

Matrix-based diagnosis of plant biomass  
response to environmental change—an  
example of warming response in permafrost  
ecosystem

Xingjie Lu, Zhenggang Du, Yuanyuan  
Huang, Yiqi Luo and other co-authors



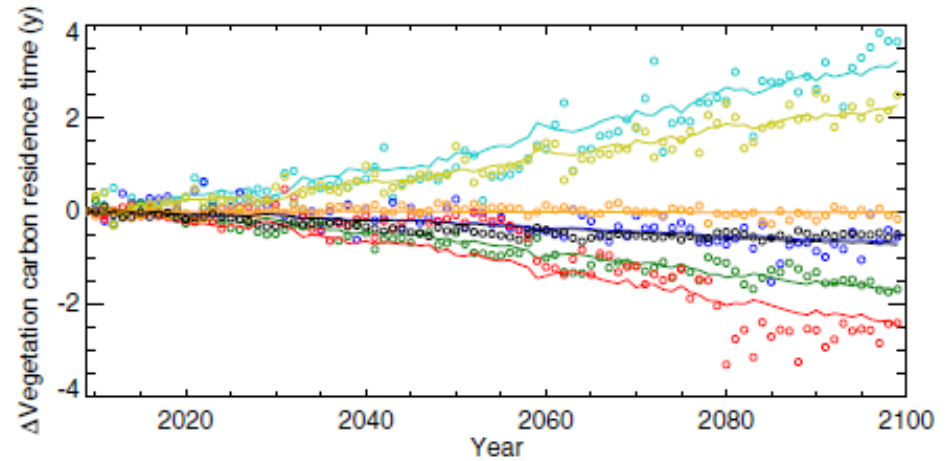
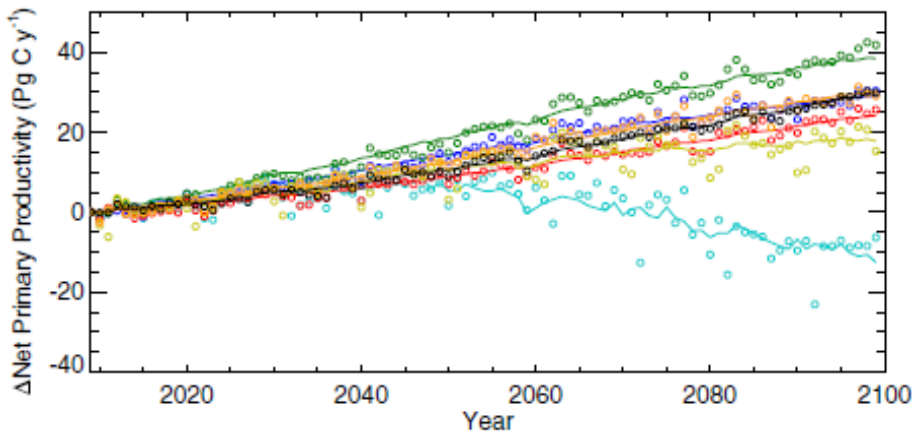
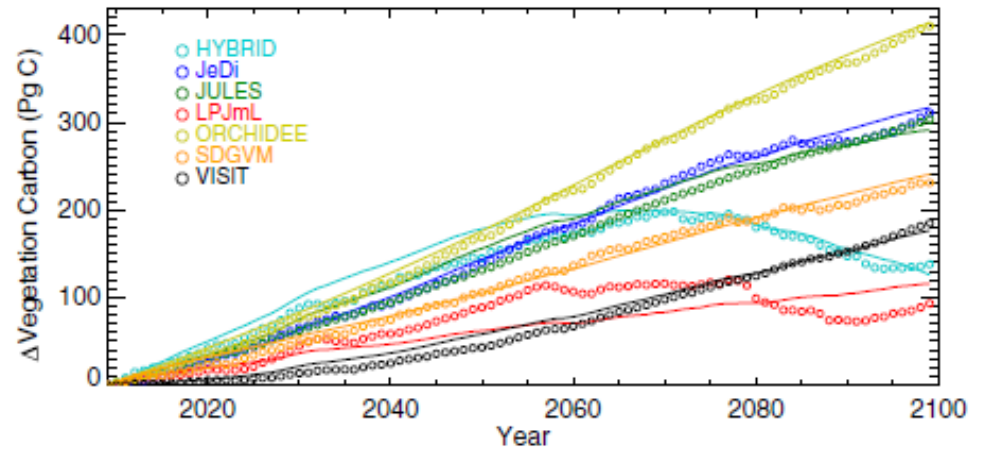
# Outline

