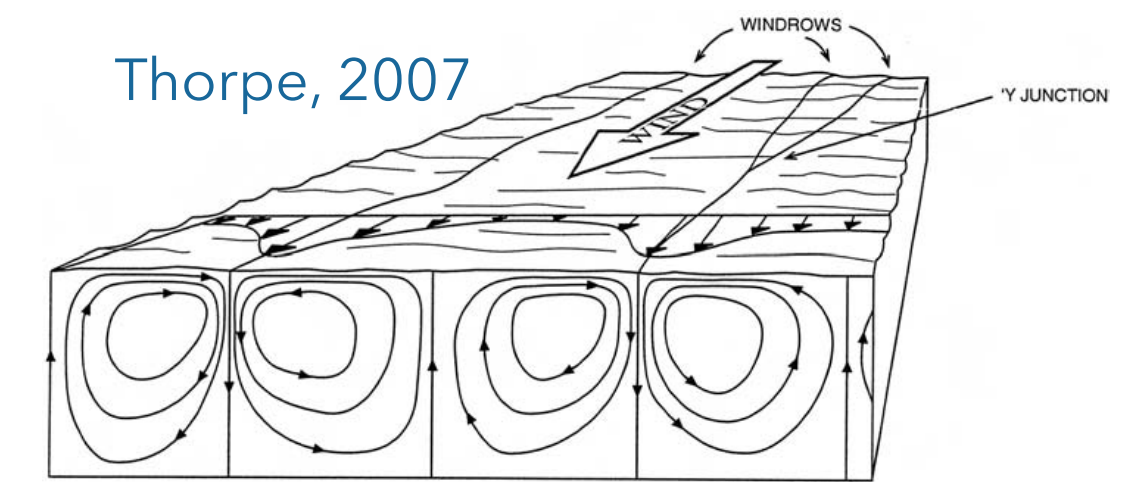


An Update on Langmuir Mixing Parameterizations in CESM2.2 & Discussions on Wave Coupling

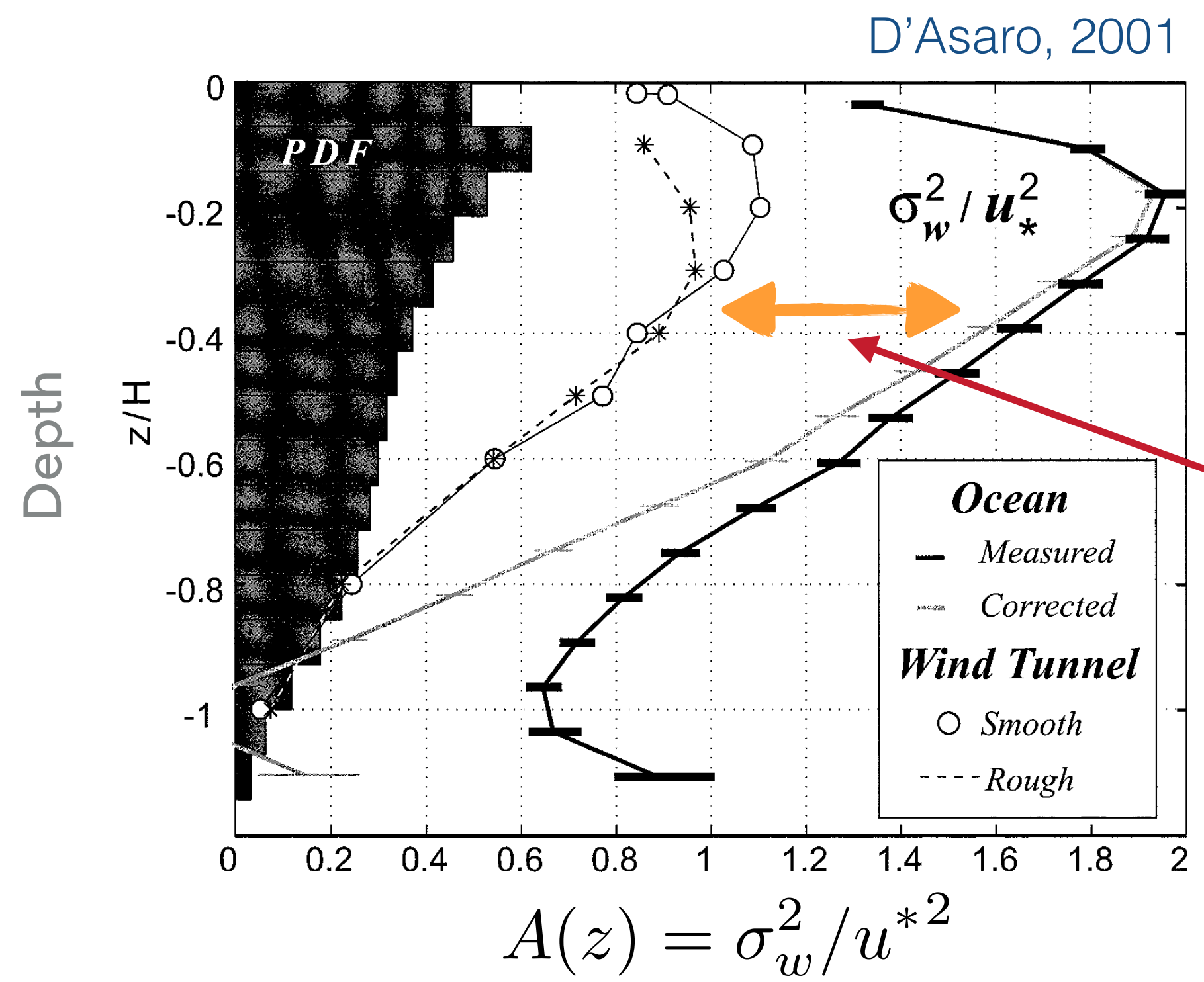
**Qing Li (Los Alamos National Laboratory)
with Alper Altuntas, Mike Levy, & many others in OMWG**

