

# Implementation of the Robert Filter in POP

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LANL

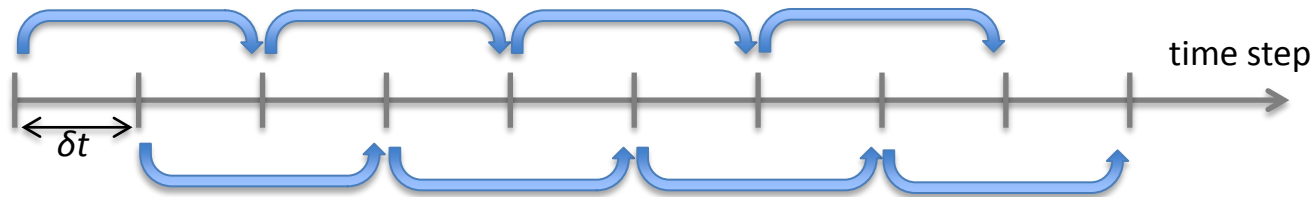
# Outline

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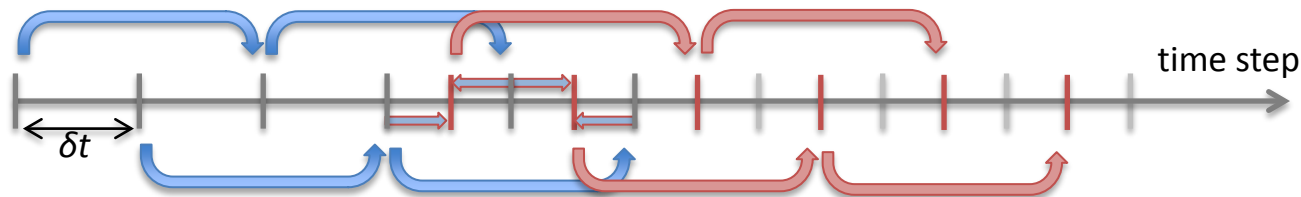
- Why do we need something different?
- Formulation of the filter
- Implementation in POP
- Results
  - Ocean only
  - Fully coupled
- What's left to do?

# Leapfrog Timestepping

- 2<sup>nd</sup> order, easy to implement
- Even/odd step decoupling is unstable



- POP solution: Average even/odd solutions every N steps



# Why Change?

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- Averaging steps worked fine for ocean-only work when the time important time boundaries when associated with data output
- For CESM, coupling interval has become definitive time segment
  - Always at least 2 averaging steps/coupling interval
  - Still ok with daily coupling
    - (23,2) (full,half) steps/day for x1
  - Too frequent with higher frequency coupling
    - (18,6) (full,half) steps/day for x1 and 4-hour coupling

# What are possible options?

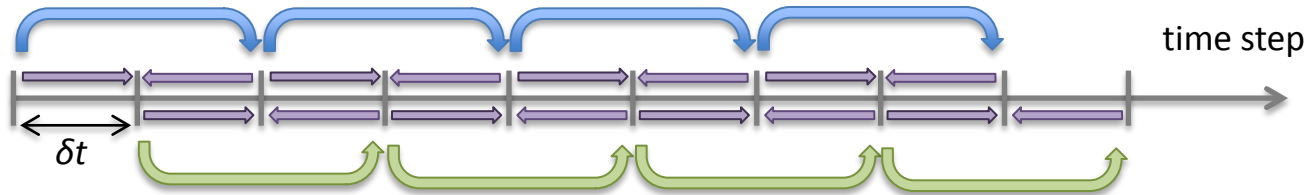
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- 2 time level scheme
  - Pro: very versatile
  - Con: large amount of code redesign
- Robert-Asselin filter
  - Pro: keep leapfrog scheme (fewer code mods)
  - Con: keep leapfrog scheme

# Robert Filter

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- Do a little averaging every timestep (weak temporal diffusion)



- Formally first order, but is “quasi 2<sup>nd</sup> order” since only a little every timestep

