



Conservation of dry air, water, and energy in CAM and its impact on tropical rainfall

August 24, 2021

Bryce Harrop¹

Mike Pritchard², Hossein Parishani², Andrew Gettelman³,

Samson Hagos¹, Peter Lauritzen³, Ruby Leung¹,

Jian Lu¹, Kyle Pressel¹, Koichi Sakaguchi¹



PNNL is operated by Battelle for the U.S. Department of Energy

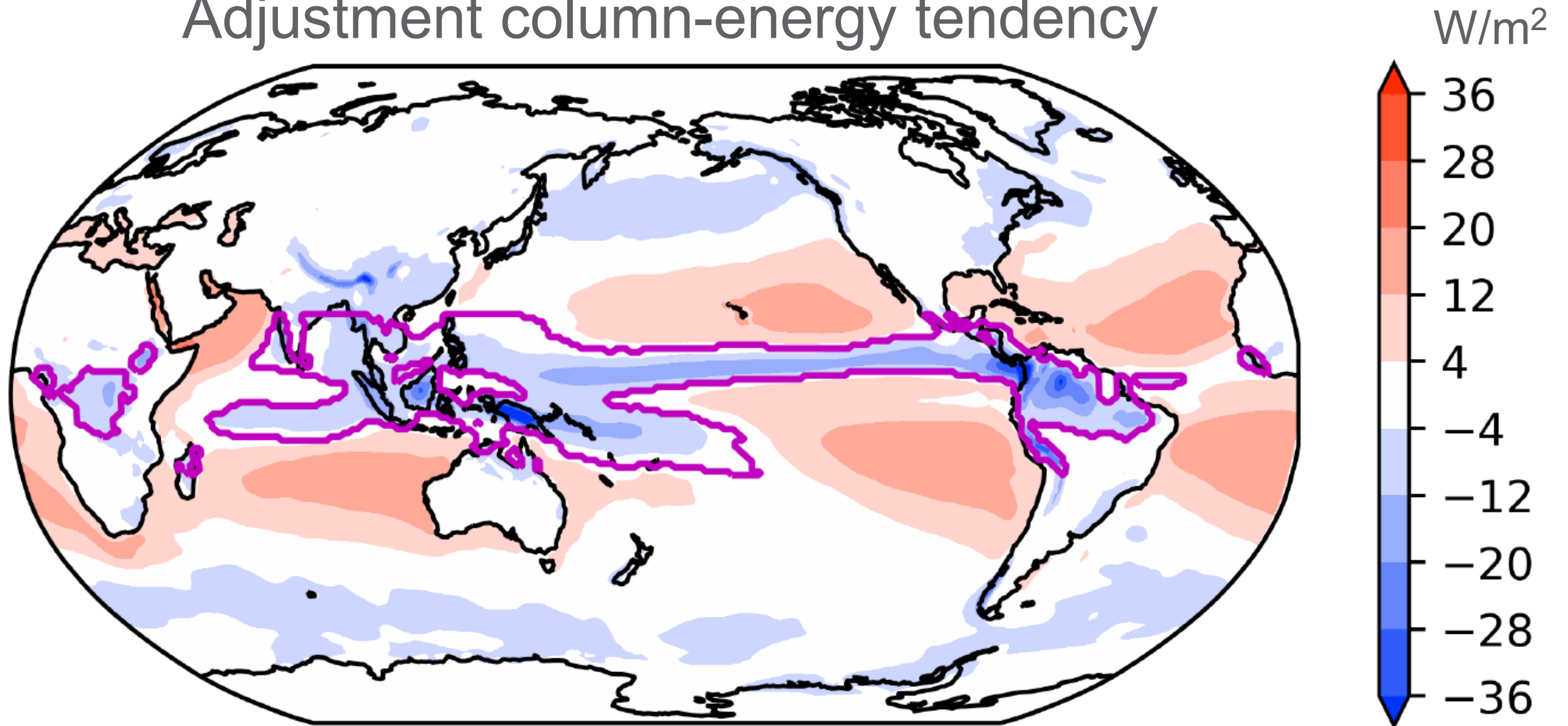
¹PNNL

²UC-Irvine

³NCAR

Closing the energy budget requires accounting for the column-energy tendency from a mass adjustment routine

Adjustment column-energy tendency

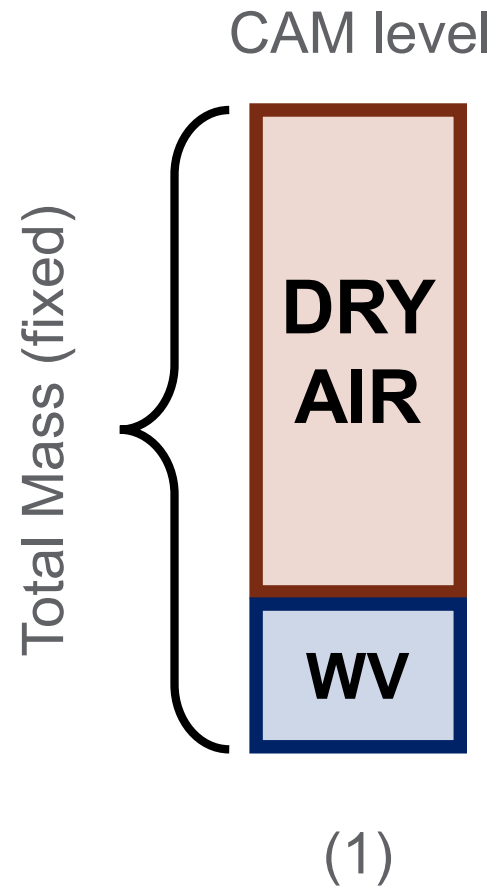


Closing the energy budget requires accounting for the column-energy tendency from a mass adjustment routine

