

# Multi-assumption modeling of photosynthesis

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# Identifying (structural) causes of model variability - Assumption Centered Modelling

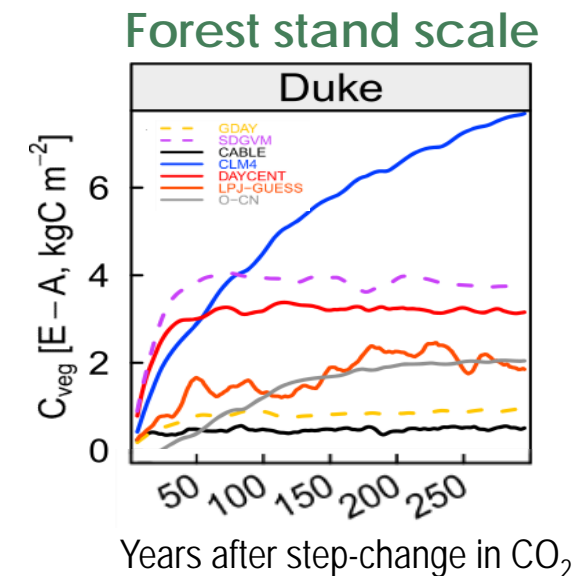
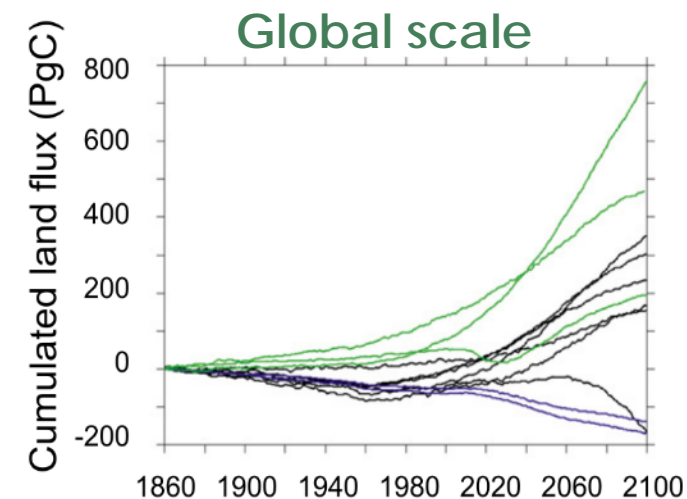
PERSPECTIVE

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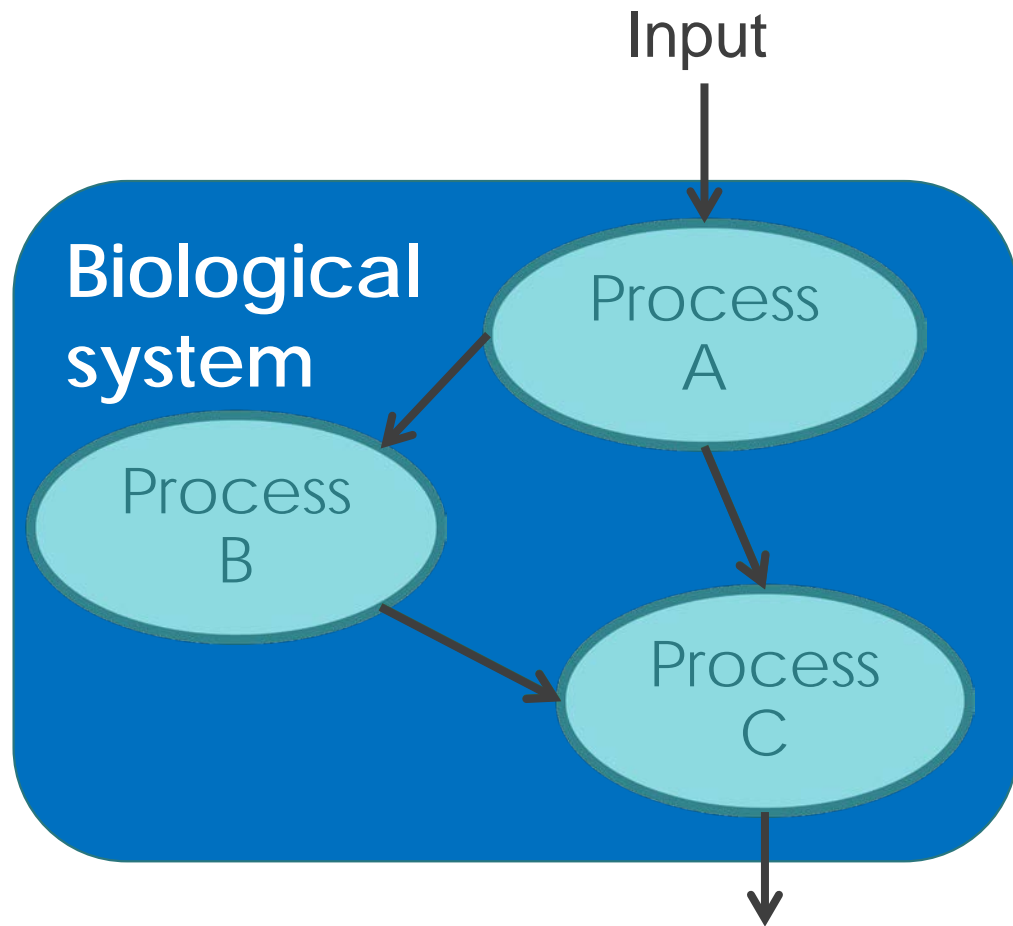
nature  
climate change

## Using ecosystem experiments to improve vegetation models

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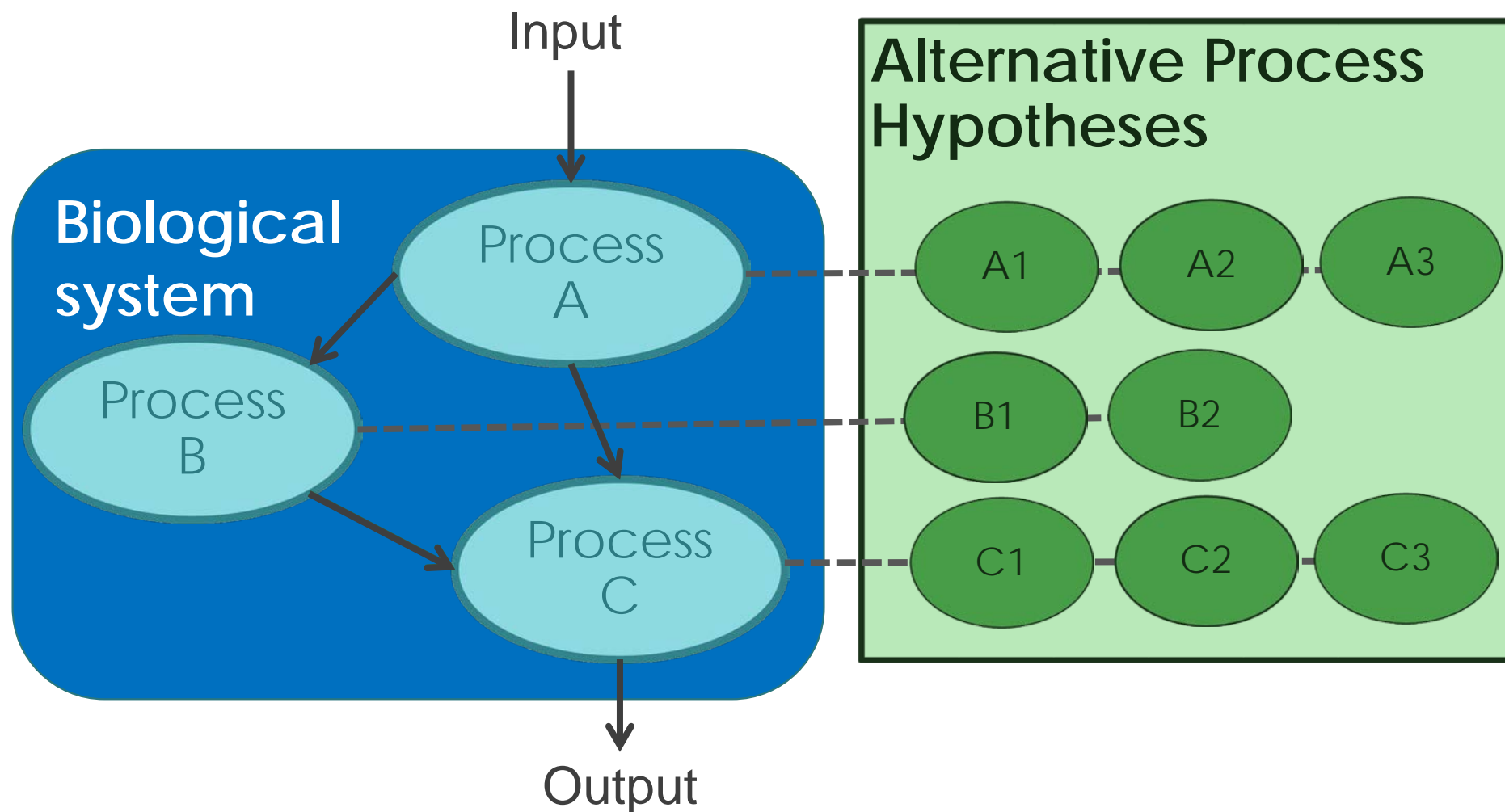