# Formulation

example: POP temperature equation

$$(1 + \xi^{n+1})T^{n+1} = (1 + \xi^{n-1})T^{n-1} + 2\delta t(F^n + Q_{sw}^n(z) + Q_{ice}^n + A + D)$$

$\frac{SSH}{dz_k} \delta_{1,k}$                       surface heat flux                      sea ice formation                      penetrative shortwave                      advection + diffusion

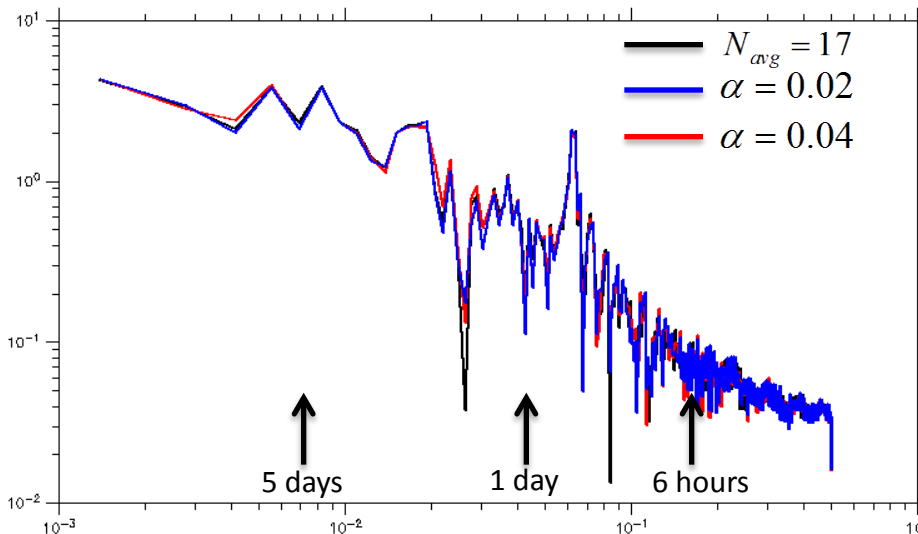
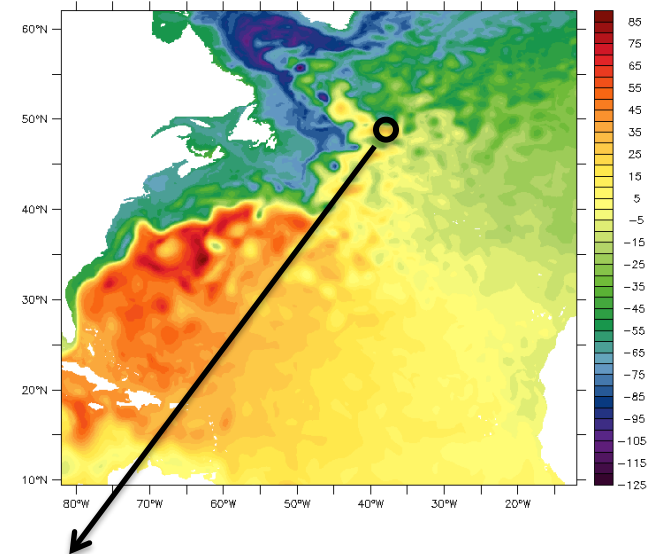
Robert Filter

$$(1 + \hat{\xi}^n)\hat{T}^n = (1 + \xi^n)T^n + \alpha \left[ (1 + \xi^{n+1})T^{n+1} - 2(1 + \xi^n)T^n + (1 + \xi^{n-1})T^{n-1} \right]$$

$$\alpha \ll 1$$

# Ocean-Only Results

- Too diffusive?
  - 1/10 North Atlantic with
  - 6-hour “Normal Year”
  - 7 minute timestep
  - 30 day run, 1 hour sampling



Spectrum of U (cyc/hour)