- Motivation
- Matrix-based CLM vegetation model
- An application example



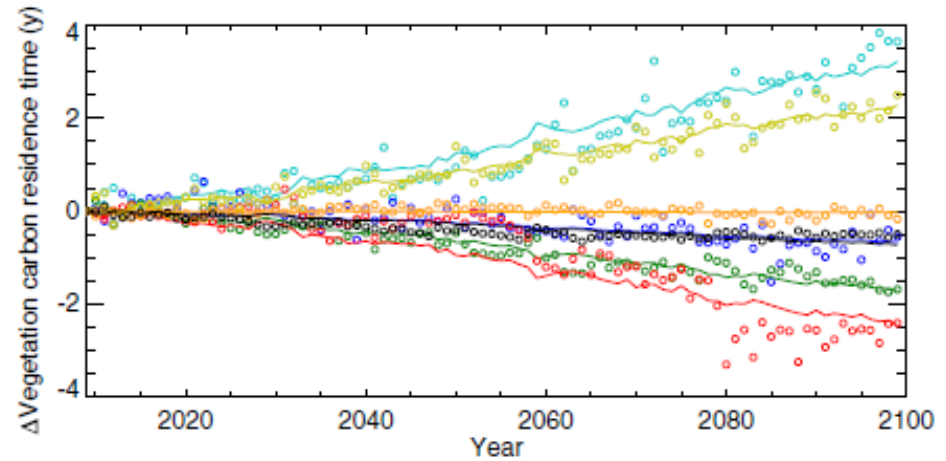
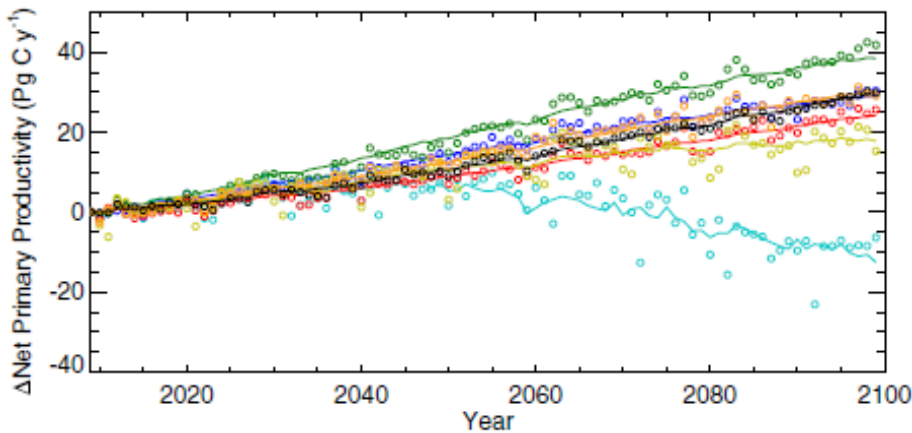
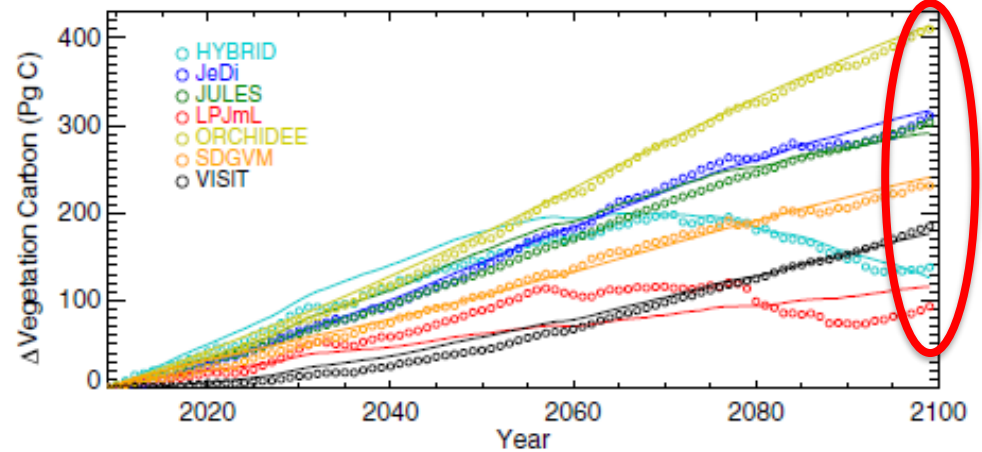
# Model uncertainties in vegetation C response

- Modeling growth in global vegetation carbon are in great uncertain among global vegetation models.