Langmuir turbulence enhances vertical mixing

- Evidence from the observations

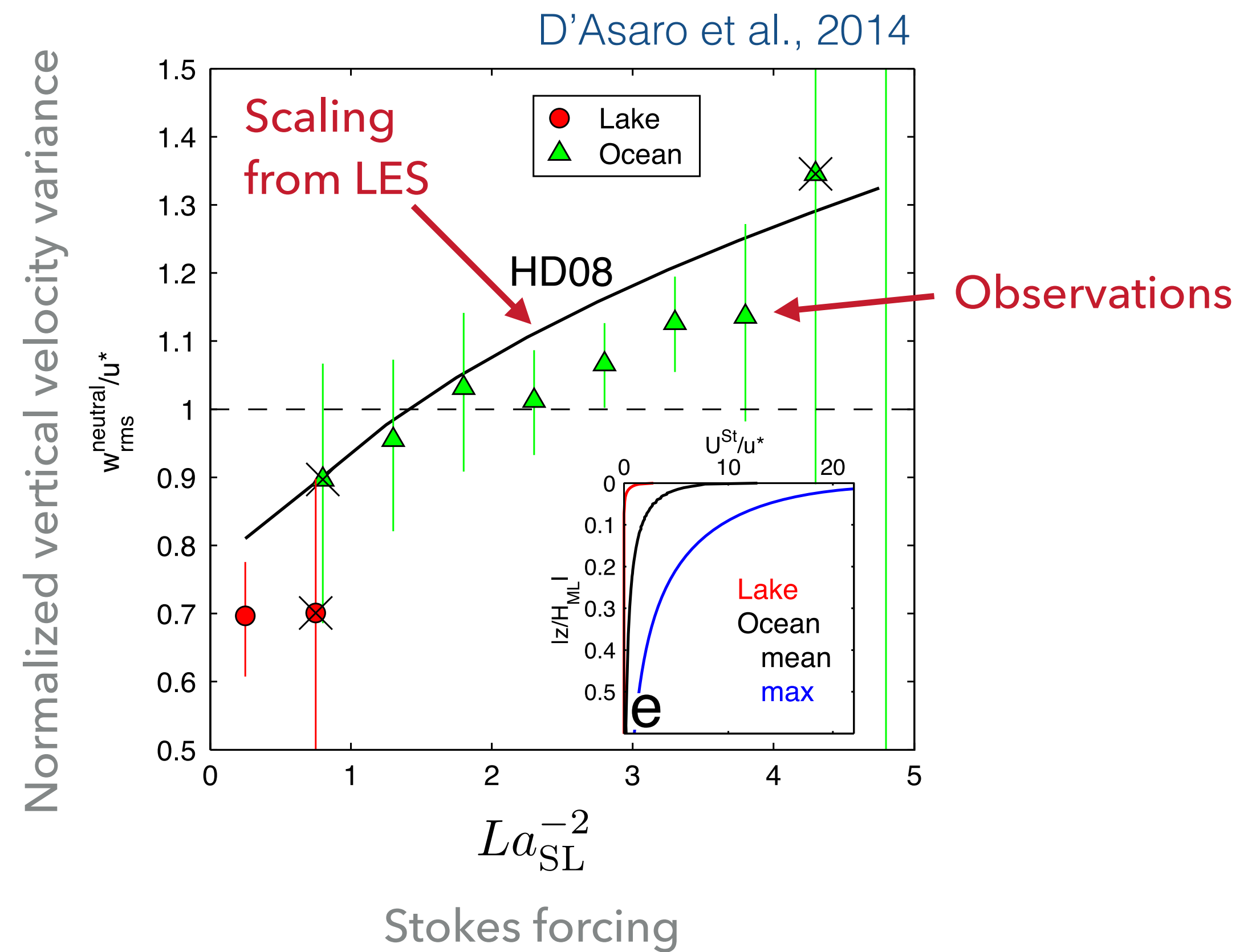


$$La^2 = \frac{\text{Surface friction velocity}}{\text{Stokes drift}}$$



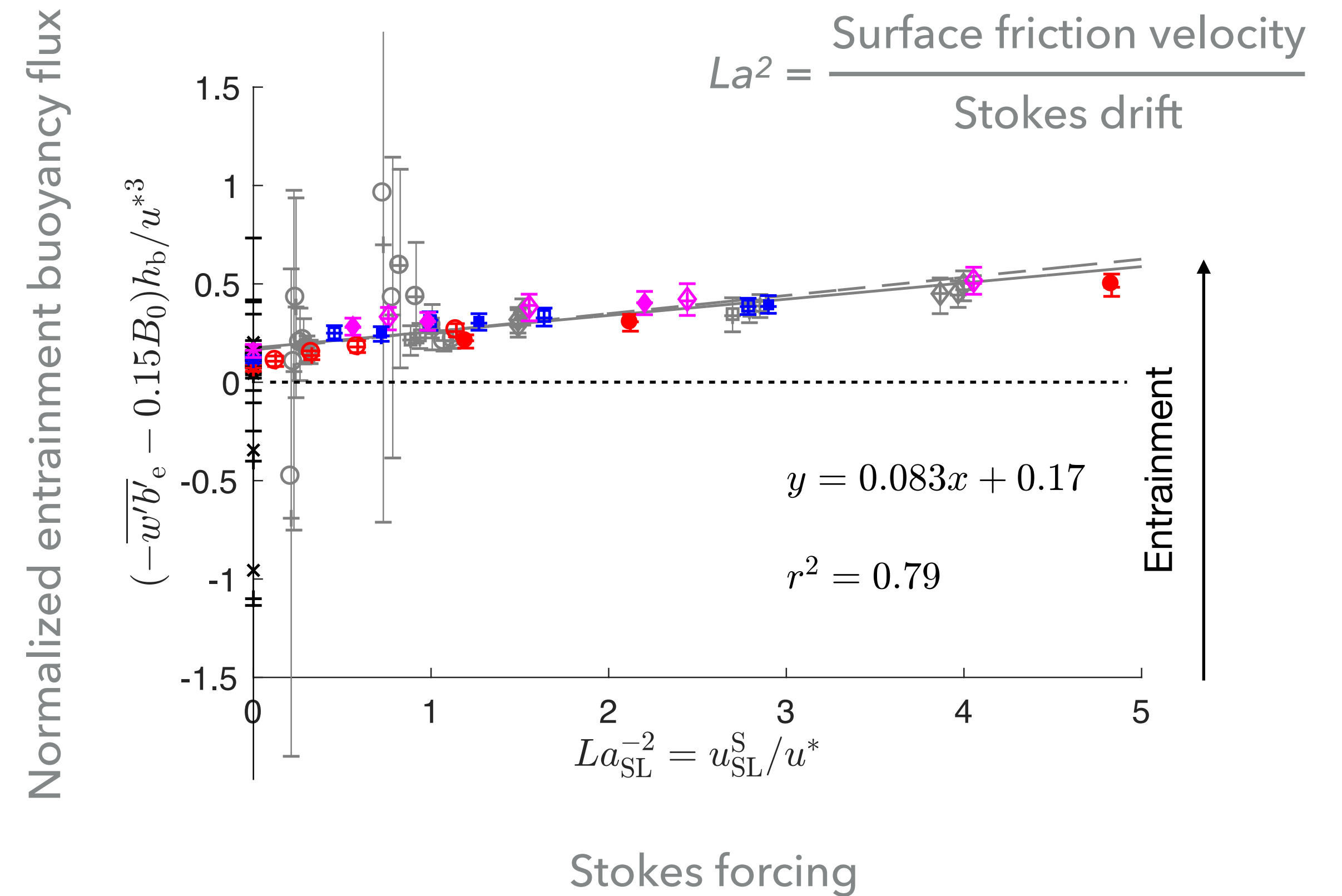
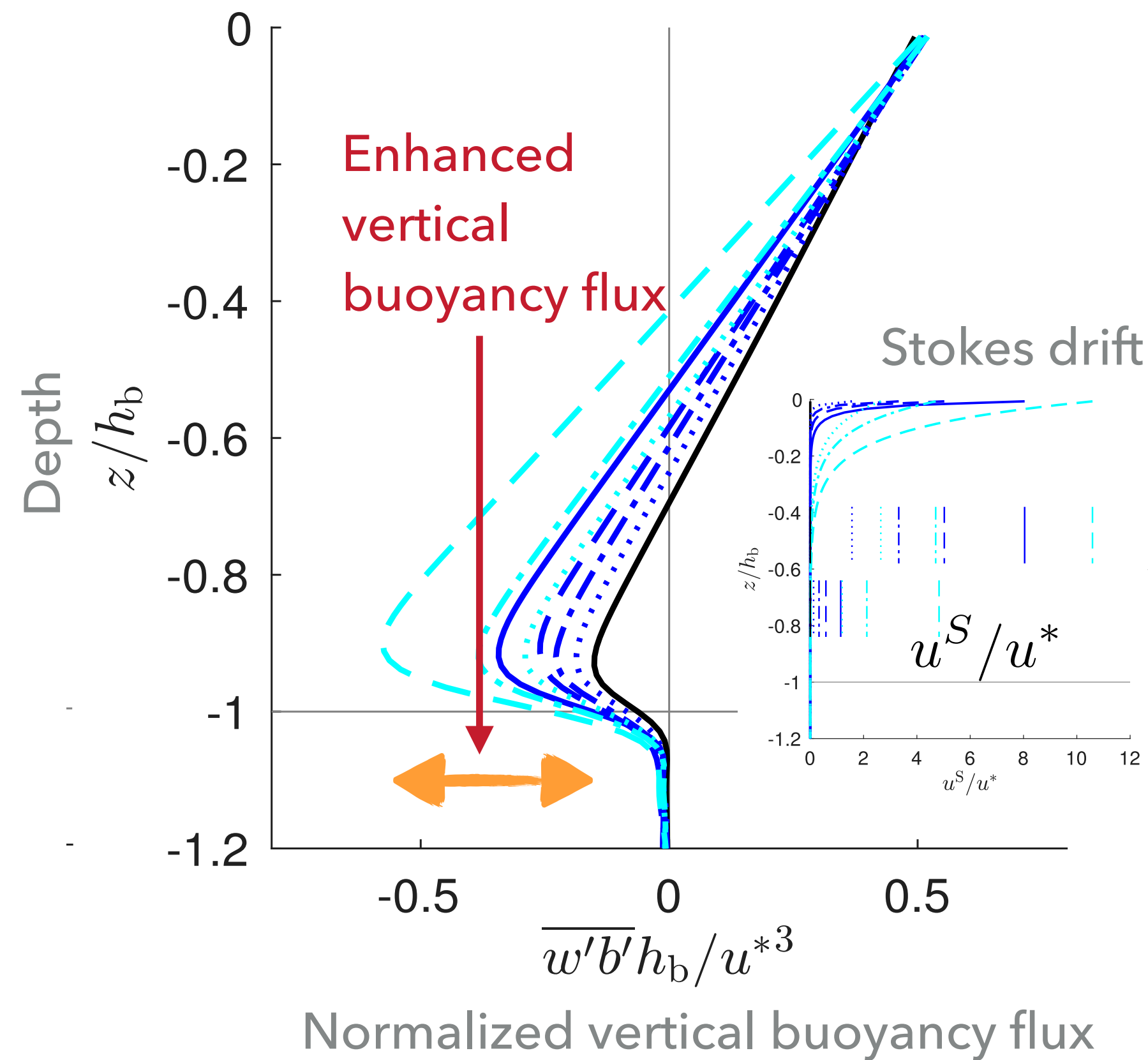
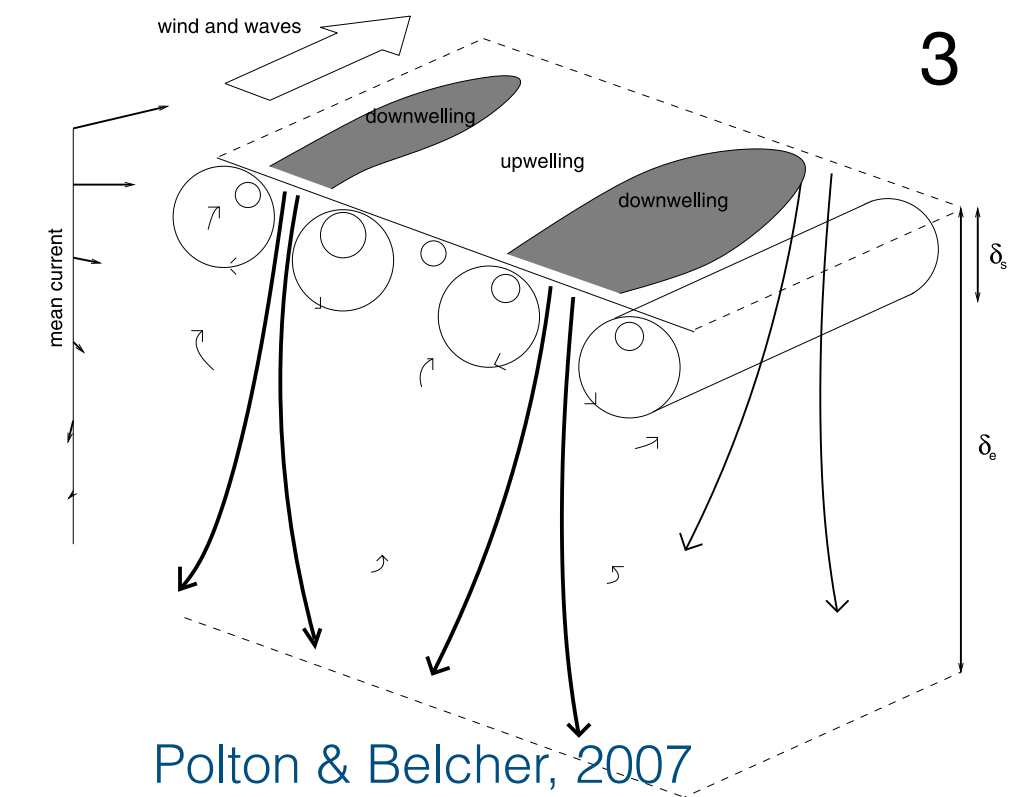
Enhanced vertical velocity variance