Adjustment column-energy tendency



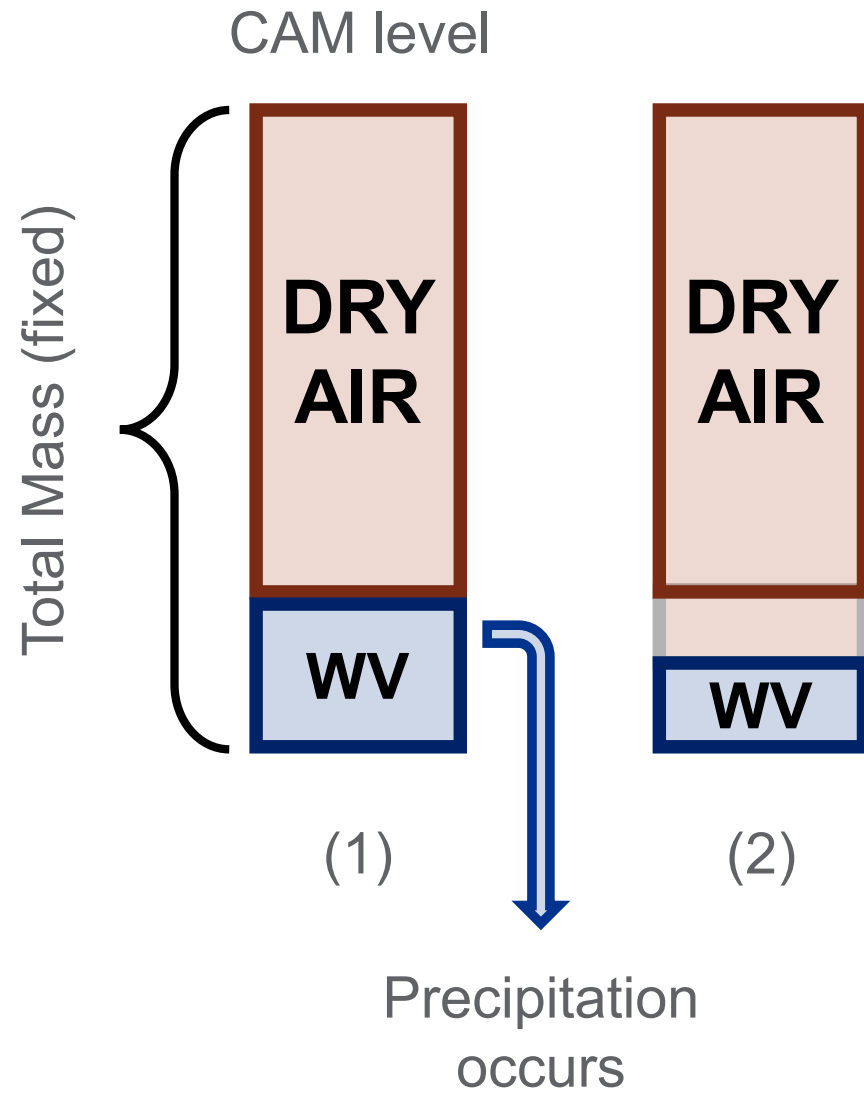
CAM use a fixed hydrostatic pressure thickness to compute mass of each vertical layer, which is the sum of dry air and vapor



