

Thermohaline Circulation Stability: A Dynamical Systems Point of View

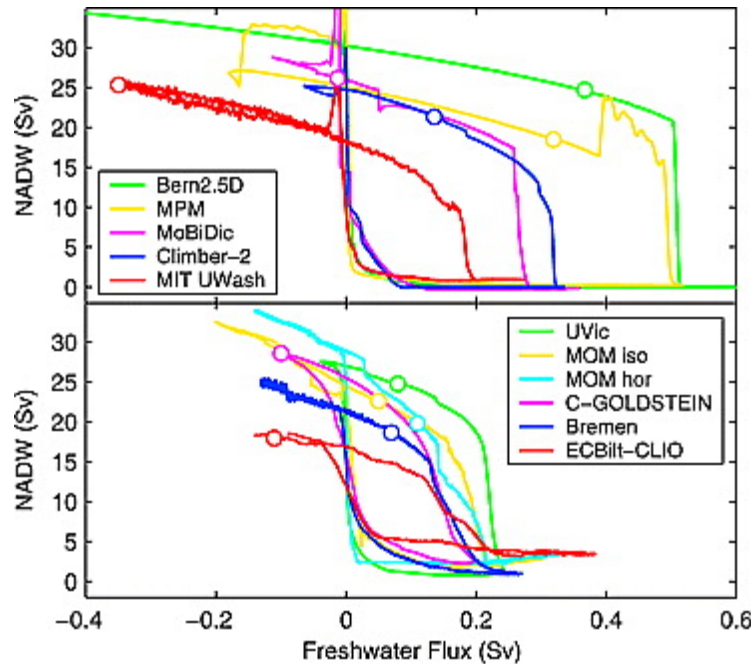
Wilbert Weijer

THC stability

- **THC stability largely determined by equilibrium structure**
- **Important questions:**
 - Is the current THC in, or close to, a regime of multiple equilibria?
 - If so, what would it take to “shut down” THC?

THC stability: what determines limit points?

- Equilibrium structure reasonably well understood in qualitative sense
- Large quantitative differences between models



