

# Initial results and performance of the GFDL Cubed-Sphere Model

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# Outline

- **Key Features**
  - Algorithm Improvements
- **Implementation Issues**
- **Initial Results**
  - Hydrostatic (APE, AMIP)
  - Computational performance and scaling
  - Non-hydrostatic
- **Future Plans**



# Key Features

## One Model ..... Two Configurations

### 1. Hydrostatic version developed from the well-known FV dynamical core

- Several improvements/modifications for the cubed-sphere
- This version is currently working well

### 2. Non-hydrostatic version

- Simple switch between hydrostatic and non-hydrostatic versions  
`hydrostatic = .false.`
- Easy transition from hydrostatic to non-hydrostatic
- Non-hydrostatic code is completely independent from the hydrostatic code.
- 30-50% more expensive than the hydrostatic version at the 4-5 km resolution




# Review of the FV dynamical core

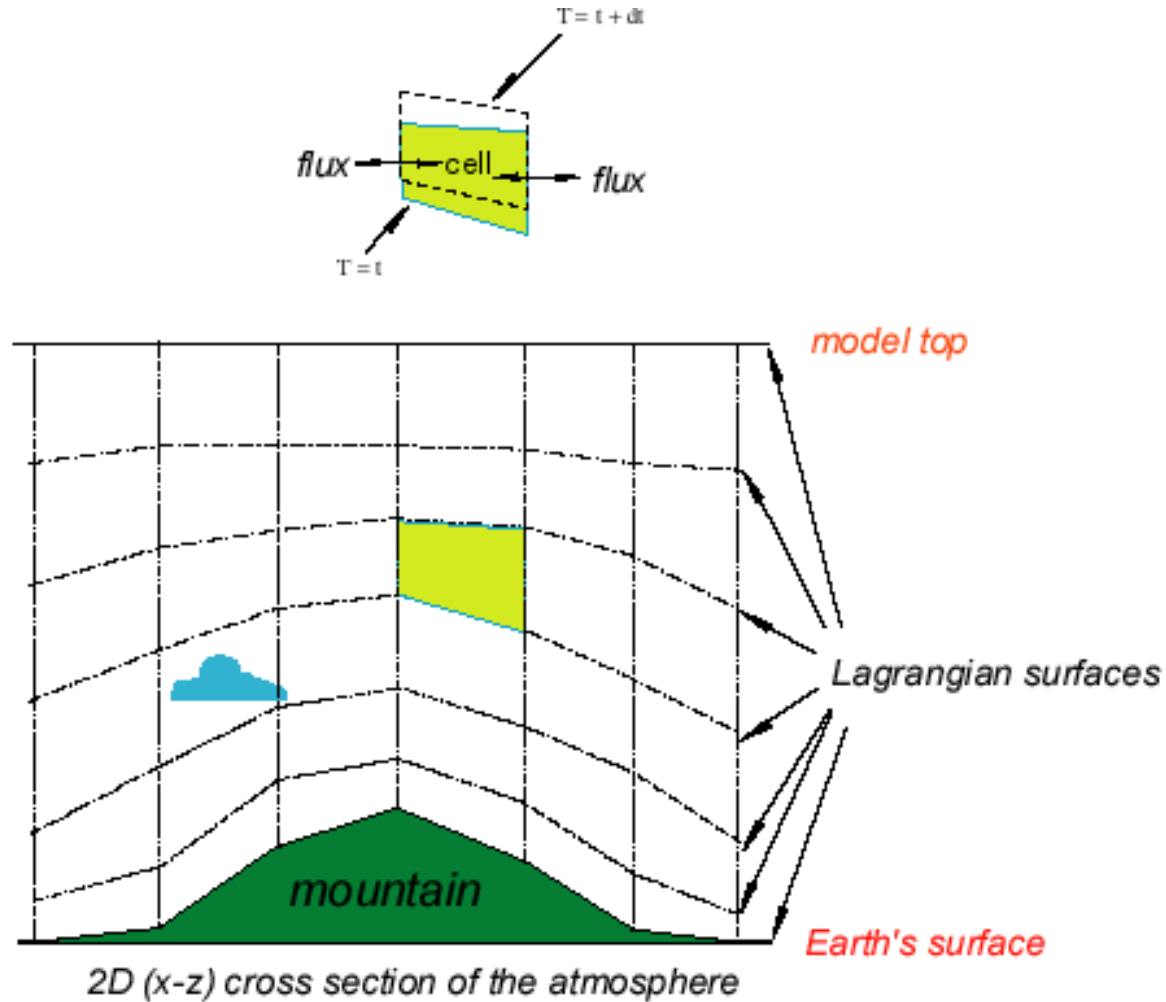
- Conservative, monotonic, flux-form semi-Lagrangian transport for all prognostic variables (*Lin and Rood 1996, MWR*).
- Consistent transport of air mass and absolute vorticity, resulting in a superior transport of the potential vorticity (*Lin and Rood 1997, QJRMS*).
- Finite-volume integration of the pressure gradient forces to more accurately handle steep terrains (*Lin 1997, QJRMS*).
- “*Vertically Lagrangian*” control-volume discretization with mass, momentum, and total energy conserving re-mapping algorithm (*Lin 2004, MWR*).



