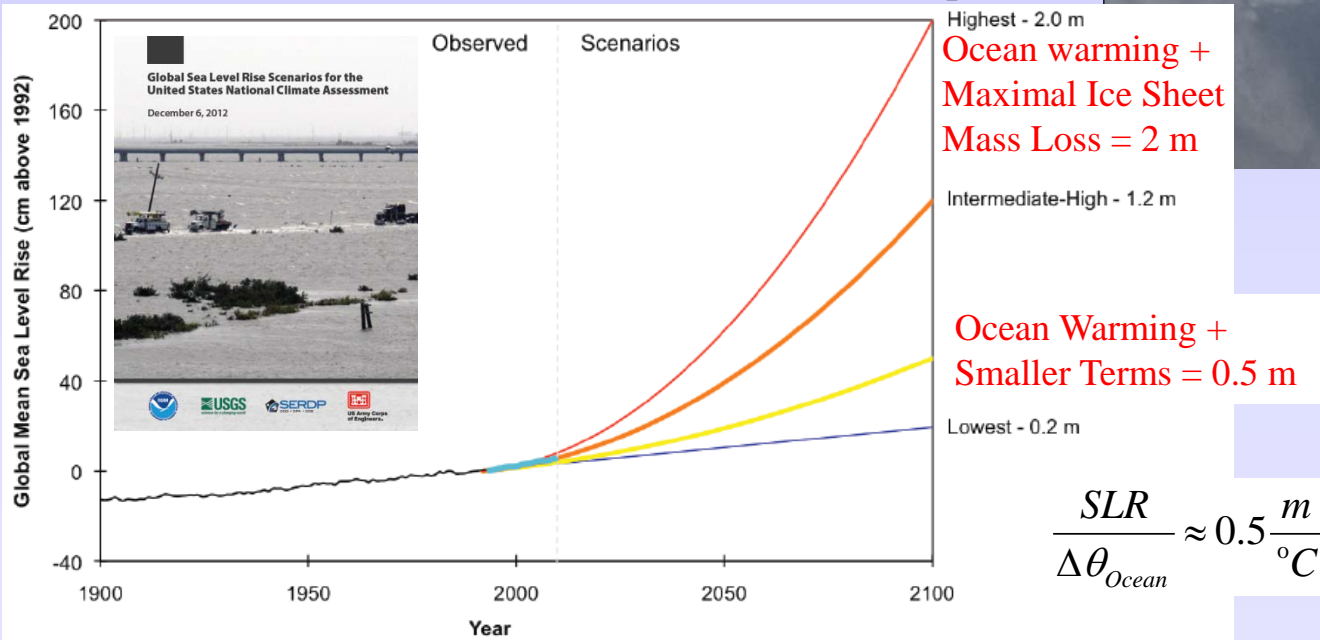


Projecting Sea Level Rise

- Sea levels are rising for a variety of reasons in oceans, mountain glaciers, ice-sheets & land
- Ocean expansion due to warming is currently the largest source of global sea level rise
- Ice sheet mass loss is the largest term and largest source of uncertainty in 21st century sea level rise projections.



Sea Level Rise Scenarios from 2012 NOAA/CPO Report





3 Ocean Modeling Challenges for Predicting Sea Level Rise

- **Controlling diapycnal diffusion in the ocean**

Numerical ocean models introduce spurious mixing.

- Arbitrary Lagrangian Eulerian (ALE) approach
- Hybrid/Isopycnal coordinates

Physically based (energetically constrained) mixing parameterizations need to regulate diapycnal mixing

- **Dynamically interactive ice-sheets**

- Continuous evolution of the ice-ocean boundaries at the grounding line and within ice-shelf cavities

- **Icebergs and ice-ocean coupled instabilities**

- (Full talk tomorrow)



The Ocean's Role in Climate Change

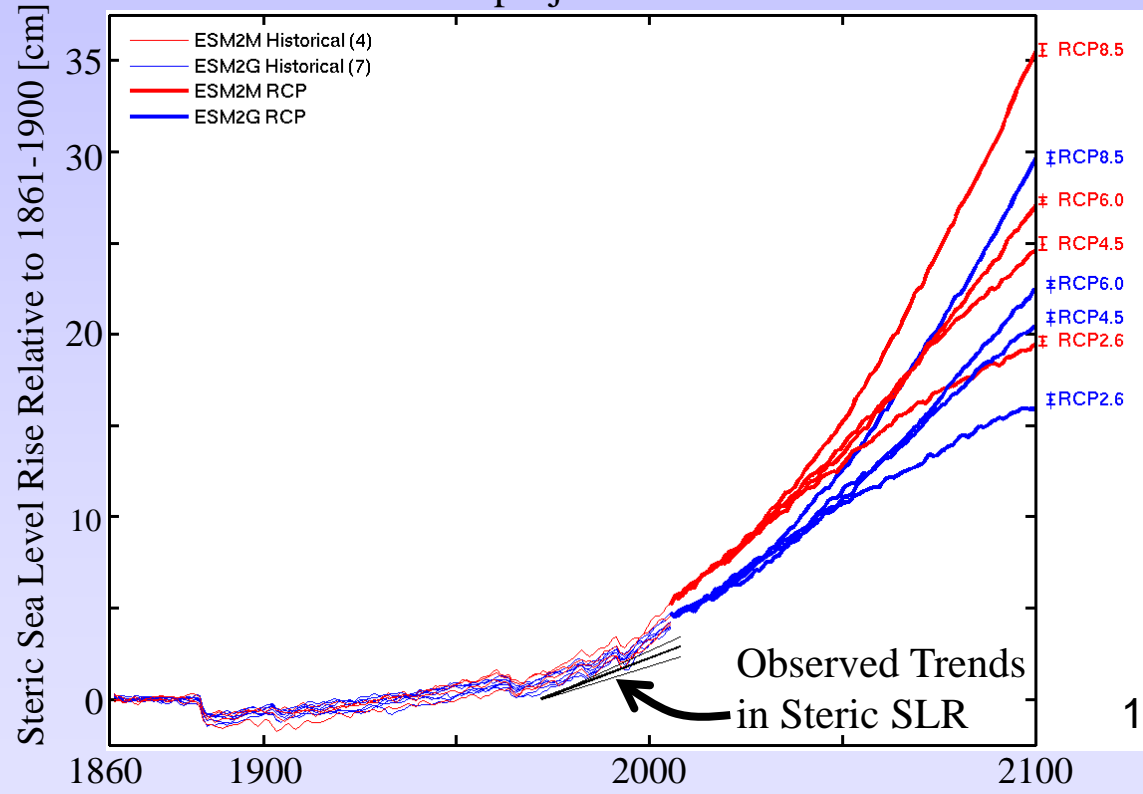
Steric Sea Level Rise

Exploring the dynamics of Sea Level Rise

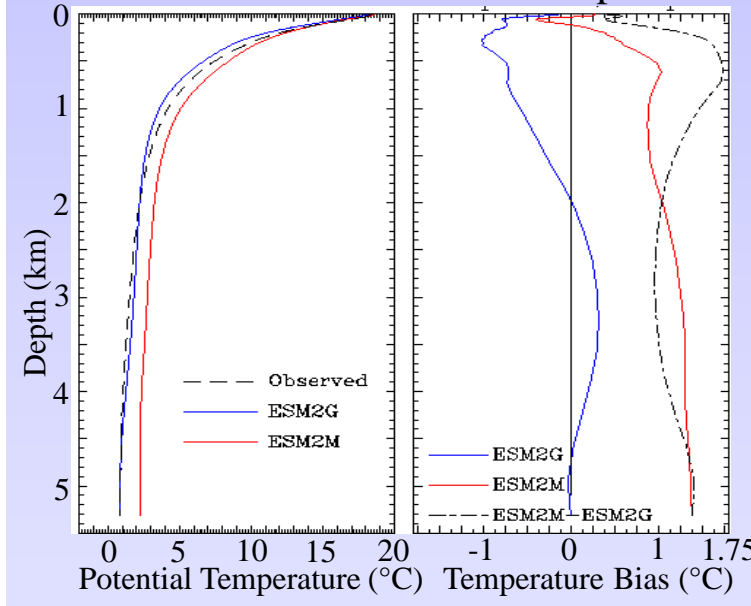
ESM2M & **ESM2G** – same atmosphere & ecosystems, different ocean models.