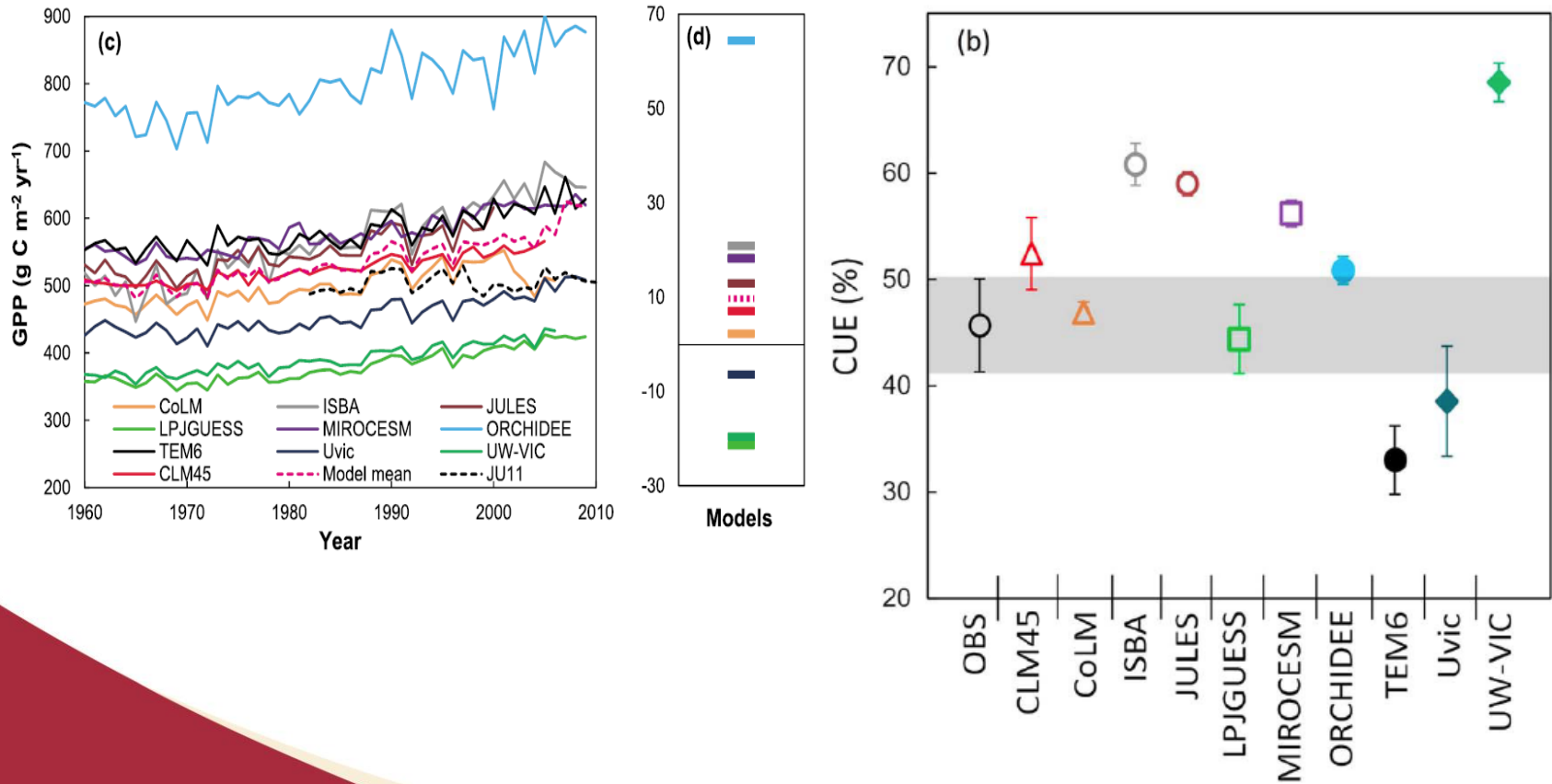


# Model uncertainties in vegetation C response

- Modeling growth in global vegetation carbon are in great uncertain among global vegetation models.