# Coupling Problem

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- Robert filter not able to conserve both globally and locally (Griffies et al)
- Leclair and Madec (2009) to the rescue
  - Split  $n$ -level forcing to  $n-1/2$ ,  $n+1/2$
  - Modify filter to account for this
  - Can achieve both local and global conservation

# Modified Formulation

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Temperature equation

$$\begin{aligned}(1 + \xi^{n+1})T^{n+1} &= (1 + \xi^{n-1})T^{n-1} + \delta t(F^{n-1/2} + Q_{sw}^{n-1/2} + Q_{ice}^{n-1/2}) \\ &\quad + \delta t(F^{n+1/2} + Q_{sw}^{n+1/2} + Q_{ice}^{n+1/2}) \\ &\quad + 2\delta t(A + D)\end{aligned}$$

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Robert Filter

$$\begin{aligned}(1 + \hat{\xi}^n)\hat{T}^n &= (1 + \xi^n)T^n + \alpha \left[ (1 + \xi^{n+1})T^{n+1} - 2(1 + \xi^n)T^n + (1 + \xi^{n-1})T^{n-1} \right] \\ &\quad + \alpha\delta t(F^{n-1/2} + Q_{sw}^{n-1/2} + Q_{ice}^{n-1/2}) \\ &\quad - \alpha\delta t(F^{n+1/2} + Q_{sw}^{n+1/2} + Q_{ice}^{n+1/2})\end{aligned}$$

# Implementation in CESM

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- Focus on fully coupled (B1850)
- 2 time levels for surface forcing
  - Latent, sensible, longwave constant over coupling interval
  - Shortwave can change every timestep
  - Shortwave needs extra 3D array
  - Ice formation only on last timestep of coupling interval
  - Extra restart fields

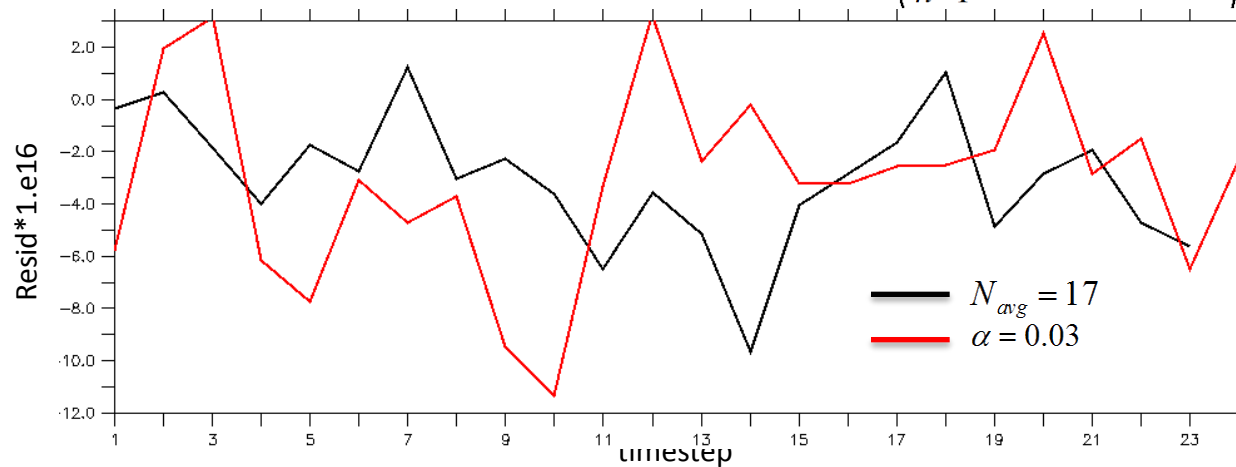
# Coupled Results

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- F09\_g\_B1850, CESM\_1.1.beta08
- Daily coupling
- 4 year “startup” runs
  - averaging timestep every 17 steps (default)
  - Robert filter,  $\alpha = 0.03$
  - Robert filter,  $\alpha = 0.02$
  - averaging timestep every 9 steps