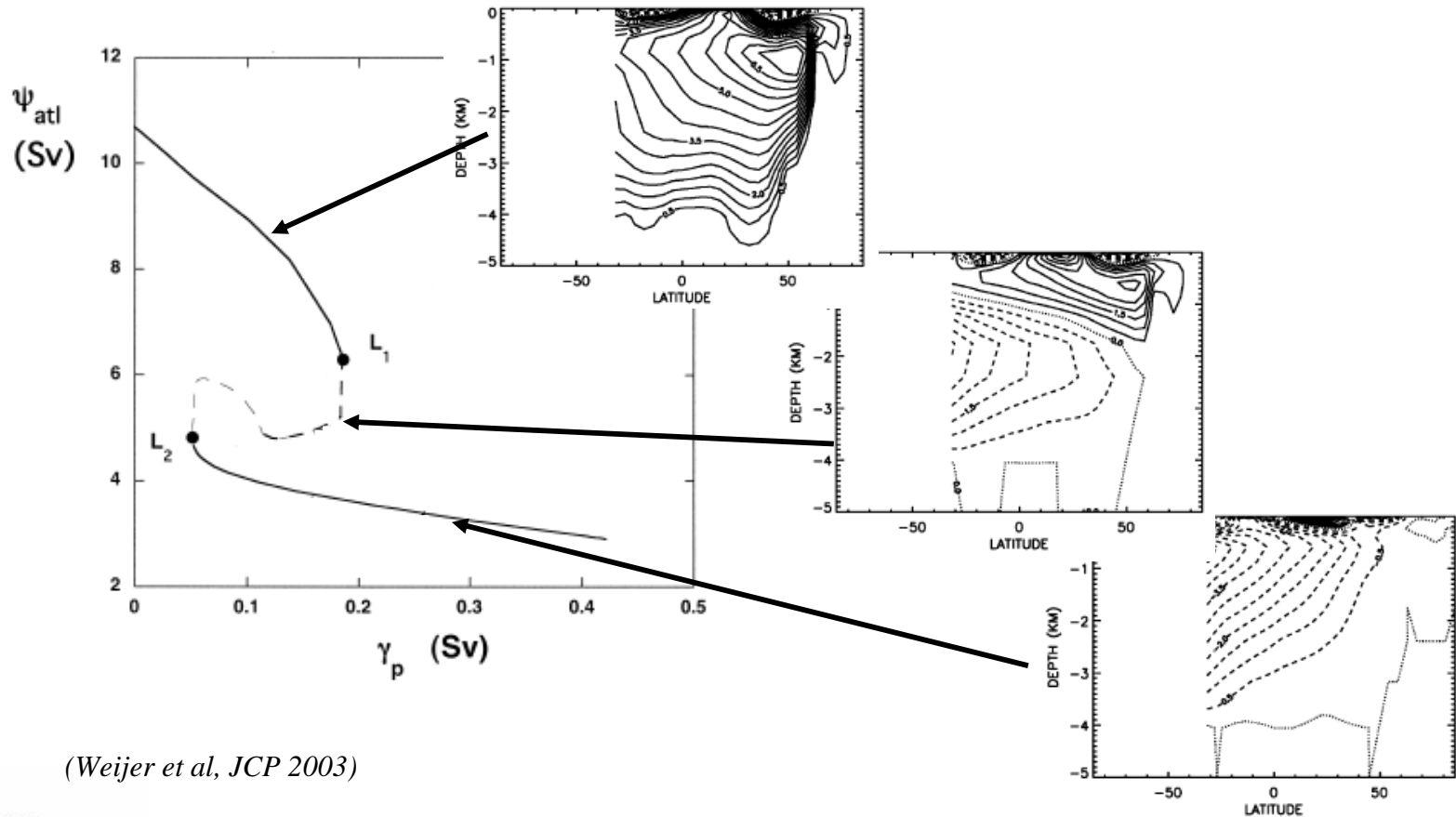
2D models

3D models

(Rahmstorf et al, GRL 2005)

THC stability: what determines limit points?

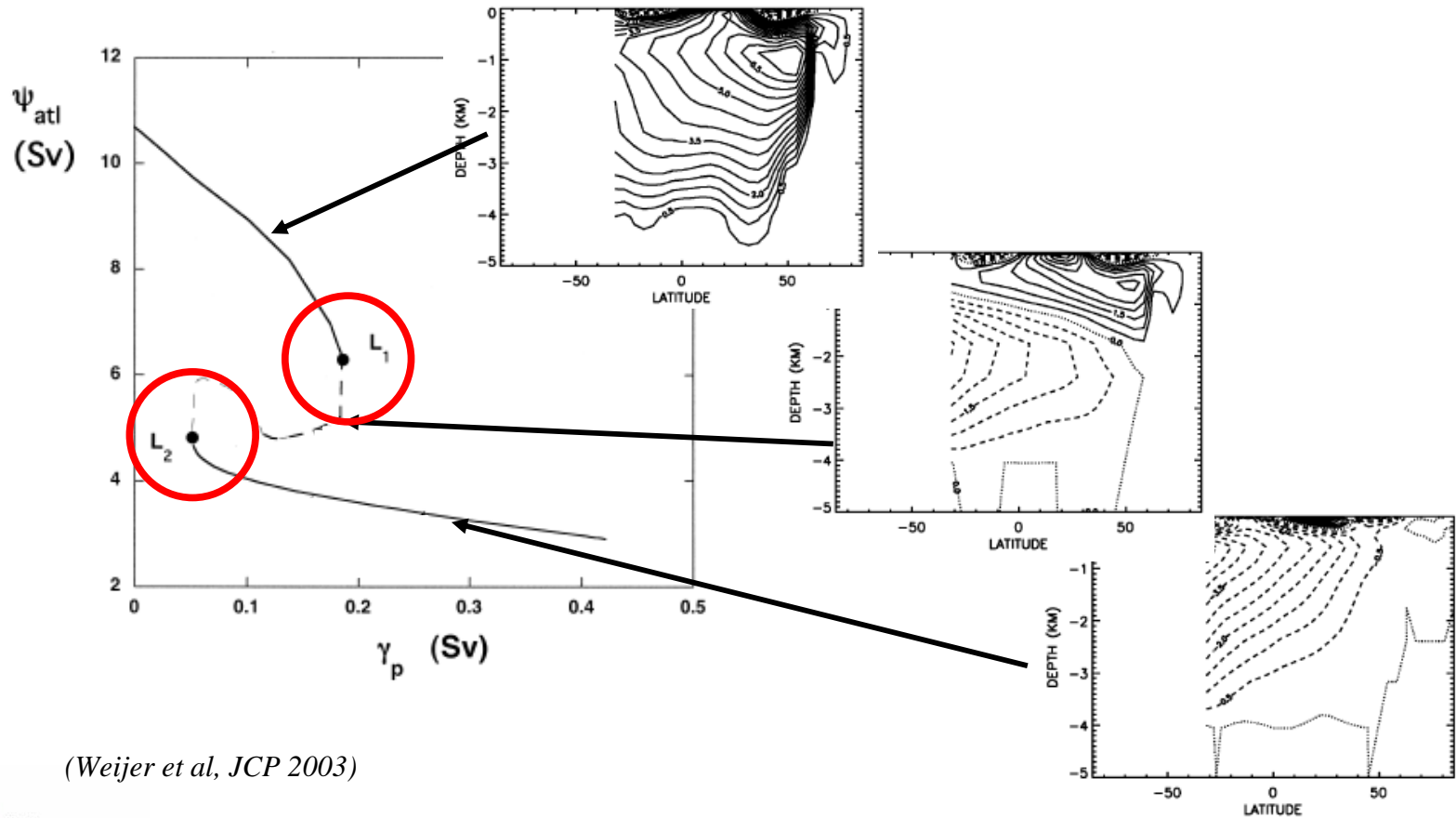
- Hysteresis diagrams reflect underlying equilibrium structure