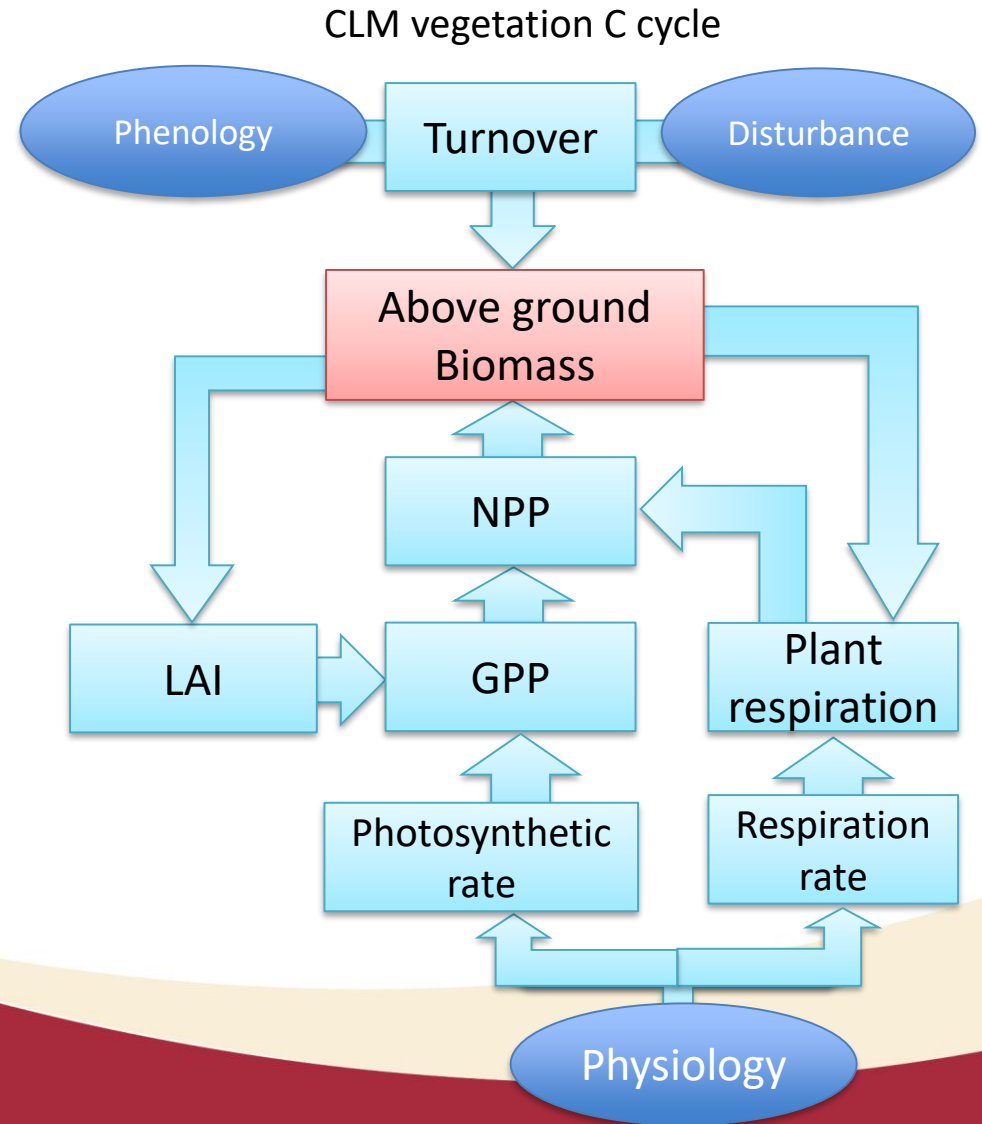
# Uncertainties in permafrost modeling



# Joint controls in vegetation C diagnosis

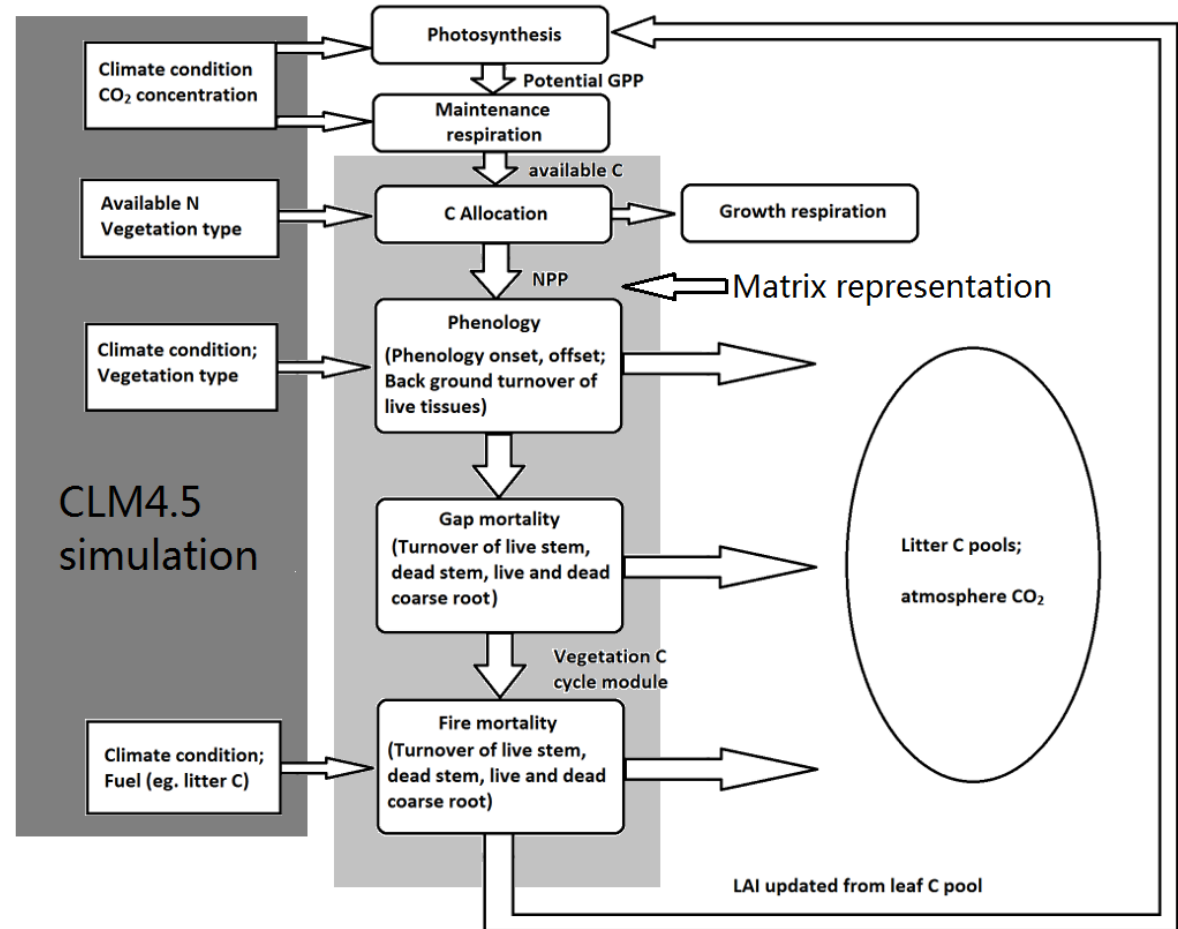
Difficulties in diagnosing modeled vegetation C cycle:

- Variables in vegetation C cycle are interacted with each other.
- Effects from different processes are hard to be isolated