# Algorithm Improvements

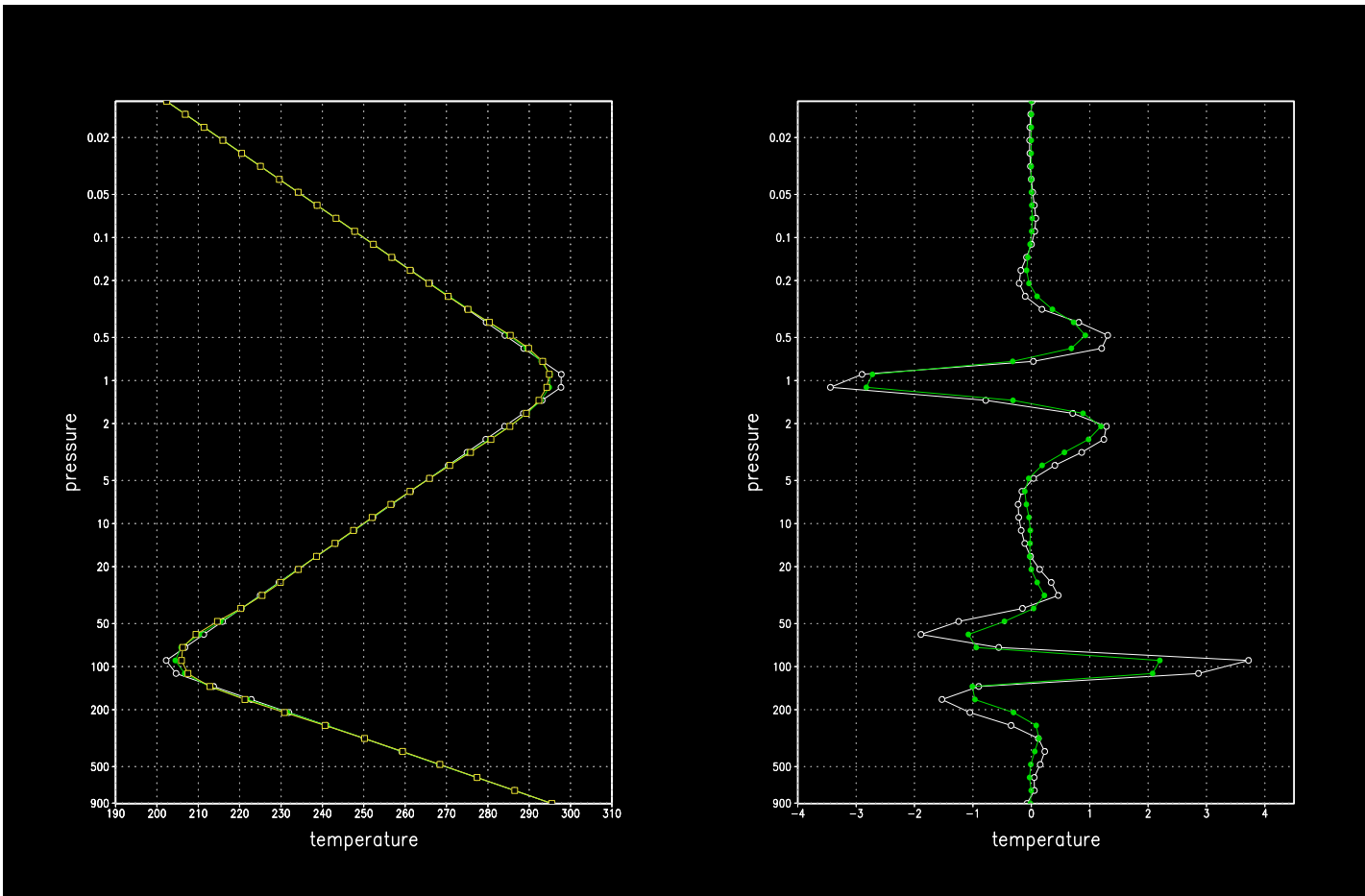
- **Generalization to non-orthogonal curvilinear coordinate**
- **Horizontal transport scheme**
  - fully monotonic for all transported variables (using the same inner and outer 1D operator enhanced stability but slightly more expensive)
  - edges between the 6 faces of the cube are correctly treated as discontinuity
- **4<sup>th</sup> order interpolation of the winds from D to C grid**
- **The vertical remapping** 
  - one-sided extrapolation at the bottom surface and at the model top using cubic polynomials that is coupled with the interior PPM sub-grid reconstruction scheme -- less numerical damping.
  - Geopotential conserving remapping by remapping virtual temperature using  $\log(p)$  – remapping is exact if the virtual temperature profile can be locally represented by piecewise parabolic polynomials.
- **Communication**
  - pure message passing; communication moved to the outer levels of the code; code is much cleaner and simpler; many OPENMP directives remain but are inactive
- **Lagrangian Riemann Solver for vertically propagating soundwaves**
  - Lin 2007, QJRMS, *in revision*

# Vertically Lagrangian Control-Volume Discretization



# Improved Remapping

*Temperature profiles*



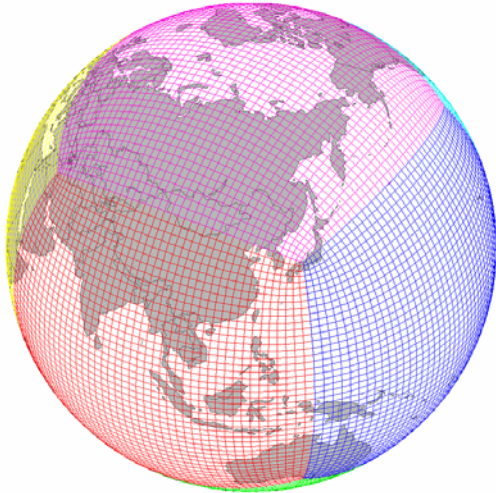
55 levels  
-----  
remapped  
1000 x



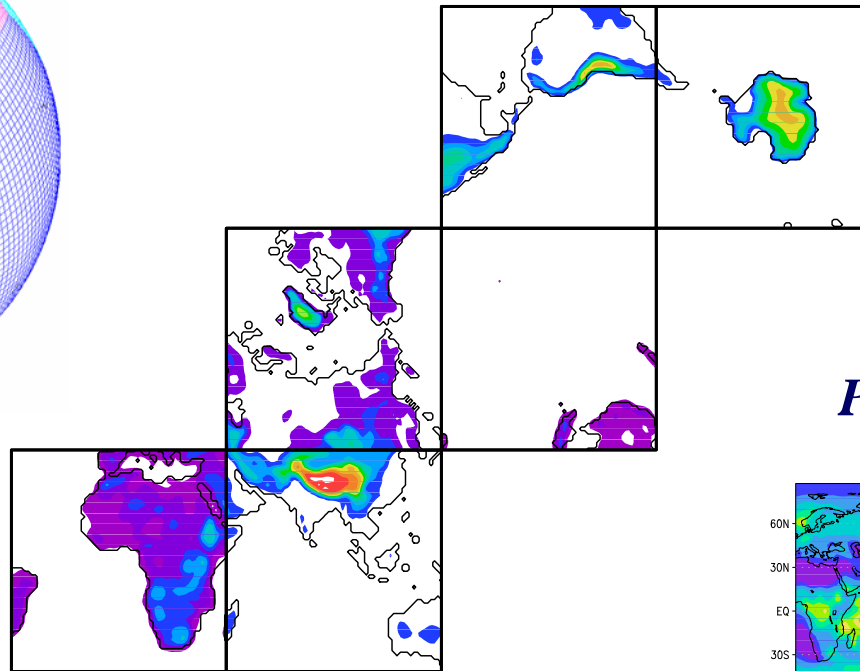
# Three ways to look at the cubed-sphere

## *Physical Domain*

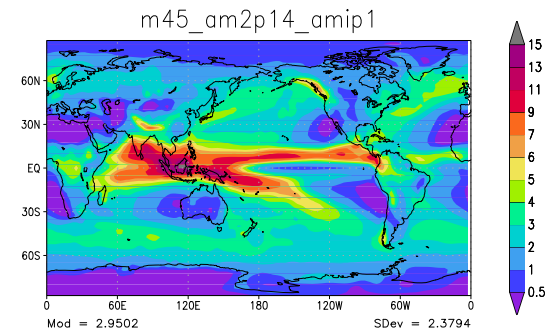
Cubed Sphere 44s44s6



## *Computational domain*



## *Post processing*





# Implementation Issues

- **Cubed-sphere grid choice** 
  - Gnomonic grid; analytic solution
  - Spring-dynamics with torsion spring; less distortion at edges and corners
- **Land Model Grid**
  - Cubed-Sphere vs. Latitude-Longitude grid?
  - River routing
- **Coupling software/exchange grid** (*3 step approach*)
  1. By-pass coupler for AMIP runs (all models use the cubed-sphere grid)
  2. CS atmos; LL land; tri-polar ocean and ice models
  3. CS atmos and land; tri-polar ocean and ice models (final configuration)
- **Input data sets**
  - Online lat-lon to cubed-sphere conservative interpolation
- **Diagnostics and post-processing (output data)**
  - Cubed-sphere to lat-lon interpolation

# Cubed-sphere grid choices

*Gnomonic grid choices compared with lat-lon and Yin-Yang grids.*

Grid scheme	Aspect ratio: $\Delta_{\text{MAX}} / \Delta_{\text{MIN}}$	
	Global grid	Local grid box
Lat-Lon	N	N
Equal distance (Sadourny 1972)	~2	~1.4
Equal angle (Ronchi et al. 1996)	~1.4	~1.4
<b>True equal-distance Gnomonic</b>	<b>~1.4</b>	<b>~1.06</b>
<i>Yin-Yang</i>	~1.4	~1.4

# FMS Coupler Overview


*Used for data exchange between models. Key features include:*

- **Conservation:** Required for long runs.
- **Resolution:** No constraints on component model time steps and spatial grid. Supports both explicit and implicit time stepping.
- **Exchange grid:** Union of component model grids, where detailed flux computations are performed (Monin-Obukhov, tridiagonal solver for implicit diffusion, ...)
- **Fully parallel:** Calls are entirely processor-local: exchange software will perform all inter-processor communication.
- **Single executable:** Serial and concurrent execution in a single executable.
- **Highly efficient:** Currently able to couple atmosphere/ocean explicitly at each ocean time step; atmosphere/land/ice implicitly at each atmospheric time step.