(Weijer et al, JCP 2003)

THC stability: what determines limit points?

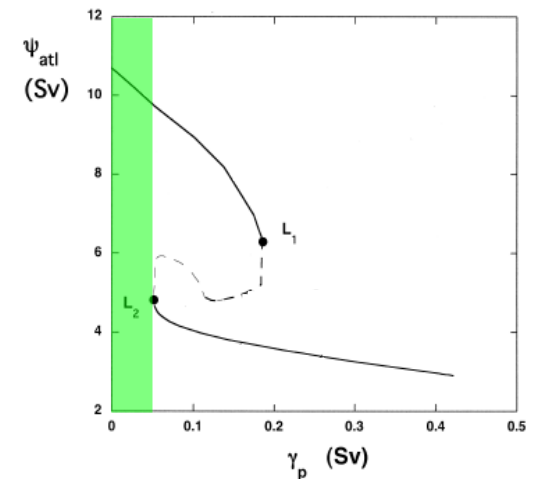
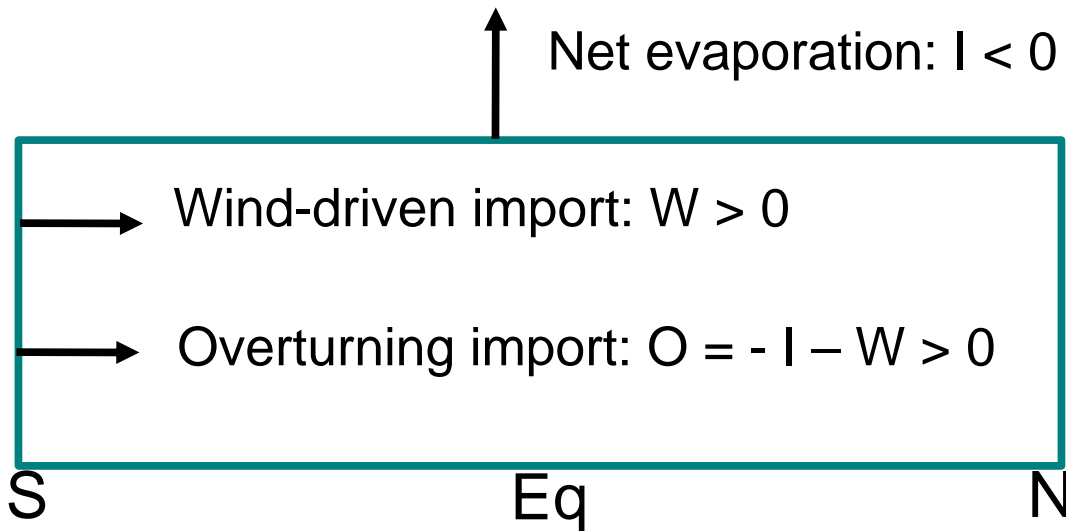
- Critical points: limit points



(Weijer et al, JCP 2003)