ESM2G – Isopycnal Coordinate Ocean
ESM2M – Z* Coordinate Ocean

Historical & Scenario-projected Steric Sea Level Rise



ESM2G & **ESM2M** 1980-2000
Horizontal-Mean Ocean Temperature



18% larger steric SLR in ESM2M

9% due to more & deeper heat uptake

7% due to warmer spun-up ocean

Ref: Hallberg et al., 2013, *J. Climate*

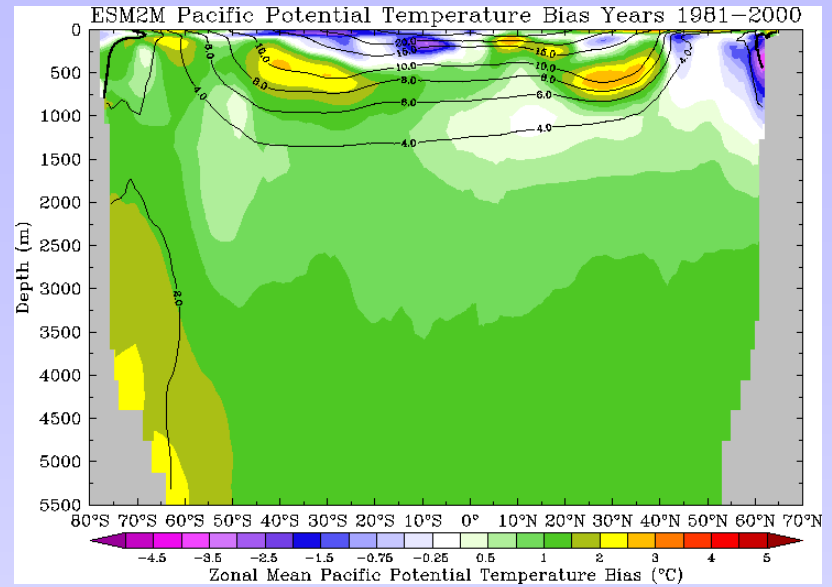
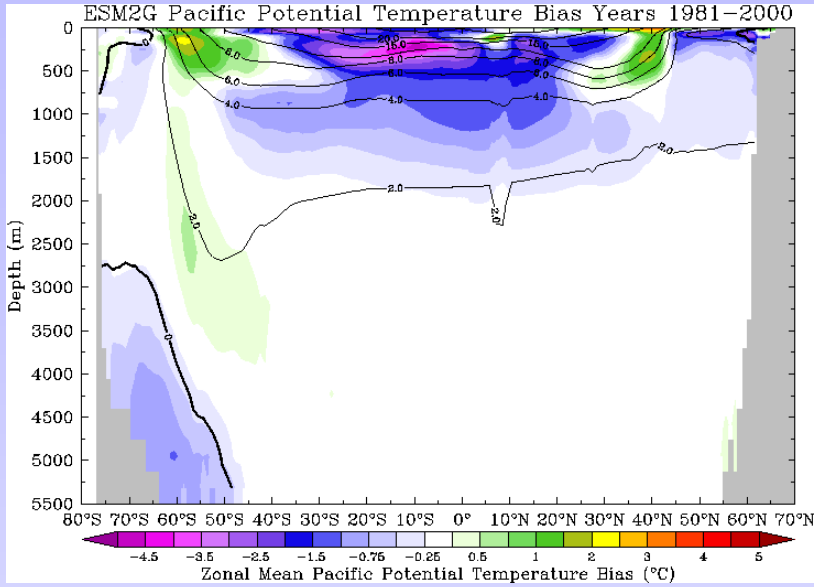


Pacific Ocean 1981-2000 Zonal-mean Biases

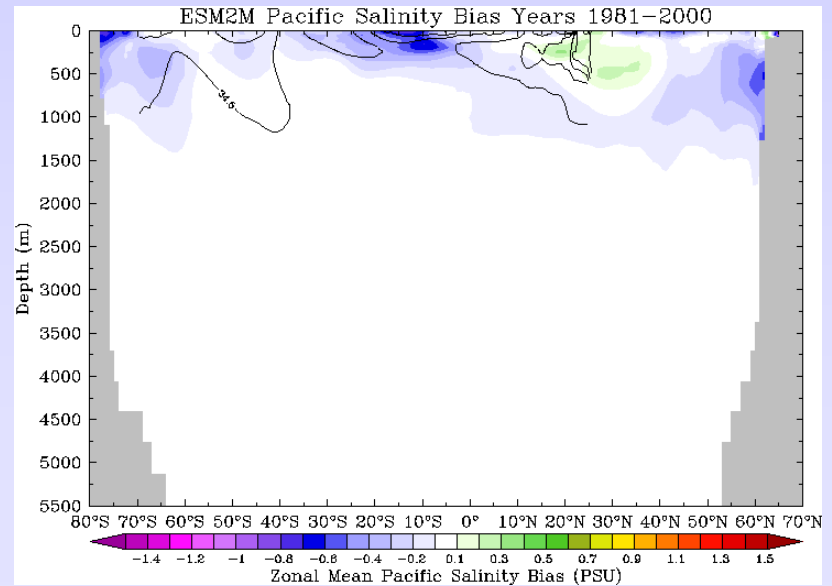
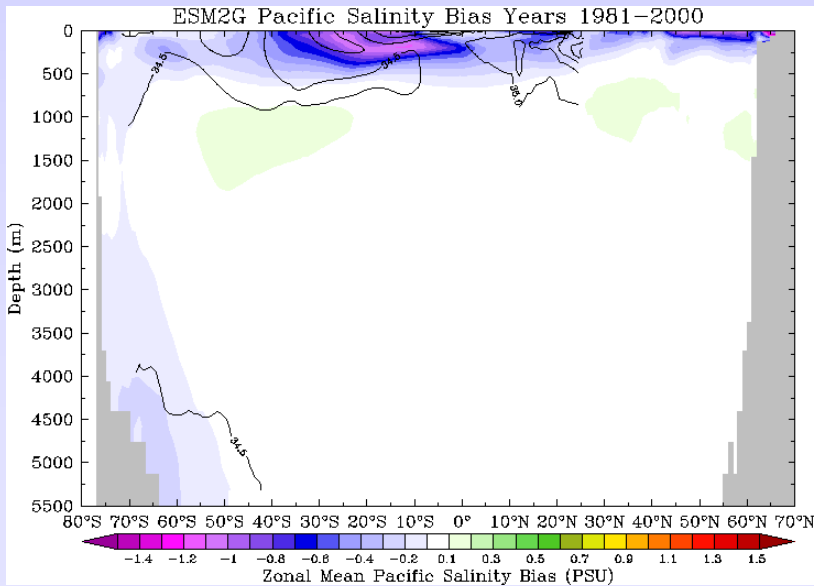
ESM2G

ESM2M

Potential Temperature



Salinity

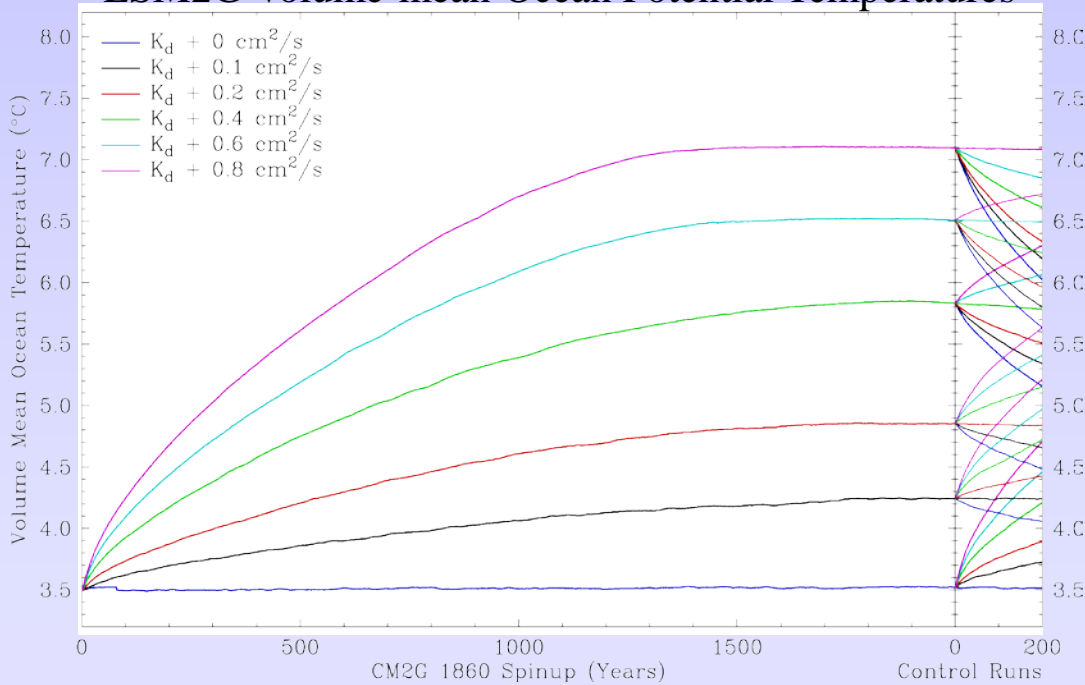




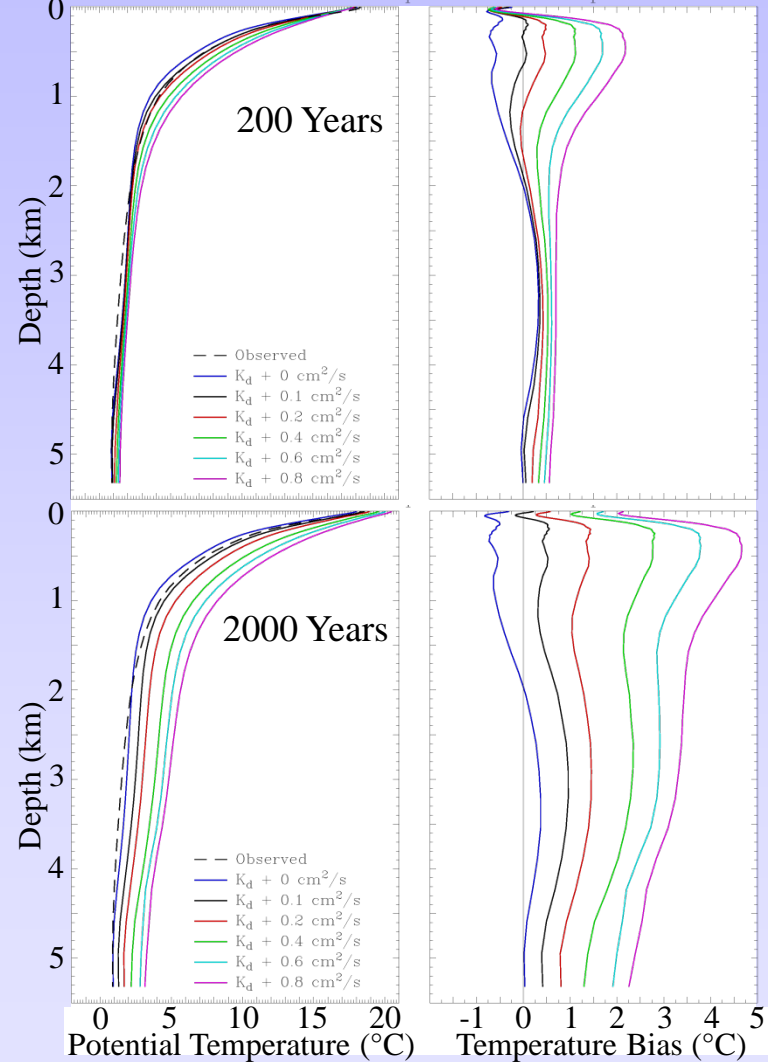
Sensitivity of the Ocean State and Steric Sea Level Rise to Diapycnal Mixing in the Ocean

Coupled model ocean drift and equilibrium bias are sensitive to the magnitude of diapycnal diffusion (mixing) in the ocean.