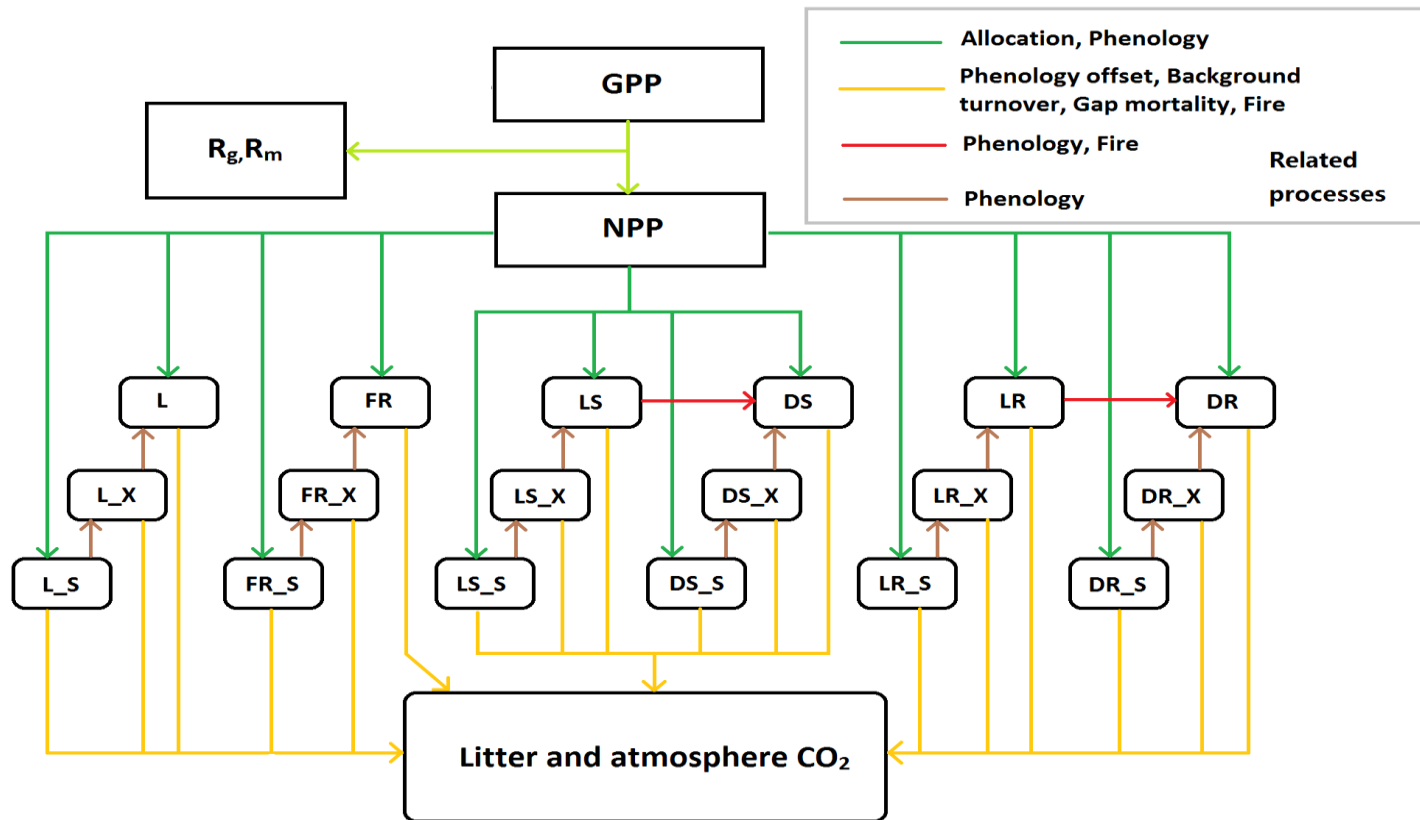


# A simple vegetation C model isolated from CLM4.5

- Aims to segregated effects from different processes
- Environmental drivers from CLM4.5 includes: canopy temperature, soil moisture, soil mineral N, snow depth and so on.



# CLM vegetation C transfers among 18 pools



L: leaf;	L_X: leaf transfer;	L_S: leaf storage
FR: fine root;	FR_X: fine root transfer;	FR_S: fine root storage
LS: live stem;	LS_X: live stem transfer;	LS_S: live stem storage
DS: dead stem;	DS_X: dead stem transfer;	DS_S: dead stem storage
LR: live coarse root;	LR_X: live coarse root transfer;	LR_S: live coarse root storage
DR: dead coarse root;	DR_X: dead coarse root transfer;	DR_S: dead coarse root storage



# Matrix representation

- Vegetation C dynamics:

$$\frac{dX(t)}{dt} = Bu(t) - (A_p(t)K_p(t) + A_mK_m + A_fK_f(t))X(t)$$

$X$  (vector): C pool sizes;

$B$  (vector): allocation;

$u$  (scalar): NPP;

$A$  (matrix): transfer ratio among pools;

$K$  (diagonal matrix): turnover rate.

Subscripts  $p$ ,  $m$  and  $f$  indicates:  
phenology, gap mortality and fire  
processes.



# How does the matrix look like?

For examples: Phenology transfer matrix

$$\begin{array}{c}
 \begin{array}{ccc}
 \text{Display pools} & \text{Transfer pools} & \text{Storage pools} \\
 \hline
 l & fr & ls & ds & lcr & dcr & l_{xfer} & fr_{xfer} & ls_{xfer} & ds_{xfer} & lcr_{xfer} & dcr_{xfer} & l_{st} & fr_{st} & ls_{st} & ds_{st} & lcr_{st} & dcr_{st}
 \end{array} \\
 A_p = \begin{pmatrix}
 -1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
 0 & -1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
 0 & 0 & 1 & -1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 & 1 & -1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & 0 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1 & 0 \\
 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & -1
 \end{pmatrix}
 \end{array}
 \begin{array}{l}
 \text{Display pools} \\
 \text{Transfer pools} \\
 \text{Storage pools}
 \end{array}
 \end{array}$$



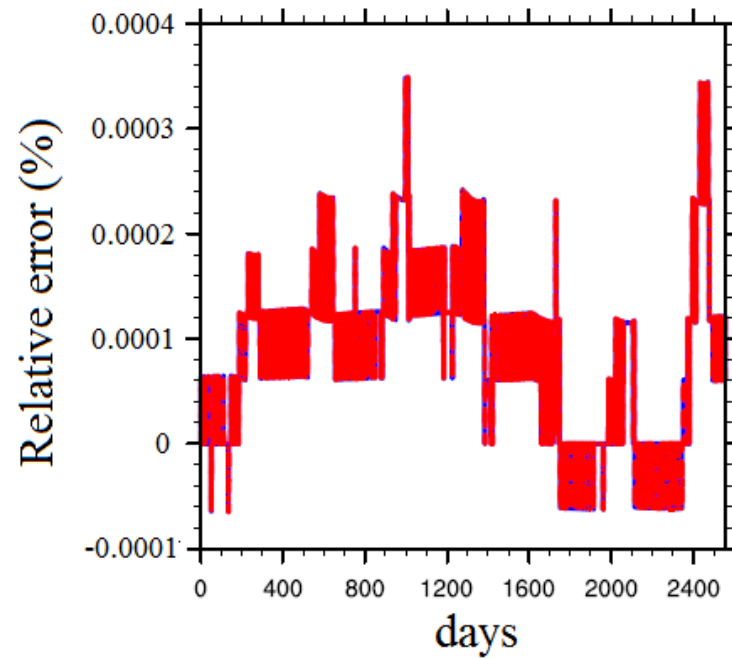
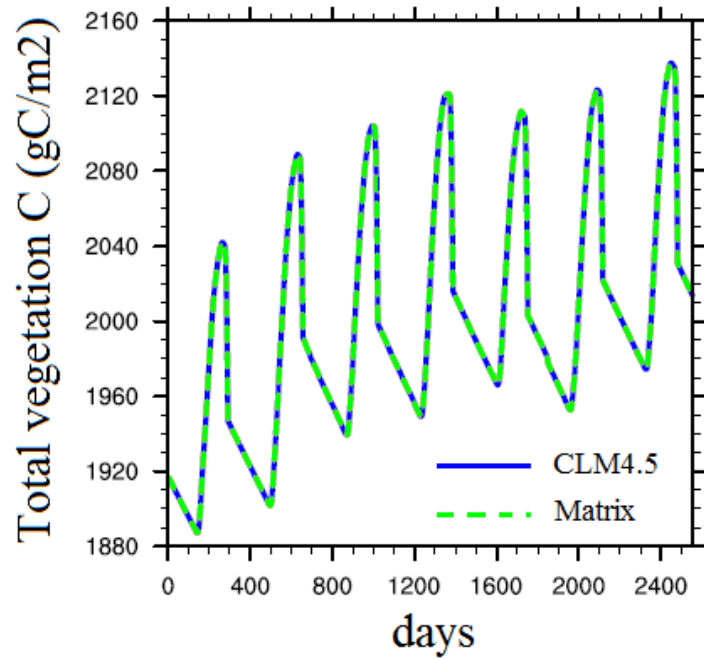
How does the matrix look like?