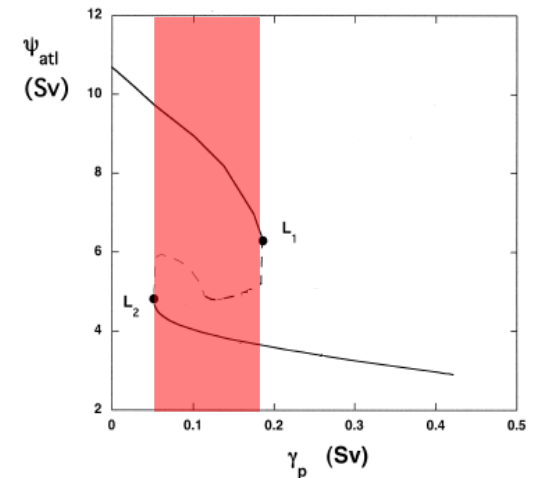
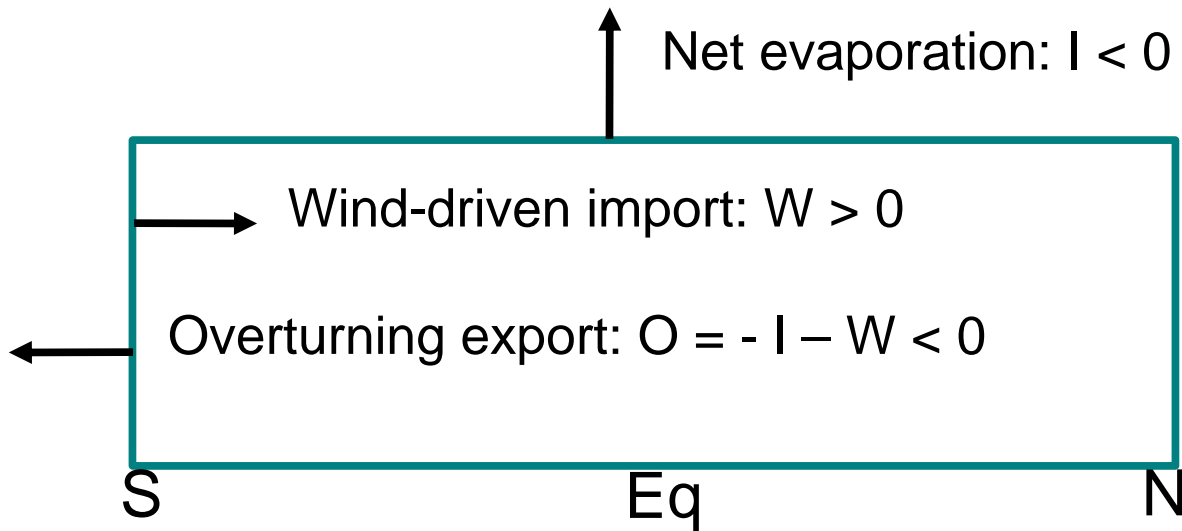
THC stability: what determines limit points?

- L_2 determined by freshwater balance of the Atlantic:
 - Mono-stable if THC salinifies



THC stability: what determines limit points?

- L_2 determined by freshwater balance of the Atlantic:
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THC stability: what determines limit points?

- **L₂ determined by freshwater balance of the Atlantic:**
 - Mono-stable if THC salinifies
 - Bi-stable if THC freshens
- **Inversion studies (e.g., Weijer 1999):**
 - $F_{35S} = + 7.0 \text{ Gg/s}$ \Rightarrow THC freshens \Rightarrow bi-stable regime!

THC stability: what determines limit points?

- L_1 diagnosed by buoyancy budget of the Atlantic?
- Rahmstorf (1996) model:

$$\beta S_0 F_{\text{crit}} = 1/4 k (\alpha \Delta T)^2 = 1/2 \alpha Q / \rho c_p$$