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# Implicit coupling and the exchange grid

*Union of component model grids,  
where detailed flux computations are performed.*

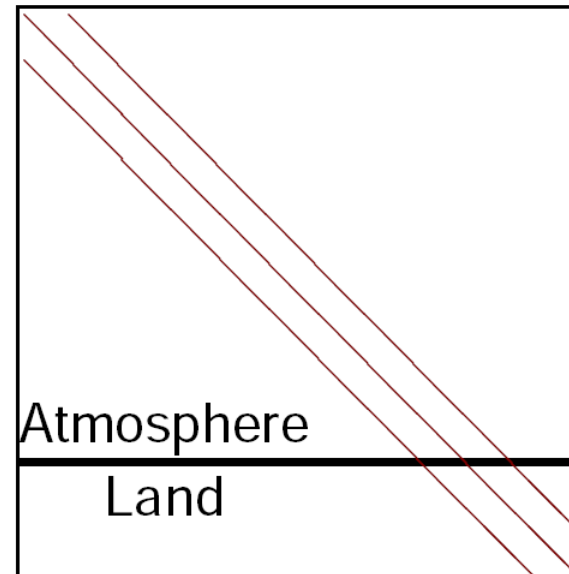
Atmosphere



Exchange



Land




# FMS Coupler: Cubed-Sphere

*The fundamentals of the exchange grid do not change as we move to the cubed sphere grid. However, there are some software issues that we are dealing with.*

- **New grid specification to accommodate multi-tile grids (mosaics)**
- **Exchange grid generation needs to handle multiple cubed-sphere grids (Atmosphere and Land)**
  - Software originally assumed one of the grids was lat-lon
- **Second-order conservative interpolation**
- **Exchange grid size will be larger**
  - Load balancing; communication costs
  - Code needs to be very efficient
- **Earth System Model (ESM) will exchange even more tracers**
  - Need for efficient code even greater



# Initial Tests (Hydrostatic Model)

- **Aqua-planet runs**
  - Neale and Hoskins (2001)
  - Specified zonally symmetric SST (Control case #1)
  - Diurnal radiation with NO annual cycle
  - Radiative gases held constant or turned off
- **AM2 physics** 
- **No coupling software**
- **Good for identifying problems at the corners**
- **Examine 3 year annual averages**

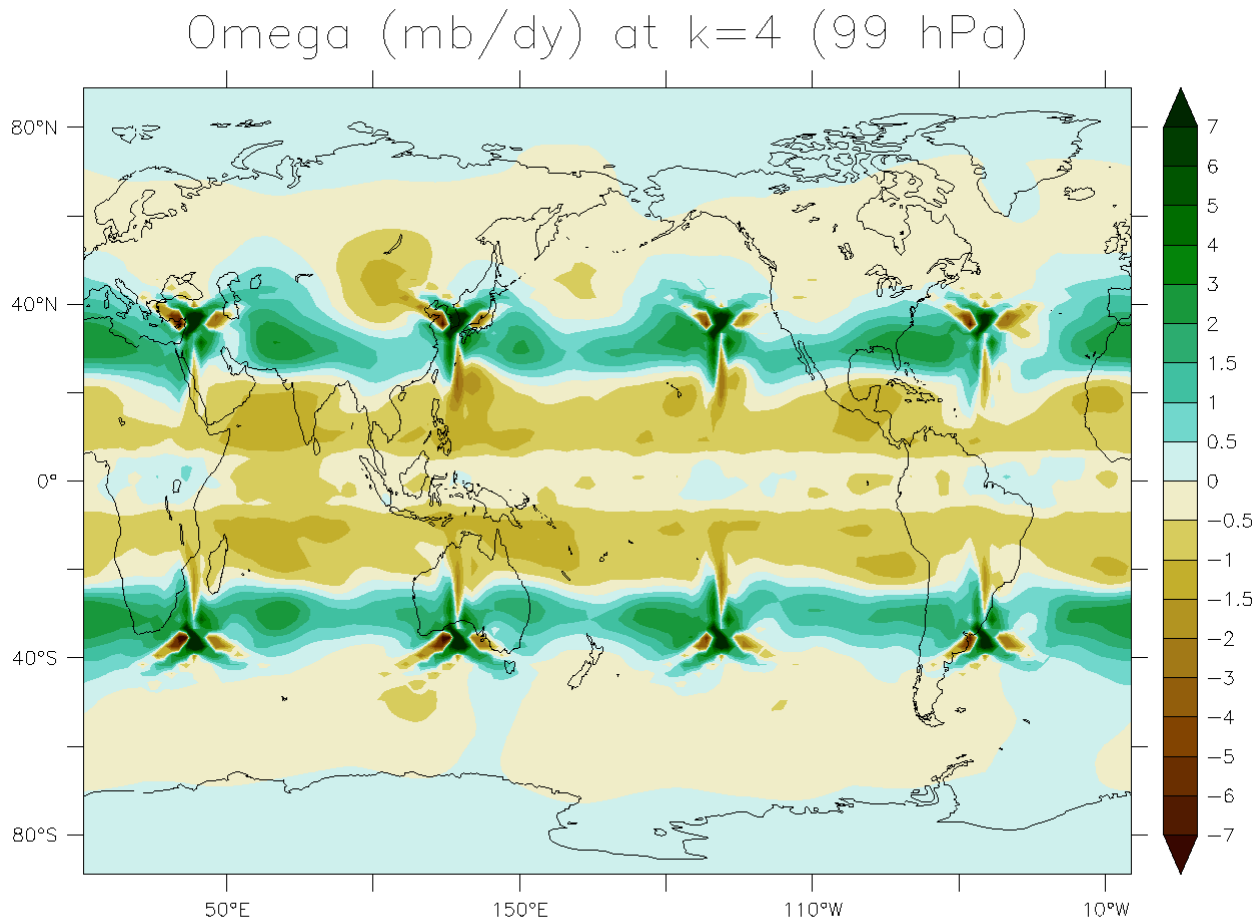
# AM2 Physics *(J. of Climate, Dec. 2004)*

- **Radiation:** Diurnal cycle with full radiation calculation every 3 h; effects of H<sub>2</sub>O, CO<sub>2</sub>, O<sub>3</sub>, O<sub>2</sub>, N<sub>2</sub>O, CH<sub>4</sub>, and four halocarbons included. **Longwave:** Simplified exchange approximation (Schwarzkopf and Ramaswamy 1999); Clough et al. (1992) CKD 2.1 H<sub>2</sub>O continuum parameterization. **Shortwave:** Exponential sum fit with 18 bands (Freidenreich and Ramaswamy 1999); liquid cloud radiative properties from Slingo (1989); ice cloud radiative properties from Fu and Liou (1993).
- **Aerosols:** Prescribed monthly three-dimensional climatology from chemical transport models; species represented include sulfate, hydrophilic, and hydrophobic carbon, dust, and sea salt.
- **Clouds:** Three prognostic tracers; cloud liquid, cloud ice, and cloud fraction; cloud microphysics from Rotstayn (1997) and cloud macrophysics from Tiedtke (1993).
- **Convection Relaxed Arakawa–Schubert:** From Moorthi and Suarez (1992); Detrainment of cloud liquid, ice, and fraction from convective updrafts into stratiform clouds; a lower bound imposed on lateral entrainment rates for deep convective updrafts (Tokioka et al. 1988); convective momentum transport represented by vertical diffusion proportional to the cumulus mass flux.
- **Vertical diffusion:** Surface and stratocumulus convective layers represented by a K-profile scheme with prescribed entrainment rates (Lock et al. 2000); surface fluxes from Monin–Obukhov similarity theory; gustiness enhancement to wind speed used in surface flux calculations (Beljaars 1995); enhanced near-surface mixing in stable conditions; orographic roughness effects included.
- **Gravity wave drag:** Orographic drag from Stern and Pierrehumbert (1988)
- **Land model:** Isothermal surface (soil–snow–vegetation); three water stores: snow, root zone, and ground water; 18 soil temperature levels to 6-m total depth; stomatal control of evapotranspiration; latent heat storage in soil; surface parameters dependent on eight soil and eight vegetation types