# Systems are composed of multiple processes

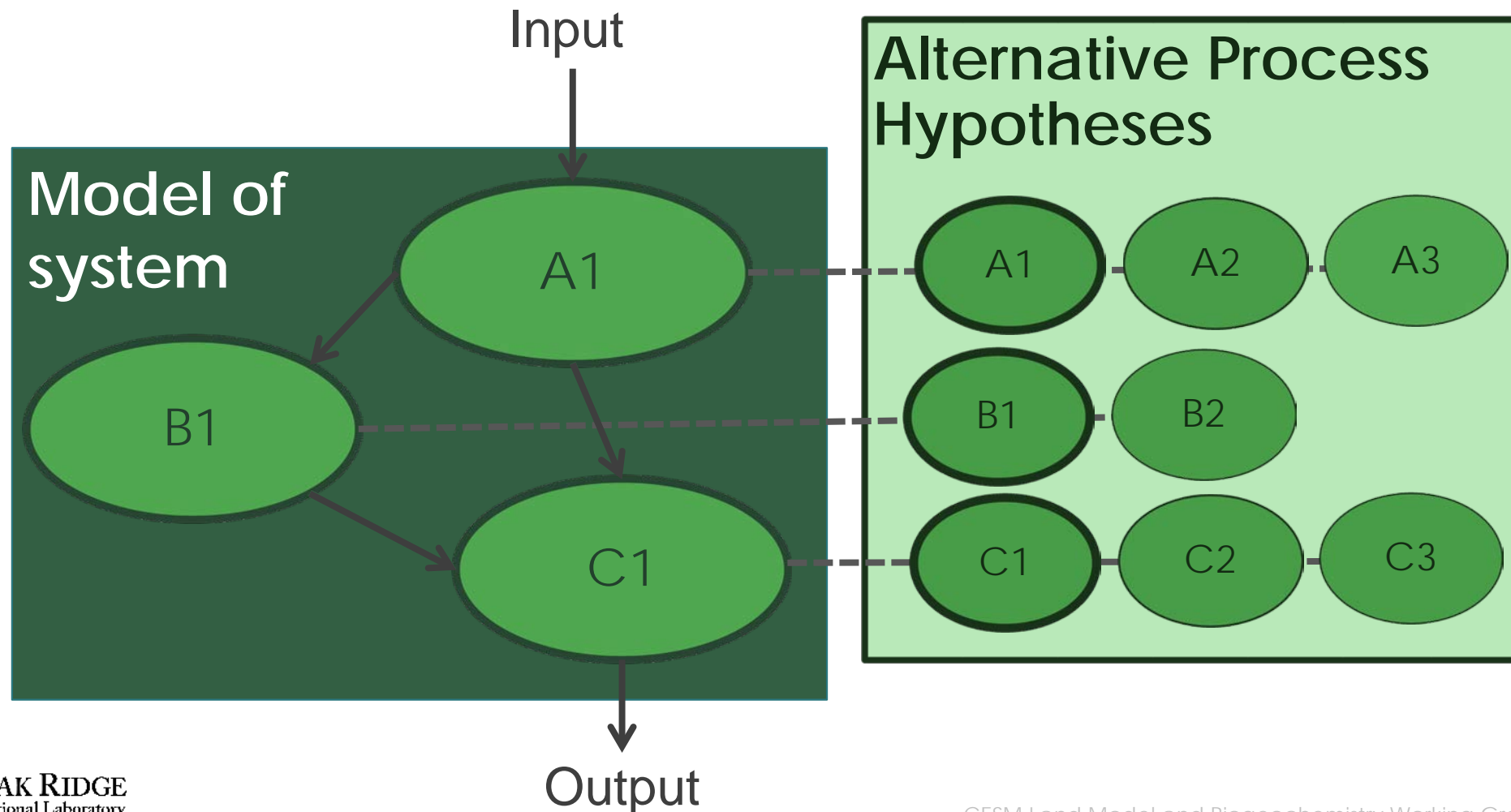


Systems are composed of multiple processes

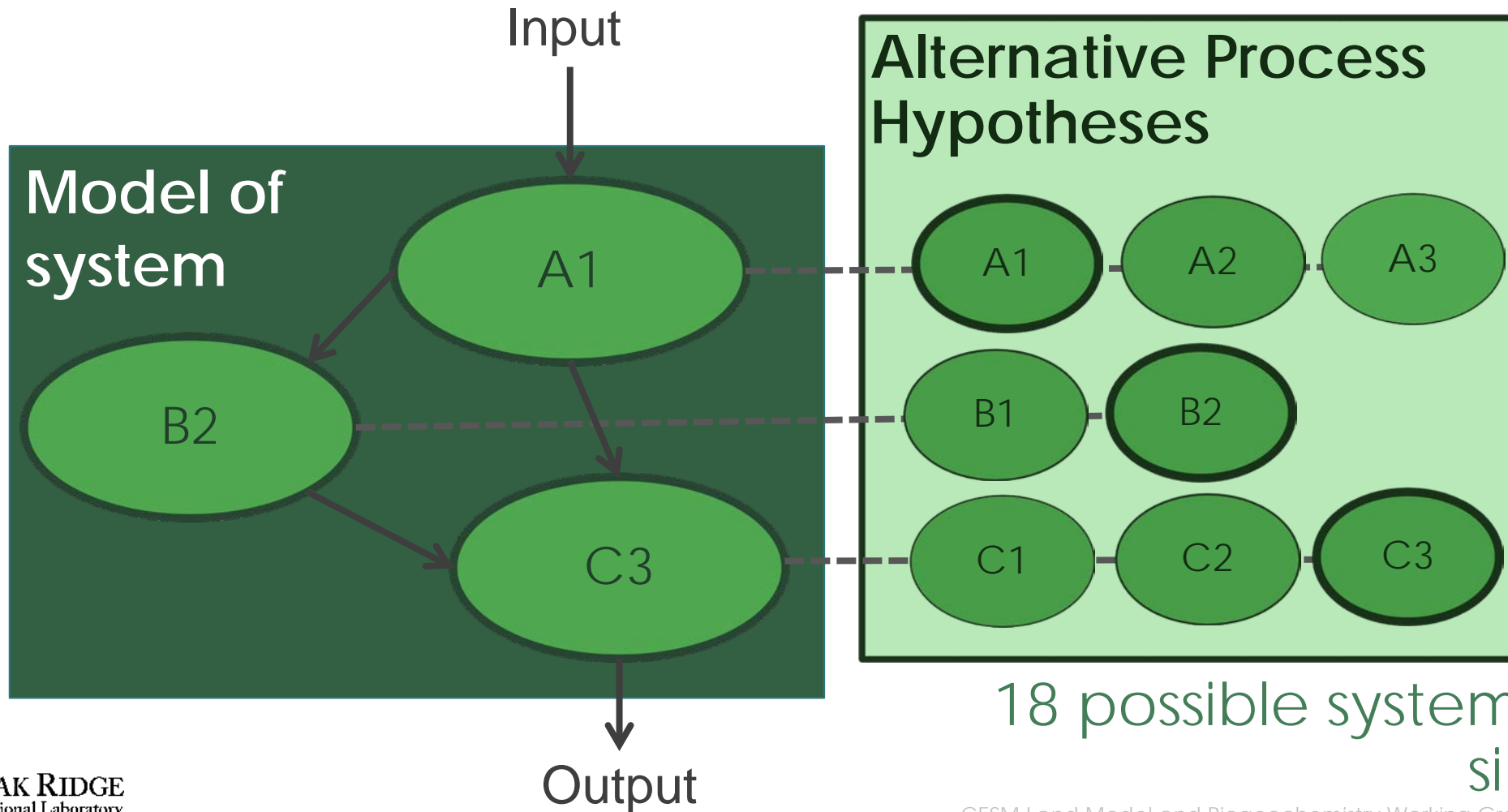
Competing hypotheses can exist for each process



Systems are composed of multiple processes  
Competing hypotheses can exist for each process  
Resulting in multiple possible models of the system



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18 possible system models in this simple example

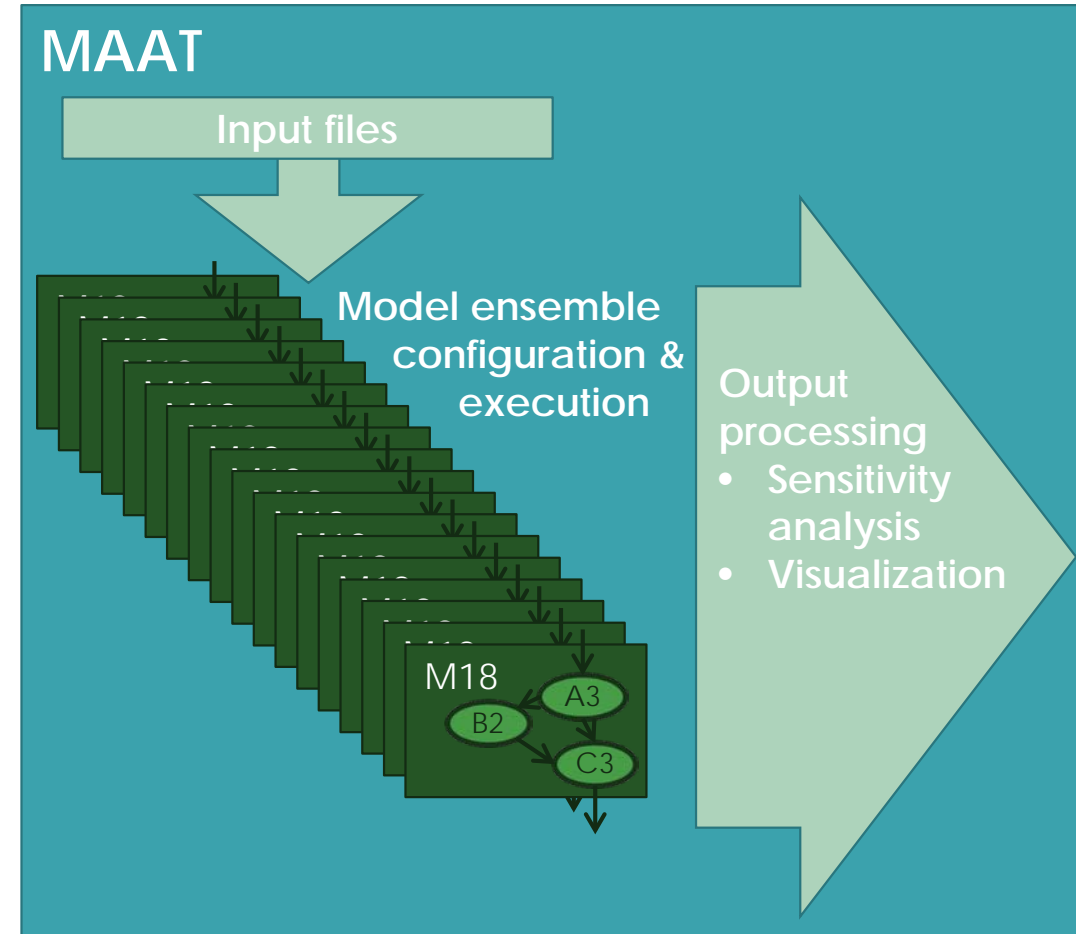
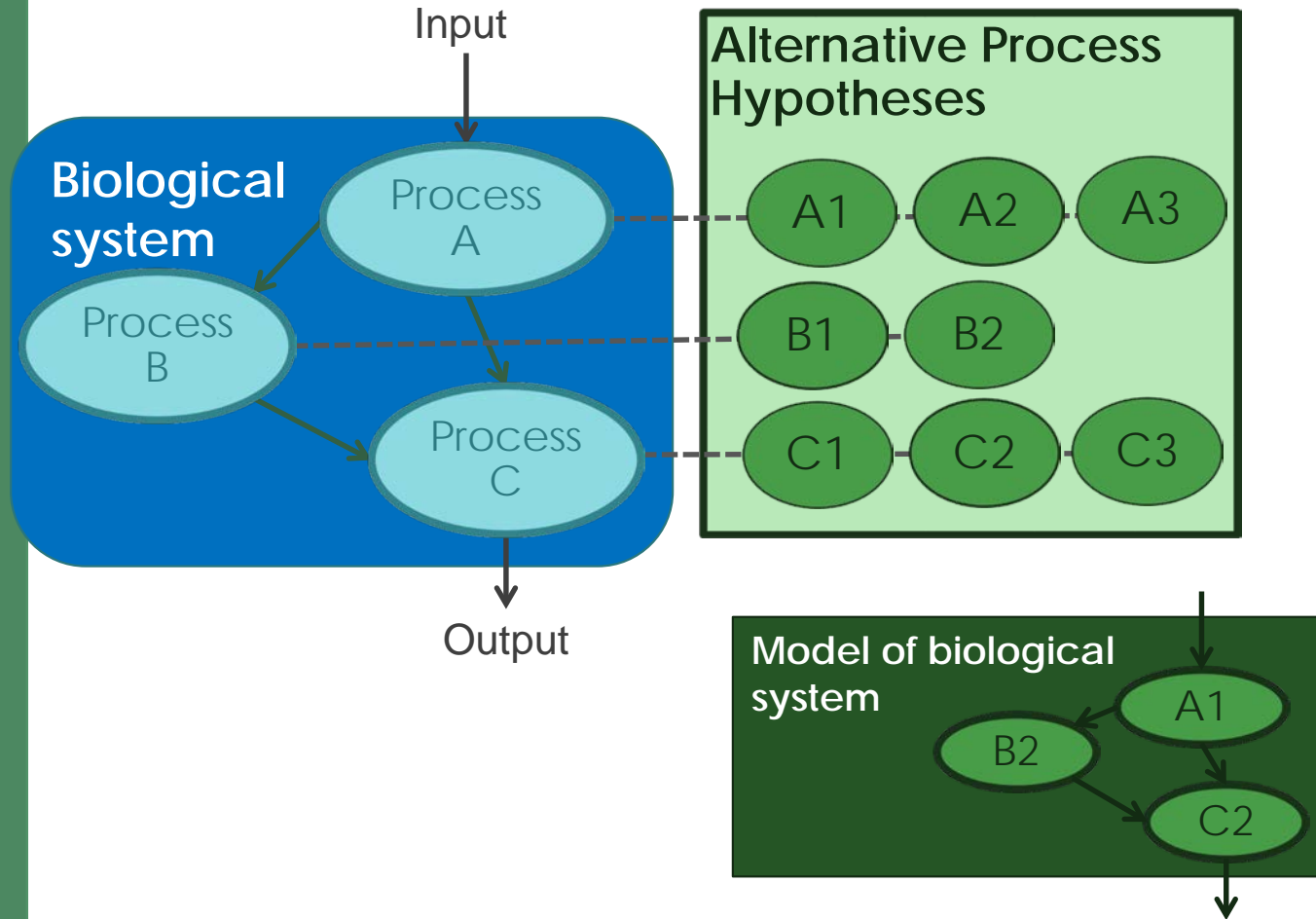
# Multi-Assumption Architecture & Testbed (MAAT)