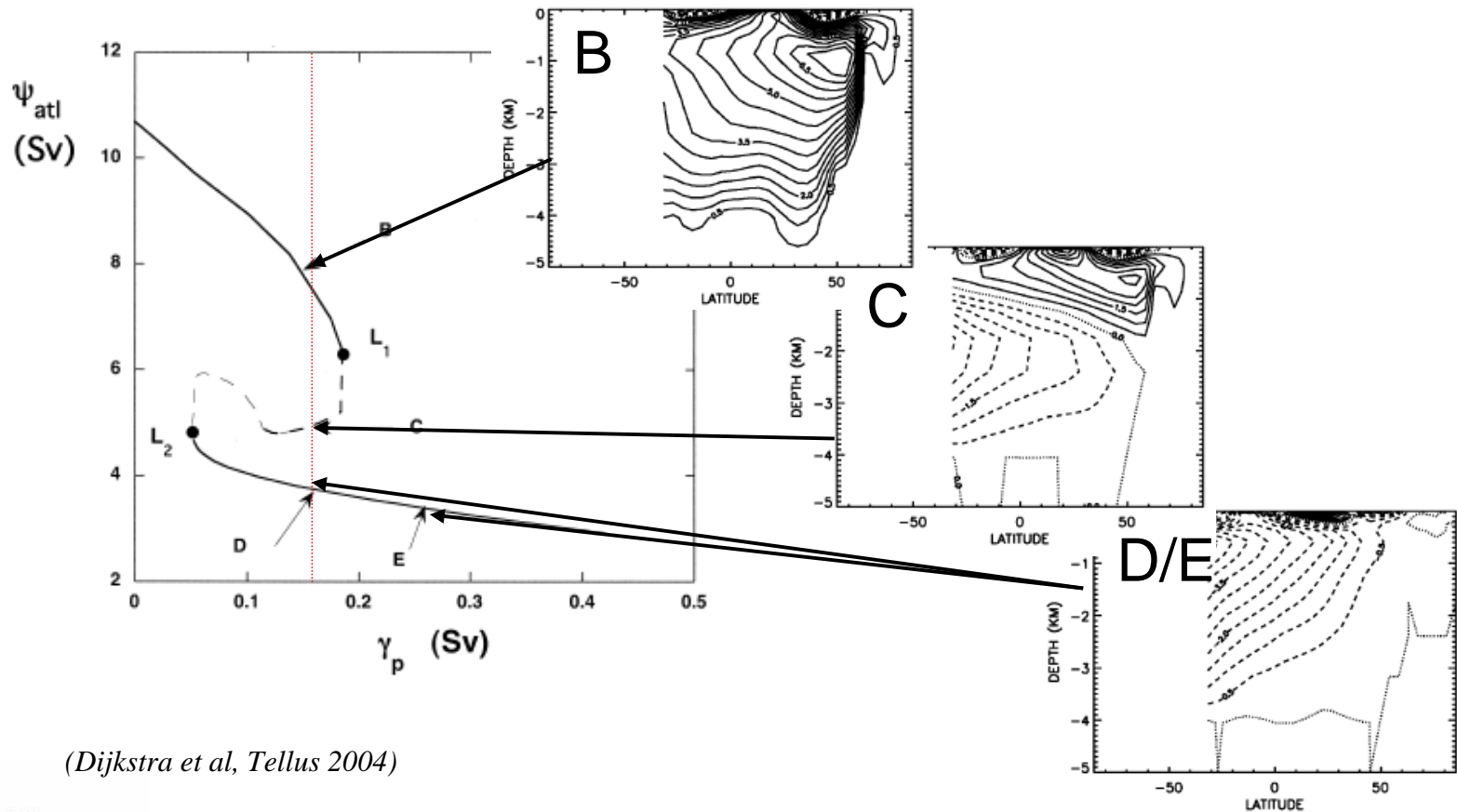
- Buoyancy gain by freshening of THC = half buoyancy loss by cooling
- Inversion study:
 - $Q_{35S} = 0.63 \text{ PW} \Rightarrow B^T = 3.2 \times 10^7 \text{ kg/s}$
 - $F_{35S} = 7.0 \text{ Gg/s} \Rightarrow B^S = -0.5 \times 10^7 \text{ kg/s}$

Transient perturbation threshold: What determines t_{crit} ?

- If in multiple-equilibria regime, what is the critical period t_{crit} of a given perturbation that will trigger a THC collapse?

Transient perturbation threshold: What determines t_{crit} ?

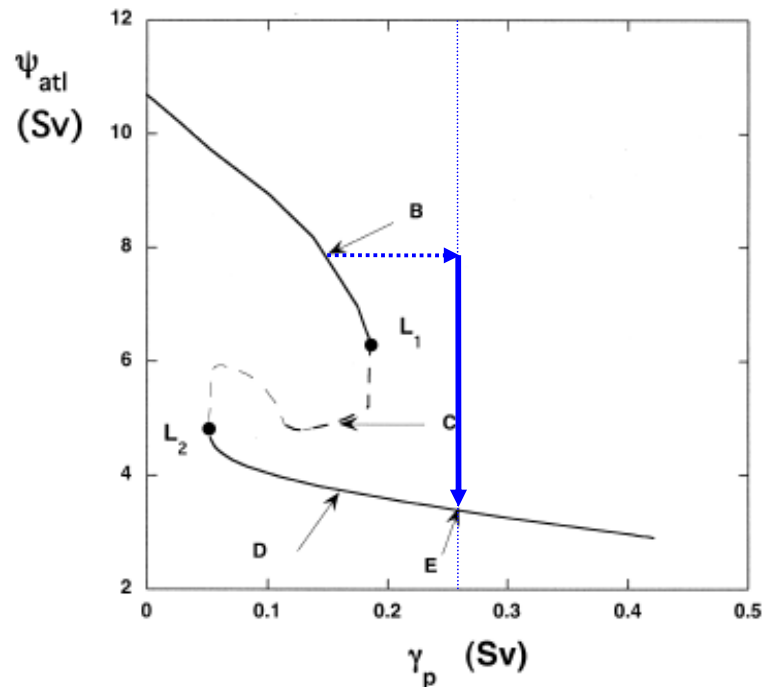
- Start from $\gamma_p = 0.15 \text{ Sv}$



(Dijkstra et al, Tellus 2004)