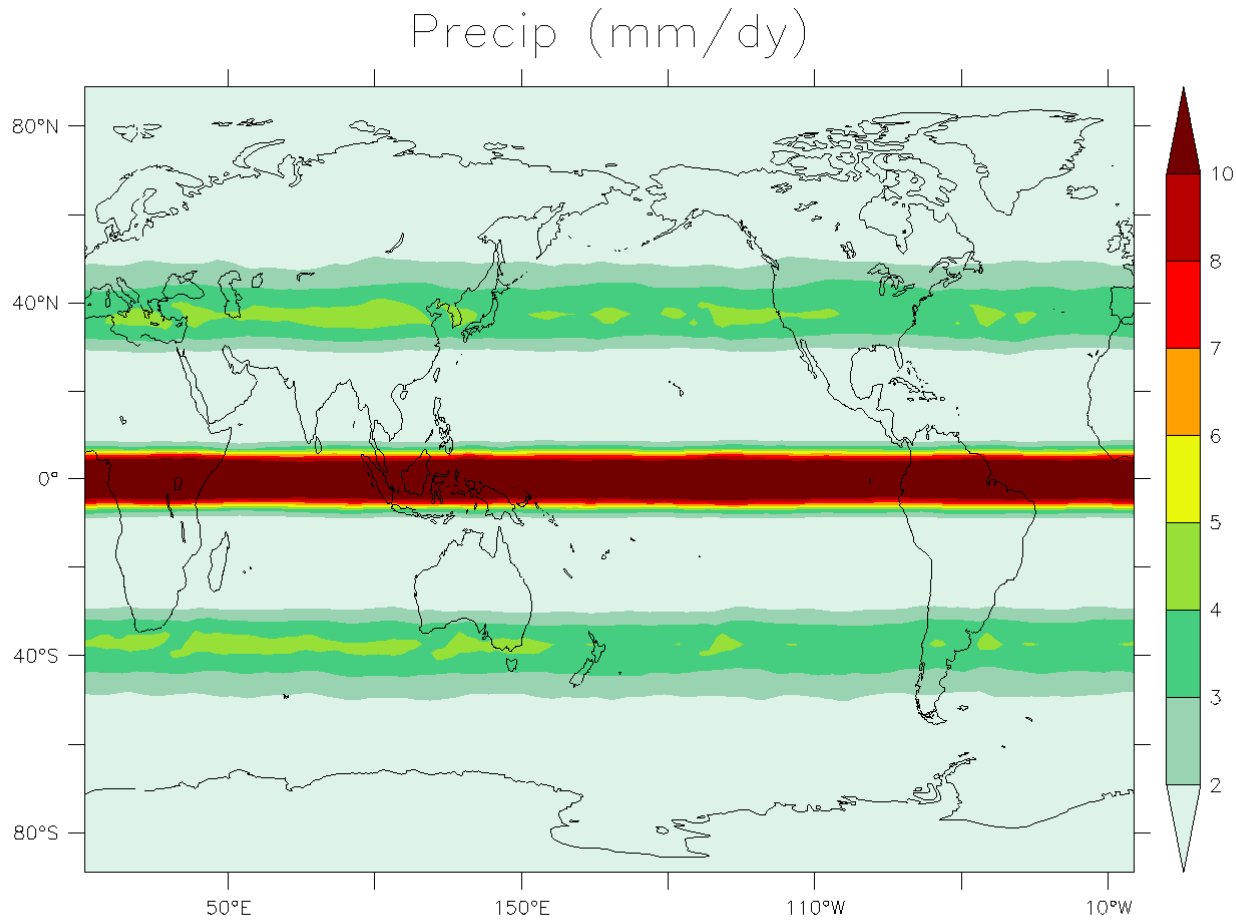




# C44 Aqua-planet experiment



# C44 Aqua-planet experiment



# Initial Tests (Hydrostatic Model)

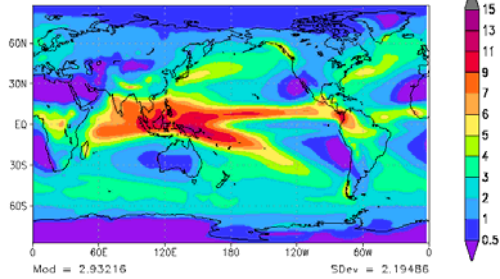
- AMIP runs
  - Same as AM2p14 except ...  
All component models are on the cubed-sphere  
No exchange grid (coupling software)
- C48 L24
  - Each face has 48x48 points; approx. 2 degree resolution  
Similar horizontal resolution to AM2p14 (M45)
  - Same vertical resolution as AM2
- 21 year integration: 1980-2000 (Hurrell SST/ICE)
- Several integrations completed at C64 and C90



# AMIP Results

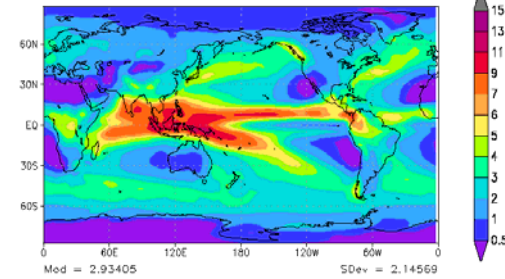
ANN PRECIP (mm/d)

m45\_am2p14\_hurrell

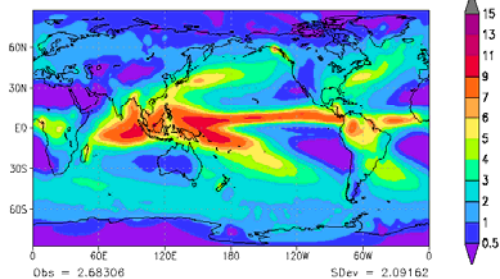


ANN PRECIP (mm/d)