ESM2G Volume-mean Ocean Potential Temperatures



Horizontal Mean Ocean Temperature and Bias with Various Added Ocean Diffusivities



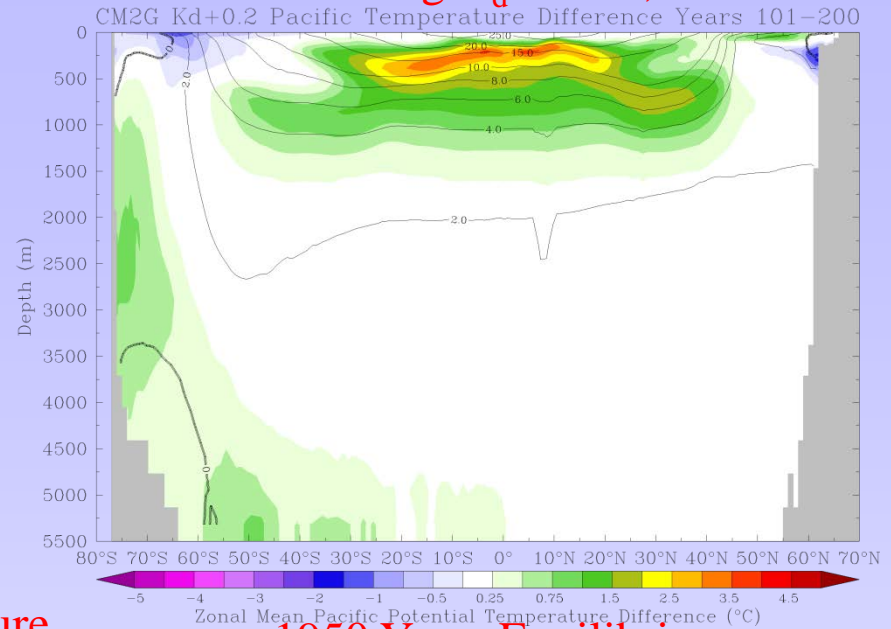
Ref: Hallberg, Melet & Samuels, 2018?



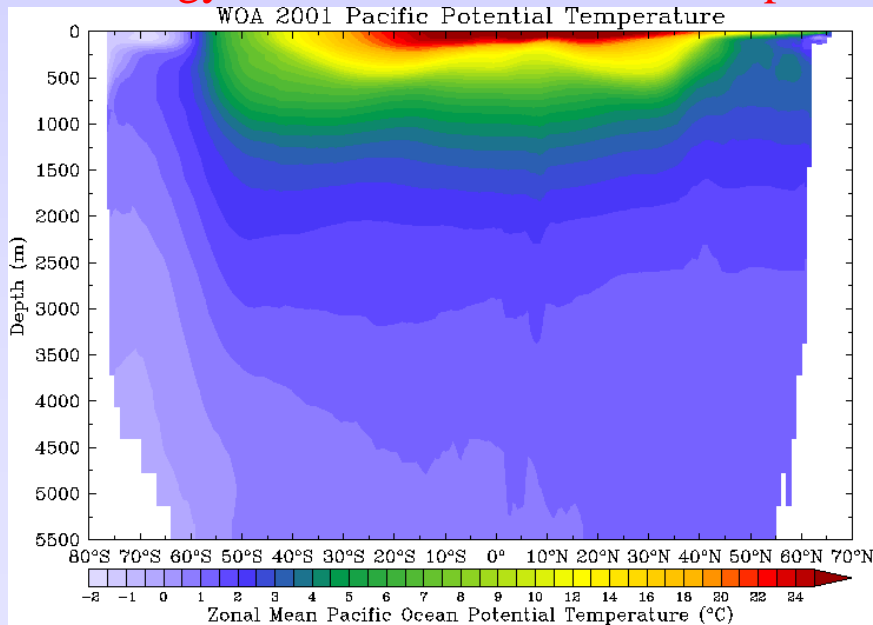
Pacific Temperature Response to Increased Diapycnal Diffusivity

- Increasing diffusivity warms the ocean
- Warming occurs first and most strongly in the main thermocline, but later throughout the ocean

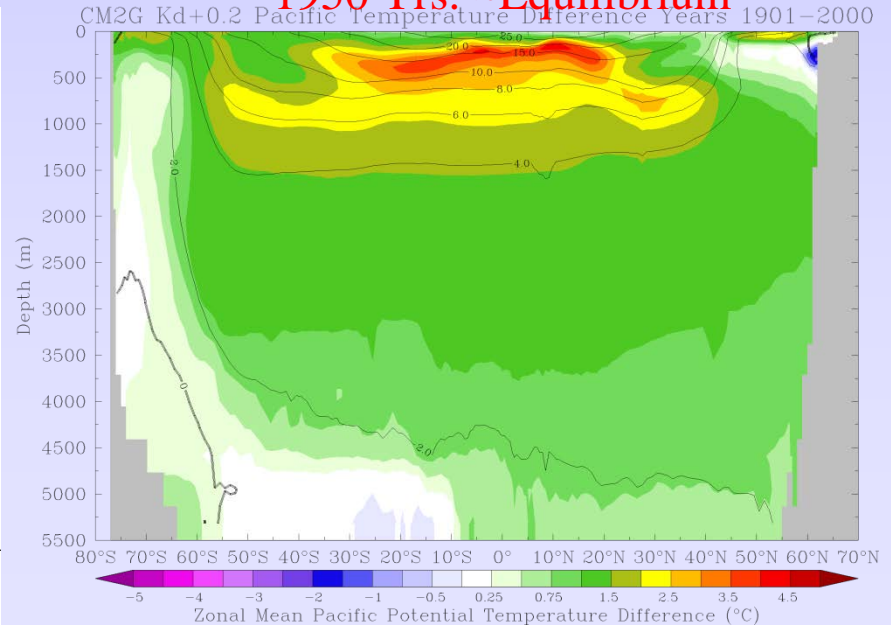
Effect of Increasing K_d 2×10^{-5} , 150 Yrs.