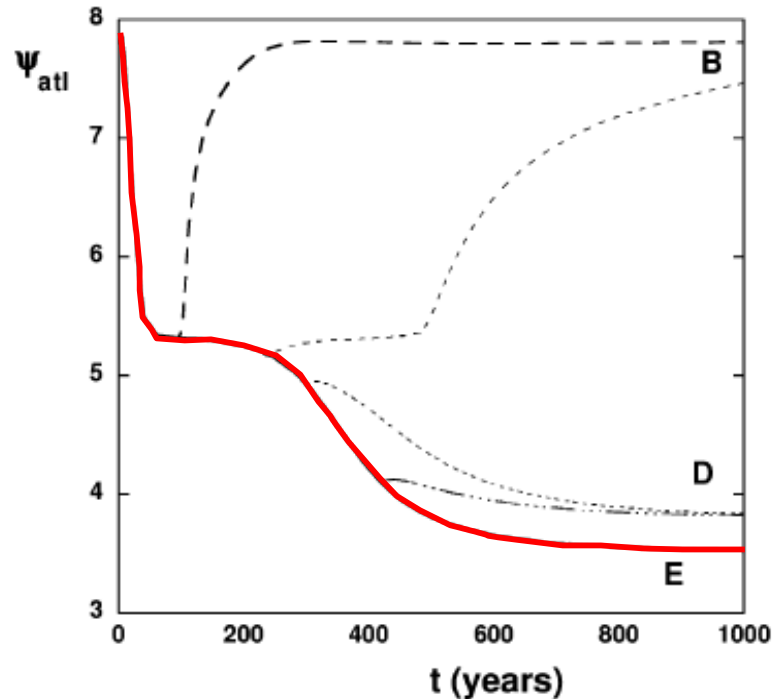
Transient perturbation threshold: What determines t_{crit} ?

- Apply perturbation: $\gamma_p = 0.23 \text{ Sv}$ for $t_m = \text{infinity}$



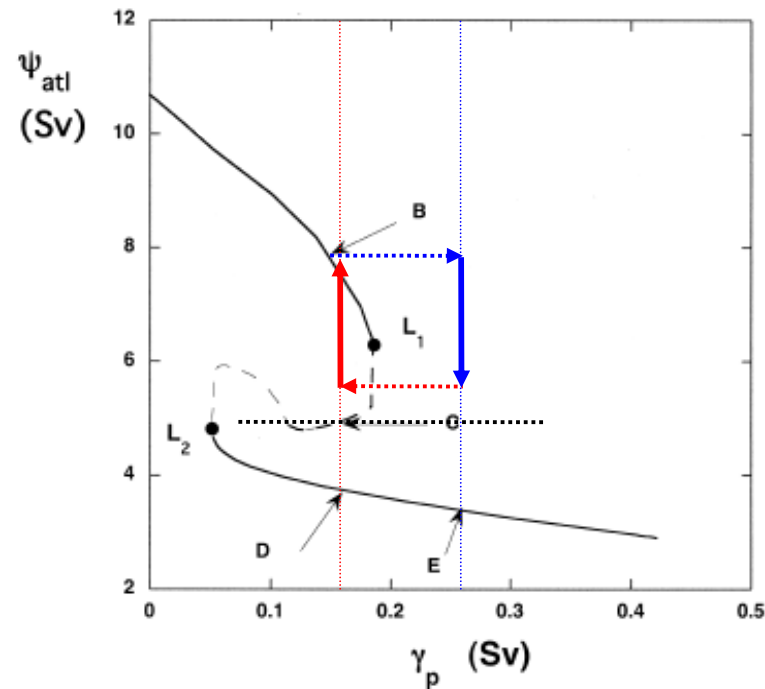
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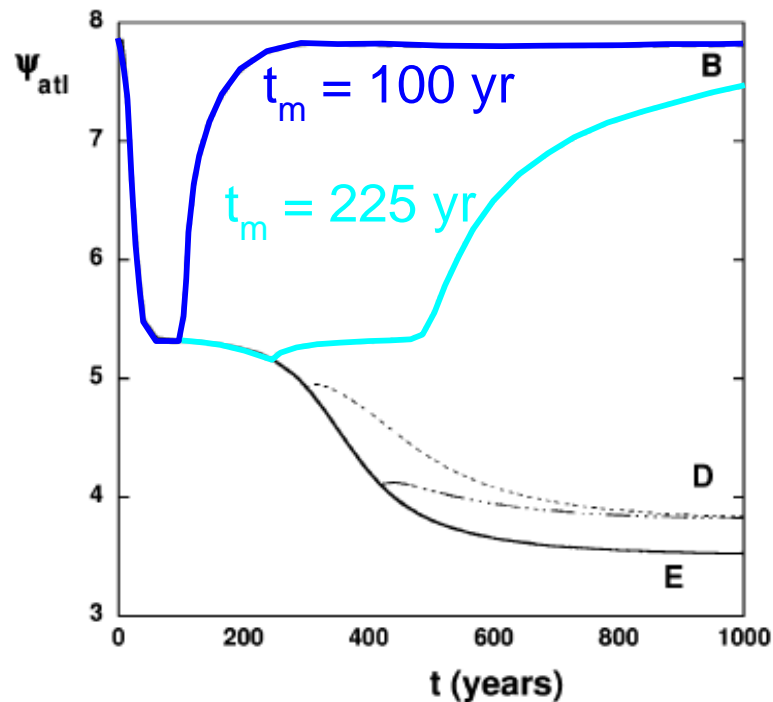
Transient perturbation threshold: What determines t_{crit} ?