# Ocean Temperature Residual

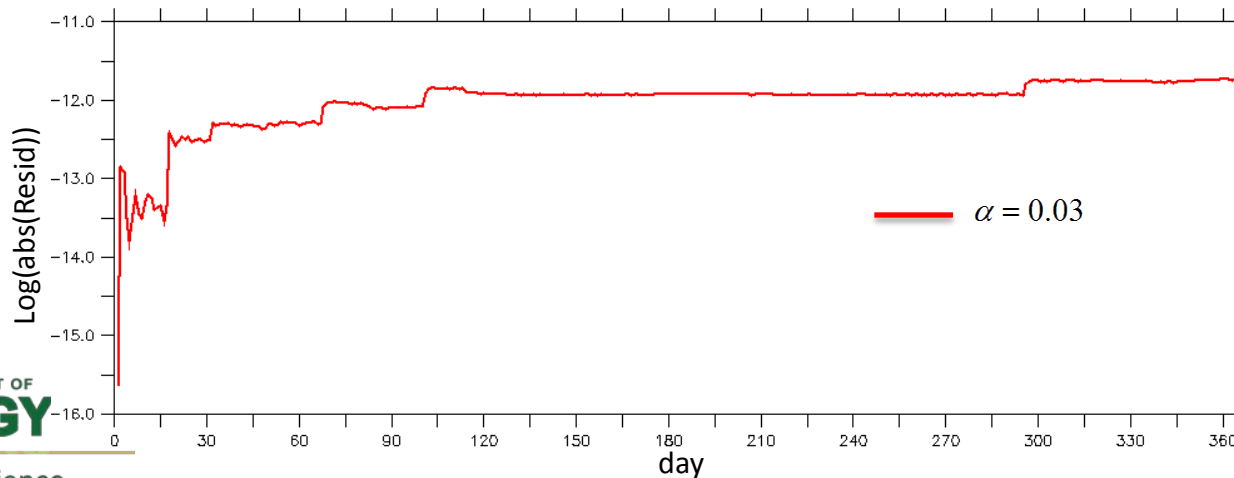
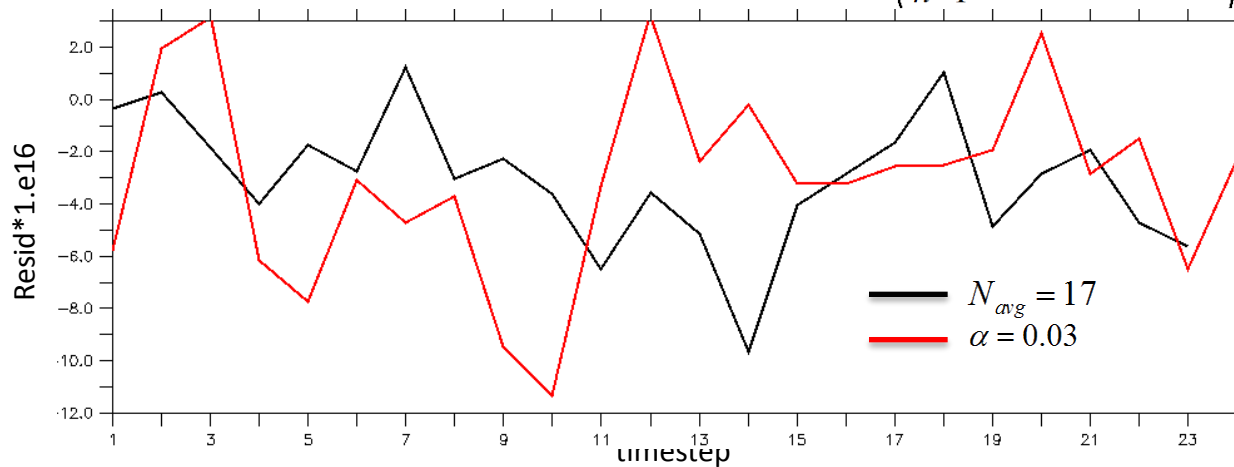
$$Resid_T(N) = \langle T(N) \rangle - \langle T(0) \rangle + \left\langle \sum_{n=1}^N Source(n) \right\rangle$$