Climatology of Zonal Mean Pacific Temperature



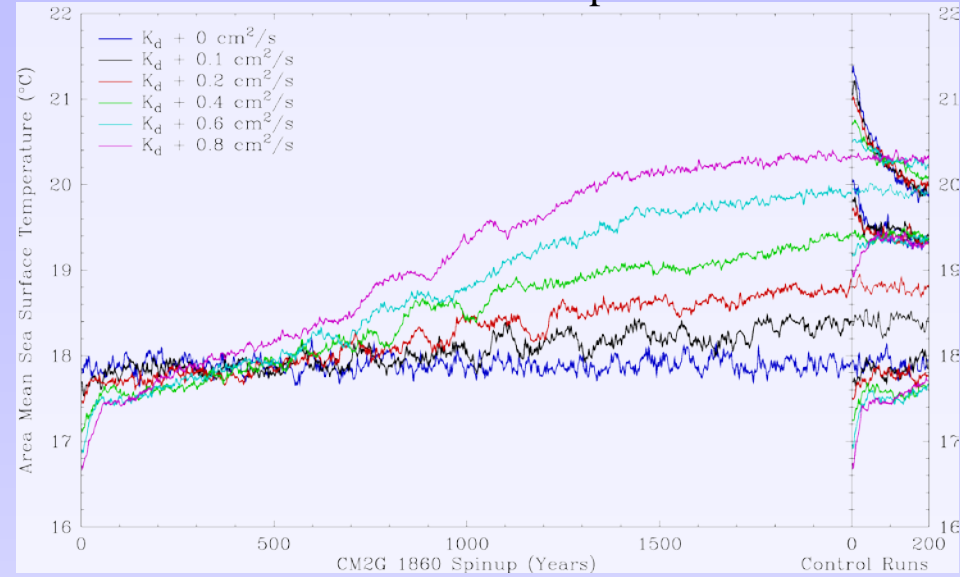
1950 Yrs. ~Equilibrium



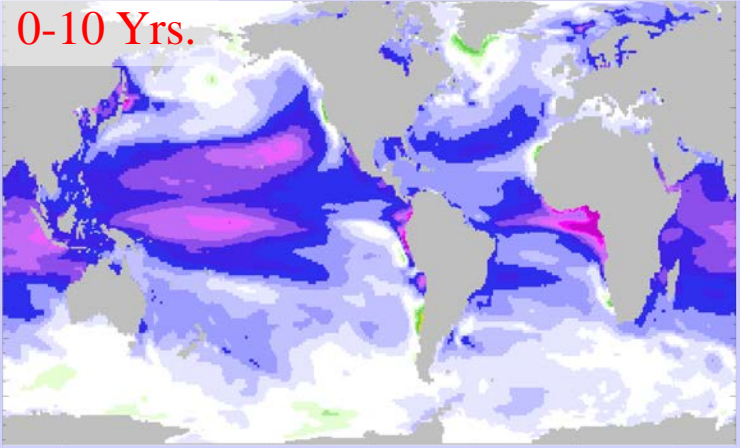


Diffusivity induced changes over time in Coupled Model Sea Surface Temperatures

Global Mean Sea Surface Temperature over Time

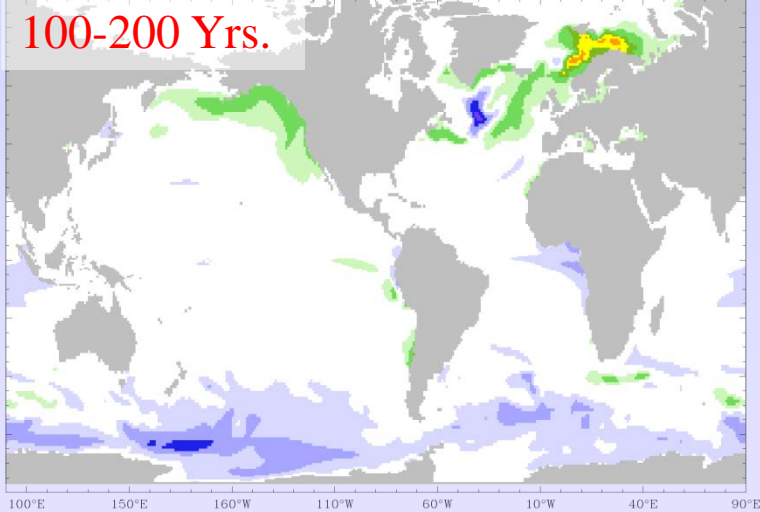


SST Change after Increasing K_d $2 \times 10^{-5} \text{ m}^2/\text{s}$



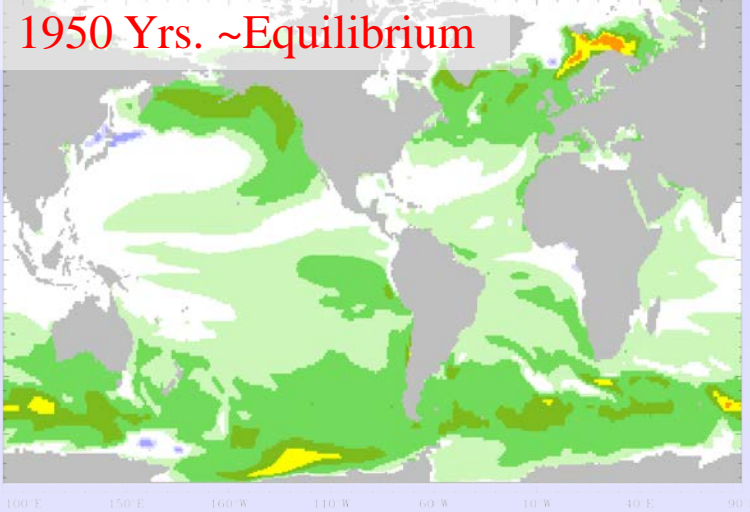
-1 Year 0-10 SST Differences (°C) 1

RMS: 0.49°C, 90°S-30°S 0.6°C, 30°S-30°N 0.29°C, 30°N-90°N 0.7°C 101-200



Sea Surface Temperature Differences (°C)

RMS: 1.08°C, 90°S-30°S 1.48°C, 30°S-30°N 0.68°C, 30°N-90°N 1.25°C 1901-2000



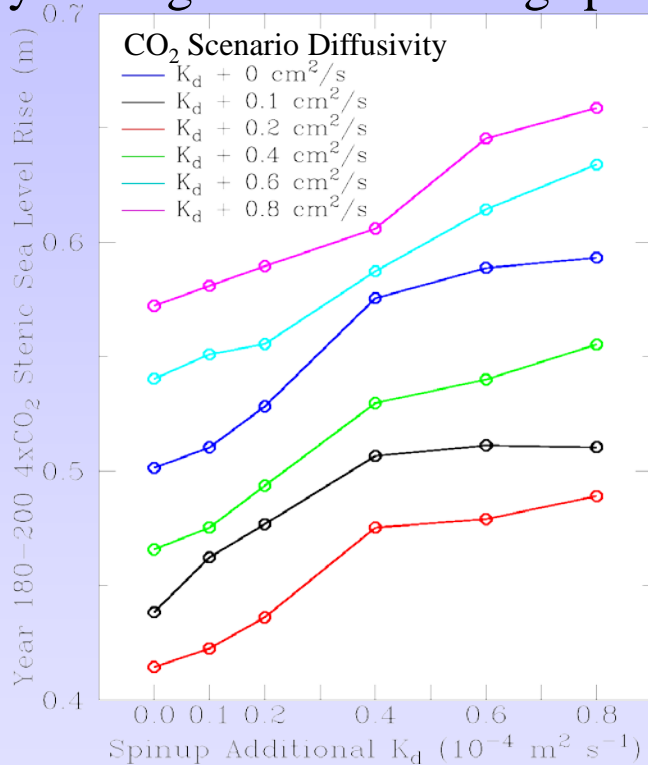
Sea Surface Temperature Differences (°C)



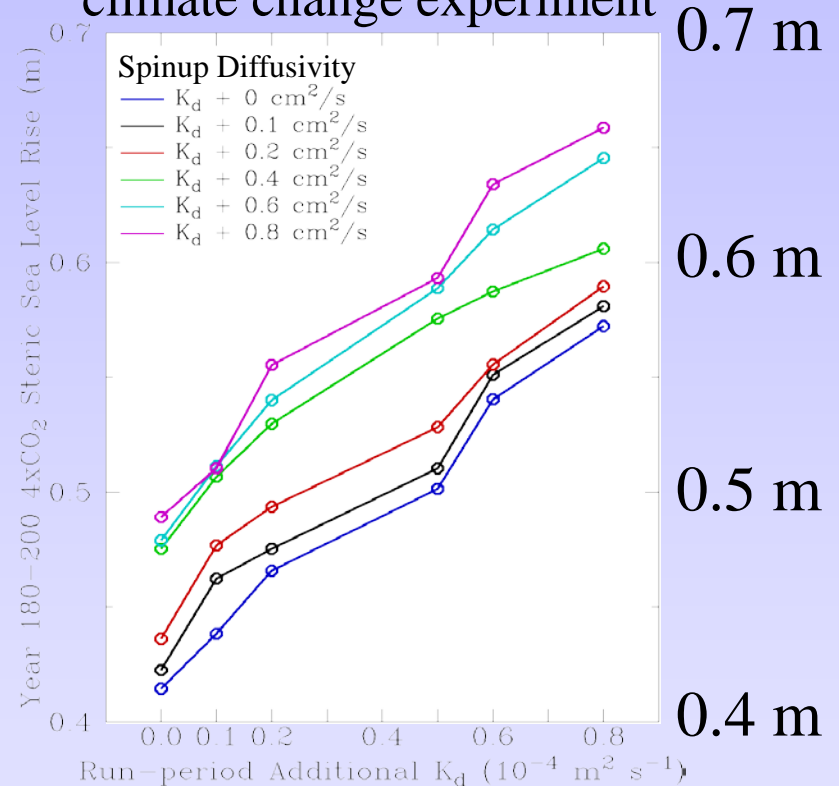
Sensitivity of Sea Level Rise to Ocean Diapycnal Mixing

Steric Sea-Level Rise after 200 Years in 1%/year to 4x CO₂ Run, Relative to Control

Changing initial conditions by adding diffusion during spinup



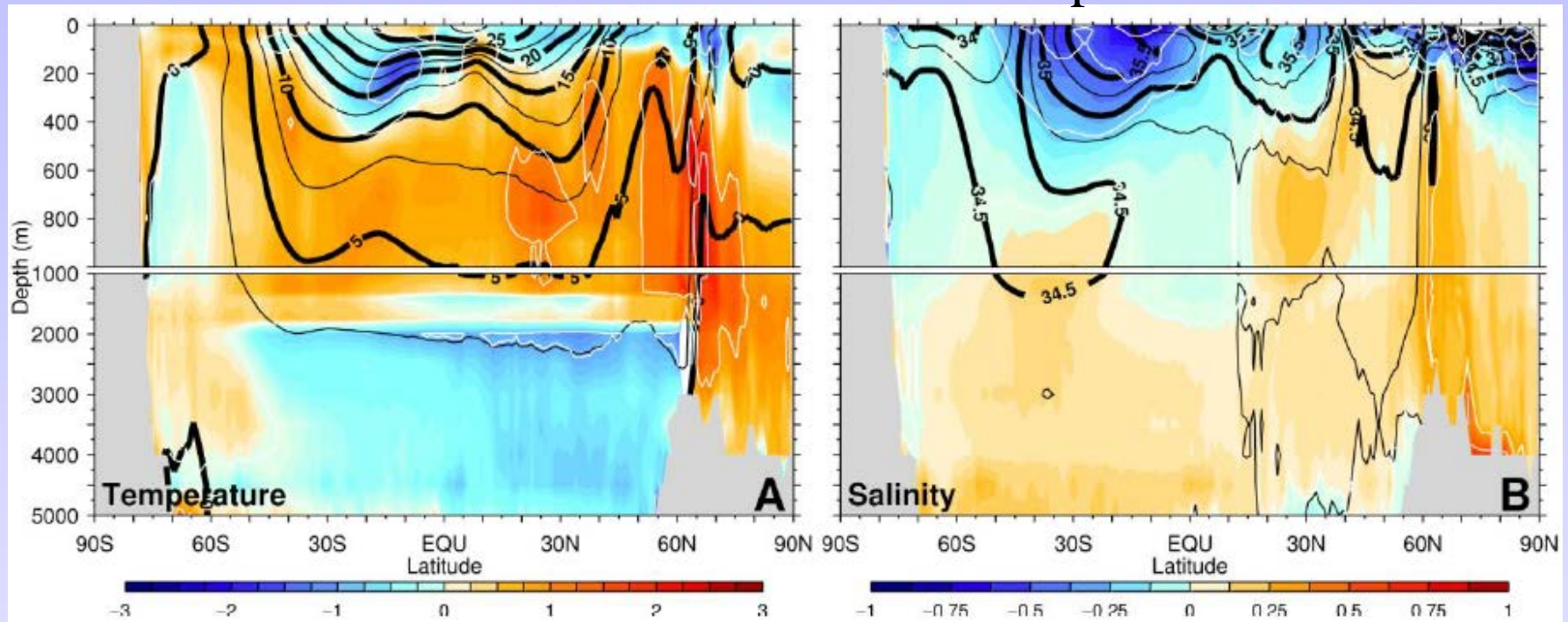
Adding diffusion during the climate change experiment



Adding diapycnal diffusion increases steric sea level rise both by increasing heat uptake and by warming the ocean (warmer water expands more when heated). Both the initial conditions and mixing during the run contribute significantly.

CMIP5 Ensemble mean biases

Zonal Mean Ocean Temperature and Salinity Biases in Ensemble Mean of CMIP5 Coupled Models



IPCC AR5 WG-I Fig. 9.13

- The majority of CMIP5 Coupled Climate Models have an overly broad and warm lower main thermocline.
- This is broadly consistent with excessive (numerical?) diapycnal diffusion.