$$\text{Layer mass} = \frac{\delta^k p}{g} = m_t = m_d + m_v$$

Assumed fixed during physics

Vapor mass can change during the physics, which breaks dry air conservation

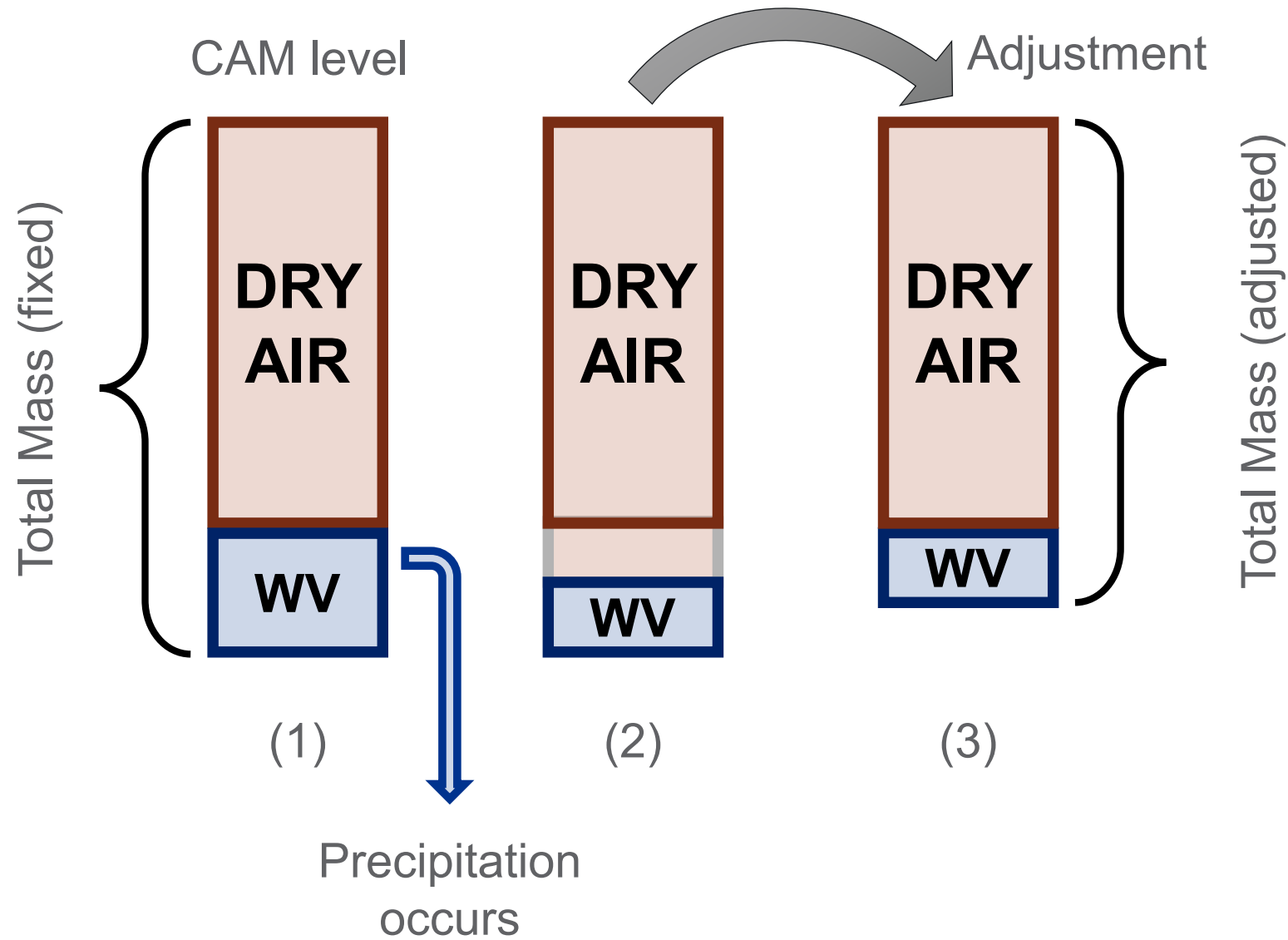


$$(1) \quad m_t = m_d + m_v$$

$$(2) \quad m_t \neq m_d + m_v^*$$

*after physics (m_v)

To avoid spurious dry mass changes, total mass changes to match water vapor mass change



$$(1) \quad m_t = m_d + m_v$$

$$(2) \quad m_t \neq m_d + m_v^*$$

$$(3) \quad m_t^* = m_d + m_v^*$$

*after physics (m_v)

*after adjust (m_t)

This adjustment happens after all of the physics parameterizations have been called.

CAM tracks column-energy budget for conservation purposes

Assumptions
Column-integrated
Hydrostatic balance

Sum over
 k levels

$$\varepsilon = \frac{1}{g} \sum_k \underbrace{c_{pd} m_t^k T^k + L_s m_v^k + L_f m_l^k}_{\text{Enthalpy}} + \underbrace{m_t^k \frac{(\mathbf{u}^k)^2}{2}}_{\text{Kinetic Energy}} + \sum_k m_t^k \Phi_s$$

Enthalpy

Kinetic
Energy

Surface
Geopotential

CAM tracks column-energy budget for conservation purposes

Assumptions
Column-integrated
Hydrostatic balance

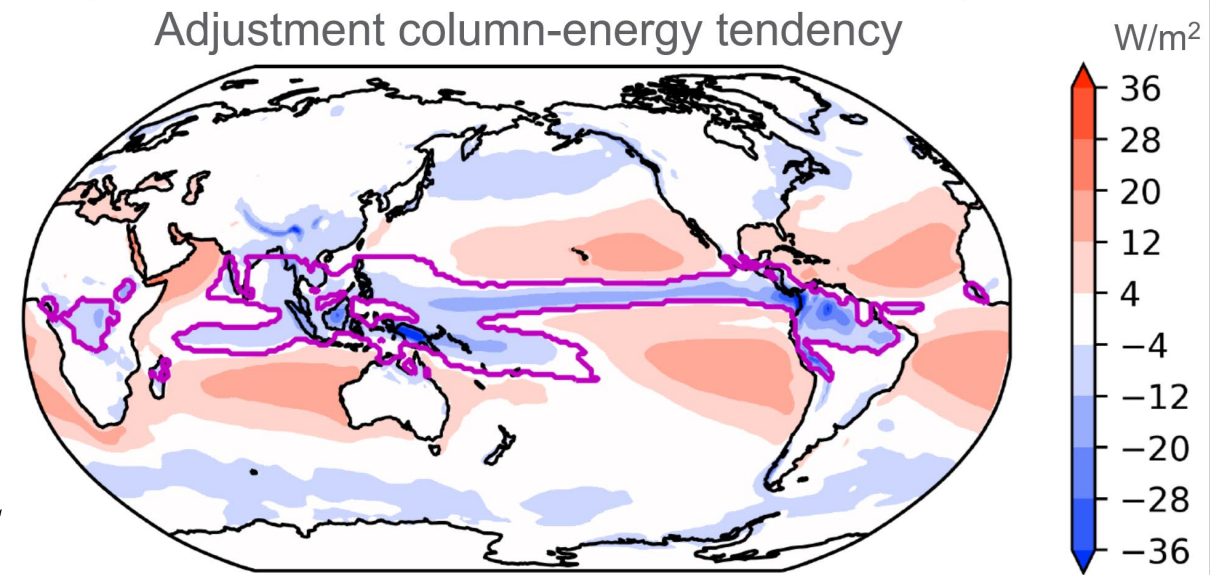
$m_t = m_d + m_v$

Sum over k levels

$$\varepsilon = \frac{1}{g} \sum_k \underbrace{c_{pd} m_t^k T^k + L_s m_v^k + L_f m_l^k}_{\text{Enthalpy}} + \underbrace{m_t^k \frac{(\mathbf{u}^k)^2}{2}}_{\text{Kinetic Energy}} + \sum_k m_t^k \Phi_s \quad \uparrow \text{Surface Geopotential}$$