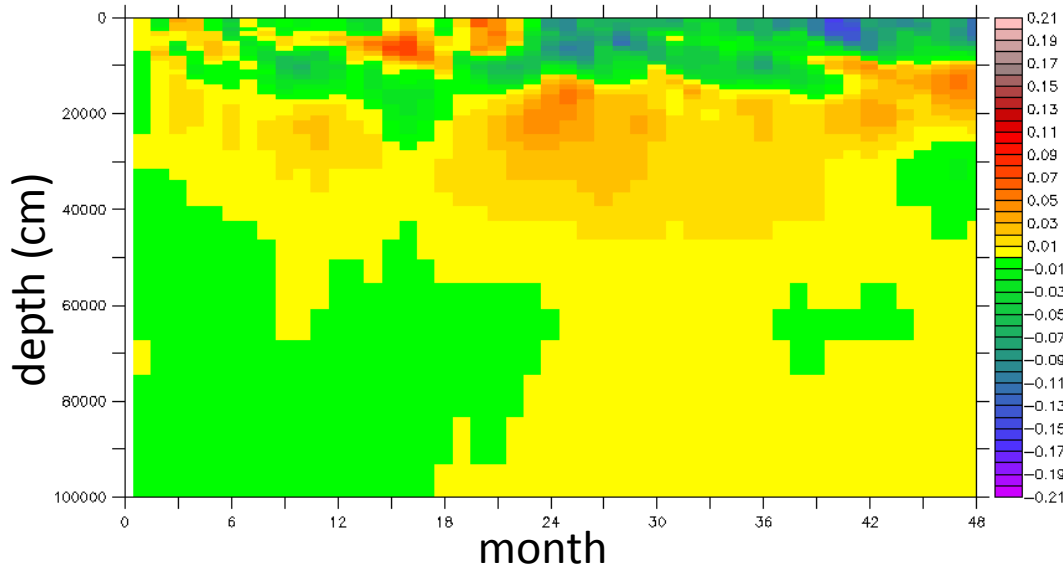
First day

# Ocean Temperature Residual

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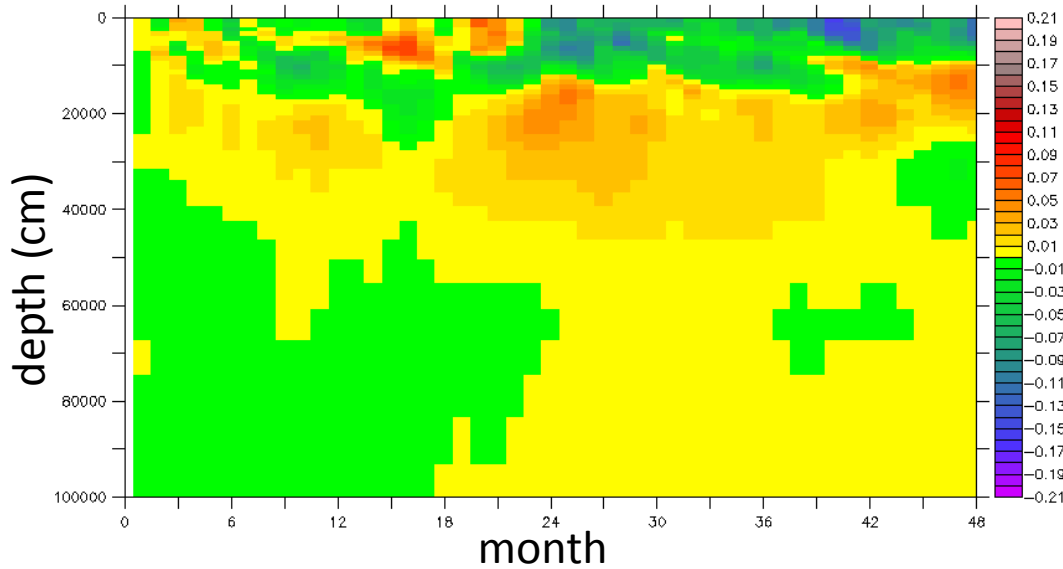