The Arbitrary Lagrangian Eulerian method

Solve equations in 2 phases:

- a **Lagrangian** dynamic update (shallow water eqns.)
- **Vertical remapping to an arbitrary (Eulerian?) coordinate**

Momentum eqn.:

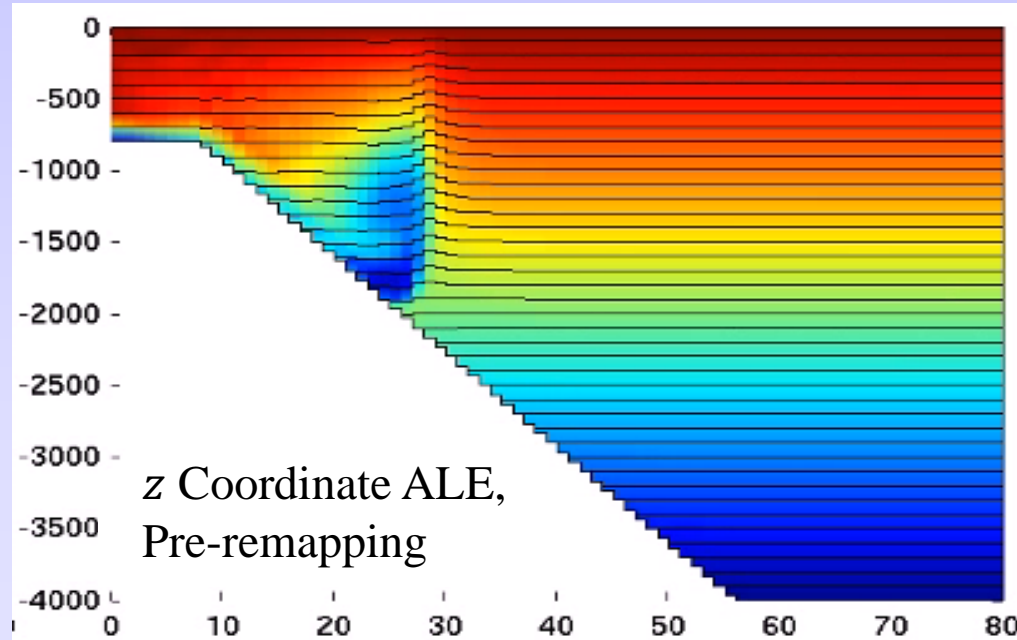
$$\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla_s \mathbf{u} + (f + \nabla_s \times \mathbf{u}) \hat{k} \times \mathbf{u} = -\frac{1}{\rho} \nabla_s p - \nabla_s \left(\phi + \frac{1}{2} \|\mathbf{u}\|^2 \right) + \frac{1}{\rho} \nabla \cdot \tilde{\tau}$$

Continuity eqn.:

$$\frac{\partial}{\partial t} \left[\left(\frac{\partial p}{\partial s} \right) \right] + \nabla_s \cdot \left(\mathbf{u} \frac{\partial p}{\partial s} \right) + \frac{\partial}{\partial s} \left[\mathbf{u} \frac{\partial p}{\partial s} \right] = 0$$

Tracer eqn.:

$$\frac{\partial}{\partial t} \left[\left(\frac{\partial p}{\partial s} \theta \right) \right] + \nabla_s \cdot \left(\mathbf{u} \frac{\partial p}{\partial s} \theta \right) + \frac{\partial}{\partial s} \left[\mathbf{u} \frac{\partial p}{\partial s} \theta \right] = Q \frac{\partial p}{\partial s}$$



ALE advantages:

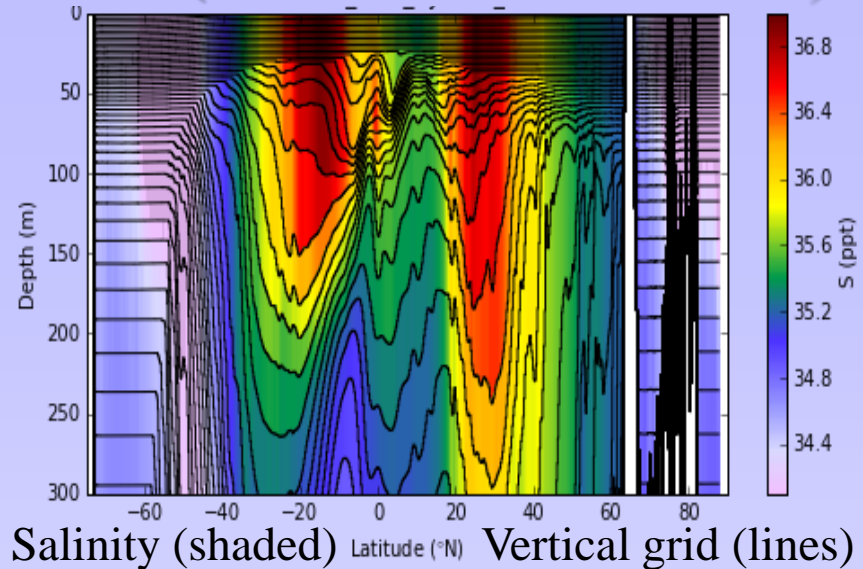
- Flexible vertical coordinates
- Remapping imposes no vertical CFL limit on timesteps
- Tracer advection not required to represent gravity waves



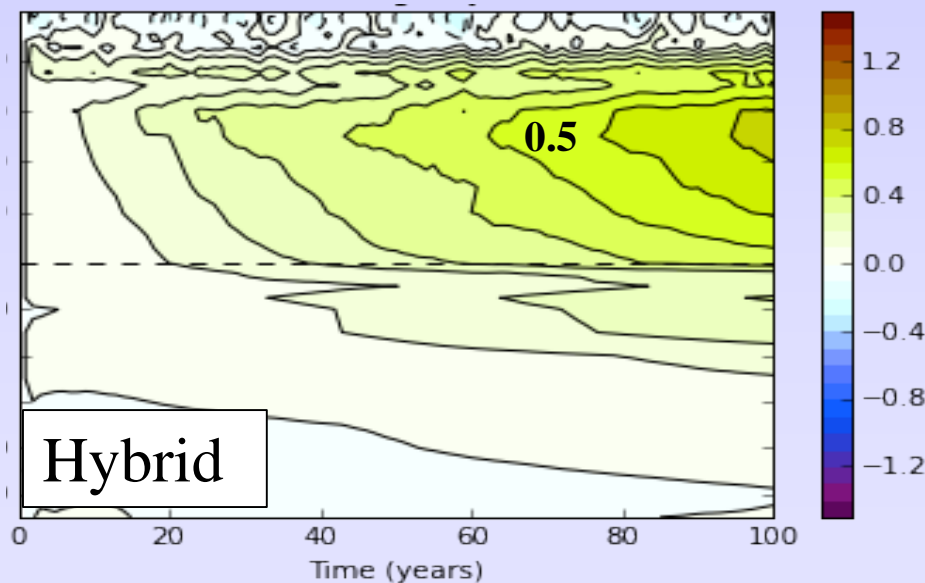
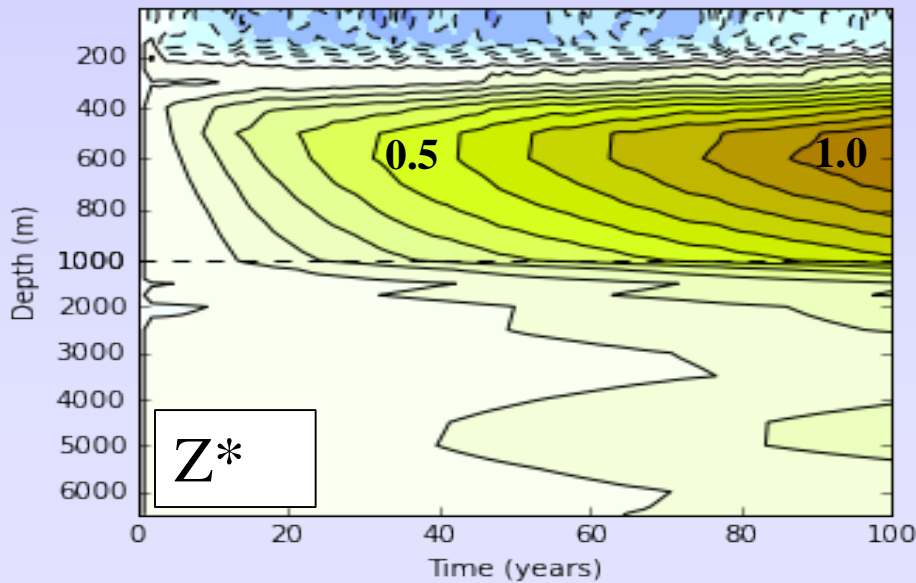
Role of vertical coordinate ($1/4^\circ$ ocean in CM4)

Changing vertical coordinate alone

- z^* to hybrid z^*/ρ_2 (a.k.a. HYCOM)
- Identical parameterizations and atmospheric models
- Reduced heat uptake by 0.27 Wm^{-2}