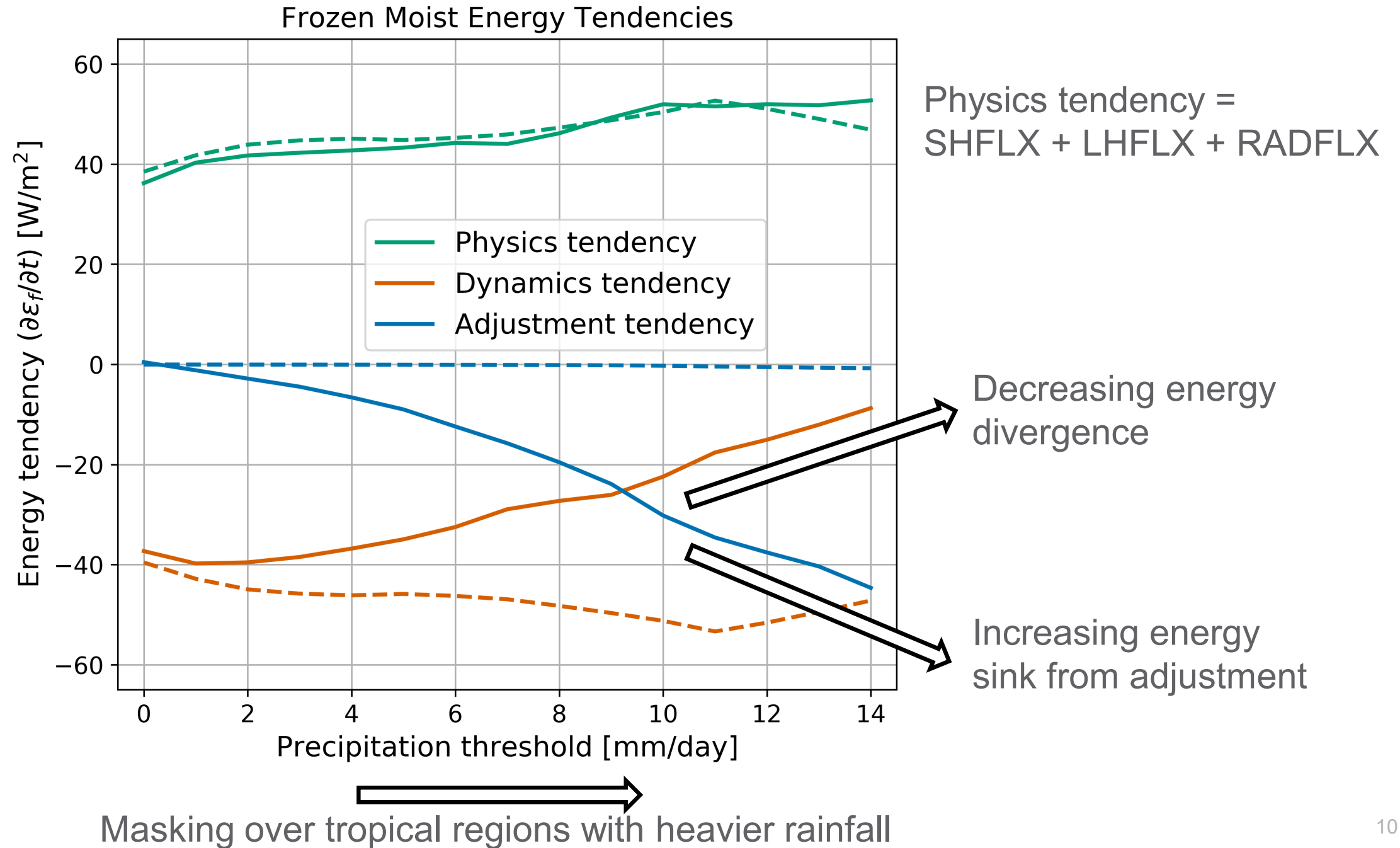
During the adjustment
 $\Delta m_t = \Delta m_v$

$$\Delta \mathcal{E}_{\text{adj}} = \sum_k \left(c_{pd} \Delta m_v^k T^k + \Delta m_v^k \frac{(\mathbf{u}^k)^2}{2} \right) + \sum_k \Delta m_v^k \Phi_s$$

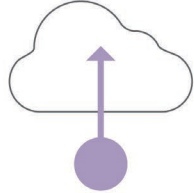
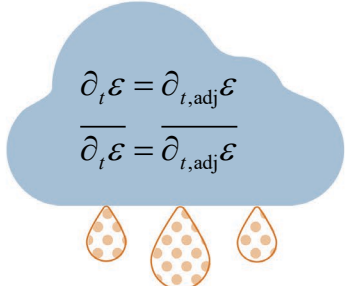
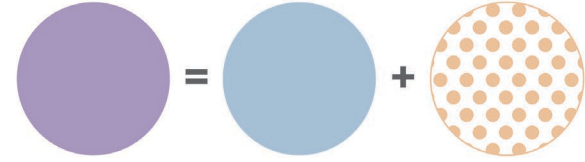
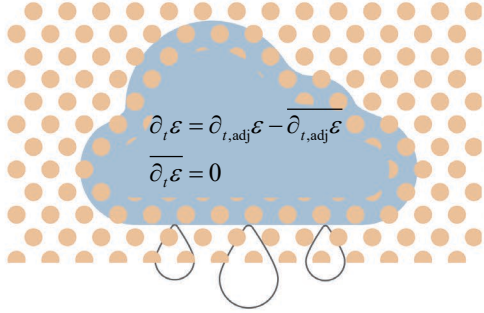
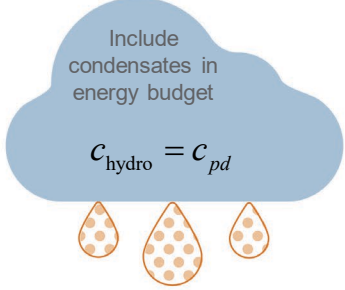
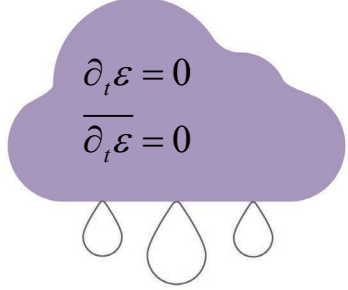
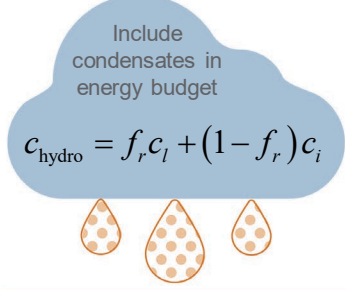


Water vapor is included in the mass used for CAM's energy expression. It has internal, potential, and kinetic energy, just like the dry air. When water vapor changes phase, only its latent energy is retained in the model. The remaining internal, potential, and kinetic energy are left to the global fixer to handle. The remaining local imbalance violates the divergence theorem.