- A multi-assumption/multi-hypothesis software framework developed to allow on-the-fly system model configuration during runtime with:
  - alternative process assumptions/hypotheses,
  - parameters (traits),
  - boundary conditions
- Designed to generate large ensembles of possible models
- Framework is general and not system specific
- Encodes a novel algorithm for process-level global sensitivity analysis (Dai, *et al.* 2017 *WRR*) and global parameter sensitivity analysis (Saltelli *et al.*, 2010)

<https://github.com/walkeranthony/MAAT>  
Walker et al. (2018) GMD

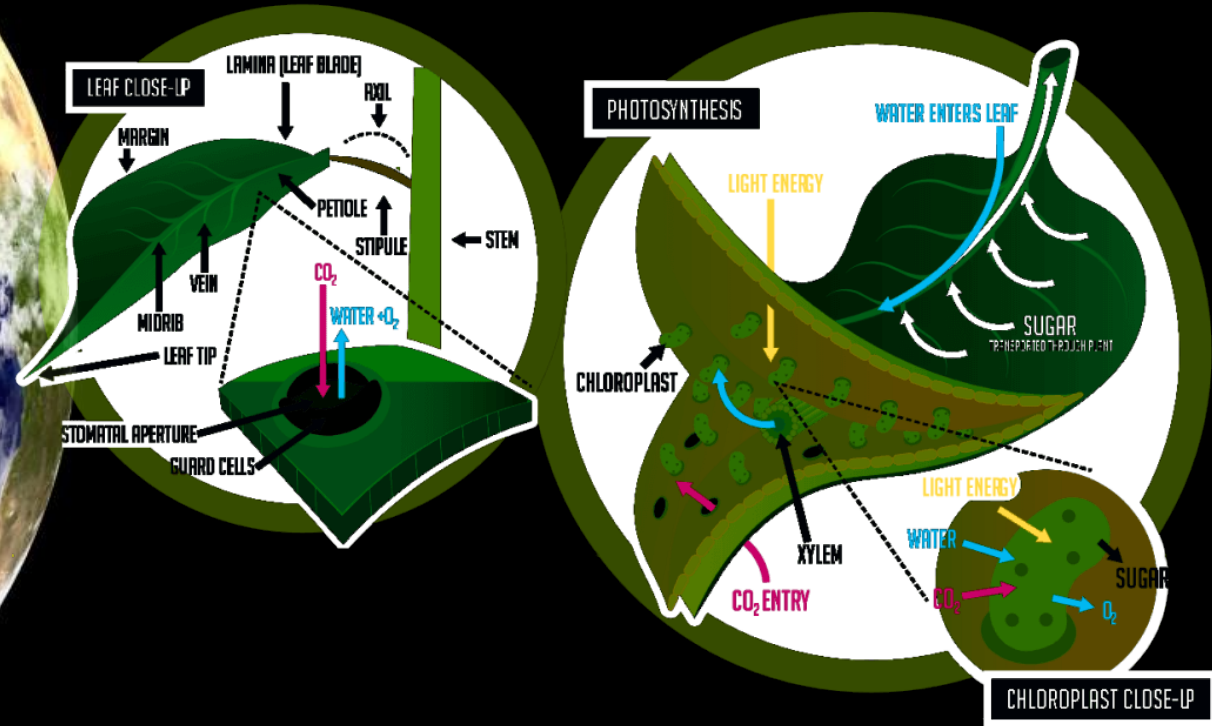


# Multi-assumption / multi-hypothesis modeling





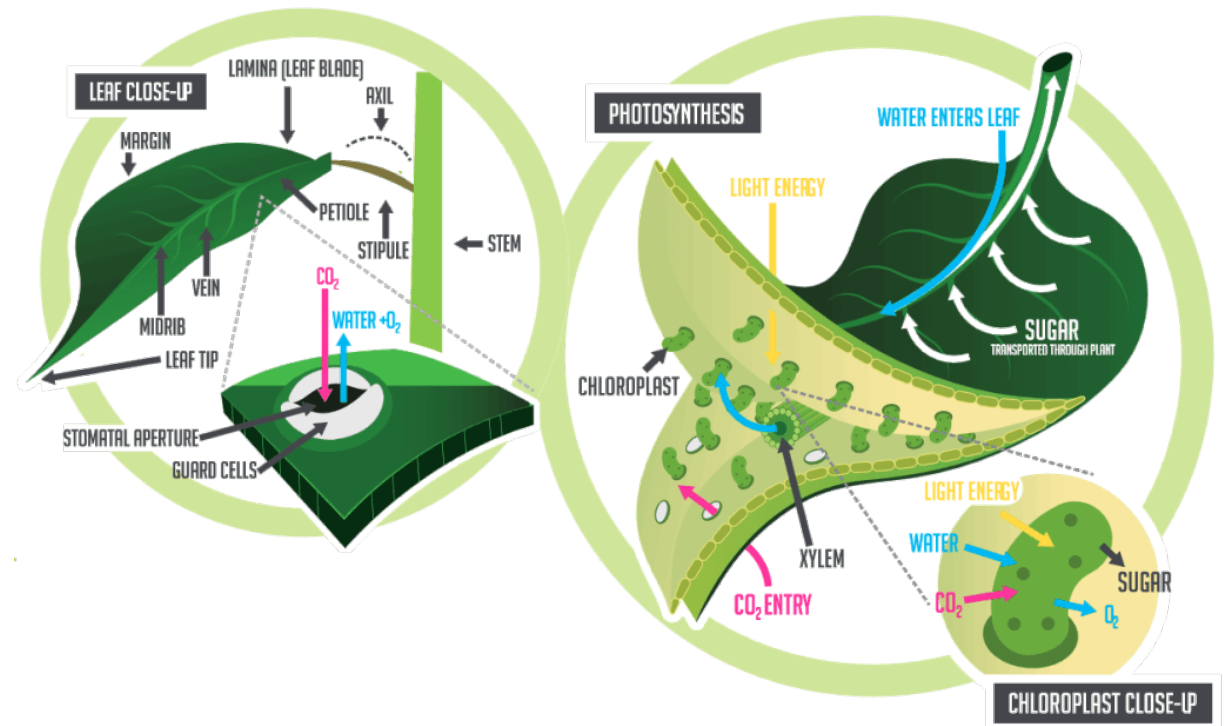
# Leaf-scale photosynthesis models are the heart of Earth-System Land Models



... to allow mechanistic simulation of physiological responses to increasing atmospheric CO<sub>2</sub>