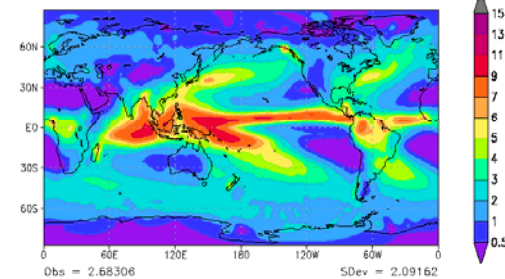
c48\_am2p14\_lowgwd



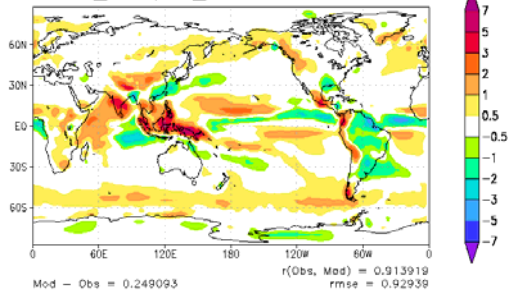
CMAP



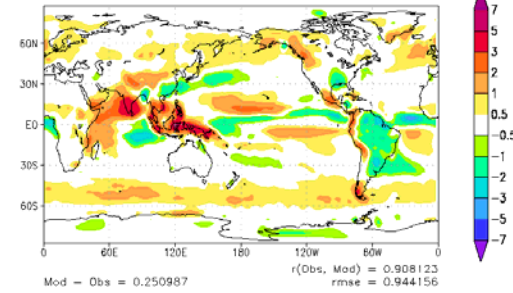
CMAP



m45\_am2p14\_hurrell minus CMAP

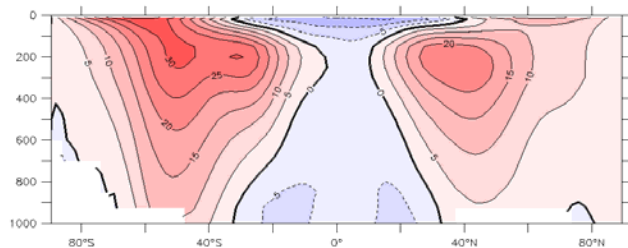


c48\_am2p14\_lowgwd minus CMAP



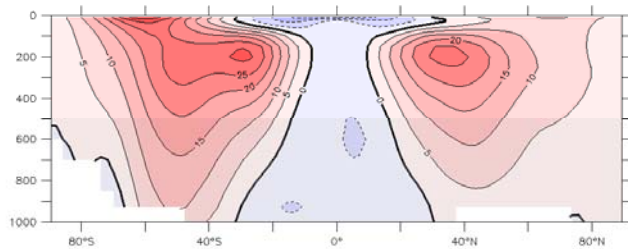
# AMIP Results

Zonal mean zonal wind, ann



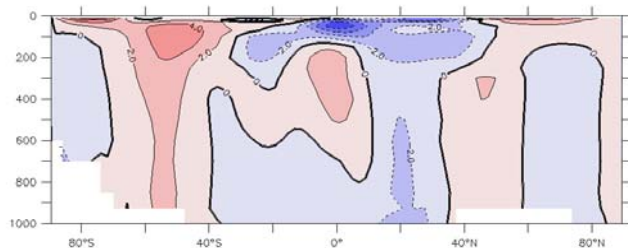
mean: 6.5907  
std dev: 9.4949

m45\_am2p14\_hurrell



mean: 6.519  
std dev: 8.7804

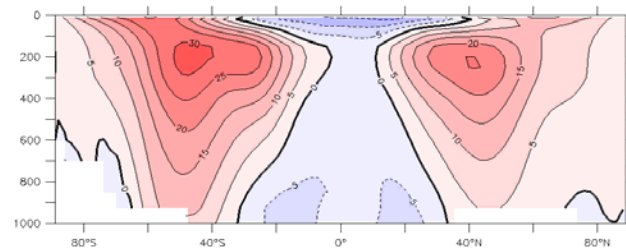
Reanalysis



mean  $\Delta$ : 0.072  
rms  $\Delta$ : 1.658  
corr: 0.9866

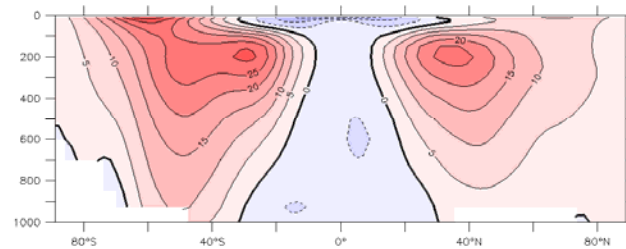
m45\_am2p14\_hurrell - Reanalysis

Zonal mean zonal wind, ann



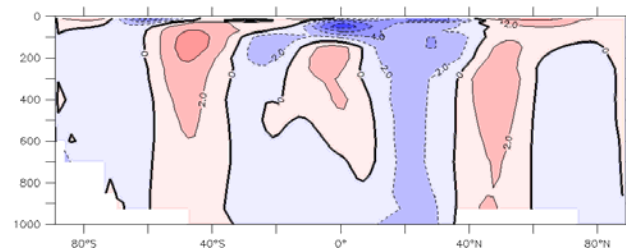
mean: 6.3649  
std dev: 9.4252

c48\_am2p14\_lowgwd



mean: 6.553  
std dev: 8.7933

Reanalysis



mean  $\Delta$ : -0.1883  
rms  $\Delta$ : 1.727  
corr: 0.9846

c48\_am2p14\_lowgwd - Reanalysis

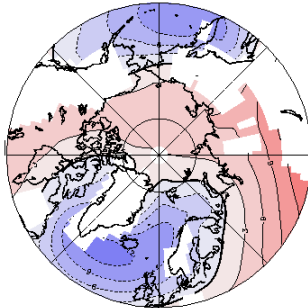


# AMIP Results

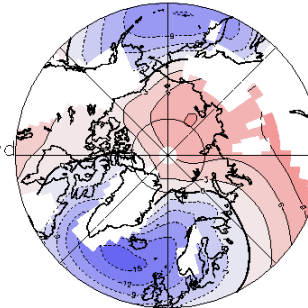
SLP – 1013.25mb, djf

SLP – 1013.25mb, djf

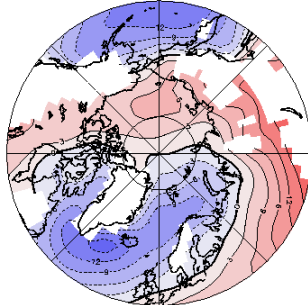
m45\_am2p14\_hurrell  
(c.int.=3mb)



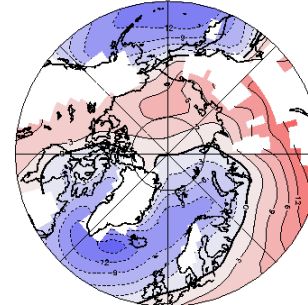
c48\_am2p14\_lowgwd  
(c.int.=3mb)



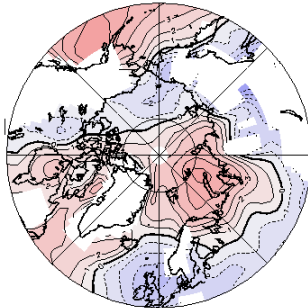
Reanalysis  
(c.int.=3mb)



Reanalysis  
(c.int.=3mb)

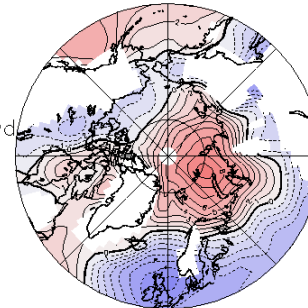


m45\_am2p14\_hurrell  
minus  
Reanalysis  
(c.int.=1mb)



RMSΔ=2.93mb  
Corr=0.922

c48\_am2p14\_lowgwd  
minus  
Reanalysis  
(c.int.=1mb)



RMSΔ=4.13mb  
Corr=0.831

# Comments on the cubed-sphere

- **Arctic climate**

Will it improve with higher horizontal resolution?

How much improvement can be gained with tuning GWD?

- **Coupler/exchange grid overhead**

More exchange grid cells and more communication.

Earth system model exchanges many more tracers.

Diagnostics of quantities on the exchange grid may also be costly.

Possible solution: Perform many *puts/gets* with the exchange grid at a time.

- **Post-processing: Cube to Lat-Lon**

Integration with the GFDL post-processing software. Interpolation to standard pressure levels should be done on the cubed-sphere grid.