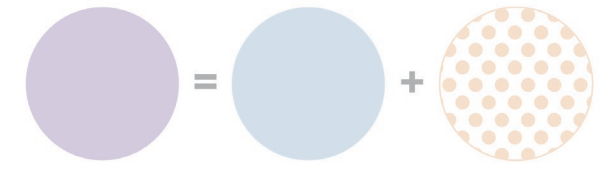
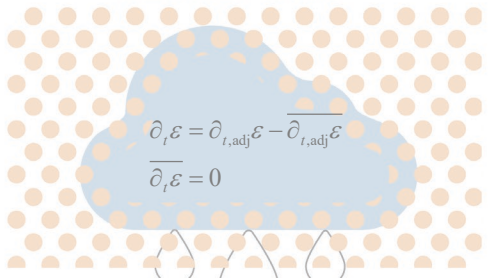
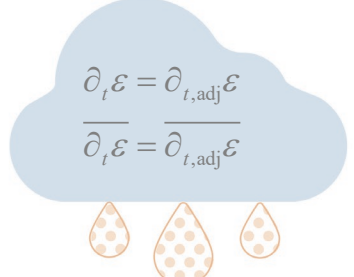
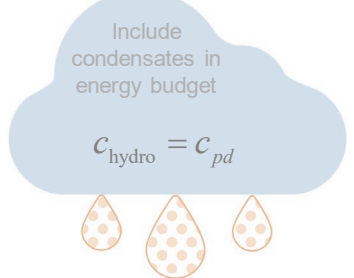
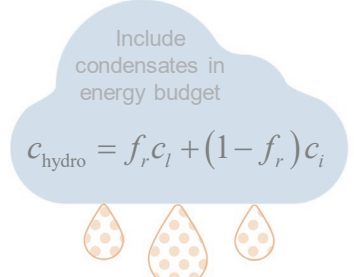
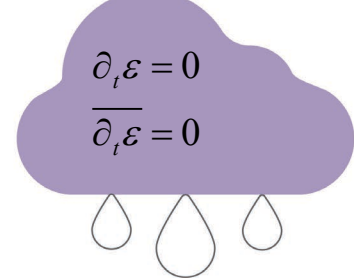
In regions of heavier rainfall, CAM diverges less energy



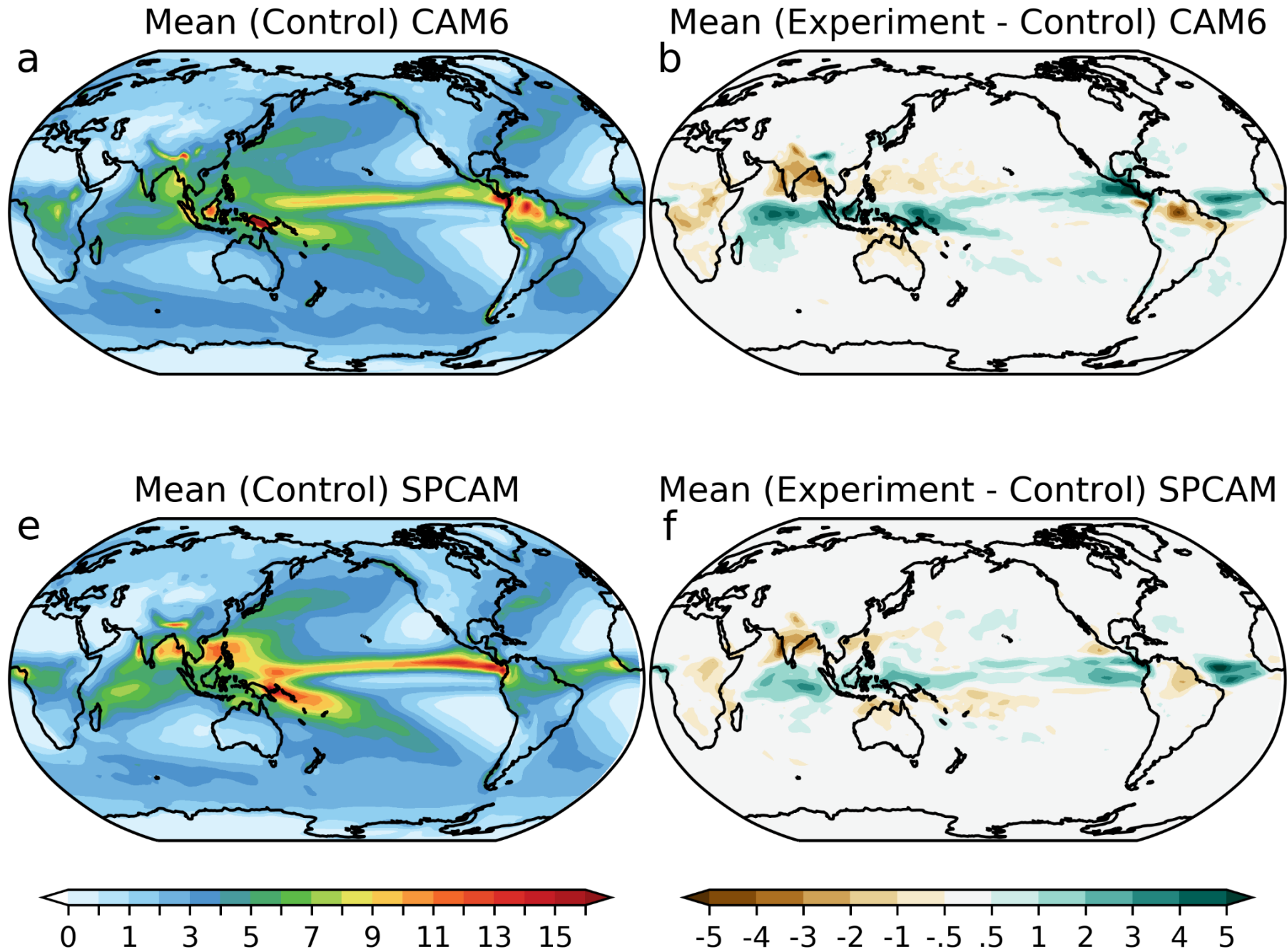
A fix is needed for CAM to satisfy the divergence theorem locally (make atm tendency match TOA + SFC fluxes)