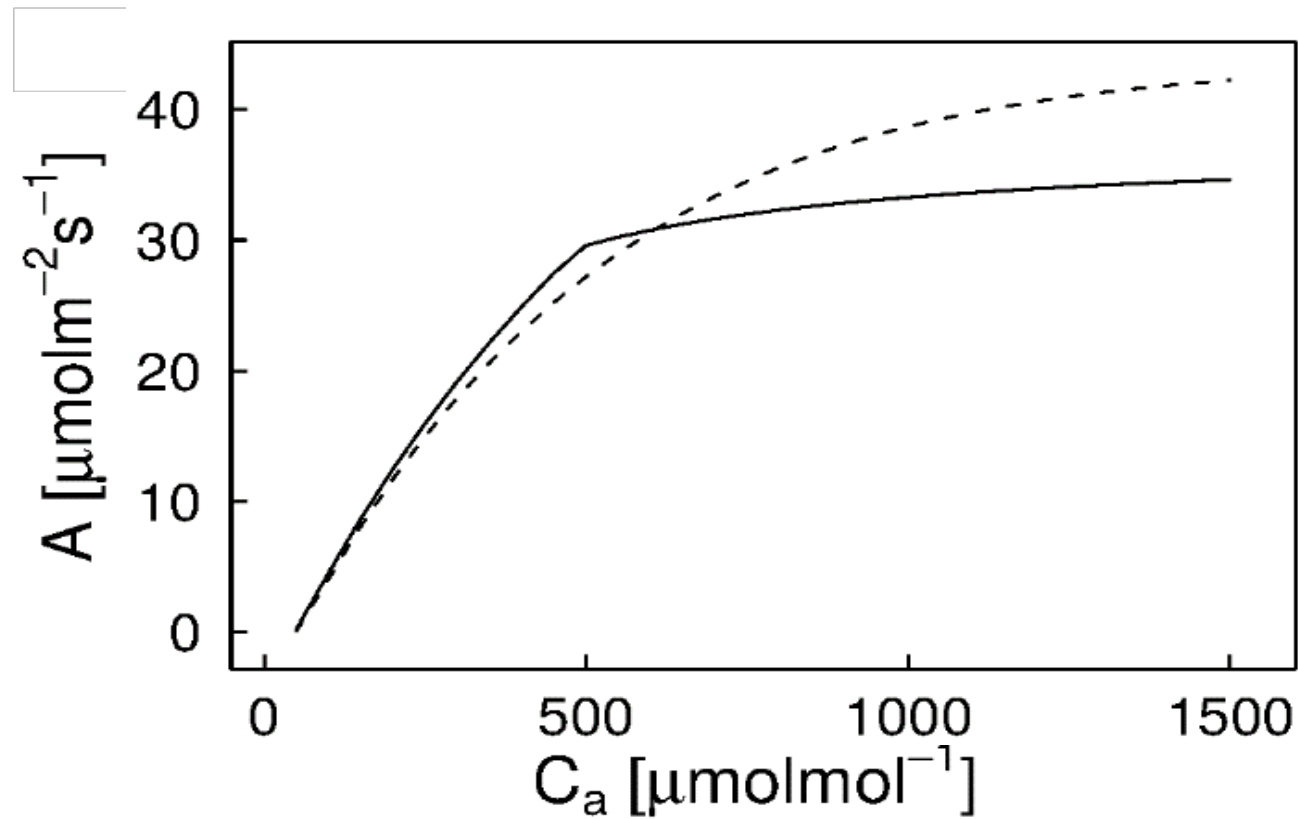
# Multi-assumption leaf photosynthesis model

- MAAT contains a leaf-scale photosynthesis model
- Can mimic FATES, CLM(4.0 & 4.5), LM3, JULES, BETHY, + others ... or can create and run all possible model combinations



# Farquhar or Collatz?

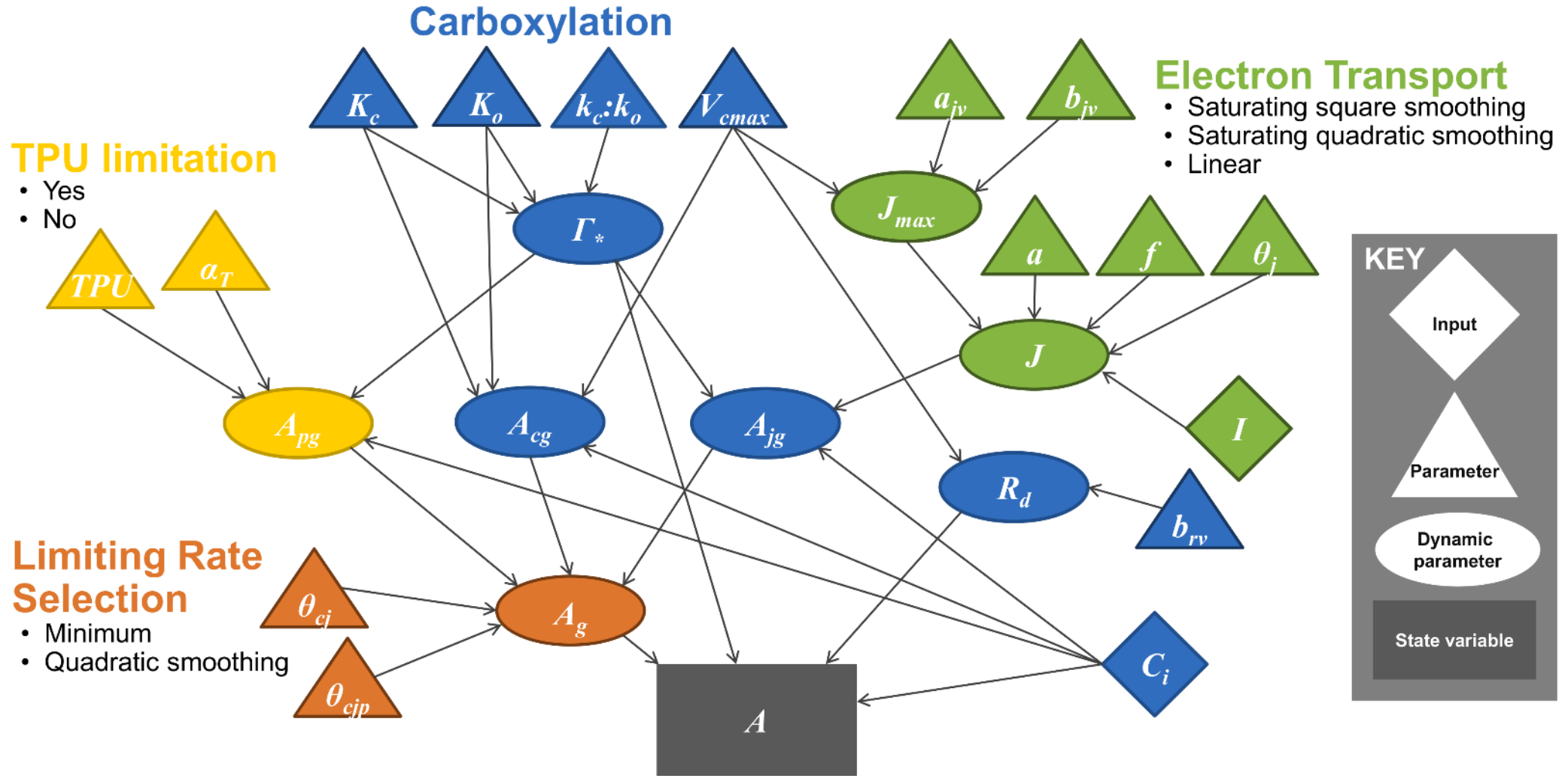
Two main flavors of photosynthesis model



# Sensitivity analysis to compare Farquhar and Collatz

- Of leaf carbon assimilation and its response to atmospheric CO<sub>2</sub>
- Four processes: electron transport (3 representations), carboxylation (1 representation), limiting rate selection (2 representations), and TPU limitation (2 representations)
- 12 system models
- 14 parameters across processes: common lit values +/- 10%, uniform distribution
- Atmospheric CO<sub>2</sub> of 280, 400, 600 ppm and PAR 200, 500, 1000  $\mu\text{mol m}^{-2} \text{s}^{-1}$
- Stomatal conductance based on Medlyn et al. (2011) fixed  $g_0$  and  $g_1$
- 25 °C i.e. no temperature scaling
- Process SA 100M member ensemble, ~2hrs on 32 processors
- Parameter SA 86.4M member ensemble, ~2hrs on 32 processors

# Farquhar enzyme kinetic model of C3 photosynthesis



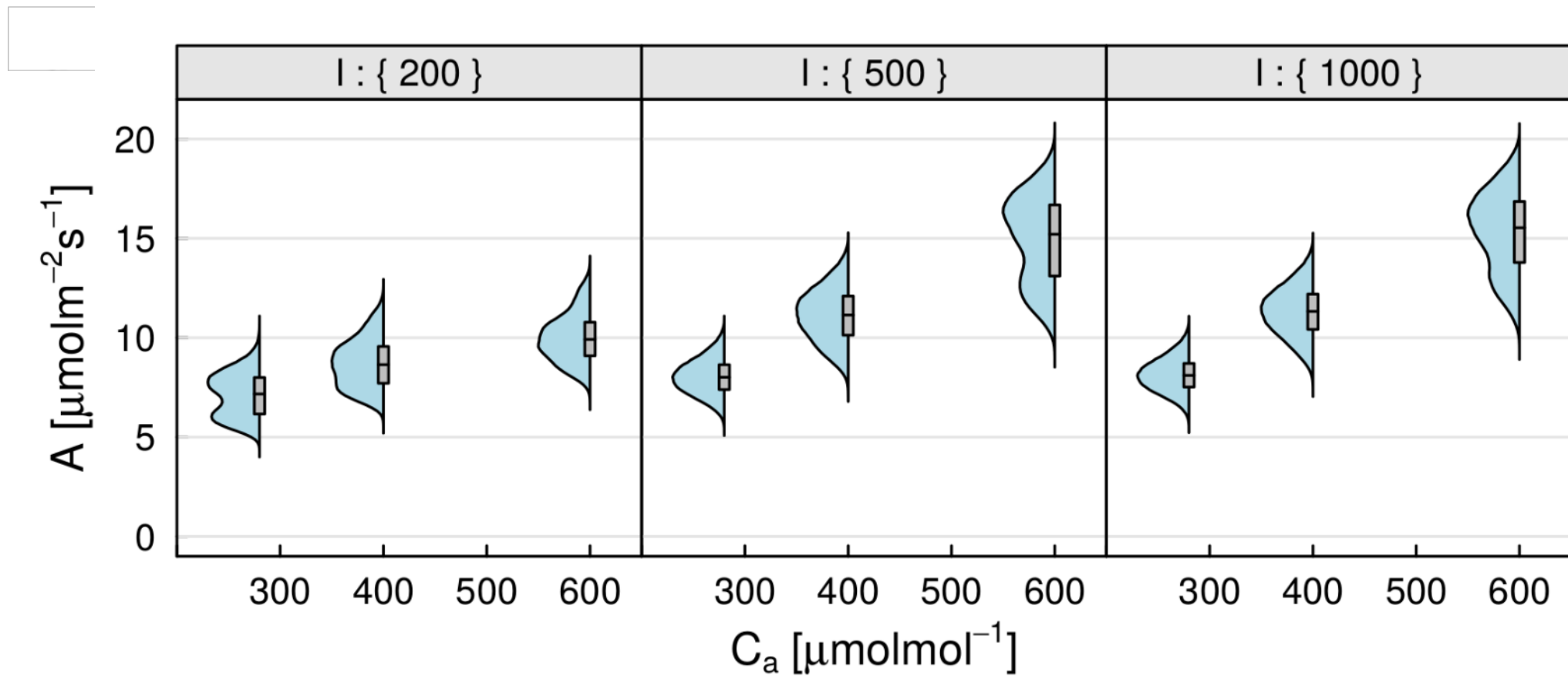
Walker et al. (in prep)