- **Interpolation of input data sets**

High-resolution lat-lon to cubed-sphere is very costly.

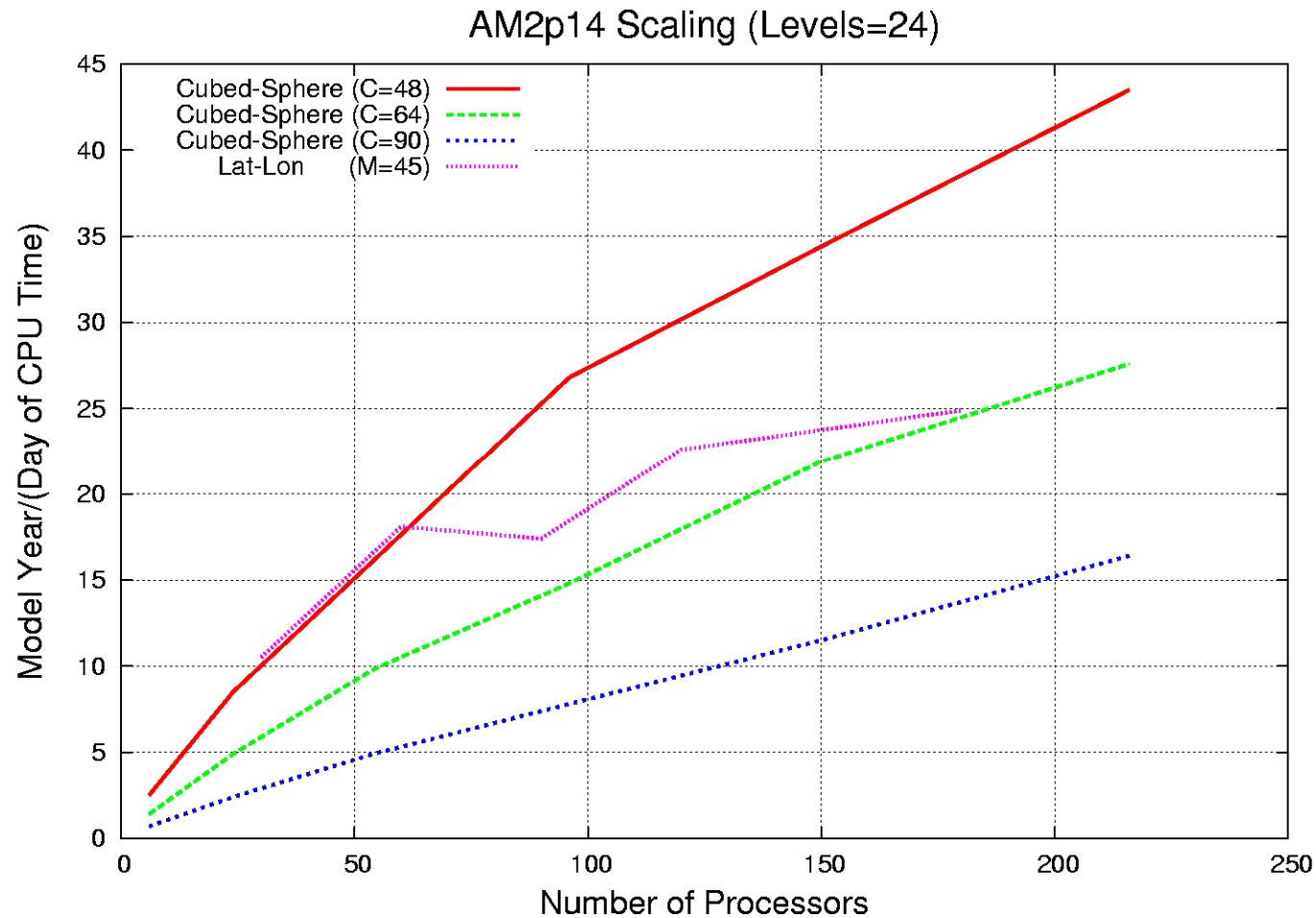
Move some online interpolation to offline?

- **Scaling**

Will the benefits of scaling out weight the issues above?