Normalized vertical velocity variance



Langmuir turbulence enhances mixed layer entrainment

- Scaling from Large Eddy Simulations



Parameterization of Langmuir turbulence in KPP

Vertical turbulent flux
of a variable λ

Down-gradient component + 'Non-local' component

$$\overline{w'\lambda'} = -K_\lambda \partial_z \bar{\lambda} + \Gamma_\lambda$$

Eddy diffusivity

$$K_\lambda(\sigma) = h_b \underbrace{w_\lambda(\sigma)}_{\text{circled}} G(\sigma), \quad \sigma = z/h_b$$

~~Boundary layer depth~~ × ~~Turbulent velocity scale~~ × ~~Shape function~~

Boundary layer depth
determined by

$$\text{Ri}_b = \frac{z[b_r - \bar{b}(z)]}{[\mathbf{u}_r - \bar{\mathbf{u}}(z)]^2 + \underbrace{U_{tL}^2(z)}_{\text{circled}}}$$

Buoyancy
Resolved shear + Unresolved shear

CESM2.1 ✓

Enhanced vertical mixing

- ▶ Enhancing the turbulent velocity scale by an enhancement factor
- ▶ Scaling derived from LES

$$\mathcal{E} = |\cos \theta_{wl}| \left[1 + (3.1 \text{La}_{\text{SLP}})^{-2} + (5.4 \text{La}_{\text{SLP}})^{-4} \right]^{1/2},$$

CESM2.2 →

Enhanced mixed layer entrainment

- ▶ Enhancing the entrainment at the base of the ocean surface boundary layer by enhancing the unresolved shear term
- ▶ Scaling derived from LES

$$U_{tL}^2(z) = \frac{C_v N(z) w_\lambda(z) |z|}{\text{Ri}_c} \left[\frac{0.15 w_*^3 + 0.17 u_*^3 (1 + 0.49 \text{La}_{\text{SL}}^{-2})}{w_\lambda(z)^3} \right]^{1/2},$$