# Parameter values

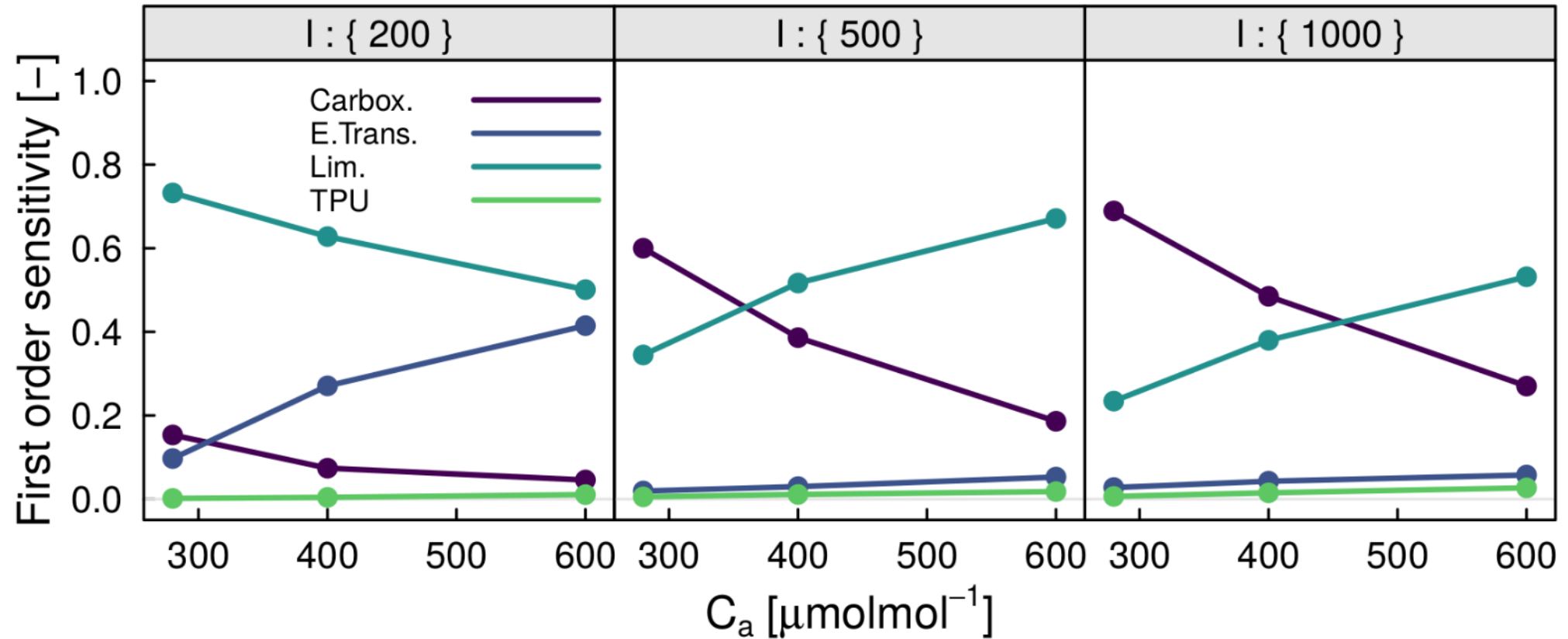
$V_{cmax}$	Maximum RuBisCO carboxylation rate	<b>45-55</b>	$\mu\text{mol CO}_2 \text{ m}^{-2} \text{ s}^{-1}$
$K_c$	Micaelis-Menten constant of RuBisCO for $\text{CO}_2$	<b>36.5-44.5</b>	Pa
$K_o$	Micaelis-Menten constant of RuBisCO for $\text{O}_2$	<b>25.0-30.6</b>	kPa
$k_o:k_c$	Ratio of RuBisCO turnover numbers for $\text{O}_2$ and $\text{CO}_2$	<b>0.19-0.23</b>	-
$a_{jv}$	Intercept $J_{max}$ to $V_{cmax}$ relationship	<b>26.2-36.0</b>	$\mu\text{mol q m}^{-2} \text{ s}^{-1}$
$b_{jv}$	Slope $J_{max}$ to $V_{cmax}$ relationship	<b>1.48-1.80</b>	$\text{mol q mol}^{-1} \text{ CO}_2$
$a$	Leaf absorbance of visible solar radiation	<b>0.72-0.88</b>	-
$f$	Fraction of absorbed light not absorbed by photosystems	<b>0.207-0.253</b>	-
$\theta_j$	Electron transport smoothing	<b>0.81-0.99</b>	-
$\theta_{cj}$	Assimilation rate smoothing 1	<b>0.81-0.99</b>	-
$\theta_{cjp}$	Assimilation rate smoothing 2	<b>0.81-0.99</b>	-
$TPU$	Triose phosphate utilisation	<b>0.150 – 0.184 <math>V_{cmax}</math></b>	$\mu\text{mol P m}^{-2} \text{ s}^{-1}$
$a_{tpu}$	Fraction of phosphate exported from chloroplast not returned	<b>0.45-0.55</b>	-
$R_d$	Dark respiration	<b>0.150 – 0.184 <math>V_{cmax}</math></b>	$\mu\text{mol CO}_2 \text{ m}^{-2} \text{ s}^{-1}$

# Variability in carbon assimilation

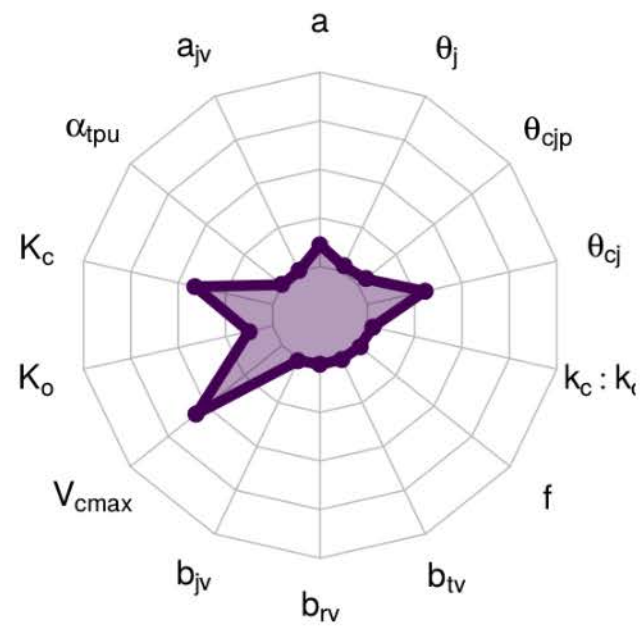




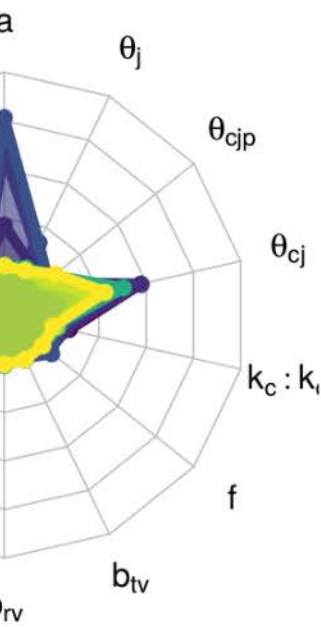
# Assimilation sensitivity to processes



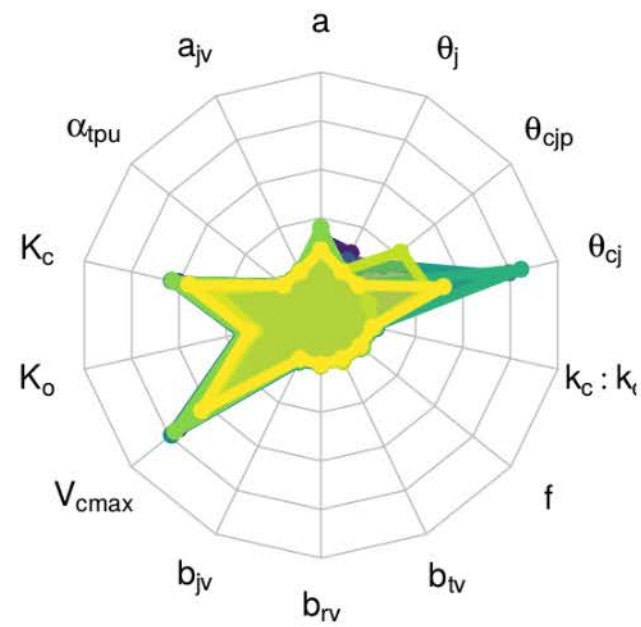
# Assimilation sensitivity to parameters