KEY	POSSIBLE ENERGY PATHWAYS		
 <p>Lofted water vapor condenses and rains out</p>		<p>A Use adj. energy tend. at surface</p>  $\partial_t \mathcal{E} = \partial_{t, \text{adj}} \mathcal{E}$ $\overline{\partial_t \mathcal{E}} = \overline{\partial_{t, \text{adj}} \mathcal{E}}$ <p>PHF = $\partial_t \mathcal{E}_{\text{adj}}$</p>	
 <p>Total water vapor energy = Latent energy + Remaining IE + KE + PE</p>	<p>DEFAULT CAM6</p>  $\partial_t \mathcal{E} = \partial_{t, \text{adj}} \mathcal{E} - \overline{\partial_{t, \text{adj}} \mathcal{E}}$ $\overline{\partial_t \mathcal{E}} = 0$ <p>PHF = $\overline{\text{PHF}} = 0$</p>	<p>B Simple enthalpy (CAM6)</p>  <p>Include condensates in energy budget</p> $c_{\text{hydro}} = c_{pd}$ <p>PHF = $c_{pd} PT_{\text{rain}}$</p>	<p>D Local energy fixer</p>  $\partial_t \mathcal{E} = 0$ $\overline{\partial_t \mathcal{E}} = 0$ <p>PHF = $\overline{\text{PHF}} = 0$</p>
<p>$\partial_t \mathcal{E}$ = Local time-tendency of column energy</p> <p>$\overline{\partial_t \mathcal{E}}$ = Global time-tendency of column energy</p> <p>PHF = Precipitation heat flux at surface</p>		<p>C Rigorous enthalpy</p>  <p>Include condensates in energy budget</p> $c_{\text{hydro}} = f_r c_l + (1 - f_r) c_i$ <p>PHF = $(f_r c_l + (1 - f_r) c_i) PT_{\text{hydro}}$</p>	

A fix is needed for CAM to satisfy the divergence theorem locally (make atm tendency match TOA + SFC fluxes)

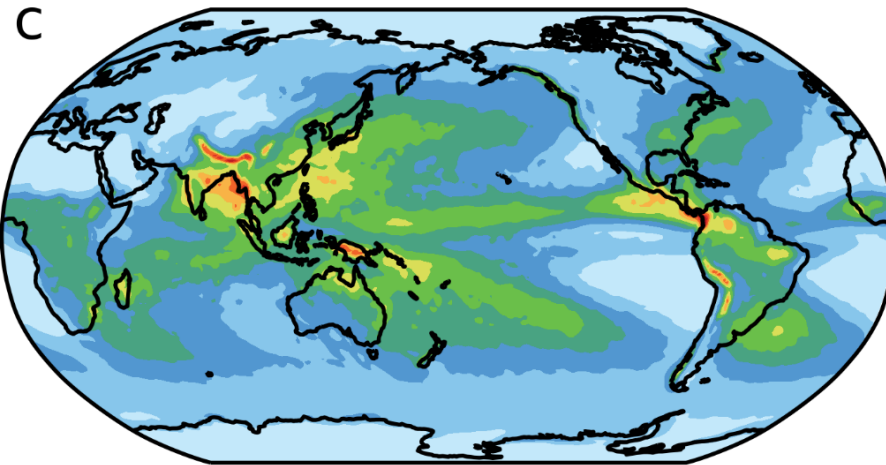
KEY	POSSIBLE ENERGY PATHWAYS		
 <p>Lofted water vapor condenses and rains out</p>			
 <p>Total water vapor energy = Latent energy + Remaining IE + KE + PE</p>	<p>DEFAULT CAM6</p>  $\partial_t \varepsilon = \partial_{t, \text{adj}} \varepsilon - \overline{\partial_{t, \text{adj}} \varepsilon}$ $\overline{\partial_t \varepsilon} = 0$ <p>PHF = $\overline{\text{PHF}} = 0$</p>		
<p>$\partial_t \varepsilon$ = Local time-tendency of column energy</p> <p>$\overline{\partial_t \varepsilon}$ = Global time-tendency of column energy</p> <p>PHF = Precipitation heat flux at surface</p>	<p>A Use adj. energy tend. at surface</p>  $\partial_t \varepsilon = \partial_{t, \text{adj}} \varepsilon$ $\overline{\partial_t \varepsilon} = \overline{\partial_{t, \text{adj}} \varepsilon}$ <p>PHF = $\partial_t \varepsilon_{\text{adj}}$</p> <p>B Simple enthalpy (CAM6)</p>  <p>Include condensates in energy budget</p> $c_{\text{hydro}} = c_{pd}$ <p>PHF = $c_{pd} PT_{\text{rain}}$</p> <p>C Rigorous enthalpy</p>  <p>Include condensates in energy budget</p> $c_{\text{hydro}} = f_r c_l + (1 - f_r) c_i$ <p>PHF = $(f_r c_l + (1 - f_r) c_i) PT_{\text{hydro}}$</p> <p>D Local energy fixer</p>  $\partial_t \varepsilon = 0$ $\overline{\partial_t \varepsilon} = 0$ <p>PHF = $\overline{\text{PHF}} = 0$</p>		