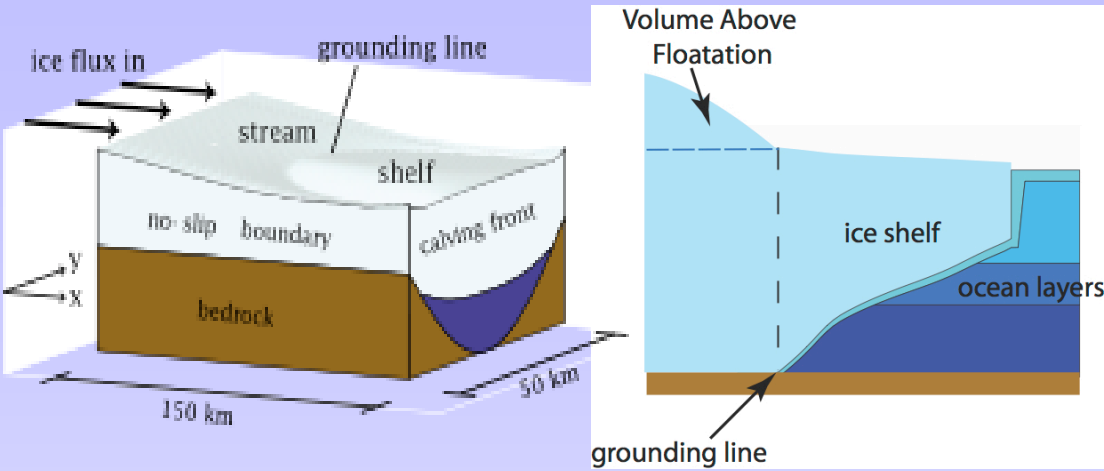


Horizontal Mean Temperature Drift

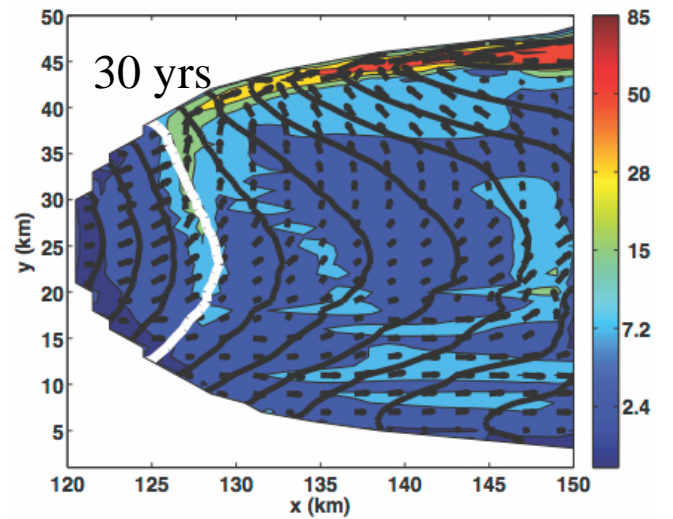
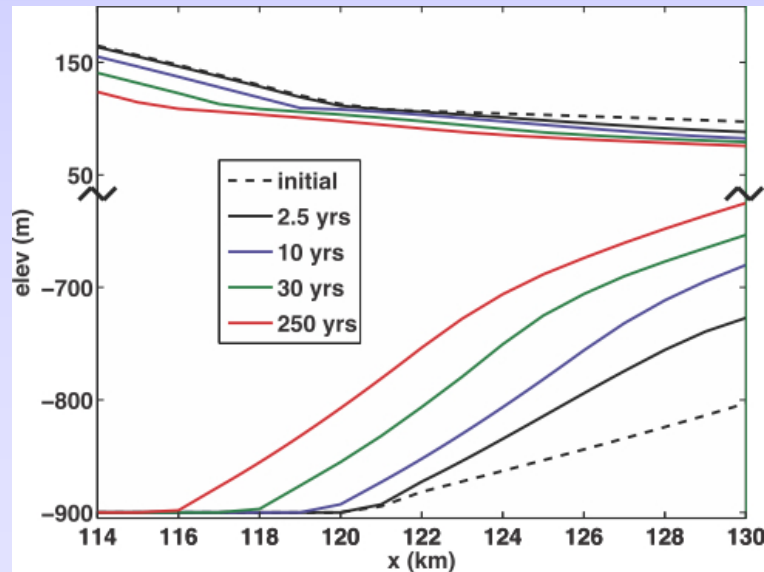
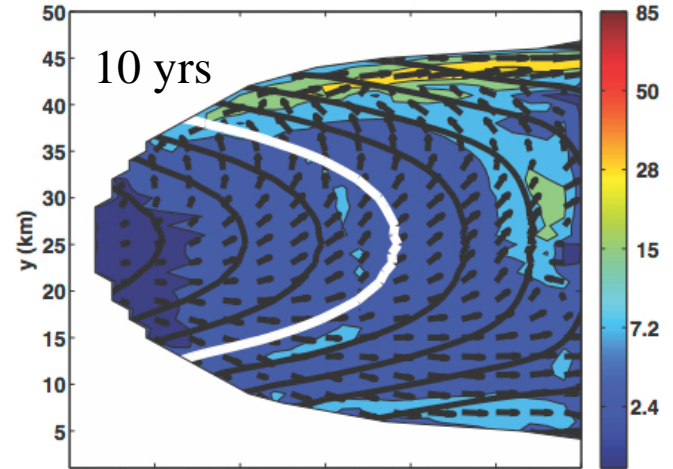




Dynamic Ice-shelf-ocean Interactions



Melt rates (m yr^{-1})



Goldberg et al., *JGR* (2012)



Dynamically Evolving Ice Shelf Cavities

- Melt-driven flow in ice shelf cavities simulated with evolving ice shelf model coupled to ocean
 - Moving upper boundary
 - Moving grounding line
- Note ocean squashed between shelf and bottom
- Preparing $\frac{1}{8}^\circ$ coupled ocean-ice-shelf global simulations



Study by Gustavo Marques (2017)



MOM6 changes to permit dynamically evolving ice-shelf cavities and moving ground lines

- Do not approximate total ocean thickness by bottom depth
- Nonlinear barotropic continuity solver, including a local linearization about the transports from the layers and appropriate limits for strong flows

$$\eta \equiv \sum_k h_k - H_{Bottom} \quad \frac{\partial h_k}{\partial t} + \nabla_s \cdot (uh_k) = 0 \quad uh_k = \frac{1}{\Delta t} \int_{-u_k \Delta t}^0 h(x) dx$$

$$\frac{\partial \eta}{\partial t} + \nabla_s \cdot \left(\sum_k uh_k \right) = 0 \quad U(\bar{u}) = \sum_k u^0 h_k + \left(\sum_k \frac{\partial uh_k}{\partial u_k} \right) (\bar{u} - \bar{u}^0)$$

$$\frac{\partial \eta}{\partial t} + \nabla_s \cdot U(\bar{u}) = 0 \quad \frac{\partial \bar{u}}{\partial t} + f\hat{k} \times (\bar{u} - \bar{u}^0) = -g\nabla(\eta - \eta^0) + \left(\sum_k h_k \frac{\partial u_k}{\partial t} / \sum_k h_k \right)$$

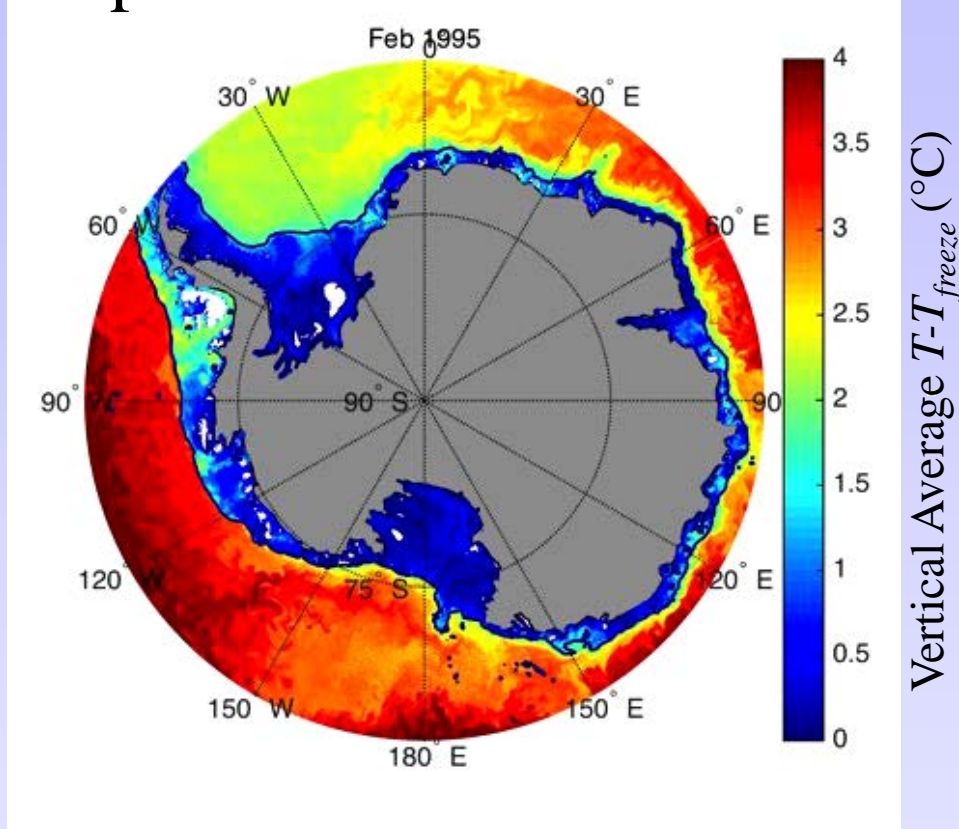
- Invert layers' piecewise parabolic method continuity solvers to find the barotropic velocity correction with the summed transport determined by the barotropic solver
- Add damping of external gravity waves by ice-shelf rigidity



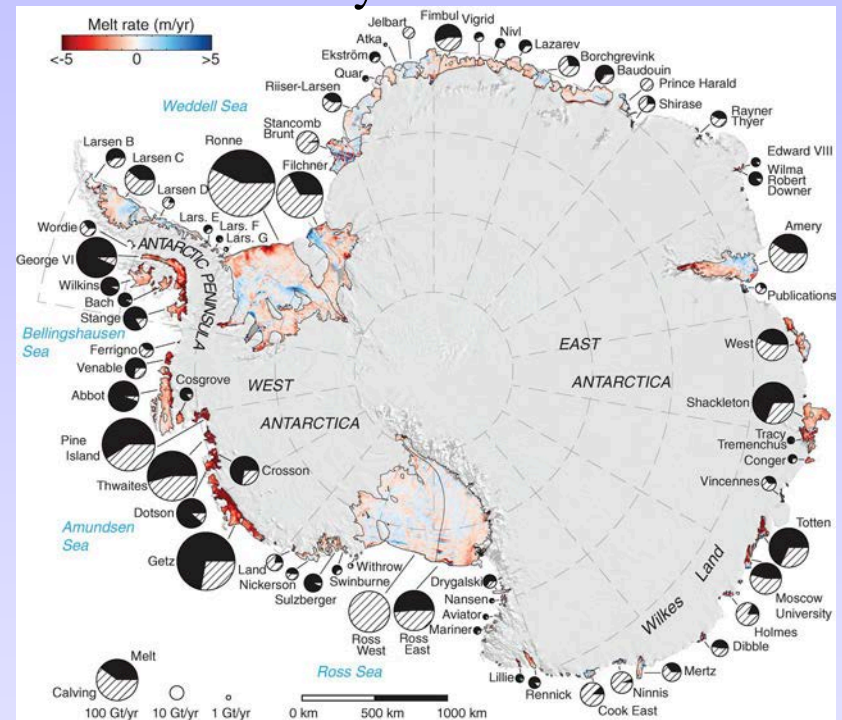
Coupled Ice-shelf-ocean Interaction

MOM6 $\frac{1}{8}^\circ$ Global Ocean Model

Coupled with Ice-Shelf/Sheet Model



Observationally Inferred Mass Loss



Rignot et al. (2013)