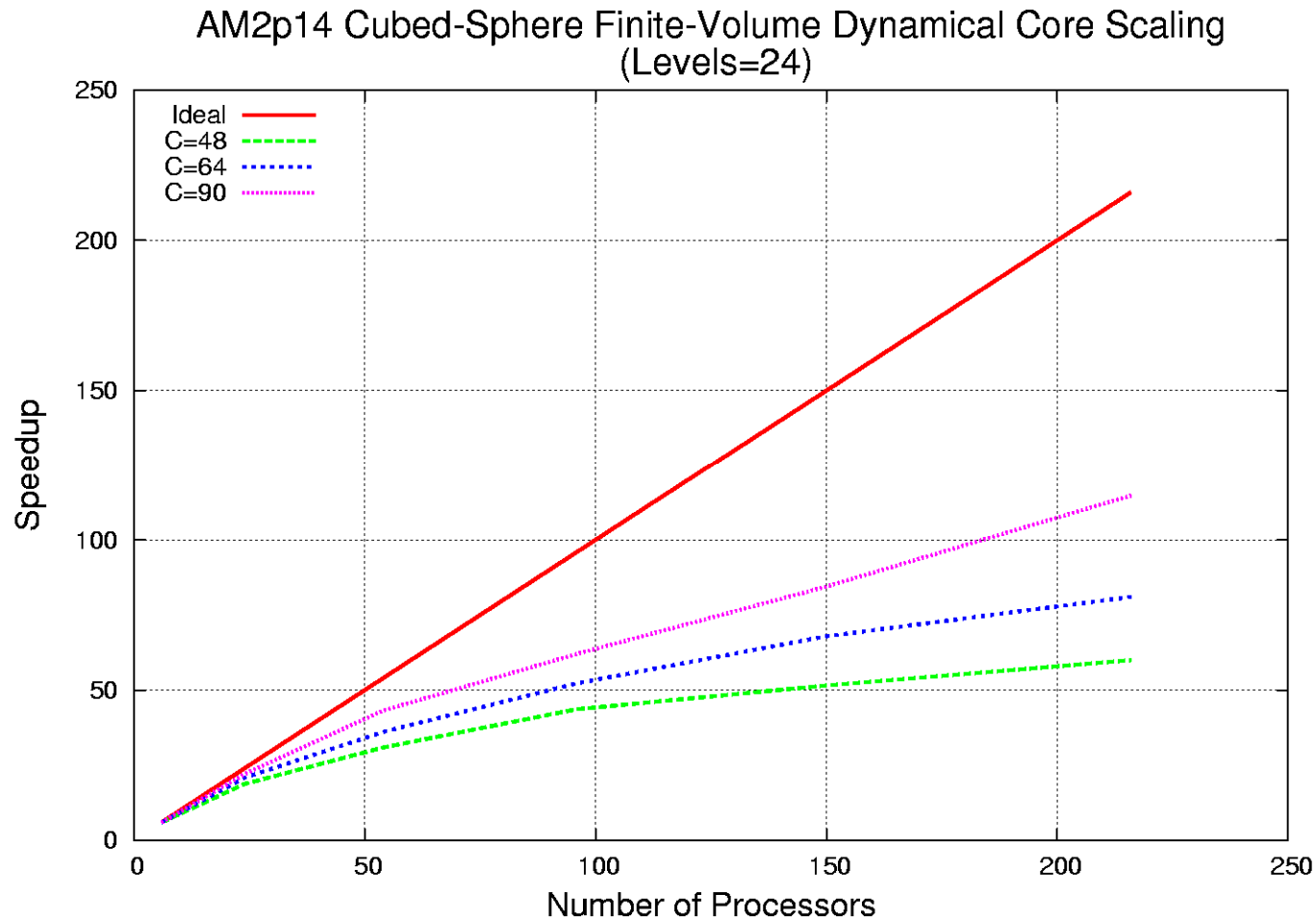


# Scaling of AMIP runs

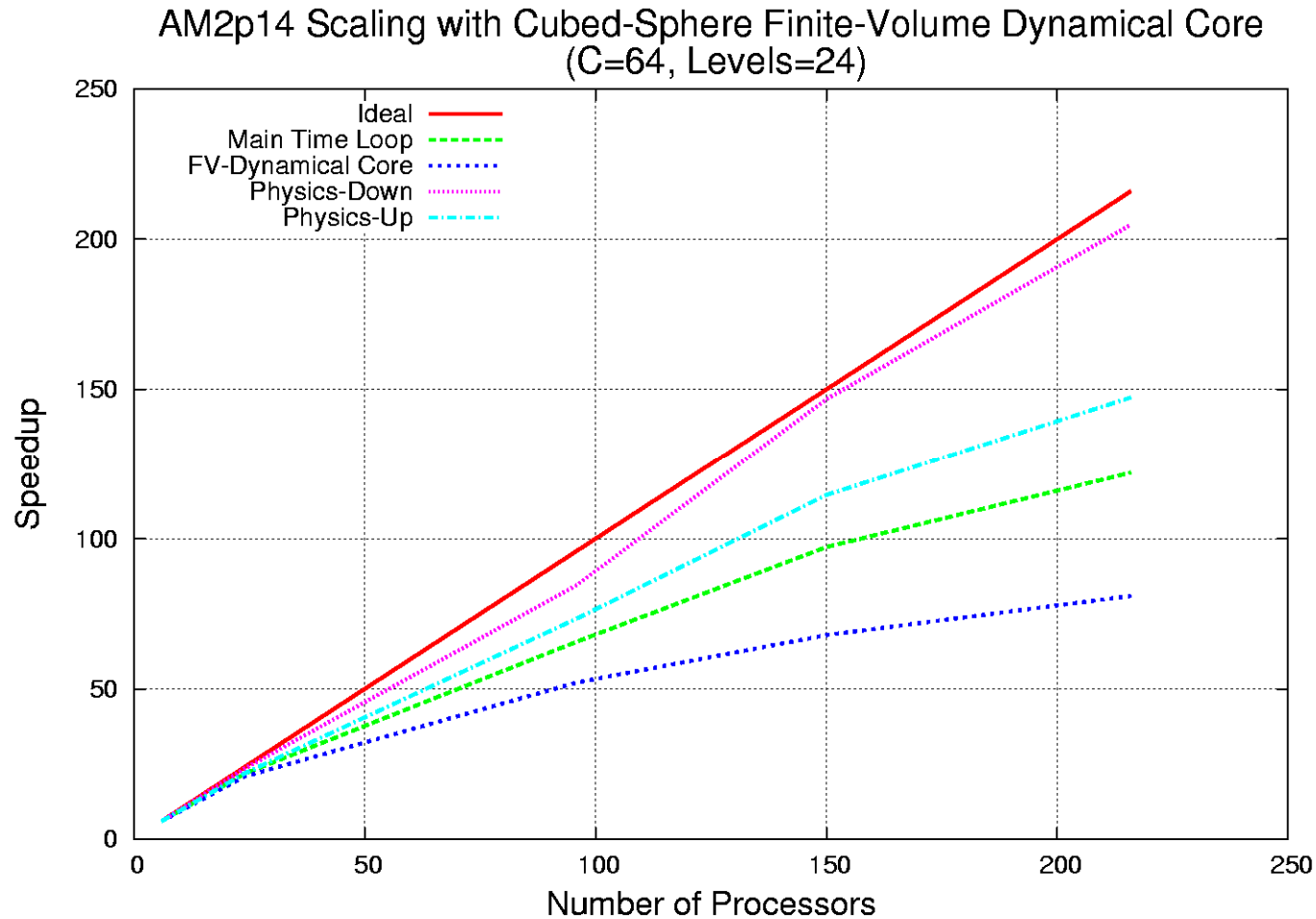




# Scaling of the dynamical core



# Scaling of C64 AMIP run



# Vertically Lagrangian Non-Hydrostatic FV Core

$$\frac{\partial}{\partial t} \delta p^* + \nabla_h \cdot [\vec{V} \delta p^*] = 0$$

$$\frac{\partial}{\partial t} (\Theta \delta p^*) + \nabla_h \cdot [\vec{V} \Theta \delta p^*] = 0$$

$$\frac{\partial}{\partial t} u - \Omega \tilde{v} \sin \alpha + \frac{\partial}{\partial x} \left( \frac{\tilde{u}u + \tilde{v}v}{2} \right) = \frac{\delta \Phi}{\delta p^*} \left[ \frac{\partial p}{\partial x} \right]_z = \frac{\delta \Phi}{\delta p^*} \left[ \frac{\partial p'}{\partial x} \right]_z + \frac{\delta \Phi}{\delta \pi^*} \left[ \frac{\partial \pi^*}{\partial x} \right]_z$$

$$\frac{\partial}{\partial t} v + \Omega \tilde{u} \sin \alpha + \frac{\partial}{\partial y} \left( \frac{\tilde{u}u + \tilde{v}v}{2} \right) = \frac{\delta \Phi}{\delta p^*} \left[ \frac{\partial p}{\partial y} \right]_z = \frac{\delta \Phi}{\delta p^*} \left[ \frac{\partial p'}{\partial y} \right]_z + \frac{\delta \Phi}{\delta \pi^*} \left[ \frac{\partial \pi^*}{\partial y} \right]_z$$

$$\frac{\partial}{\partial t} (w \delta p^*) + \nabla_h \cdot [\vec{V} w \delta p^*] = g \delta p'$$

**optional**

$$\delta m = \delta p^* / g = -\rho \delta z$$

$$p = p^* + p'$$

$$\frac{\partial}{\partial t} \delta z + \delta \left[ \vec{V} \cdot \nabla_h z \right] = \delta w$$

**hydrostatic** →

$$\delta z = \frac{1}{g} C_p \Theta \delta \pi^*$$

[A Riemann solver is used for the non-hydrostatic adjustment]

# Lagrangian Riemann solver *versus* semi-implicit finite differencing

- Advantages

- Acoustic waves are treated more accurately.
- No staggering of prognostic variables is necessary. The exact Riemann solver provides, in effect, an analytic way of staggering for pressure gradient computation.
- Computationally more efficient at cloud-resolving scales