- Ca 280; I 200
- Ca 400; I 200
- Ca 600; I 200
- Ca 280; I 500
- Ca 400; I 500

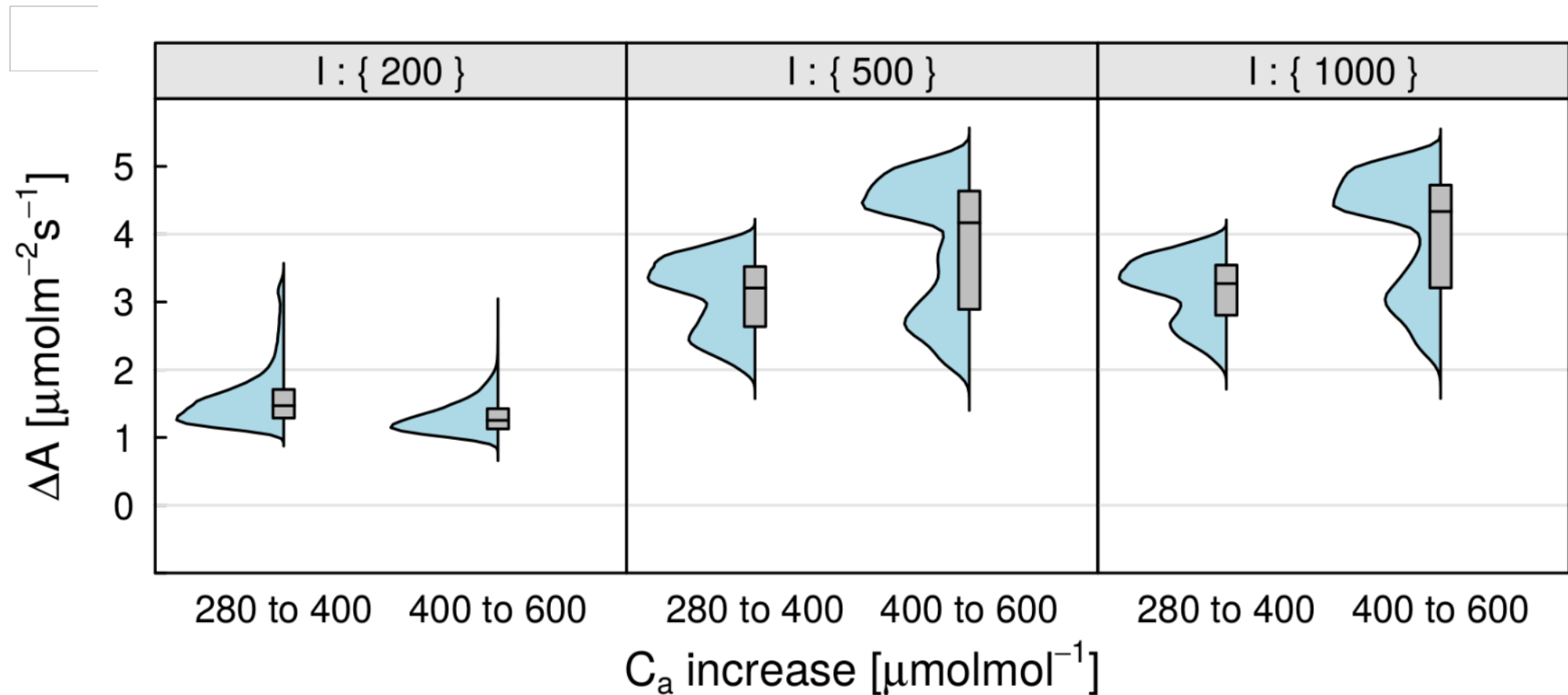


- Ca 600; I 500
- Ca 280; I 1000
- Ca 400; I 1000
- Ca 600; I 1000

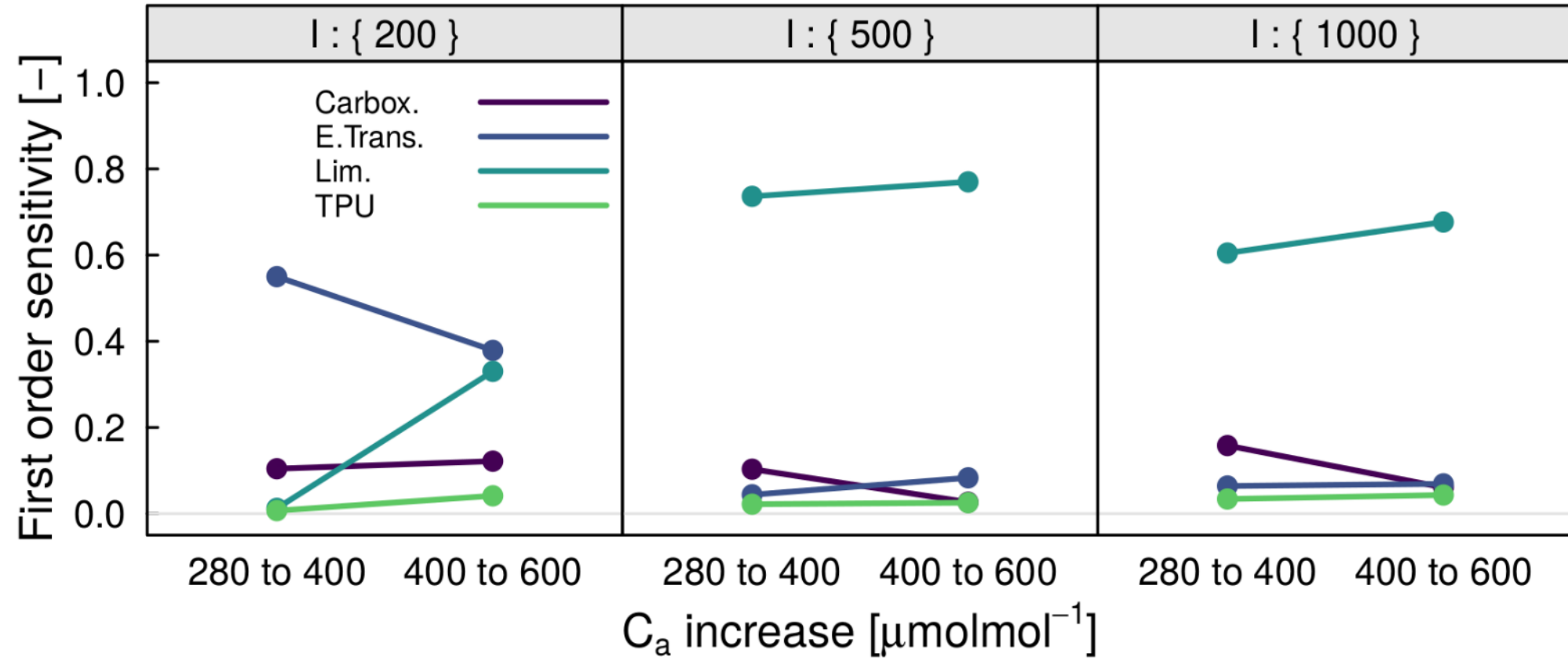


- M1
- M2
- M3
- M4
- M5
- M6
- M7
- M8
- M9
- M10
- M11
- M12

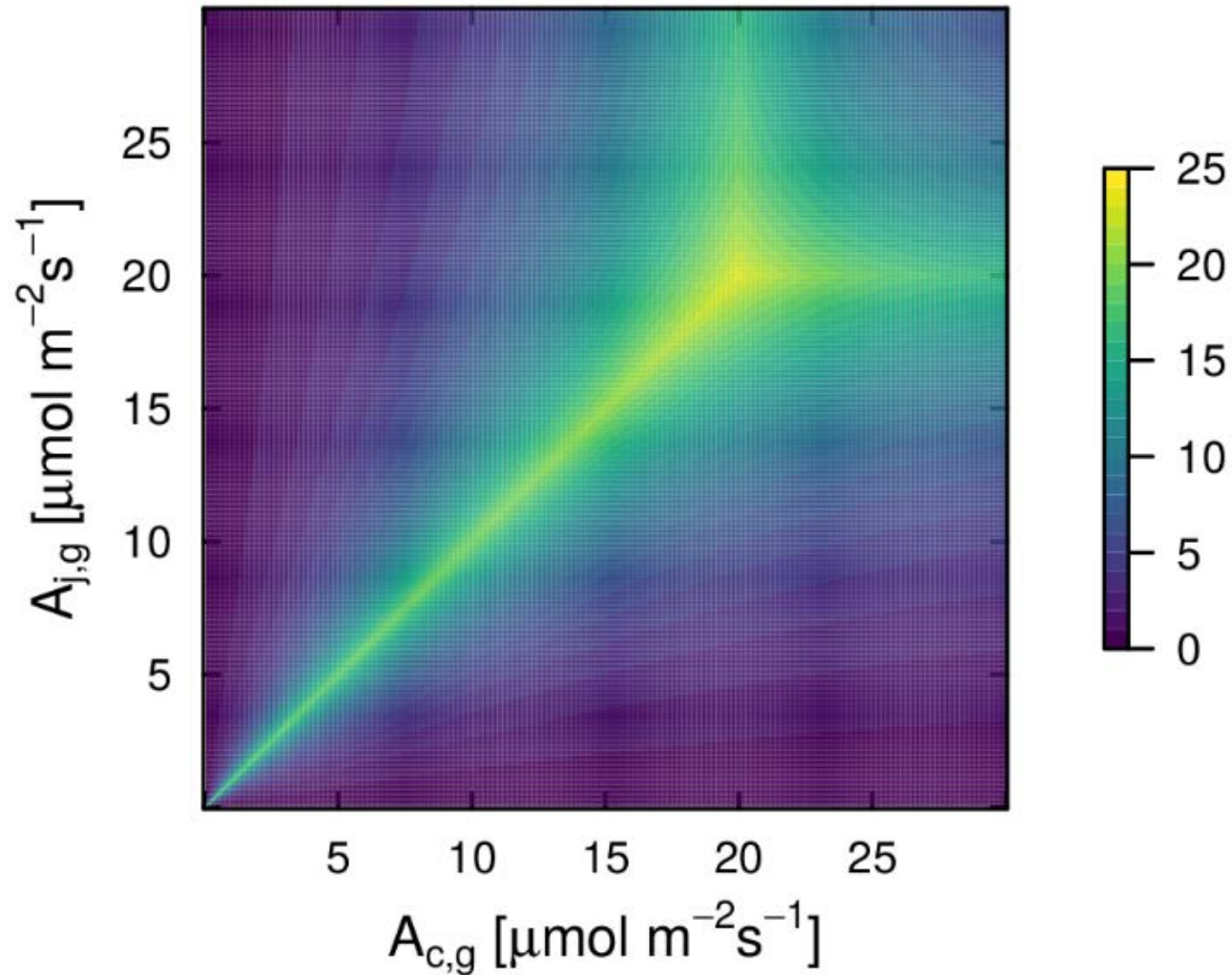
# Variability in assimilation response to CO<sub>2</sub> increase



# Assimilation response sensitivity to processes



# Gross assimilation reduction with smoothed vs. minimum limiting rate selection



# Summary

- Competing hypotheses are a key component of model variability / predictive uncertainty.
- Even for a relatively well-understood model of photosynthesis, multi-hypothesis methods have revealed substantial variability and surprising sensitivities.
  - i.e. sensitivity to the non-mechanistic process of limiting rate selection (under the conditions of the SA, environment, parameter values,  $\pm 10\%$ ).
- Limiting rate selection?
- With tools like MAAT (and others) the influence of competing hypotheses can be approached in a less *ad hoc* way.
- Allow rapid detailed investigation: e.g. faster photosynthesis solve.



Thank you.



Terrestrial  
Ecosystem  
Science SFA  
OAK RIDGE  
National Laboratory

Atmospheric CO<sub>2</sub>



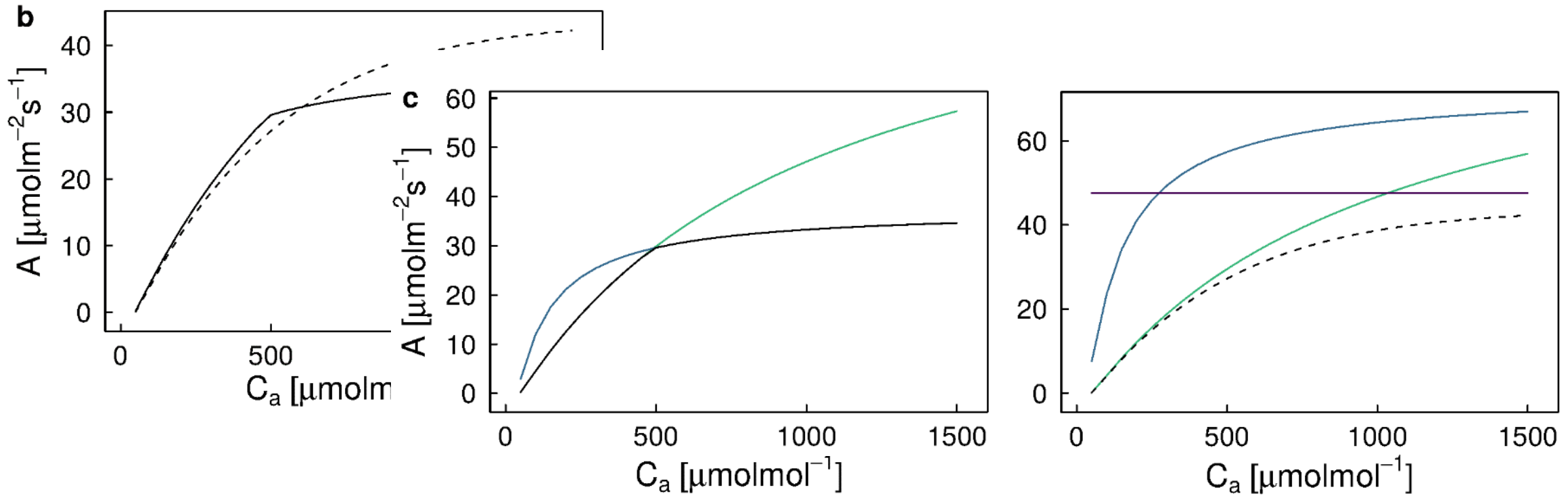
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[github.com/walkeranthony/MAAT](https://github.com/walkeranthony/MAAT)