Summer MLD

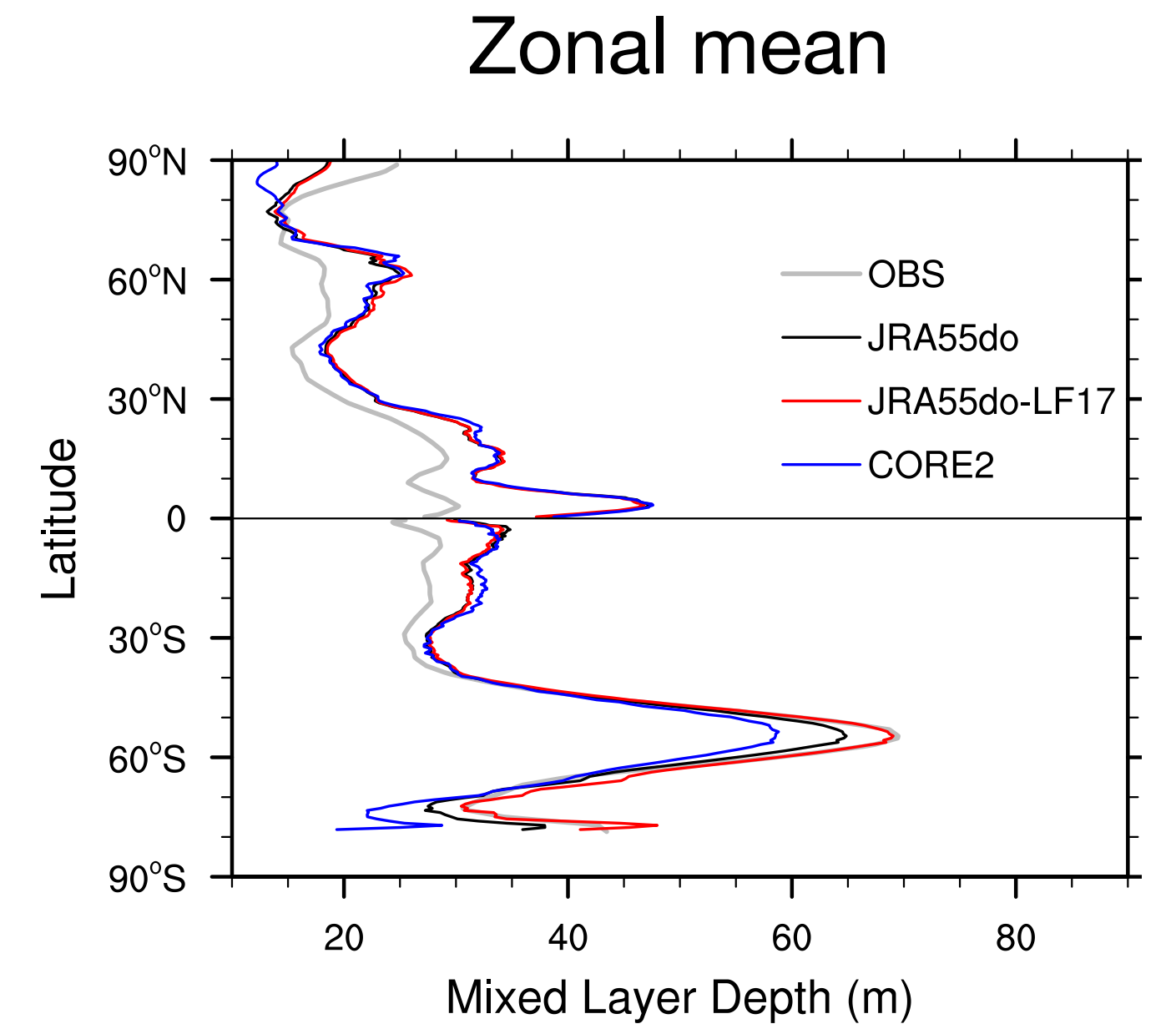
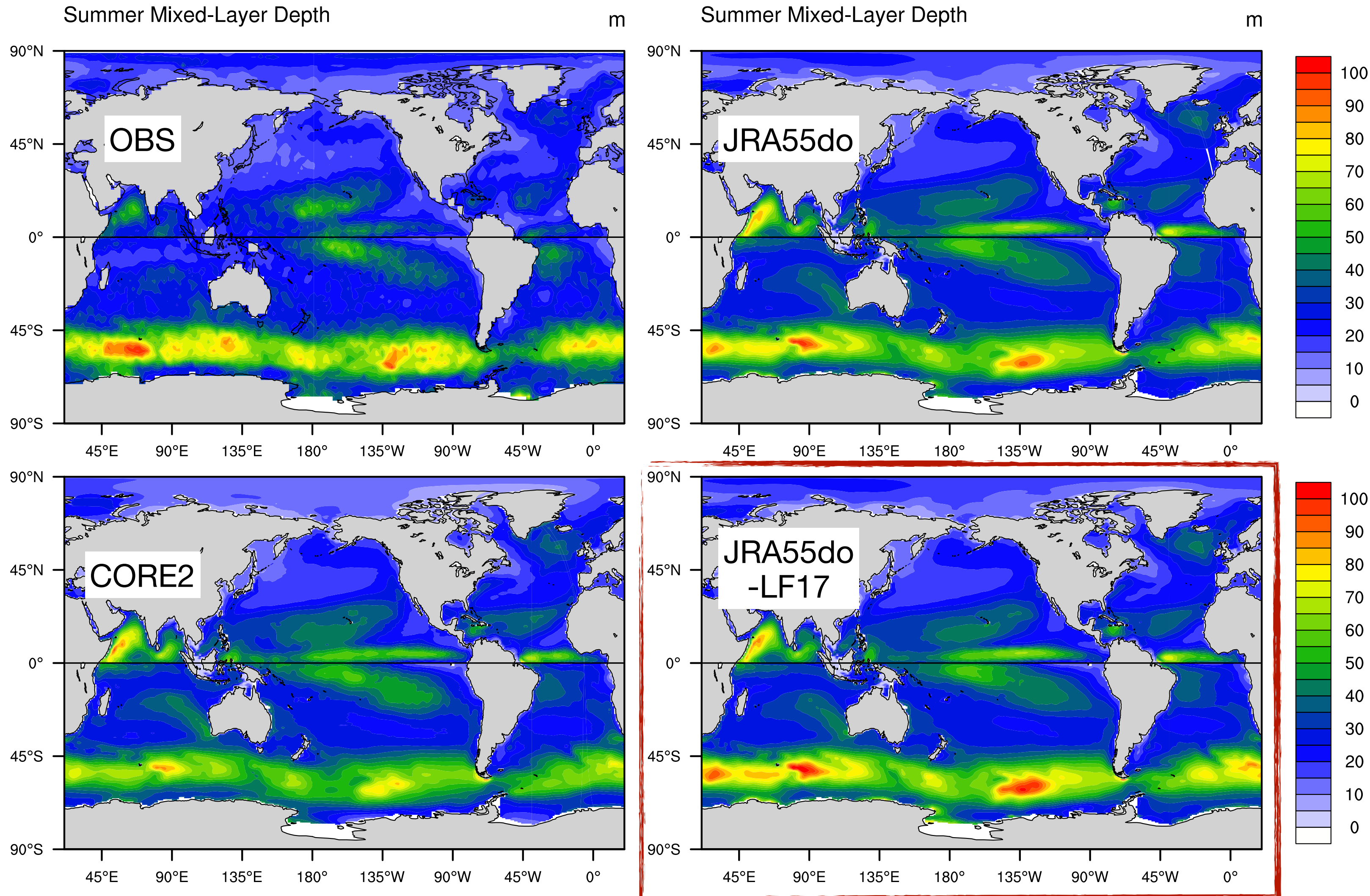
1980-2009: years 23-52 for JRA55do & 33-62 for CORE2

OBS: de Boyer Montégut et al. (2004)

JRA55do: g.e21.GOMIPECOIAF_JRA.TL319_g17.CMIP6-omip2.001

CORE2: g.e21.GOMIPECOIAF.T62_g17.CMIP6-omip1.001

JRA55do-LF17: 20200517_LF17_GOMIPECOIAF_JRA-1p4-2018_TL319_g17



RMSE (m)

	Global	S of 30S	30S-30N
JRA55do	7.65	7.04	8.80
JRA55do-LF17	7.57	7.06	8.63
CORE2	8.54	9.09	9.16