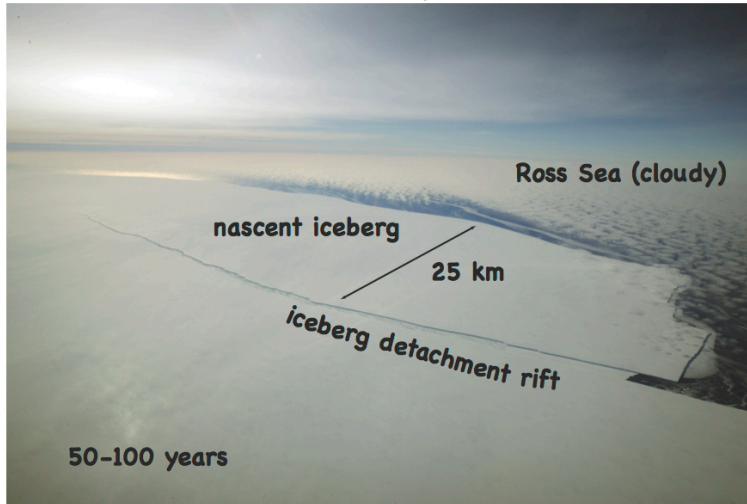
Vertically Averaged Ocean Temperature
above the in-situ Freezing Point

Sergienko, Harrison and Hallberg (2018?)