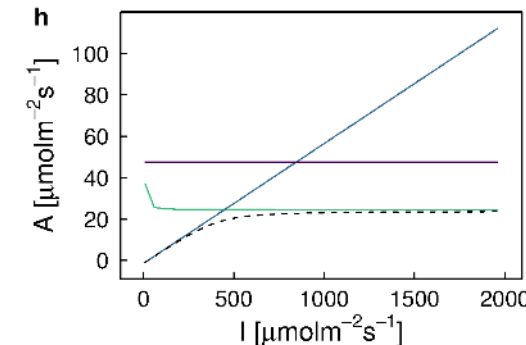
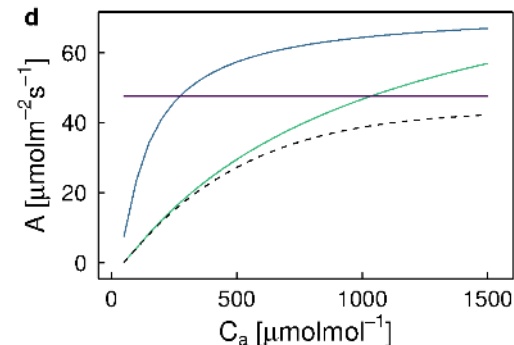
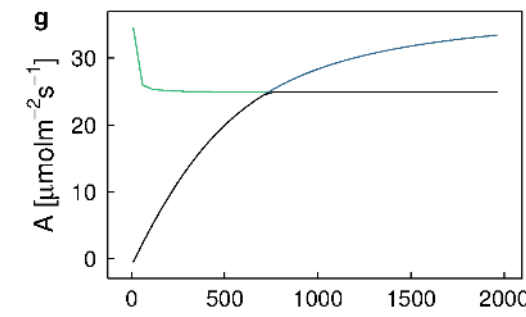
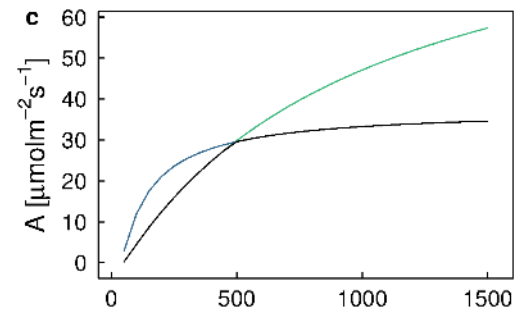
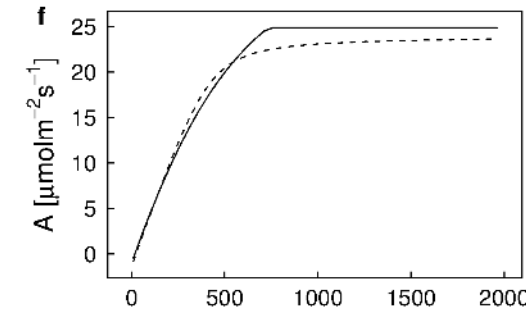
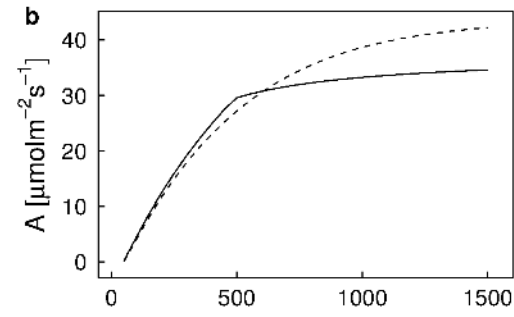
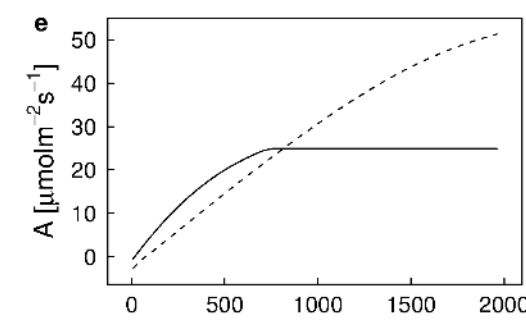
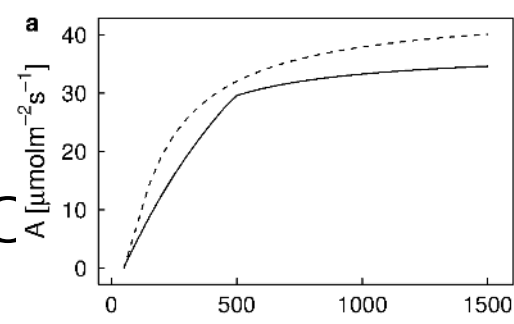
# Farquhar or Collatz?

Two main flavors of photosynthesis model



# Farquhar or Collatz?

## Two main flavours



# Faster photosynthesis solve



# Leaf-scale photosynthesis models can be costly to solve & are solved many times at each timestep

Canopy scaling requires multiple leaf solves:

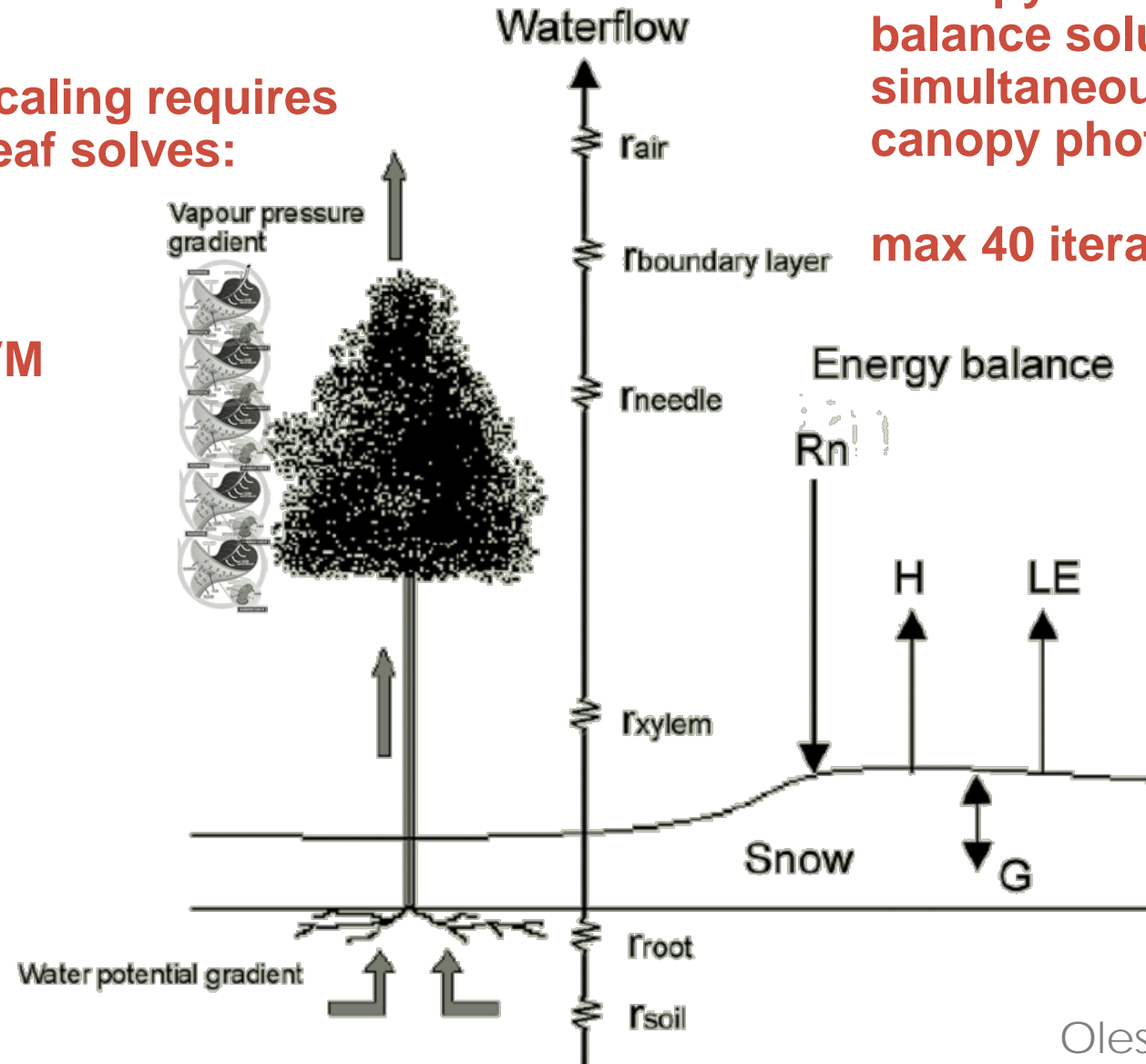
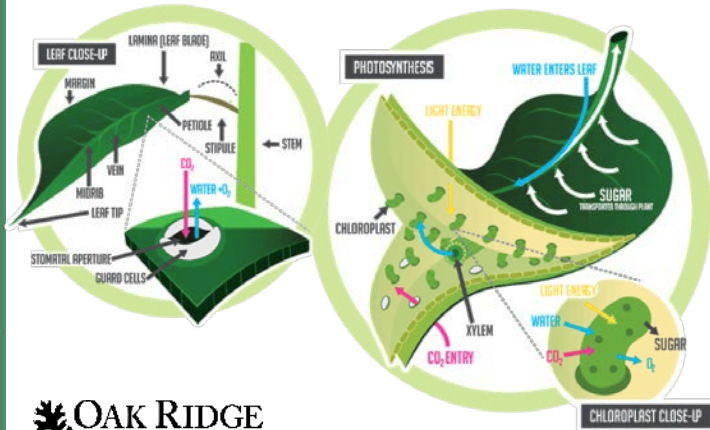
10 FATES  
2 CLM  
LAI SDGVM