- Apply perturbation: $\gamma_p = 0.23 \text{ Sv}$ for $t_m < t_{crit}$



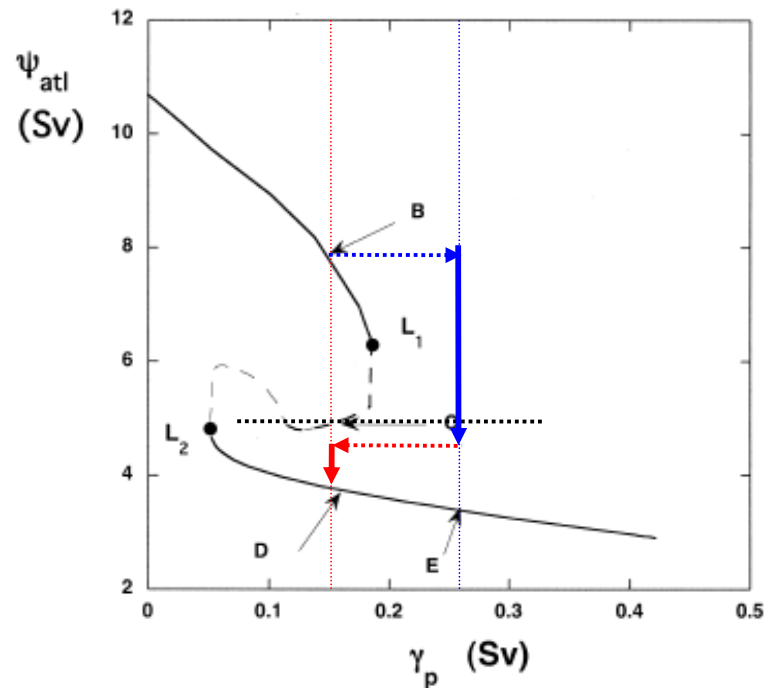
Transient perturbation threshold: What determines t_{crit} ?

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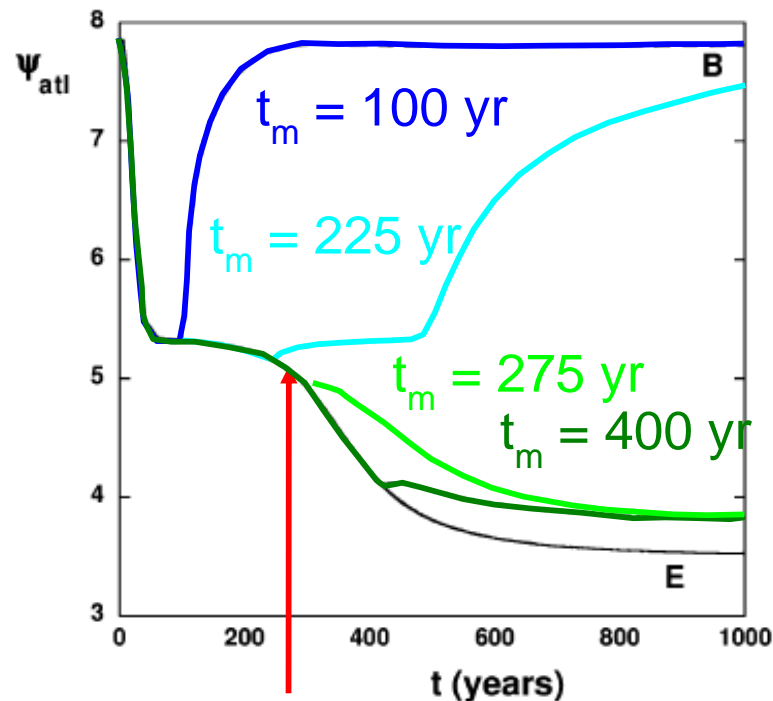
Transient perturbation threshold: What determines t_{crit} ?