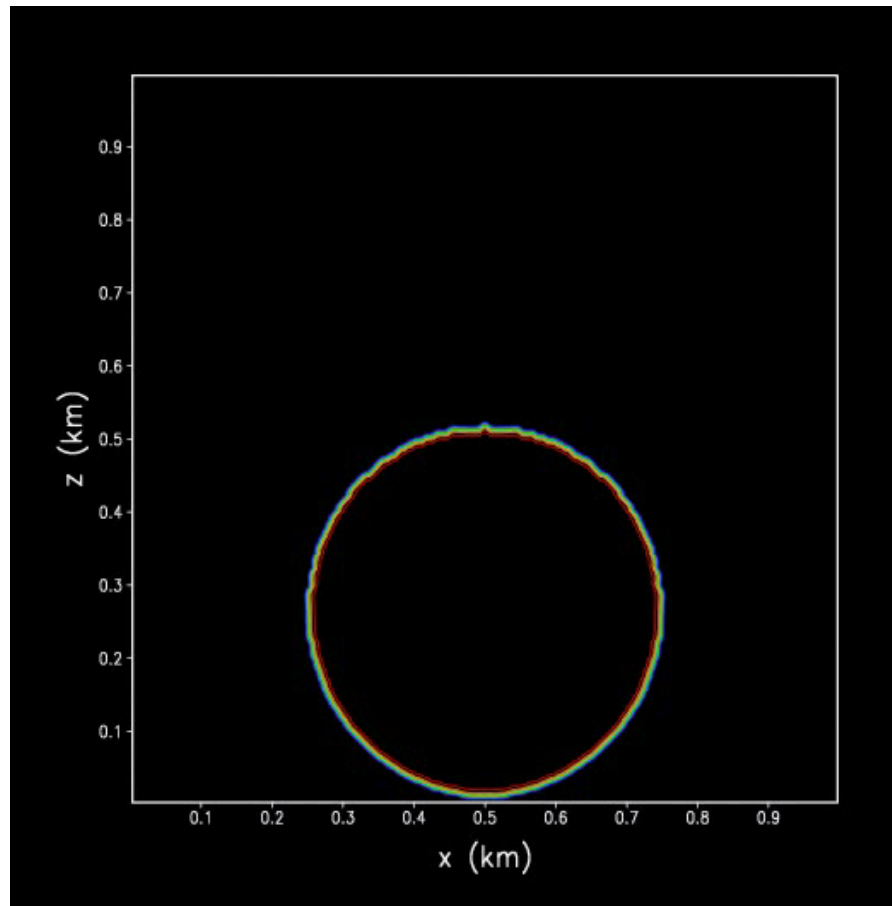
- Disadvantages

- There is a physical limit on the size of the time; sub-cycling becomes necessary if the resolution is near the hydrostatic regime ( $\sim 10\text{km}$  and beyond). Therefore, it is slower than semi-implicit algorithm for hydrostatic scales.
- Not applicable for Eulerian coordinate systems.



# Non-hydrostatic test case

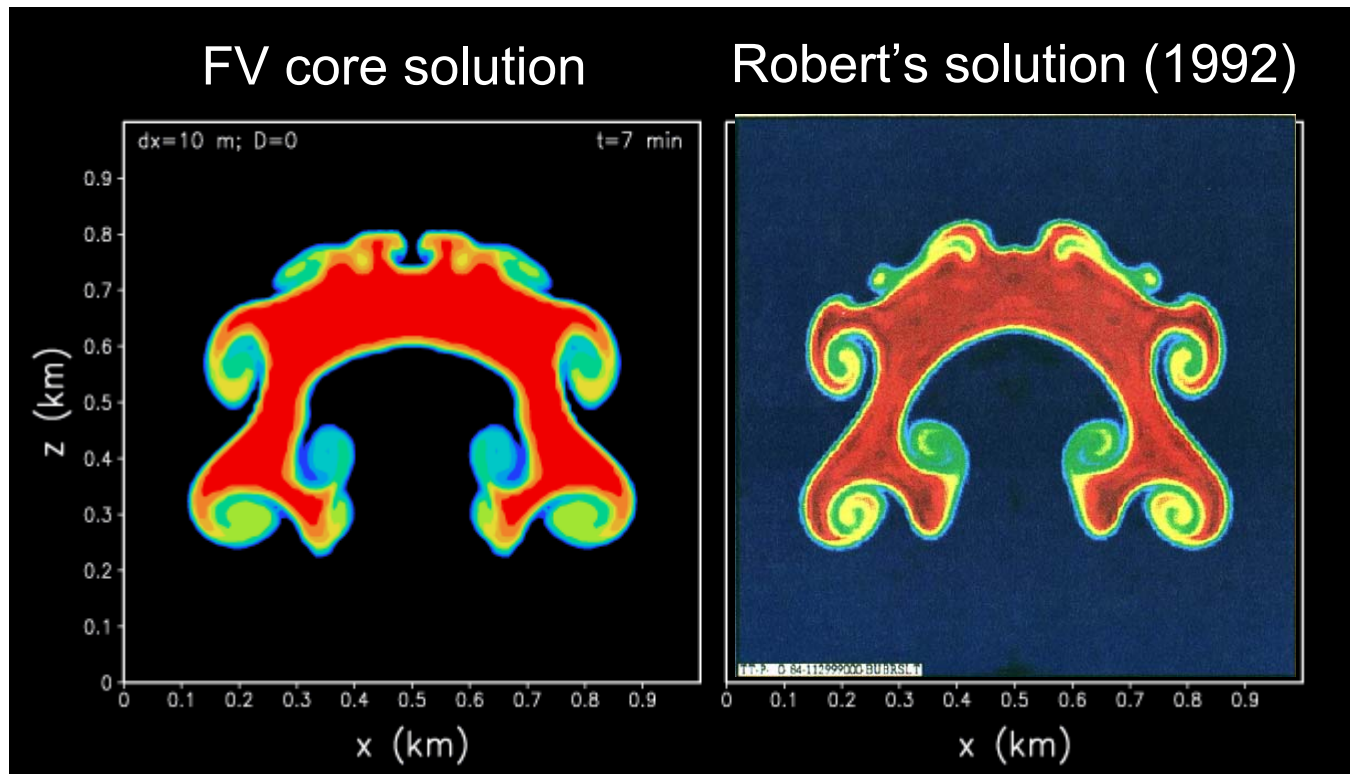
Warm bubble experiment (Robert 1992):  $\Delta x = \Delta z = 5\text{m}$ ,  $D = 0.1$ ,  $\Delta t = 0.1\text{s}$



Initial condition:  
isentropic with  
warm bubble perturbation  
Contours:  
potential temperature

# Non-hydrostatic test case

*Warm bubble (Robert 1992)*



# Global Non-Hydrostatic Core

- Test cases run at C1000 and C2000
  - C2000 is approximately 4-5 km resolution
  - Jablonowski & Williamson (2006) with 4 tracers
- 864 processors used on the GFDL SGI Altix 4700
  - computational domain on a single processor of ~ 167 x 167 x 26 points



# Global Non-Hydrostatic Core

*Performance at various horizontal resolutions*

Model	Grid size (km)	Physics & remapping time step (seconds)	2D Lagrangian dynamics time step (seconds)	Riemann solver time step (seconds)	Throughput (days/day)
C720 26L	10.9~15.4	360	15	5	~64*
C1000 26L	7.8~11.1	240	12	4	~32
C2000 26L	3.9~5.5	120	6	3	~4.2





# Global Non-Hydrostatic Core

*Timing breakdown for C2000 resolution (1 day run)*

<b>Total</b> (seconds)	20265.8	100%
Horizontal Advection (20 sub-cycles within the Lagrangian dynamics)	7463.4	36.8
Riemann Solver (3 sub-cycles per small step)	7411.1	36.6
Message Passing	1410.4	7.0
Lagrangian to Eulerian Remapping	1093.74	5.4
Pressure gradients (C+D core)	680.7	3.4
Tracer advection (large-time-step)	544.3	2.2
Others (initialization, diagnostics, etc.)	1662.2	8.4



# Future Plans

- Incorporate into AM3 (*our next AM*)
- Doubly-periodic limited-area model
  - Test bed for physics, import cloud micro-physics
- Global high-resolution hydrostatic model
  - C360 ( $1/4^\circ$ ), AMIP mode, less obtrusive convection
- Global cloud-resolving non-hydrostatic model
  - C2000 (4-5 km), short term forecasts, proof of concept run
- Regional grids and nesting



# C90 Movie

01-JAN