Winter MLD

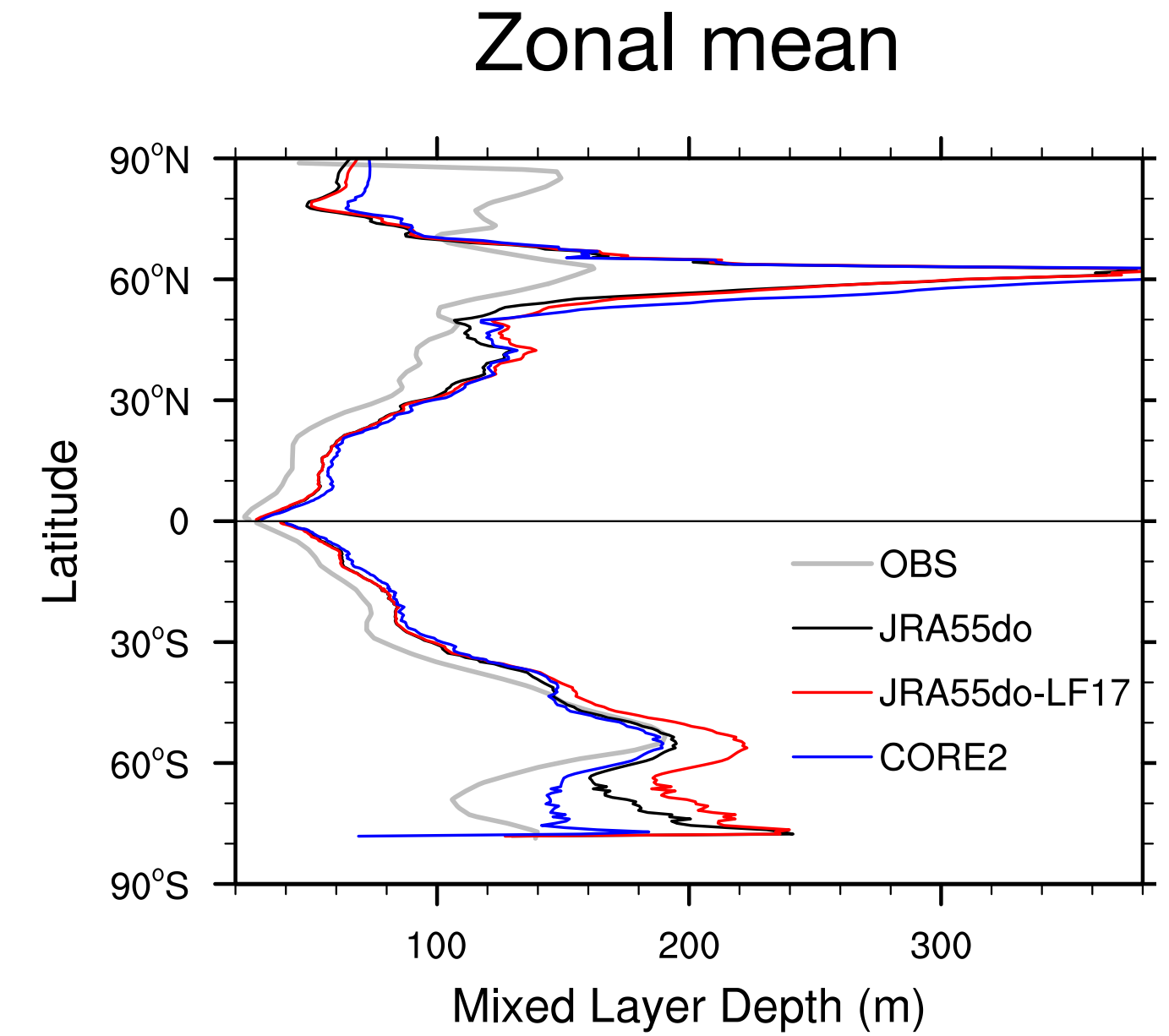
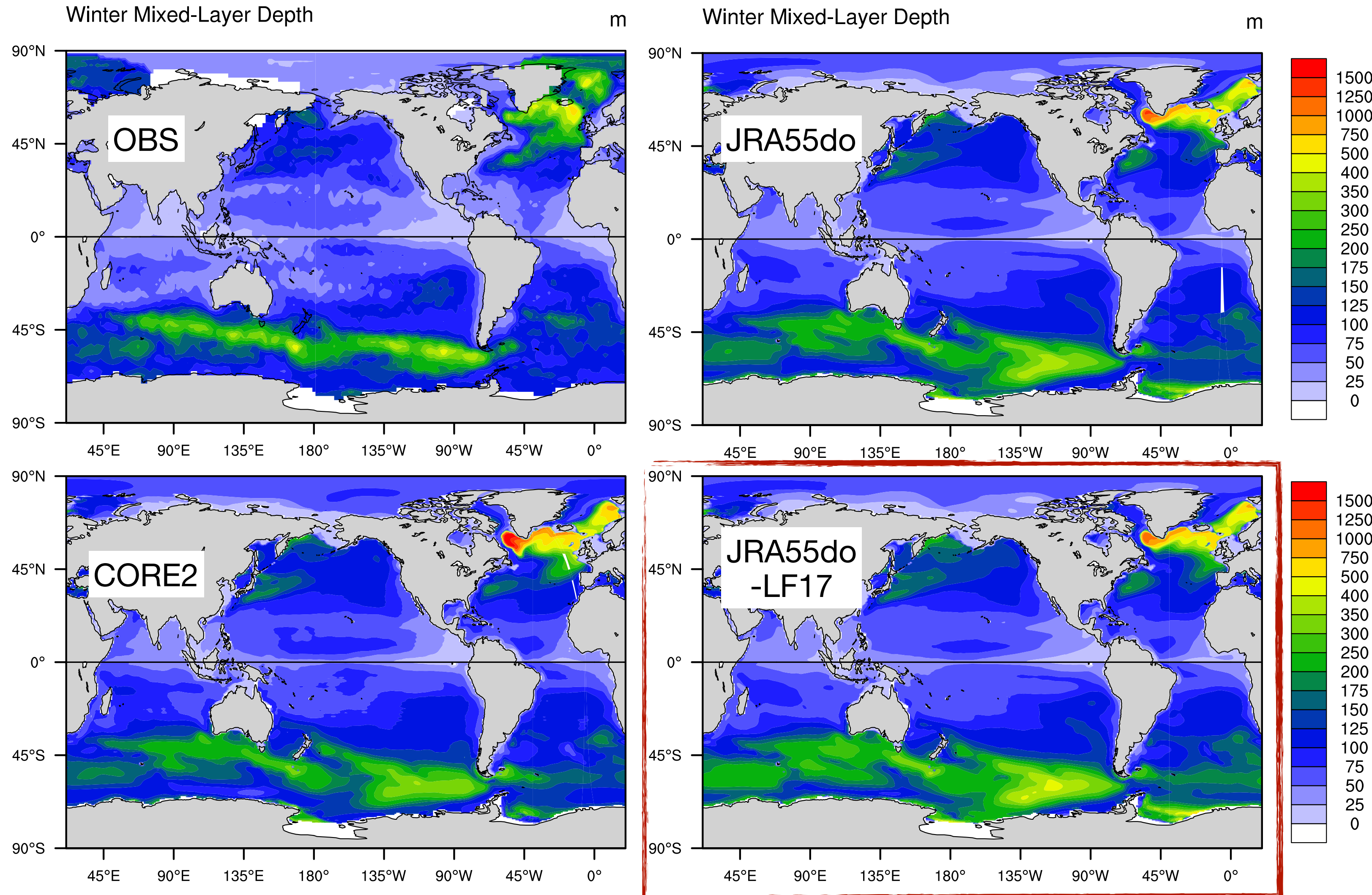
1980-2009: years 23-52 for JRA55do & 33-62 for CORE2

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JRA55do: g.e21.GOMIPECOIAF_JRA.TL319_g17.CMIP6-omip2.001

CORE2: g.e21.GOMIPECOIAF.T62_g17.CMIP6-omip1.001

JRA55do-LF17: 20200517_LF17_GOMIPECOIAF_JRA-1p4-2018_TL319_g17



RMSE (m)

	Global	S of 30S	30S-30N
JRA55do	47.40	47.16	16.89
JRA55do-LF17	50.67	57.81	16.89
CORE2	62.74	45.20	20.55

The “Theory Wave”

An empirical estimate of the Stokes drift

Surface layer averaged Stokes drift
-> Stokes drift profile

Empirical wave spectra + Directional spreading of wind waves

$$u_{SL}^S \approx u_0^S \left\{ \begin{aligned} &0.715 \\ &+ \left(\frac{0.151}{k_p H_{SL}} - 0.840 \right) [1 - T_1(k_p, H_{SL})] \\ &- \left(0.840 + \frac{0.0591}{k_p H_{SL}} \right) T_2(k_p, H_{SL}) \\ &+ \left(\frac{0.0632}{k_p^* H_{SL}} + 0.125 \right) [1 - T_1(k_p^*, H_{SL})] \\ &+ \left(0.125 + \frac{0.0946}{k_p^* H_{SL}} \right) T_2(k_p^*, H_{SL}) \end{aligned} \right\},$$

Empirical relations between wind & waves

$$\begin{aligned} u_0^S &\approx 0.016 U_{10}, \\ V^S &\approx 2.67 \times 10^{-5} g U_{10}^3, \\ k_p &\approx 0.176 \frac{u_0^S}{V^S}, \\ k_p^* &= 2.56 k_p, \\ H_{SL} &= H_{BL}/5, \\ T_1(k, z) &= e^{2kz}, \\ T_2(k, z) &= \sqrt{2\pi k|z|} \operatorname{erfc}\left(\sqrt{2k|z|}\right), \end{aligned}$$