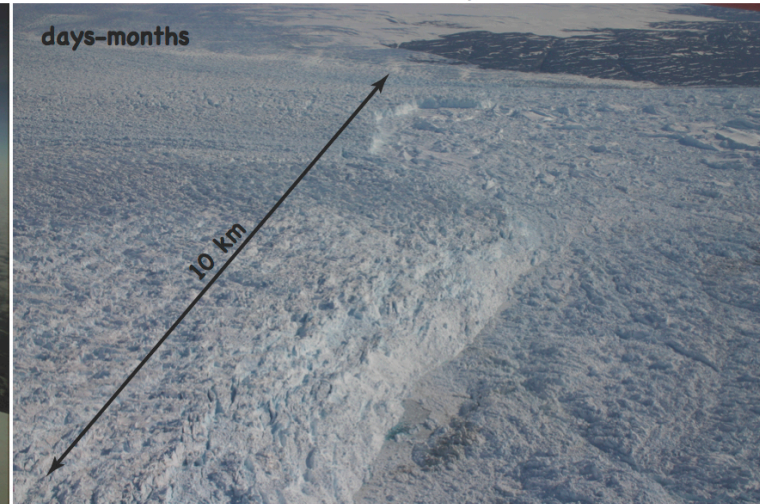


Calving of Icebergs

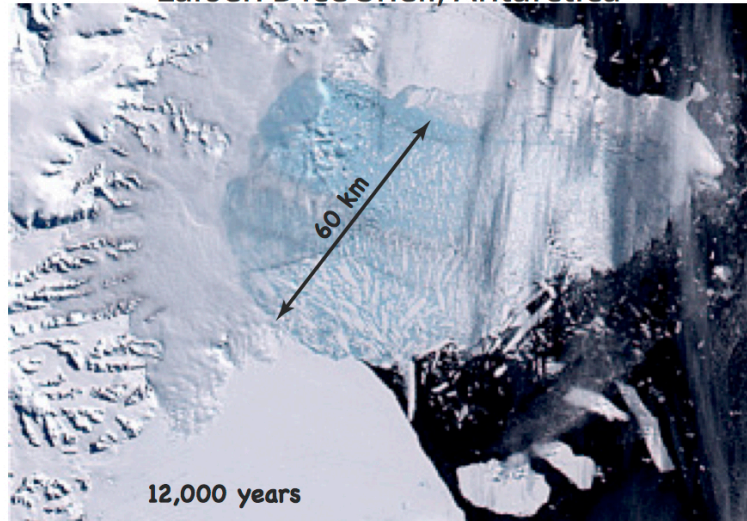
Ross Ice Shelf, Antarctica



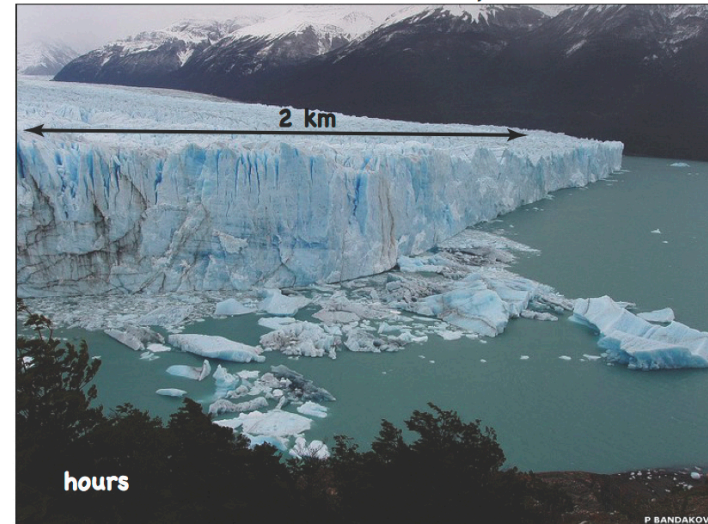
Jakovshavn Isbræ, Greenland



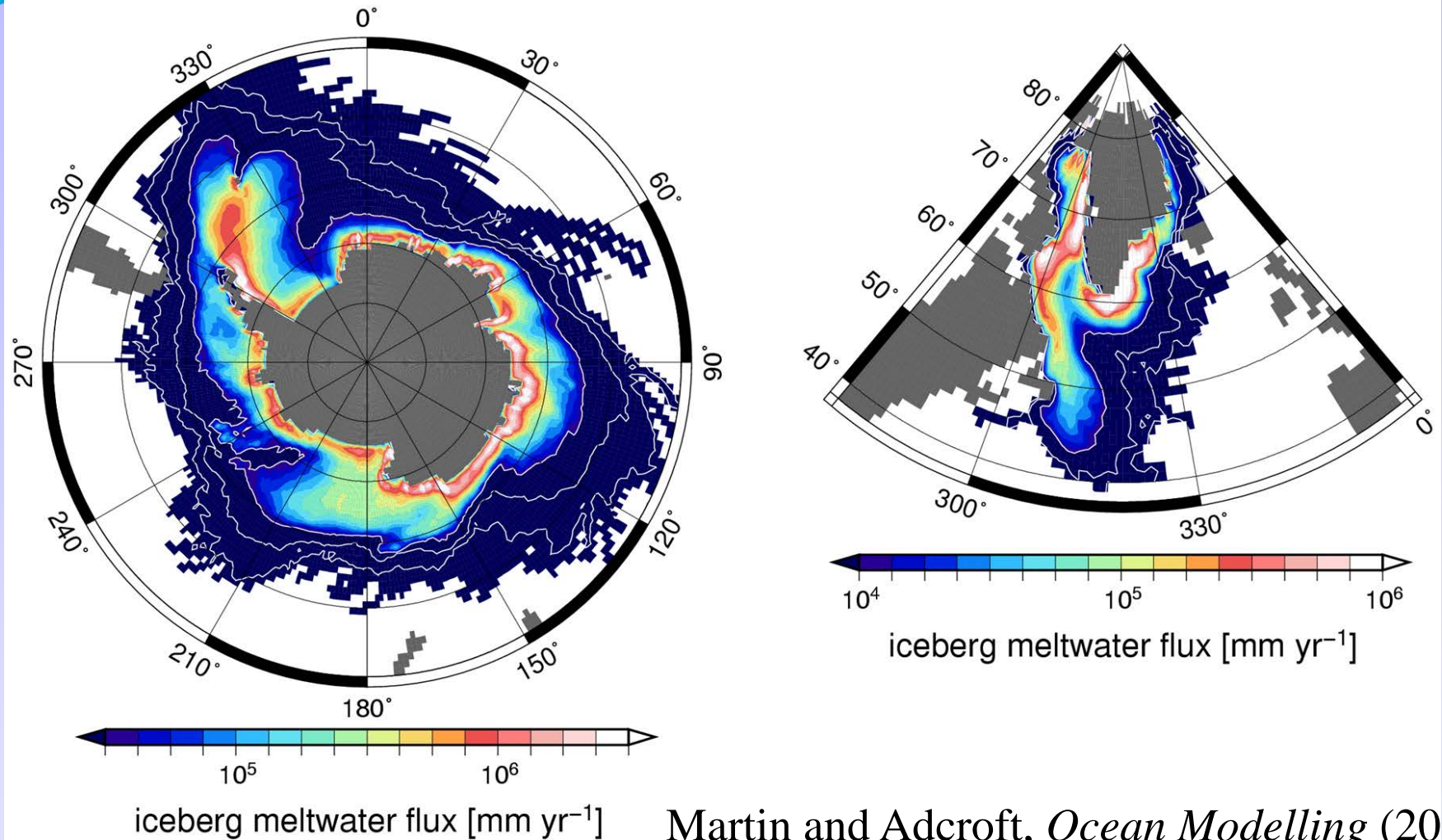
Larsen B Ice Shelf, Antarctica



Columbia Glacier, Alaska



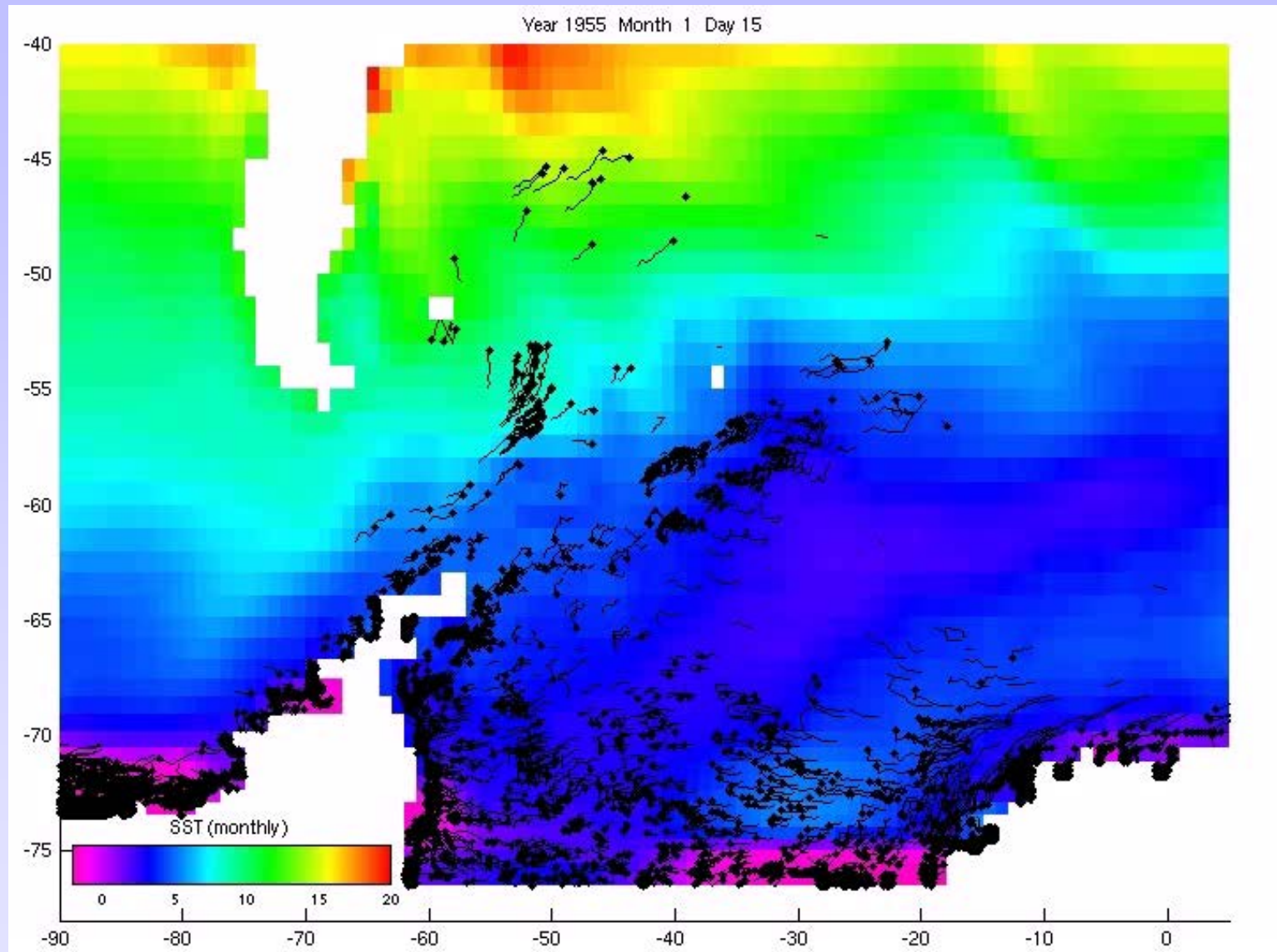
Iceberg Fresh Water Fluxes



Objective is to replace current point-iceberg representation in GFDL climate models with extensive icebergs and calving induced changes in ice-shelf extent.

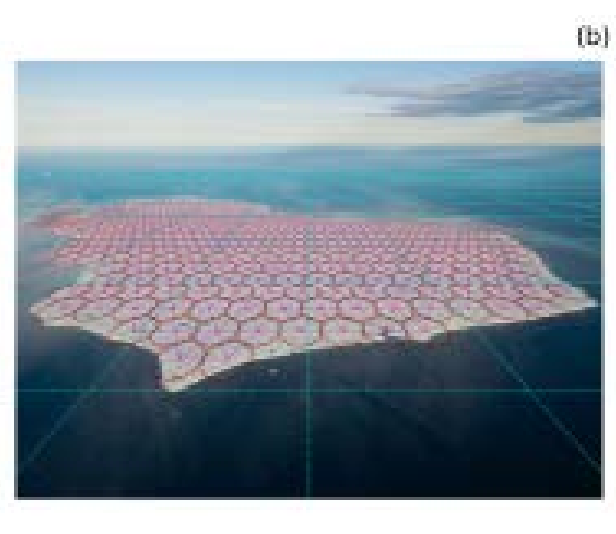
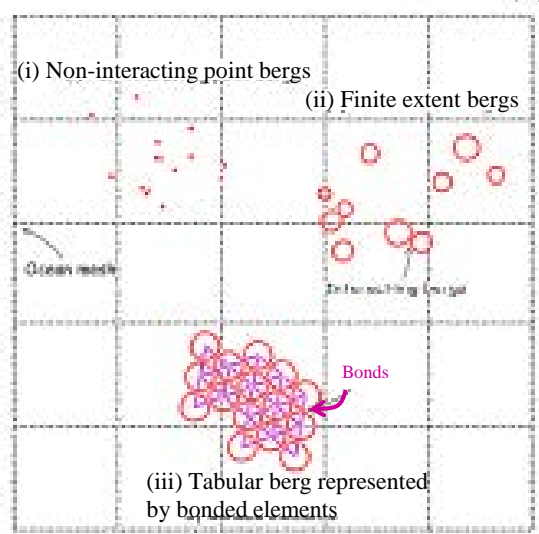
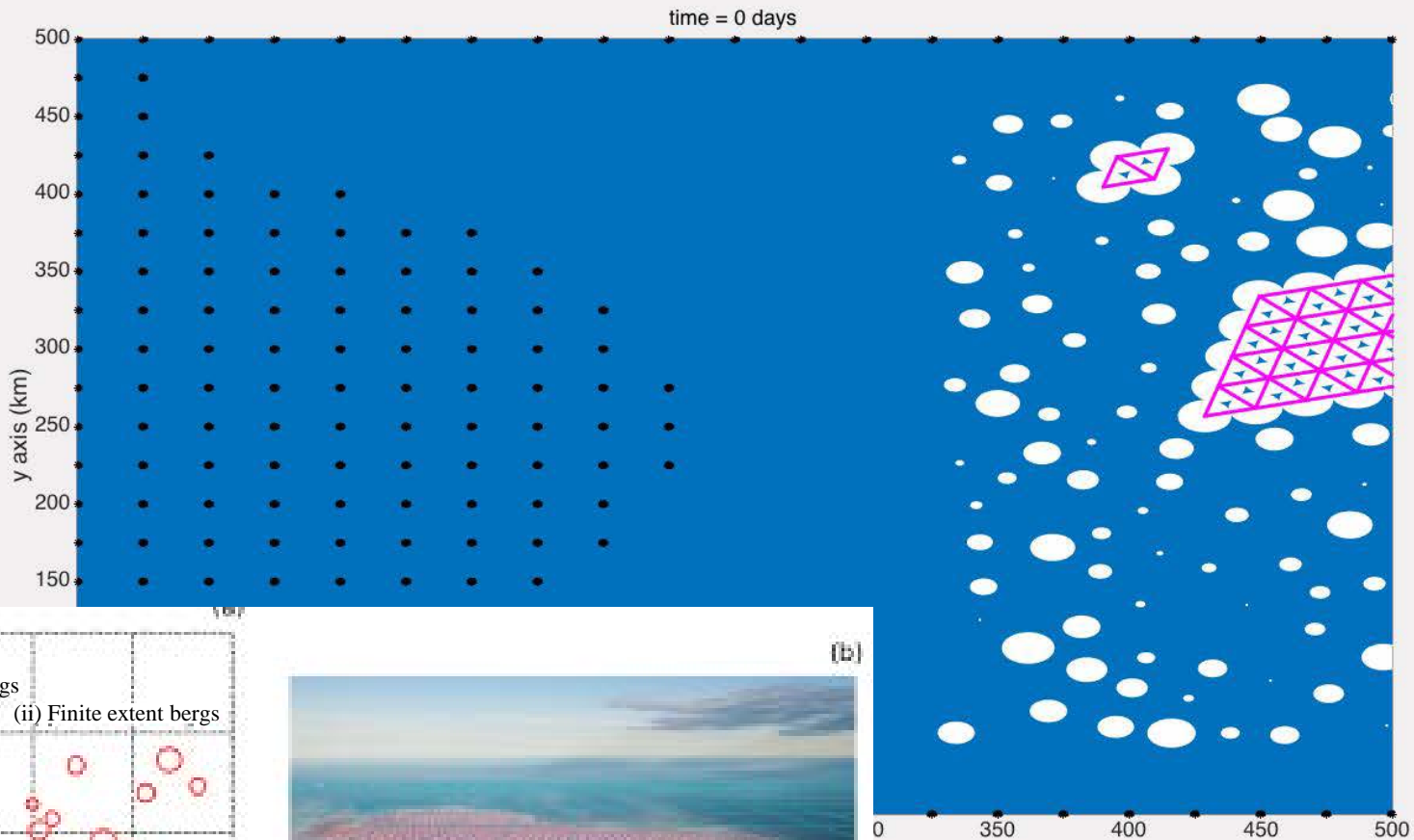


Point-Particle Model of Icebergs



Martin and Adcroft, *Ocean Modelling* (2010)

Tabular Icebergs as Bonded Particles



Courtesy Alon Stern
Stern et al. (JAMES 2017)



Iceshelf cavities and interactions with icebergs

- Iceshelf simulated by tabular iceberg model coupled to ocean

Top View

Side View
(Along Dashed Line)



Alon Stern &
Gustavo Marques



Take-Home Messages

MOM6 is eliminating unphysical assumptions and behavior to improve its ability to answer questions about sea level rise

- MOM6 works in configurations that limit numerically induced mixing
- MOM6 offers lots of physical mixing parameterization options
- MOM6 numerics are robust to continual and large changes in ocean geometry

Progress is toward more physically consistent interactions of marine ice (icebergs and sea ice) with the ocean

MOM6 code is freely available and welcomes contributions to shared development