# Globally Averaged Ocean Temperature Difference

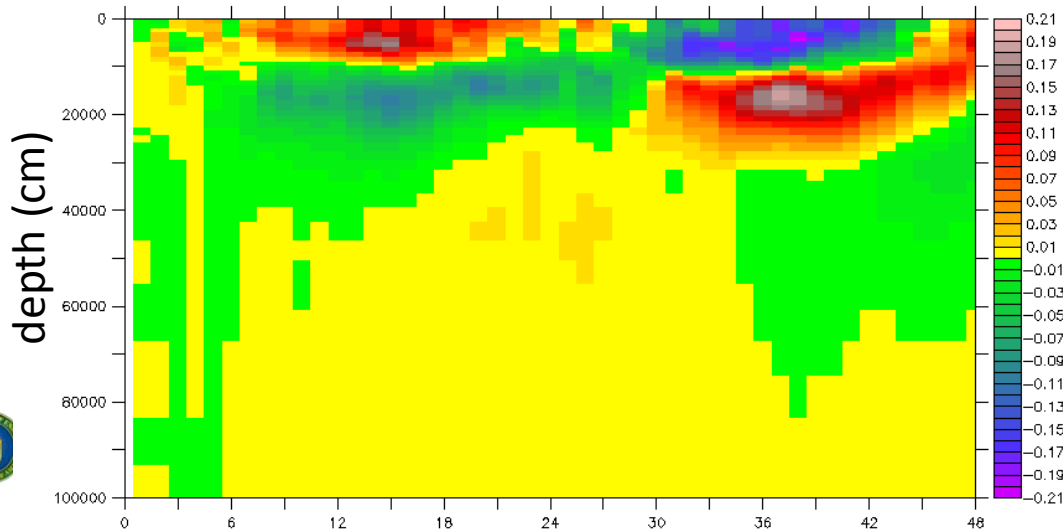


Standard ( $N_{avg} = 17$ ) – Robert ( $\alpha = 0.03$ )