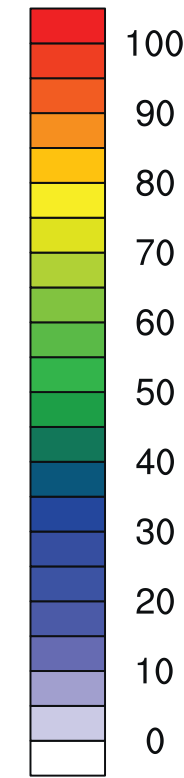
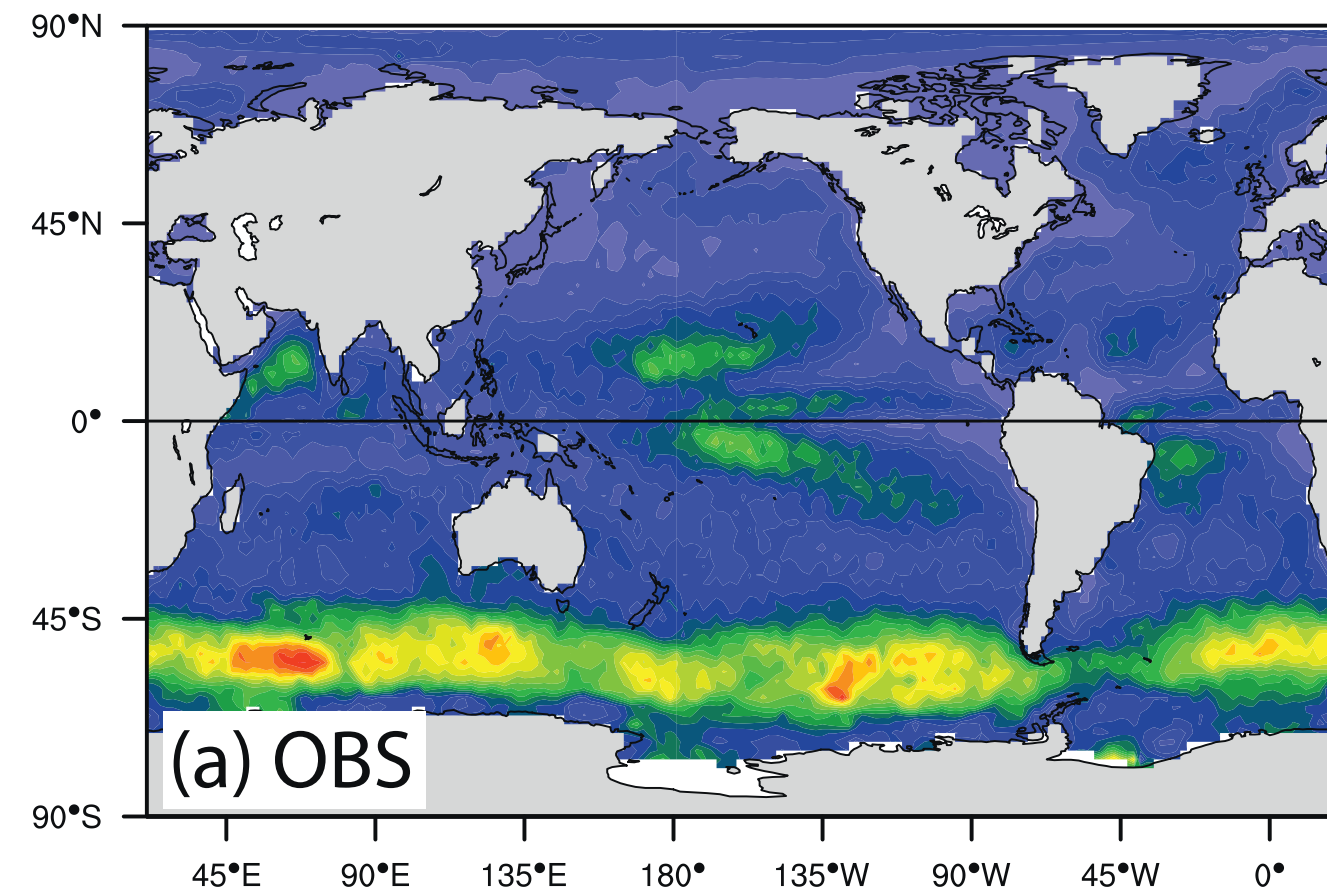
Langmuir number $La_{SL} = \sqrt{\frac{u^*}{u_{SL}^S}},$

Langmuir enhancement factor $\mathcal{E} = \sqrt{1 + (1.5La_{SL})^{-2} + (5.4La_{SL})^{-4}}.$

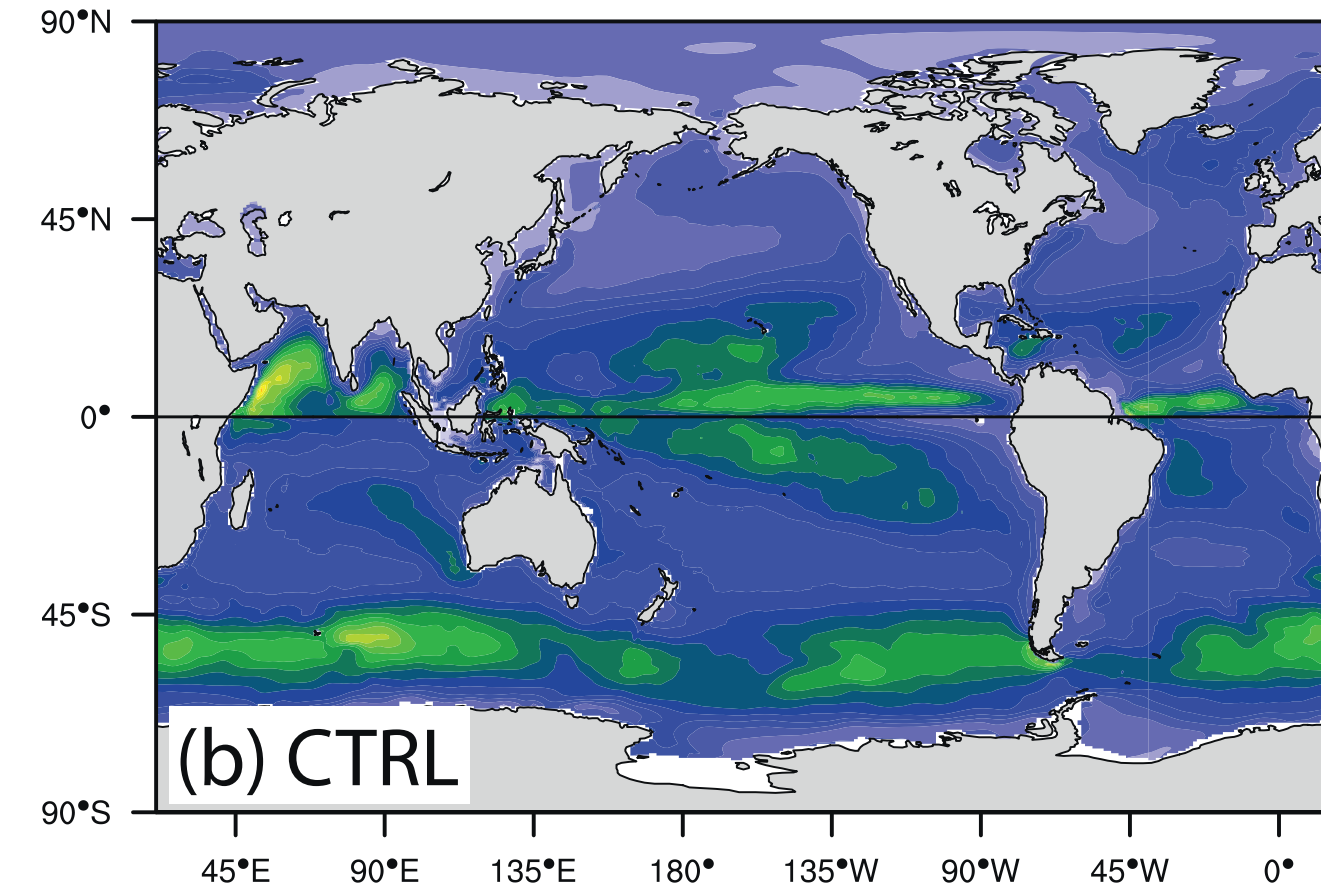
The “Theory Wave”