- $$K_p = \begin{pmatrix} -k_{leaf} & \cdots & 0 \\ \vdots & \ddots & \vdots \\ 0 & \cdots & -k_{dcr\_st} \end{pmatrix}$$

- $k_i = \text{turnover } C / \text{original } C \text{ pool size}$

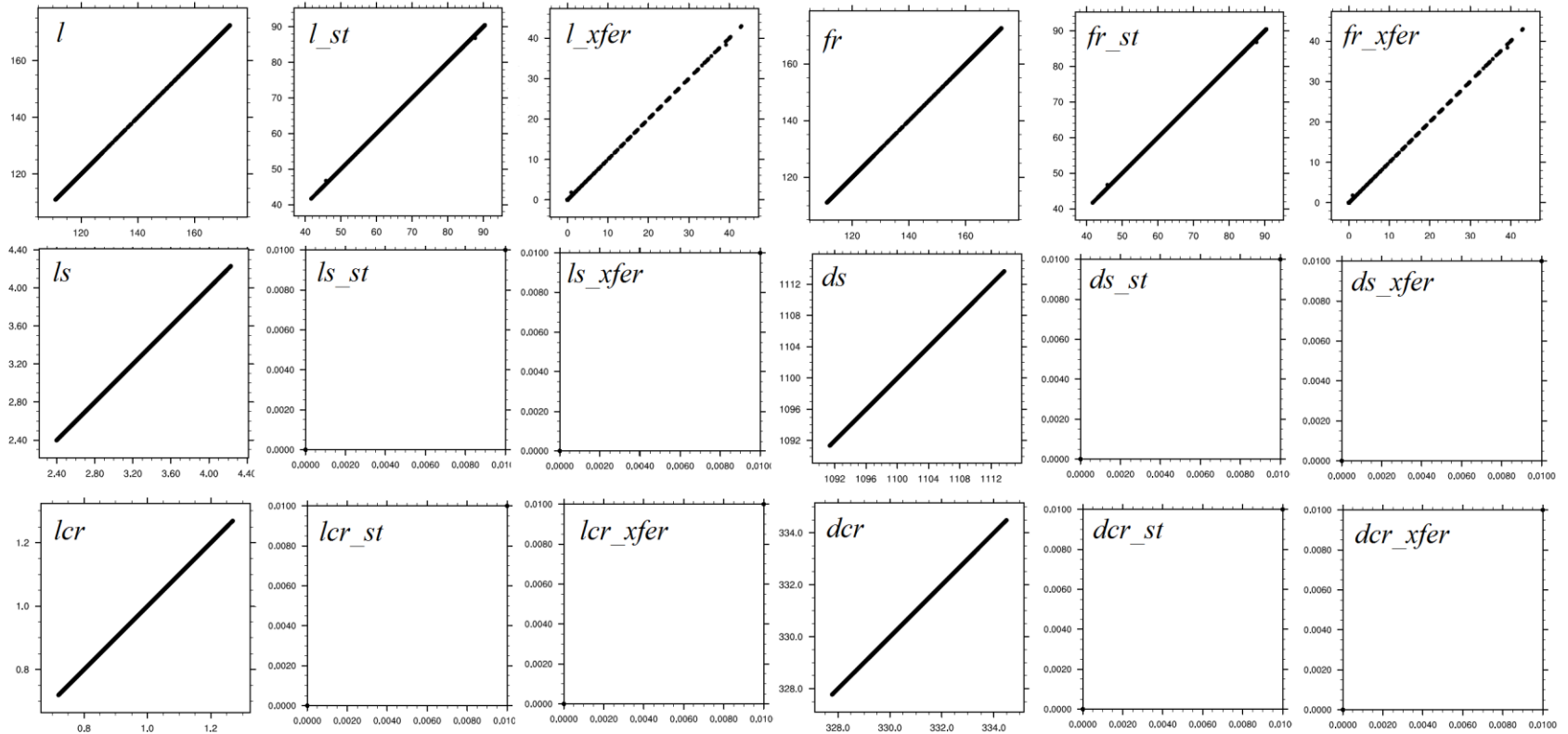
- $$B = \begin{pmatrix} a_{leaf} \\ \vdots \\ a_{dcr\_st} \end{pmatrix}$$