Canopy stability/energy balance solution requires simultaneous solve of canopy photosynthesis:

max 40 iterations in CLM

Leaf A numerical solution:

max 5 iterations FATES  
max 40 iterations CLM



Oleson et al., 2013

# A maximum of 2000 leaf photosynthesis calculations (400 solves) per timestep

Time spent in CLM5 on canopy stability solve

- Prescribed vegetation mode (CLM5SP) - 26%
- Prognostic biogeochemistry (CLM5BGC-crop) - 8%
- Prognostic BGC with isotopes (CLM5BGC-crop-iso) - 4%

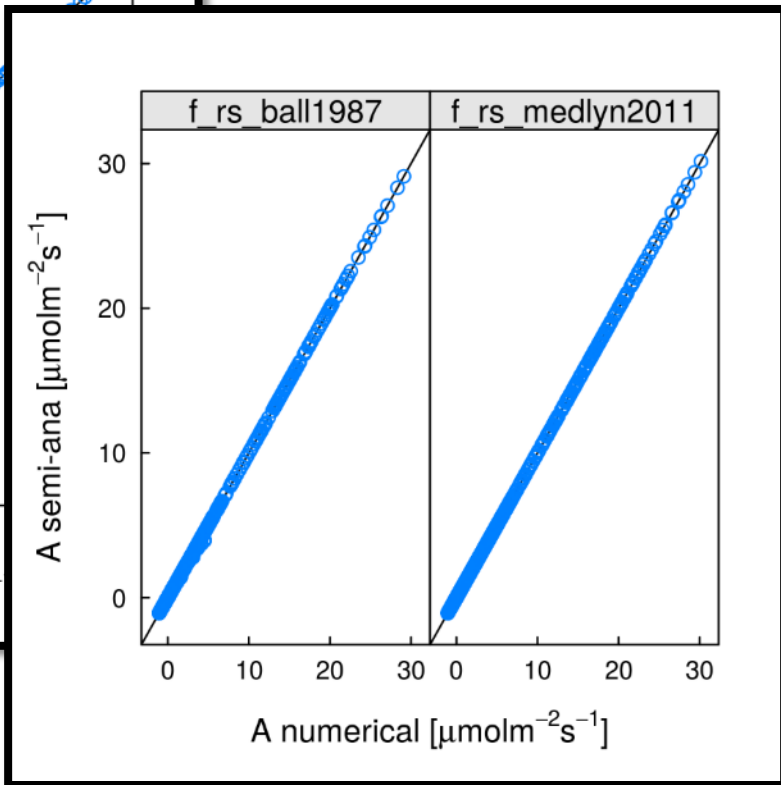
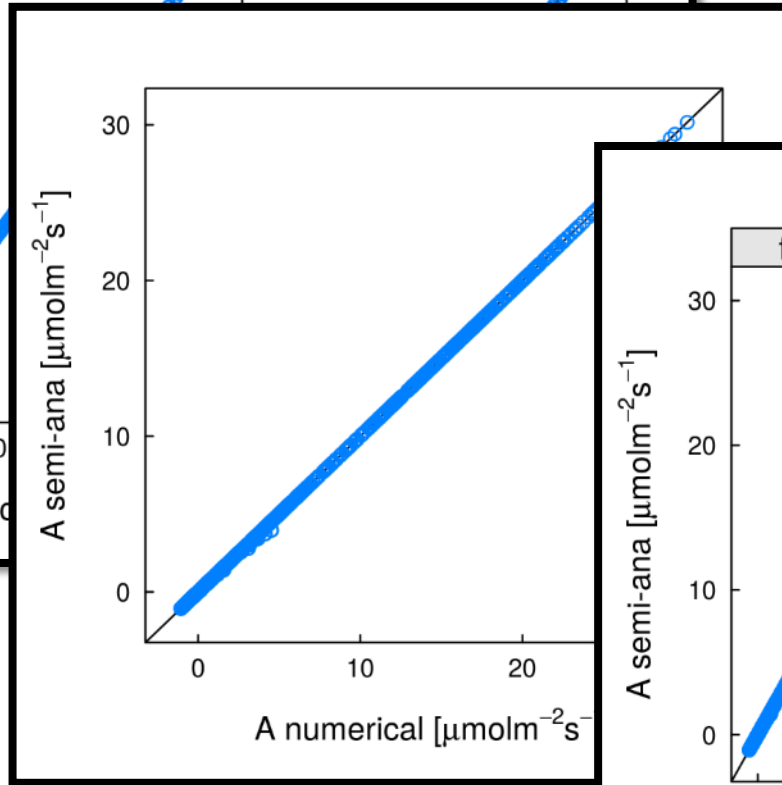
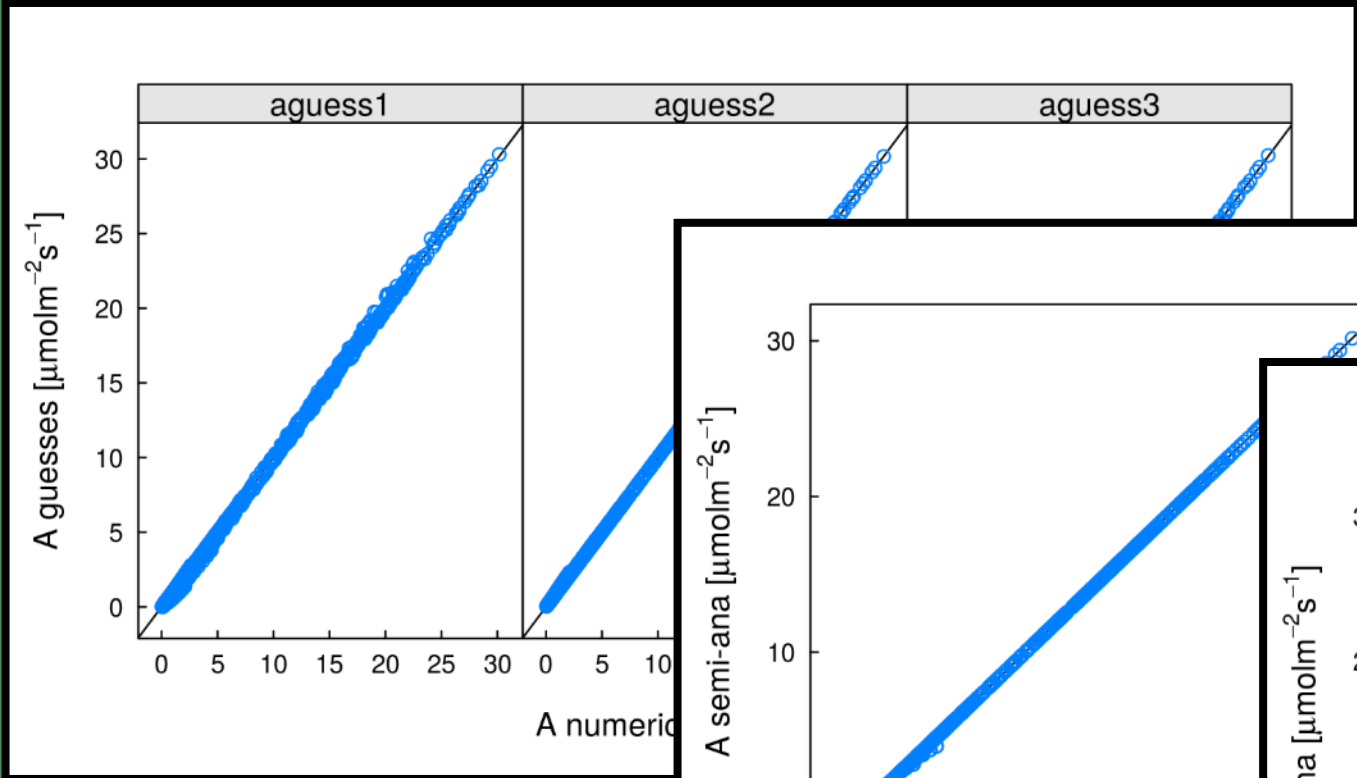
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# Semi-Analytical Method: Educated guess, guaranteed span

$g_s$ function	Medlyn, Ball
Lim. Rate selection	Farquhar, Collatz
$V_{cmax,25}$ ( $\mu\text{mol m}^{-2} \text{s}^{-1}$ )	10 to 100 by 10
$\text{CO}_2$ ( $\mu\text{mol mol}^{-1}$ )	50, 400, 1000
Temp. ( $^{\circ}\text{C}$ )	2, 25, 40
VPD (kPa)	0.1, 1, 3
PAR ( $\mu\text{mol m}^{-2} \text{s}^{-1}$ )	10, 500, 1000

9720 combinations

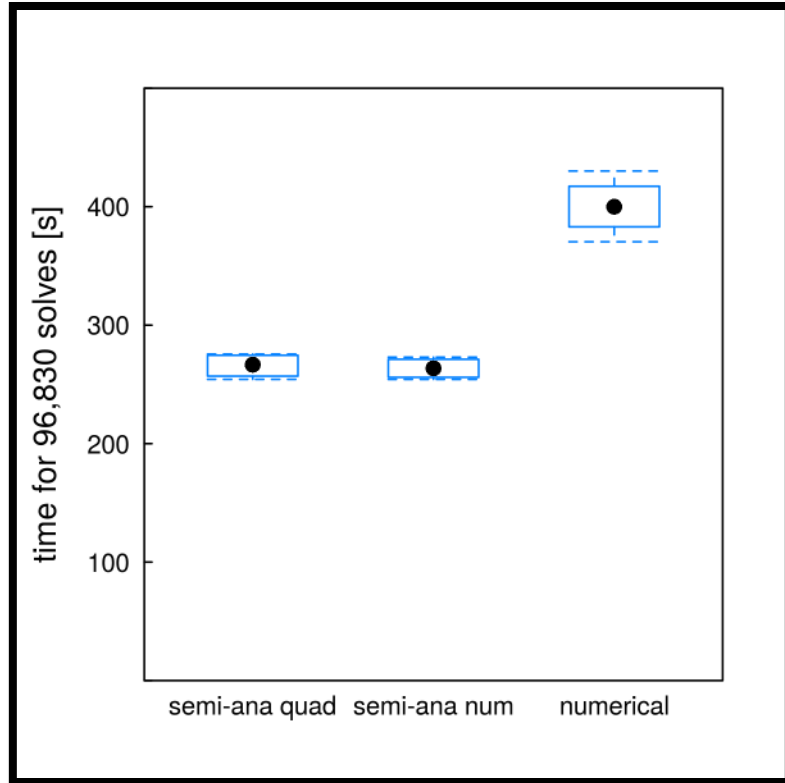




# Speed improvement over numerical solve

MAAT ~34 % decrease in leaf solve runtime

FATES / CLM ~? %



# Summary

- Developed a method (EGGS) to solve leaf photosynthesis semi-analytically
- Accurate (>99.9 % cases), 34 % speed increase in solves
- Need to fine tune algorithm when initial guess < 0
- Final algorithm development in MAAT, translate to FATES & test