Tested in both parameterized-convection CAM6 and SPCAM. Responses are similar

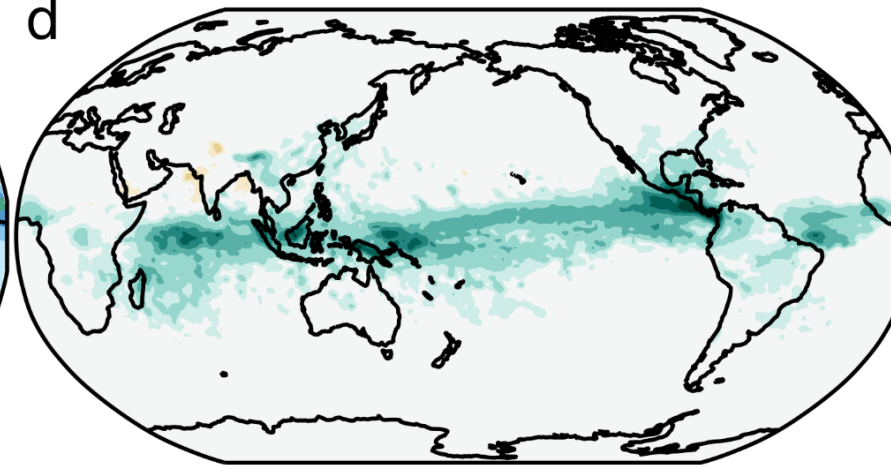


Large increases in daily rainfall variability across the Tropics

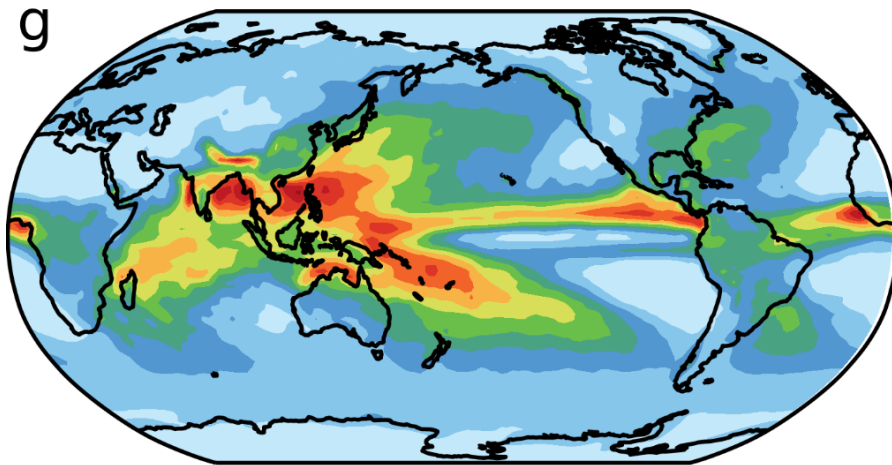
Std. Dev. (Control) CAM6



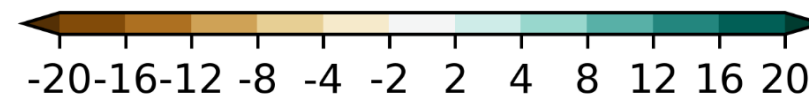
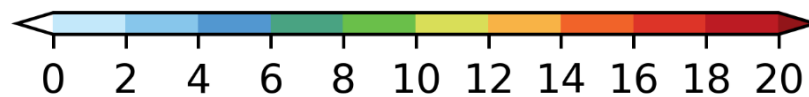
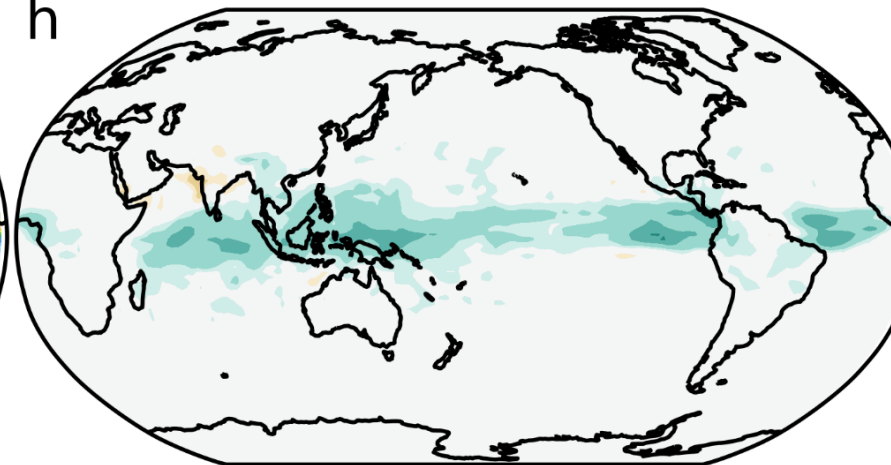
Std. Dev. (Experiment - Control) CAM6



Std. Dev. (Control) SPCAM

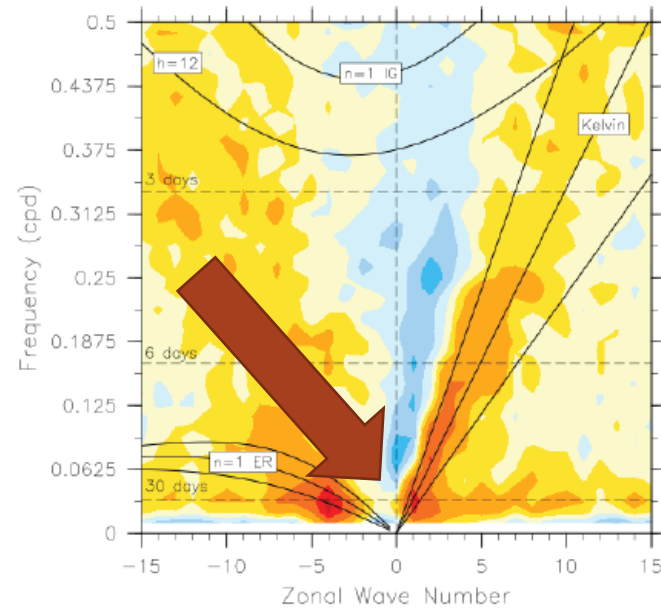


Std. Dev. (Experiment - Control) SPCAM

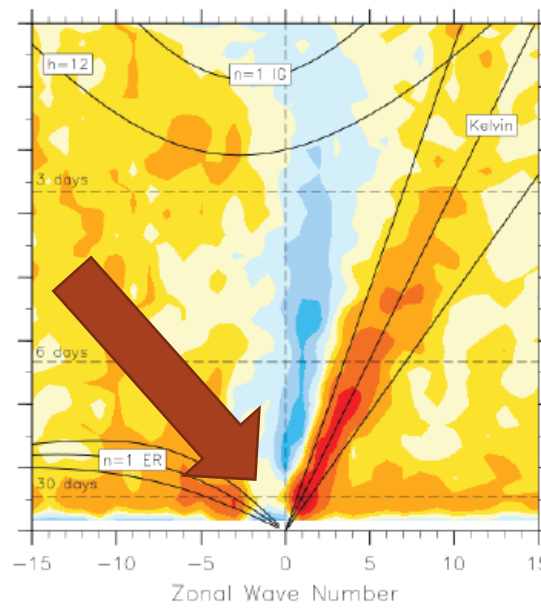


Increase in strength of MJO between Experiment and Control similar to the increase between SPCAM and CAM.