Tests in CESM1 forced by CORE-II

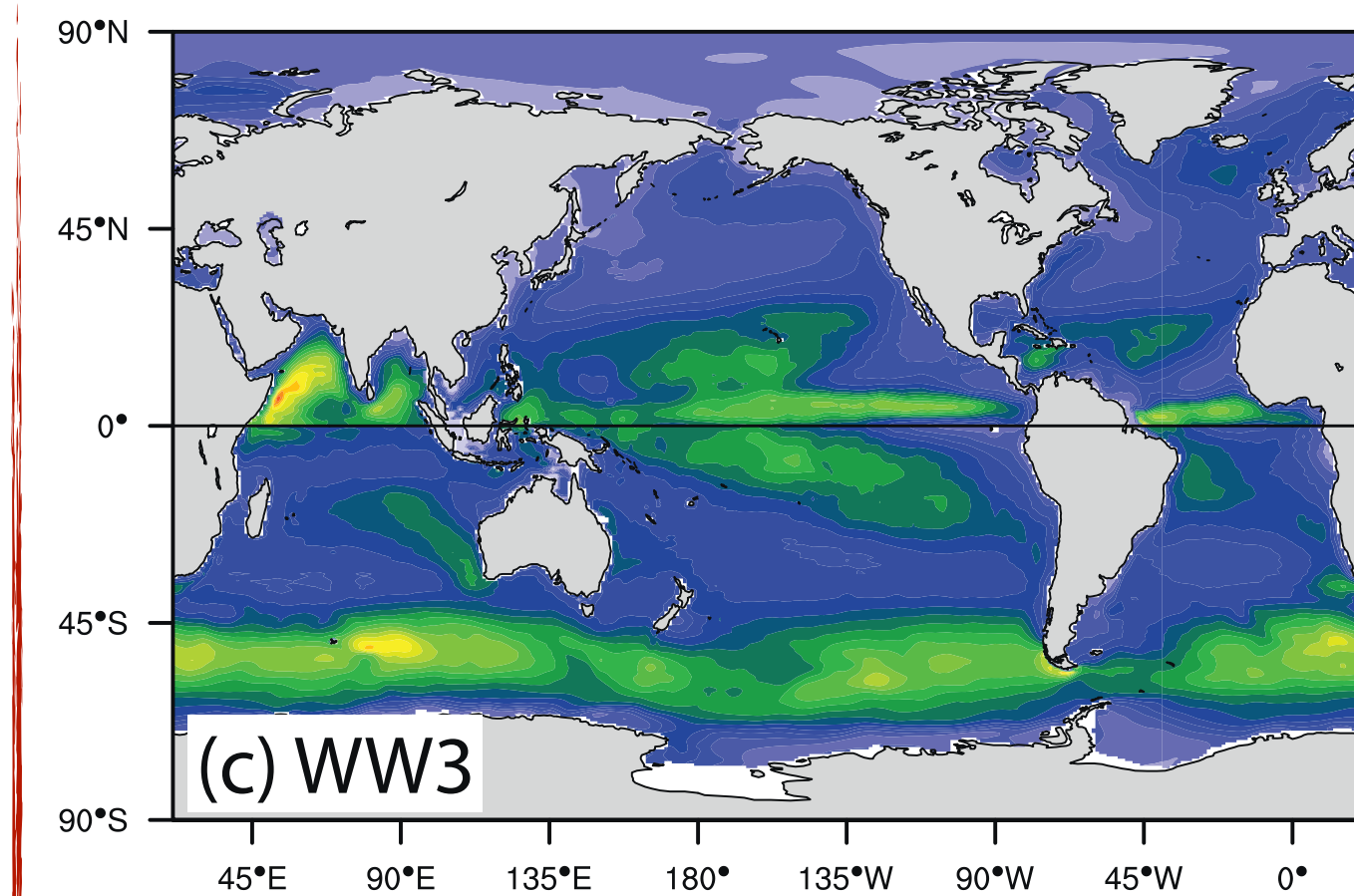
Observation



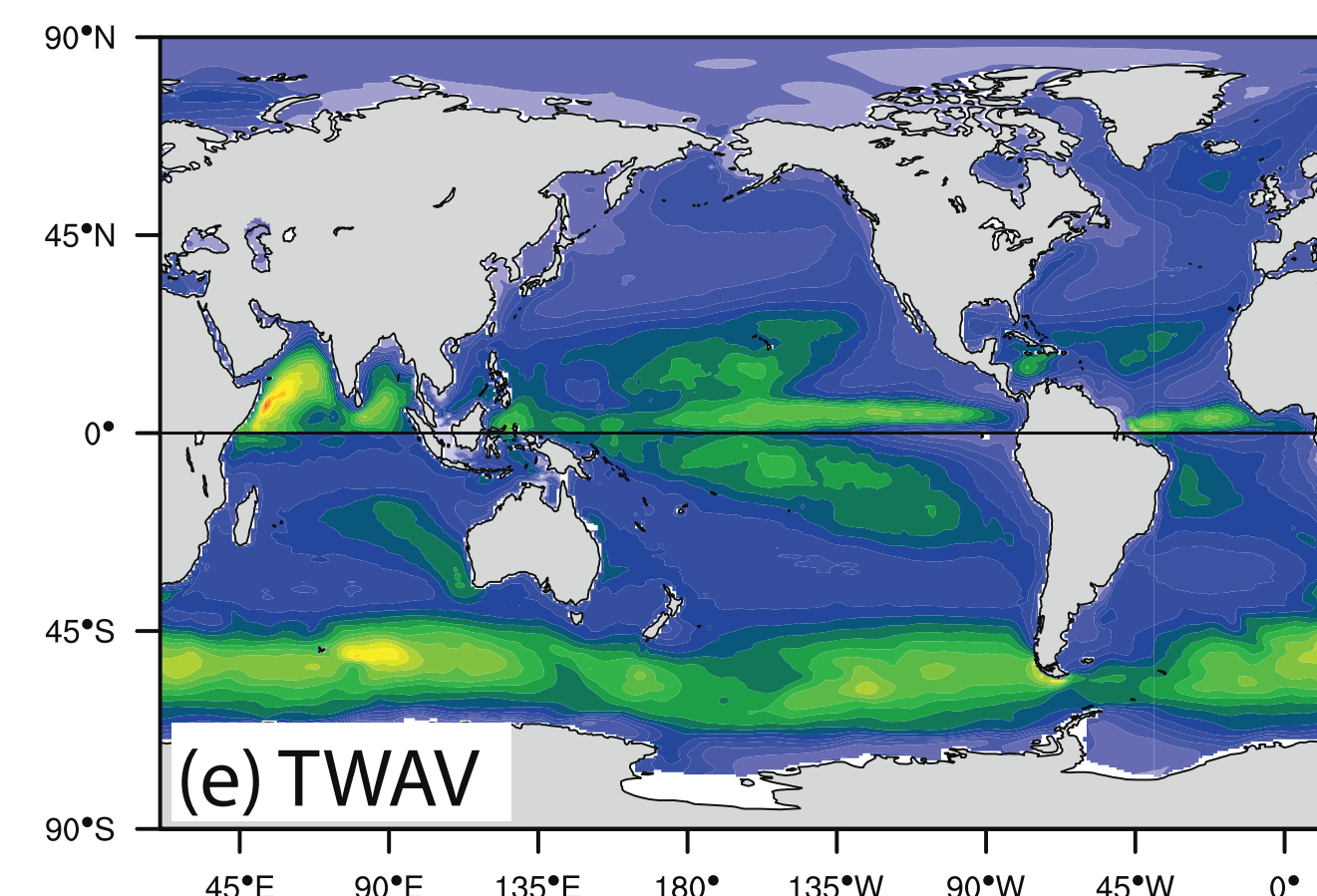
No Langmuir mixing



Langmuir mixing with WW3



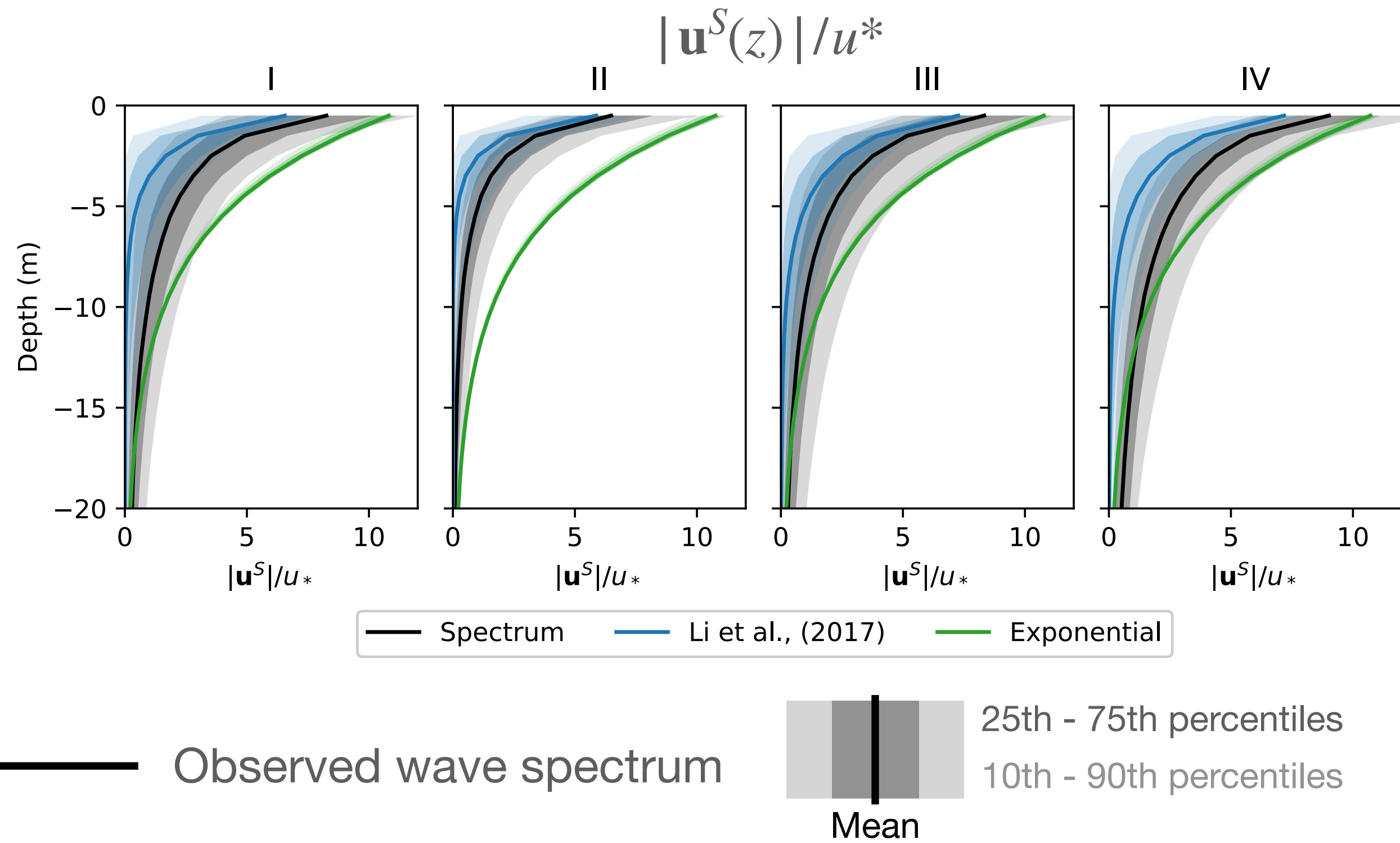
Langmuir mixing with “Theory Wave”



Summer mean mixed layer depth (m)

The “Theory Wave”

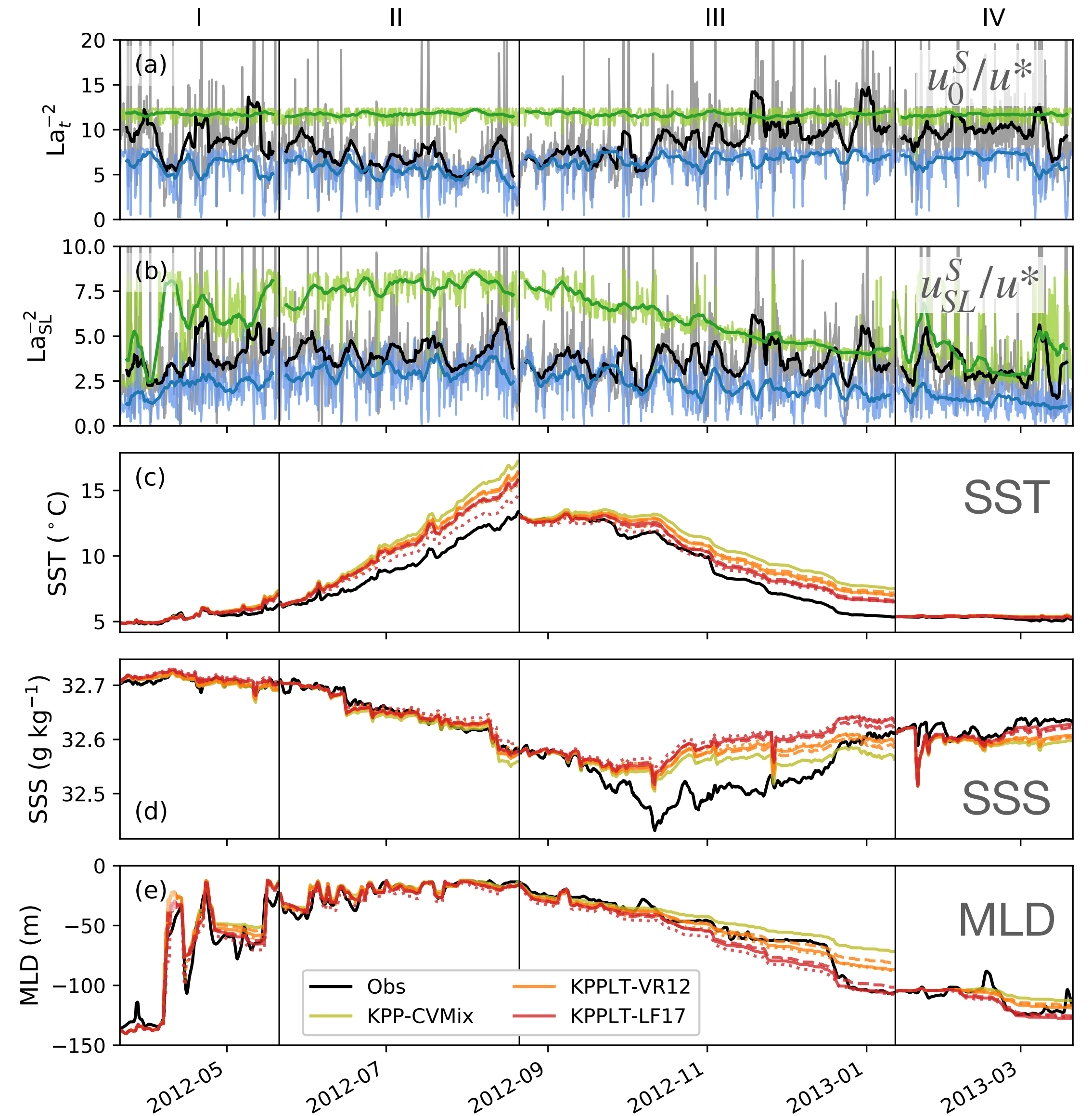
An example at Ocean Station Papa



— Observed wave spectrum

- - - “Theory Wave”

⋯ Exponential ($La_t = 0.3, \delta^S = 5 \text{ m}$), $\mathbf{u}^S(z) = \mathbf{u}_0^S \exp\left(\frac{z}{\delta^S}\right)$



An annual cycle at Ocean Station Papa

Wave coupling

- Wave component in CESM
 - WW3
 - A “theory wave” option in the “data wave” mode (DWAV)
 - An estimate of the Stokes drift profile -> Langmuir number & Langmuir enhancement factor for Langmuir mixing parameterizations
 - Other wave parameters?
- Wave coupling interface
 - Wave statistics passed to the coupler

Wave statistics

- Stokes drift (e.g., surface Stokes drift partitions)
- Momentum fluxes, energy fluxes, breaking waves, etc
- COWCLIP wave statistics — (significant wave height, mean wave period, mean wave direction, swell wave height)
 - COWCLIP standard: diagnosed offline from 6-hourly output
 - mean, maximum, 10th, 50th, 90th, 95th, 99th percentiles (monthly, seasonal and annual)
- CESM standard output from the coupler, but keep the option to turn on the WW3 output in the native format

Moving forward

- Langmuir turbulence parameterization in MOM6 via CVMix
- The “theory wave” as an option in the “data wave” mode (DWAV)
- Update WW3 to the latest version, wave grid
- Wave coupling interface:
 - Wave variables for parameterizations (e.g., Langmuir turbulence, wave-ice interactions)
 - Wave statistics for wave climate analysis (e.g., COWCLIP)

Thank you!