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Transient perturbation threshold: What determines t_{crit} ?

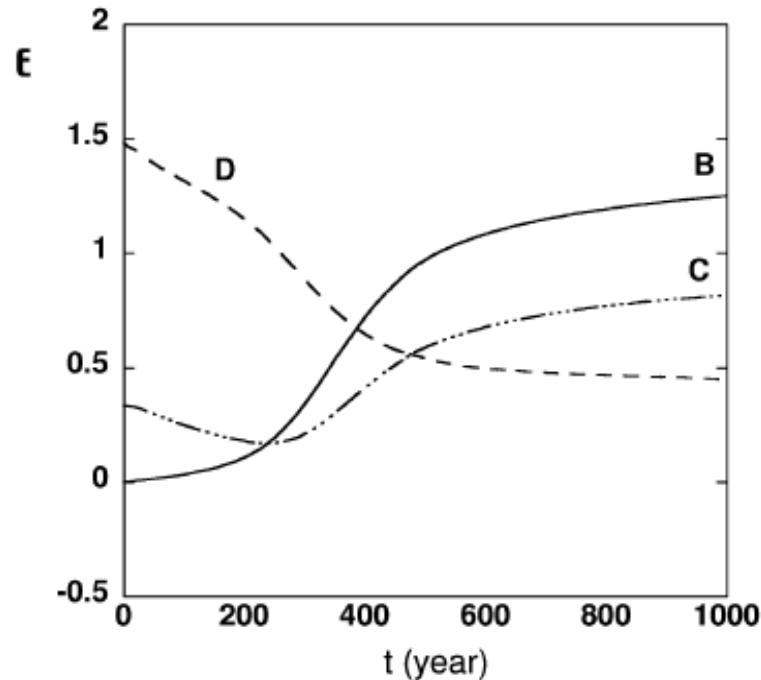
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t_{crit} between 225 and 275 years

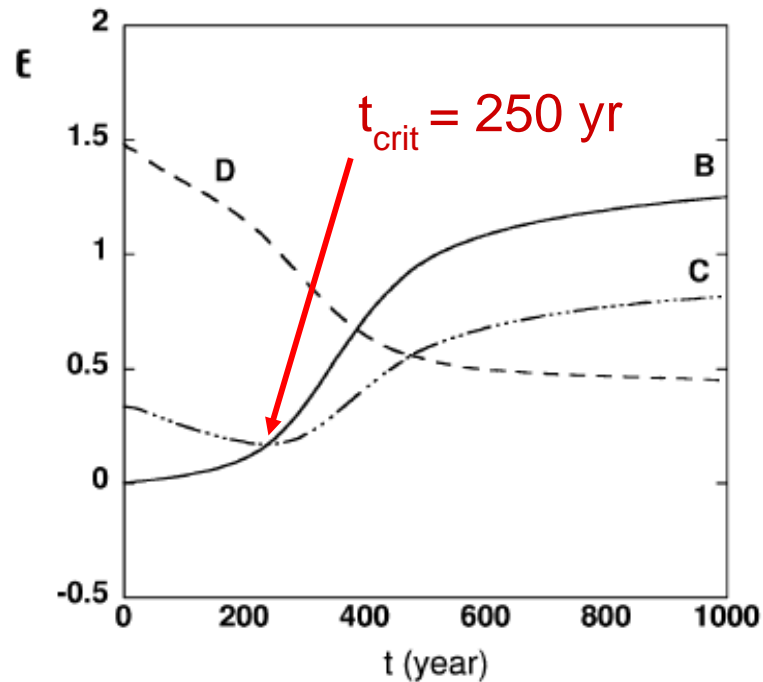
Transient perturbation threshold: What determines t_{crit} ?

- Unstable equilibrium C is on separatrix of basins of attraction of B and D
- Define “distance” between transient state and equilibria B, C and D as an **energy functional**: $E_i = \langle (\rho_i - \rho)^2 \rangle$
- Calculate E_i for transition from B to E



Transient perturbation threshold: What determines t_{crit} ?

- Minimum distance with respect to unstable equilibrium C: **250 years**



Conclusions

- **THC stability determined by equilibrium structure**
- **Limit points**
 - Limit point 2 determined by freshwater balance (surface plus wind-driven)
 - Can limit point 1 be diagnosed by buoyancy budget?
- **Transient perturbation threshold**
 - Critical duration of perturbation can be diagnosed by tendency of energy functional
 - Just one integration necessary, provided that all (including unstable!) equilibria are known