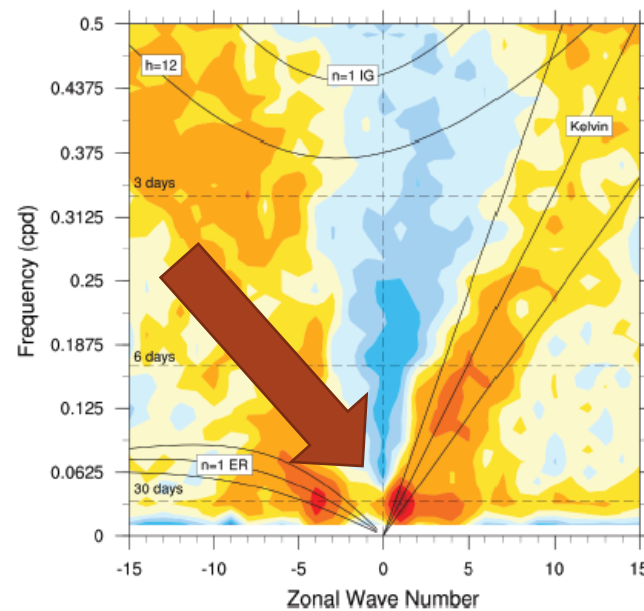
a) Control



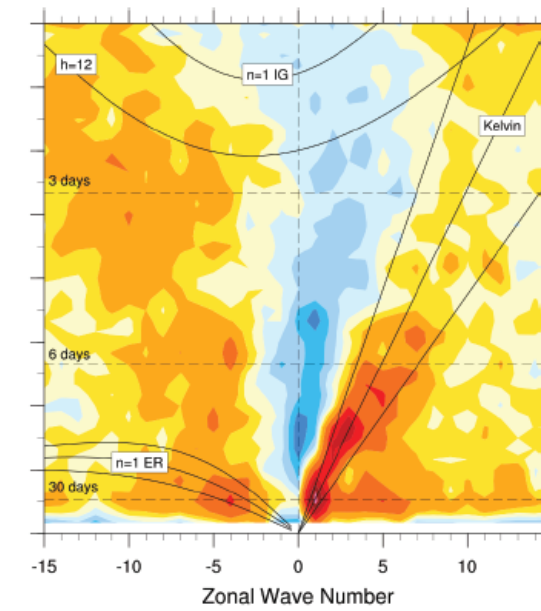
b) Experiment



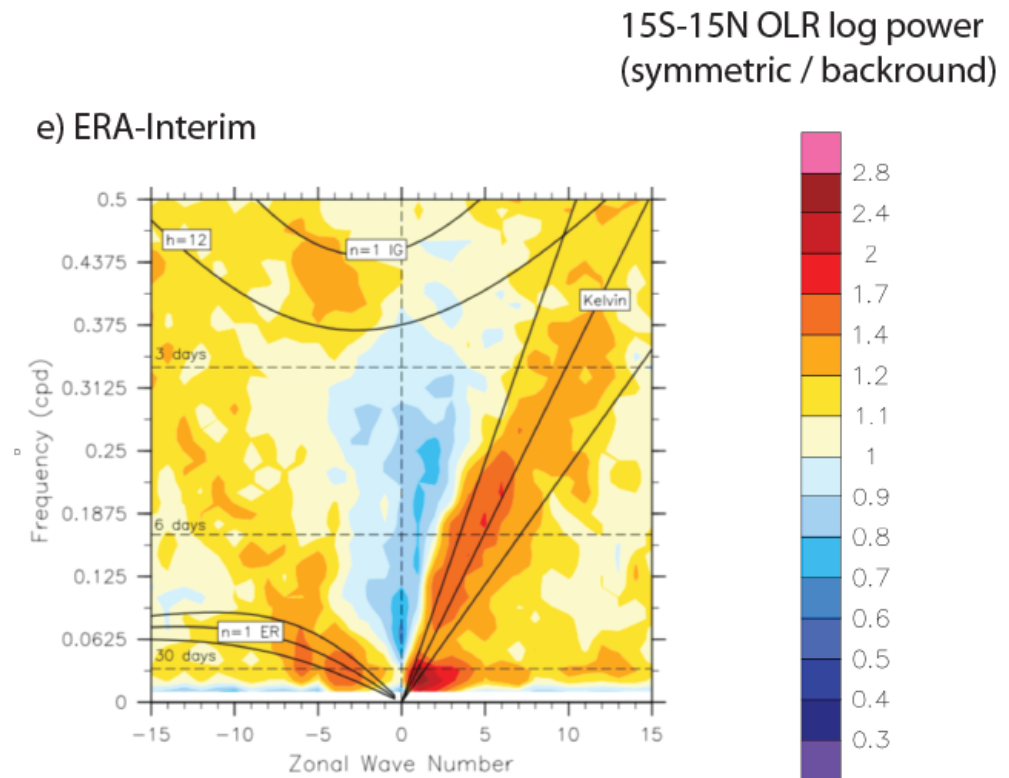
c) Superparameterized Control



d) Superparameterized Experiment



e) ERA-Interim



What do we takeaway from all of this?

- In CAM, **water vapor has internal, kinetic, and potential energy, but when it condenses only its latent energy is retained by the model,** while the remaining energy is thrown out and left to the global fixer to handle.
- This problem is exposed during a mass adjustment routine, giving it the energy tendency shown
- This **energy error has profound impacts on the hydrologic cycle,** motivating a need to address this issue



**Pacific
Northwest**
NATIONAL LABORATORY

Thank you

Extra slides

A realistic option that includes all phases of water in the energy budget may have a similar response to our sensitivity experiment, though not as strong