# Matrix model validation



# Matrix model validation (individual pool)

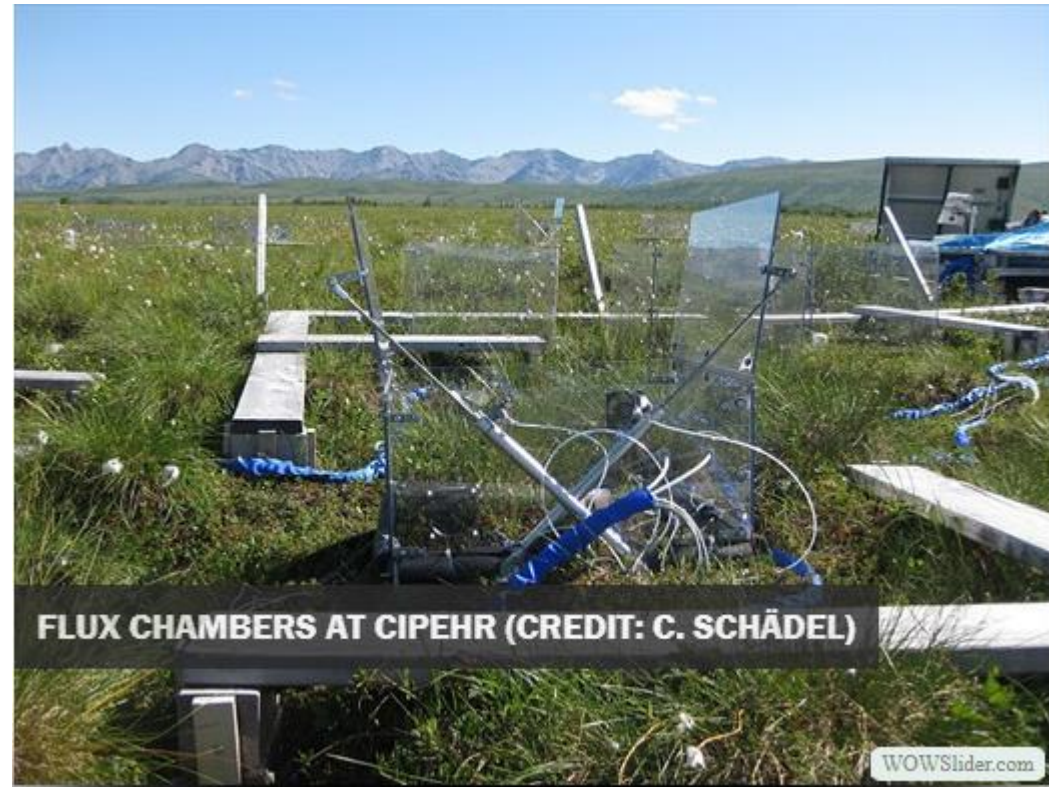
Matrix equations simulated C pool size (gC/m<sup>2</sup>)



CLM simulated C pool size (gC/m<sup>2</sup>)

# Simulations on an air warming experiment

- The Carbon in Permafrost Experimental Heating Research (CiPEHR) in Alaska established in 2008
- Air warming experiments use open top chamber (OTC) to increase air temperature by 2°C during summer season.



<https://www2.nau.edu/schuurlab-p/CiPEHR.html>

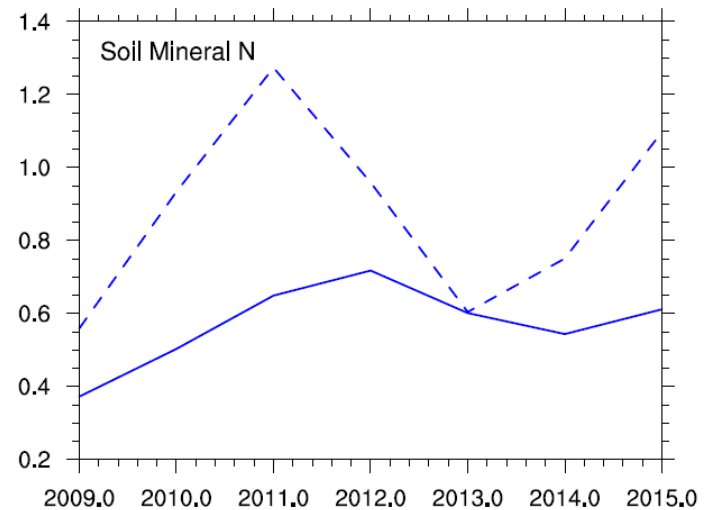
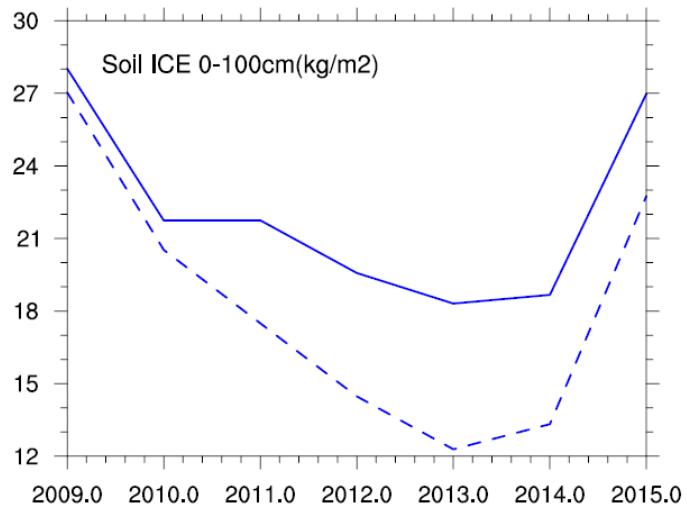
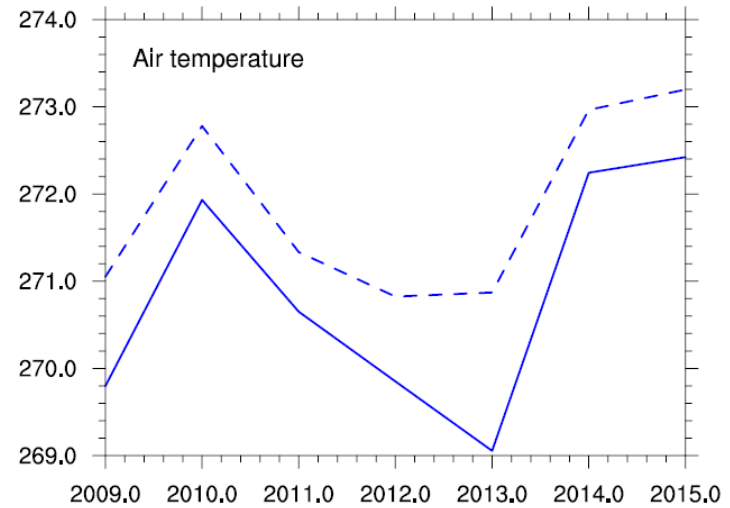
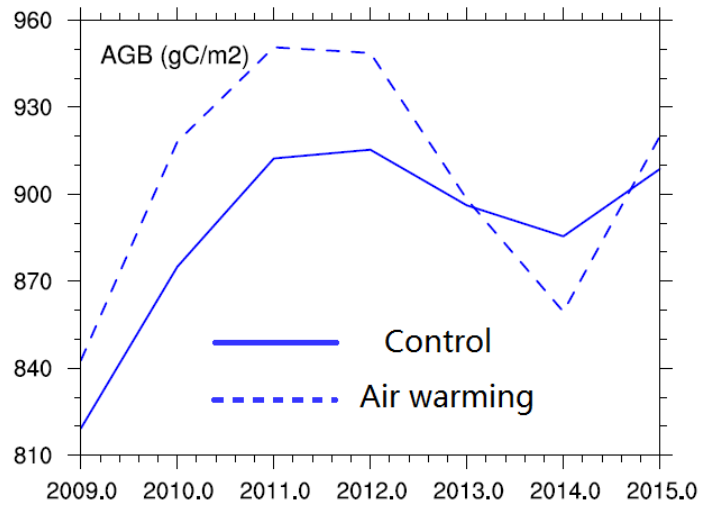