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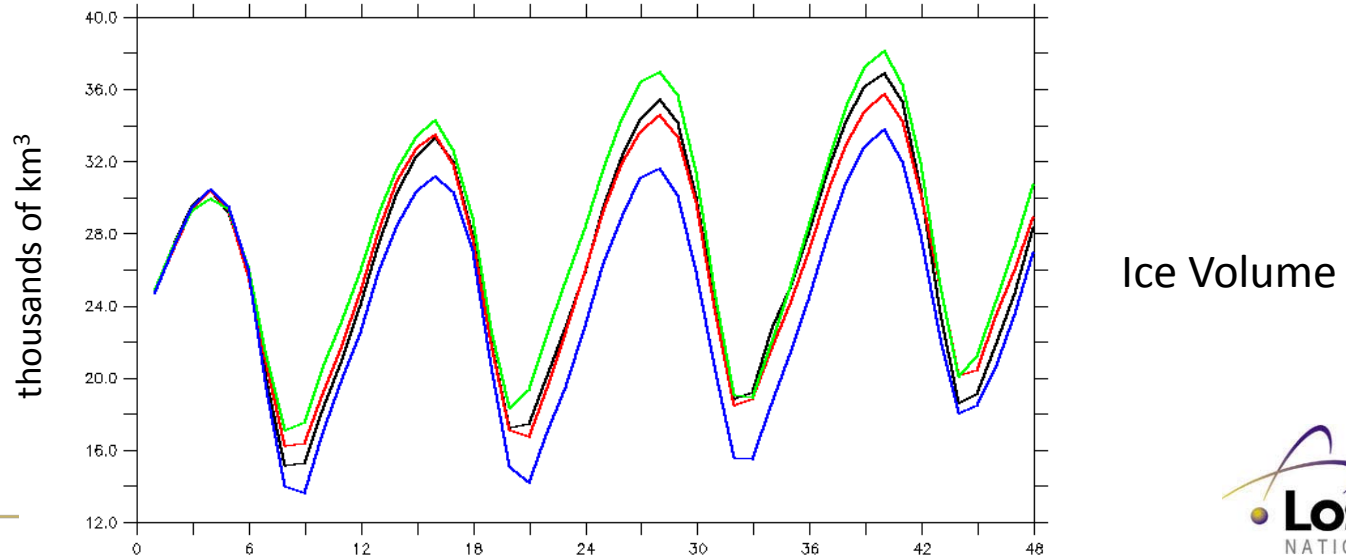
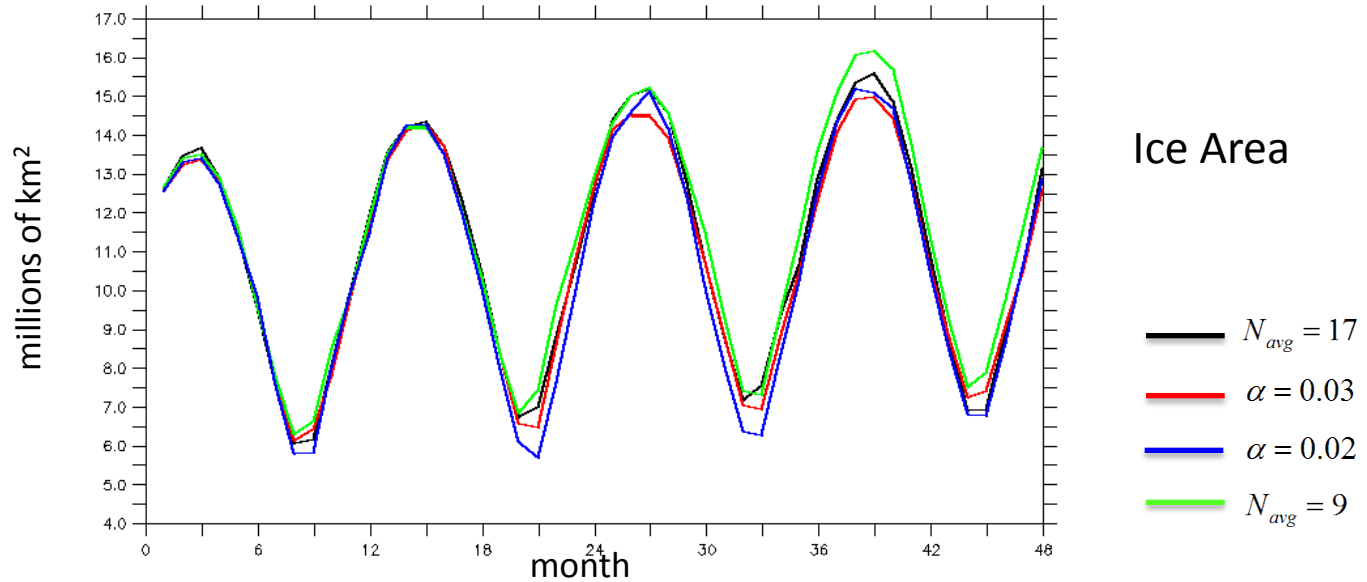


Standard ( $N_{avg} = 17$ ) – Standard ( $N_{avg} = 9$ )





# Arctic Sea Ice



# Future

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- Complete robust implementation
  - Passive tracers
- More thorough testing in variety of configurations
  - Multi-century control run
- Extend to the higher order variant of Williams (2009)
  - Also filters the  $n+1$  time level
- Make compatible with  $z^*$