# CLM simulation setup

- CLM4.5 simulation is initialized in 1901 using spin up vegetation and soil C pool sizes.
- Spin up is driven by using cycled 1901-1910 CRUNCEP forcing (QIAN, Version7)
- Historical simulation is from 1901 to 2008 to enable vegetation and soil steadily increase in a transient state.
- Two runs (air warming vs. control) use adjusted temperature and precipitation based on site-level annual observation data.



# Warming response from CLM4.5





# Matrix-based diagnosis

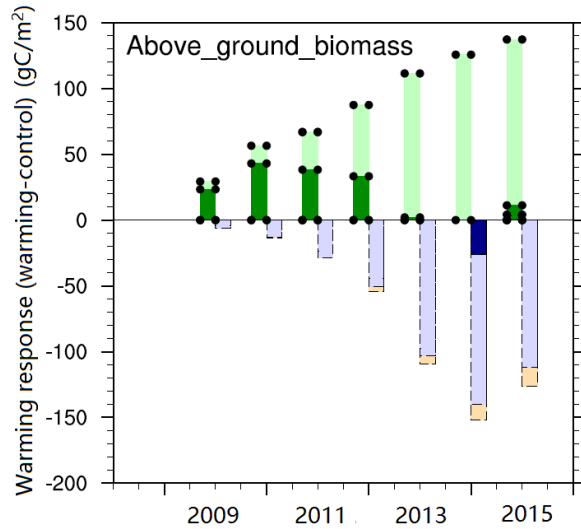
$$\frac{dX(t)}{dt} = Bu(t) - (A_p(t)K_p(t) + A_m K_m + A_f K_f(t))X(t)$$

$$u(t) = f(psn, r_m(T), LAI(psn, r_m, A_p, K_p, A_m, K_m, A_f, K_f))$$

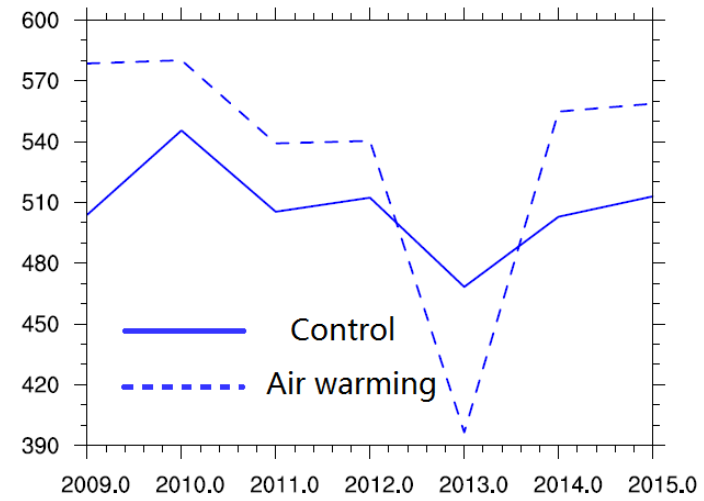
Simulation abbreviation	Physiology component	Phenology matrix	Disturbance matrix
S_pgd	psn_c, r_m_c	A_p_c, K_p_c	A_m_c, K_m_c, A_f_c, K_f_c
S_Pgd	psn_w, r_m_w	A_p_c, K_p_c	A_m_c, K_m_c, A_f_c, K_f_c
S_PGd	psn_w, r_m_w	A_p_w, K_p_w	A_m_c, K_m_c, A_f_c, K_f_c
S_PGd	psn_w, r_m_w	A_p_w, K_p_w	A_m_w, K_m_w, A_f_w, K_f_w



# Response in above ground biomass



sunlit leaf photosynthetic rate (gC/m<sup>2</sup>/yr)



## Future application

- Data assimilation  
30 times faster than original CLM.
- Spin up:

$$X_C = (A_p(t)K_p(t) + A_mK_m + A_fK_f(t))^{-1}B(t)$$



# Summary

- Matrix representation is a useful tool to segregate effects from vegetation C cycle processes with strong interaction.
- Simulated warming response in plant biomass and productivity in permafrost ecosystem is mainly controlled by two processes--phenology (positive) and physiology (negative).



Thanks for your attention